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**Algorithm 1** NEH Heuristic

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Calculate the total processing time of each job as  $S[1, \dots, n]$   
Sort  $S[1, \dots, n]$  in the descending order

**Require:**  $n \geq 0 \vee x \neq 0$

**Ensure:**  $y = x^n$

$y \leftarrow 1$

**if**  $n < 0$  **then**

$X \leftarrow 1/x$

$N \leftarrow -n$

**else**

$X \leftarrow x$

$N \leftarrow n$

**end if**

**while**  $N \neq 0$  **do**

**if**  $N$  is even **then**

$X \leftarrow X \times X$

$N \leftarrow N/2$

**else**  $\{N \text{ is odd}\}$

$y \leftarrow y \times X$

$N \leftarrow N - 1$

**end if**

**end while**

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**Algorithm 2** NEH Heuristic

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Calculate the total processing time of each job as  $S[1, \dots, n]$   
Sort  $S[1, \dots, n]$  in the descending order

**Require:**  $n \geq 0 \vee x \neq 0$

**Ensure:**  $y = x^n$

$y \leftarrow 1$   
**if**  $n < 0$  **then**  
     $X \leftarrow 1/x$   
     $N \leftarrow -n$   
**else**  
     $X \leftarrow x$   
     $N \leftarrow n$   
**end if**  
**while**  $N \neq 0$  **do**  
    **if**  $N$  is even **then**  
         $X \leftarrow X \times X$   
         $N \leftarrow N/2$   
    **else**  $\{N \text{ is odd}\}$   
         $y \leftarrow y \times X$   
         $N \leftarrow N - 1$   
    **end if**  
**end while**

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**Algorithm 3** Hill Climbing

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$\pi := \text{NEH\_Heuristic}$   
 $\pi := \text{Local\_Search}(\pi)$   
 $\text{iter} := 0$   
**while**  $\text{iter} < \text{MAX\_ITERATIONS}$  **do**  
     $i, j := \text{Random\_Integers}(0, n)$   
    Swap  $(\pi_i, \pi_j)$   
     $\pi' := \text{Local\_Search}(\pi)$   
    **if**  $C_{\pi'} < C_{\pi}$  **then**  
         $\pi := \pi'$   
    **end if**  
     $\text{iter} := \text{iter} + 1$   
**end while**

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**Algorithm 4** Simulated Annealing

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```
 $\pi := \text{NEH\_Heuristic}$ 
 $\pi := \text{Local\_Search}(\pi)$ 
iter := 0
temperature := Osman\_Initialization( $\pi$ )
while iter < MAX\_ITERATIONS do
  i, j := Random\_Integers(0, n)
  Swap ( $\pi_i, \pi_j$ )
   $\pi' := \text{Local\_Search}(\pi)$ 
  diff :=  $C_{\pi'} - C_{\pi}$ 
  acceptance\_criterion := exp(-diff/temperature)
  probability := Random\_Real (0, 1)
  if  $C_{\pi'} < C_{\pi}$  then
     $\pi := \pi'$ 
  else if probability < acceptance\_criterion then
     $\pi := \pi'$ 
  end if
  iter := iter + 1
  if iter % ITER\_PER\_EPOCH == 0 then
    temperature := temperature * annealing\_rate
  end if
end while
```

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**Algorithm 5** Genetic Algorithm

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population := Initialize\_Chromes()
population := Local\_Search (population)
generation := 0
while generation < MAX\_GENERATION do
  new\_population := Select\_Chromes(population)
  new\_population := CrossOver\_Chromes(new\_population)
  new\_population := Mute\_Chromes (new\_population)
  new\_population := Local\_Search (new\_population)
  if  $\max(C_{\text{new\_population}}) < \max(C_{\text{population}})$  then
    population := new\_population
  end if
  generation := generation + 1
end while
```

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