Errata File for Second Edition

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October 25, 2025

This errata file contains a list of errors, short clarifications and modifications to the manuscript's second edition.

1. Page 170, bottom half of the page, bracket missing:
   CHANGE:
   $$\mathrm{Var}\,(\hat{a} - a) = \mathrm{E}_y(\mathrm{Var}(a|y)$$
   TO.
   $$\mathrm{Var}\,(\hat{a} - a) = \mathrm{E}_y\,(\mathrm{Var}(a|y))$$

2. Page 171, the first partial derivative below Eq. (4.62).
   CHANGE:
   $$\frac{\partial \ln p\,(a, b|y, b_0, a_0, B, G, R)}{\partial b} = -B^{-1}(b - b_0) + XR^{-1}\,(y - Xb - Za)$$
   TO:
   $$\frac{\partial \ln p\,(a, b|y, b_0, a_0, B, G, R)}{\partial b} = -B^{-1}(b - b_0) + X'R^{-1}\,(y - Xb - Za)$$

3. Page 172, top.
   CHANGE: "When B^{-1} implying $B = \infty$ ..."
   TO: "When and if $B^{-1} = 0$ implying $B = \infty$ ..."

4. Page 172,
   CHANGE:
   Finally, add and subtract $\hat{\theta}'\,(W'R^{-1}W + \Sigma)\,\hat{\theta}$ and rearrange to yield
   $$y'R^{-1}y + \left(\theta - \widehat{\theta}\right)'\left(W'R^{-1}W + \Sigma\right)\left(\theta - \widehat{\theta}\right)' - \widehat{\theta}'\left(W'R^{-1}W + \Sigma\right)\widehat{\theta}$$
   $$+\theta_0'\Sigma\theta_0$$

TO:
Finally, add and subtract $\hat{\theta}'\left(W'R^{-1}W+\Sigma\right)\hat{\theta}$ and rearrange to yield

$$y'R^{-1}y+\left(\theta-\widehat{\theta}\right)'\left(W'R^{-1}W+\Sigma\right)\left(\theta-\widehat{\theta}\right)-\widehat{\theta}'\left(W'R^{-1}W+\Sigma\right)\widehat{\theta}$$
$$+\theta_0'\Sigma\theta_0$$

5. Page 172, equation at the bottom,
CHANGE:

$$\ln p\left(\theta|y,\theta_0,B,G,R\right)\propto-\frac{1}{2}\left(\theta-\widehat{\theta}\right)'\left(W'R^{-1}W+\Sigma\right)\left(\theta-\widehat{\theta}\right)'$$

TO:

$$\ln p\left(\theta|y,\theta_0,B,G,R\right)\propto-\frac{1}{2}\left(\theta-\widehat{\theta}\right)'\left(W'R^{-1}W+\Sigma\right)\left(\theta-\widehat{\theta}\right)$$

6. Page 263,
CHANGE,

$$v_\beta^*=v+1,$$

TO:

$$v_\beta^*=v_\beta+1,$$

7. Page 266,
CHANGE:
The maximisation involves the following operations:

$$\begin{aligned}\frac{\partial\left[-\frac{1}{2\sigma_e^2}\left(y-X\alpha-g\right)'\left(y-X\alpha-g\right)-\frac{1}{2}g'G^{-1}g\right]}{\partial\alpha} &= 0,\\ \frac{\partial\left[-\frac{1}{2\sigma_e^2}\left(y-X\alpha-g\right)'\left(y-X\alpha-g\right)-\frac{1}{2}g'G^{-1}g\right]}{\partial g} &= 0,\end{aligned}$$

where $G=X\left(D^{[t]}\right)^{-1}X'$. This yields

$$\left[\begin{array}{ll}Z'Z & Z'\\ I & I+\sigma_e^2G^{-1}\end{array}\right]\left[\begin{array}{l}\alpha^{[t+1]}\\ g^{[t+1]}\end{array}\right]=\left[\begin{array}{c}Z'y\\ y\end{array}\right]. \tag{5.81}$$

TO:
The maximisation involves the following operations:

$$\begin{aligned}\frac{\partial\left[-\frac{1}{2\sigma_e^2}\left(y-Z\alpha-g\right)'\left(y-Z\alpha-g\right)-\frac{1}{2}g'G^{-1}g\right]}{\partial\alpha} &= 0,\\ \frac{\partial\left[-\frac{1}{2\sigma_e^2}\left(y-Z\alpha-g\right)'\left(y-Z\alpha-g\right)-\frac{1}{2}g'G^{-1}g\right]}{\partial g} &= 0,\end{aligned}$$

where $G = X\left(D^{[t]}\right)^{-1}X'$. This yields

$$\begin{bmatrix} Z'Z & Z' \\ Z & I+\sigma_e^2 G^{-1} \end{bmatrix} \begin{bmatrix} \alpha^{[t+1]} \\ g^{[t+1]} \end{bmatrix} = \begin{bmatrix} Z'y \\ y \end{bmatrix}. \tag{5.81}$$

8. Page 266,
   DELETE the following:
   To retrieve marker effects from (5.81) use (5.80) and write

$$\begin{bmatrix} \beta^{[t+1]} \\ g^{[t+1]} \end{bmatrix} \sim SN\left(\begin{bmatrix} 0 \\ 0 \end{bmatrix}, \begin{bmatrix} \left(D^{[t]}\right)^{-1} & \left(D^{[t]}\right)^{-1}X' \\ X\left(D^{[t]}\right)^{-1} & X\left(D^{[t]}\right)^{-1}X' \end{bmatrix}\right).$$

   Then

$$E\left(\beta^{[t+1]}|g^{[t+1]}\right) = \left(D^{[t]}\right)^{-1}X'\left(X\left(D^{[t]}\right)^{-1}X'\right)^{-1}g^{[t+1]}. \tag{5.82}$$

9. Page 353, Eq. (7.41), remove "comma" before "$i = 1, \ldots, m$"
   CHANGE:

$$y|\mu,\alpha,\delta,\sigma^2 \sim N\left(1\mu + \sum\nolimits_{i=1}^{m} X_i\left(\alpha_i\delta_i\right), I\sigma^2\right), \quad , i = 1, \ldots, m \tag{7.41}$$

   TO:

$$y|\mu,\alpha,\delta,\sigma^2 \sim N\left(1\mu + \sum\nolimits_{i=1}^{m} X_i\left(\alpha_i\delta_i\right), I\sigma^2\right), \quad i = 1, \ldots, m \tag{7.41}$$

10. Page 373, paragraph above Eq. (8.23), defines the number of false discoveries $V(A)$, given that k hypotheses are rejected, as binomially distributed $Bi(k, \Pr(H = 0|z \in A)$. Another definition can be found on page 376, paragraph above Eq. (8.33), concerning the expected number of false discoveries. Both may benefit from a little explanation that is provided below.

Background

Let the binary random variable $V_i = 1$ if hypothesis i is rejected and if hypothesis i is a true null; $V_i = 0$, otherwise. Using the notation on page 363, we can write $V_i = I(H_i = 0, R_i = 1)$, where $R_i = 1$ if $z_i \in A$ and z_i is the observed value of the scalar random variable Z_i. Treating the hypotheses as random, it follows that V_i is a Bernoulli random variable with probability $\Pr(H_i = 0, Z_i \in A)$; that is $V_i \sim Br(\Pr(H_i = 0, Z_i \in A)$.

$$V_i \sim Br(\Pr(H_i = 0, Z_i \in A).$$

- **Page 373**. Consider the binary random variable $V_i|R_i = 1$ that takes the value 1 if $H_i = 0$ and 0 otherwise. Then $[V_i|R_i = 1] \sim Br(\Pr(H_i = 0|Z_i \in A)$, a Bernoulli distributed random variable. If in a series of independent trials the total number of rejections is $R = k$, among these k rejections, the total number of false discoveries is binomially distributed:

  $$[V|R = k] \sim Bi(k, \Pr(H = 0|Z \in A).$$

  The expected number of false discoveries among the k rejections is

  $$\mathrm{E}(V|R = k) = k \ \Pr(H = 0|Z \in A).$$

  The subscript i has been omitted because $\Pr(H_i = 0|Z_i \in A)$ is the same for each i.

- **Page 376**. Consider an experiment where m independent hypotheses are tested. Given the definition of V_i and the independence assumption, the total number of false discoveries, $V = \sum_{i=1}^{m} V_i$, is then binomially distributed

  $$V \sim Bi(m, \Pr(H = 0, Z \in A)),$$

  with expected value

  $$\mathrm{E}(V) = m \ \Pr(H = 0, Z \in A)) = m \ \Pr(Z \in A|H = 0)\pi_0,$$

  where $\pi_0 = \Pr(H = 0)$, the prior probability of a true null.

Note that: (i) hypotheses H_i are treated as random (with a common prior π_0), (ii) random vectors (H_i, Z_i), $i = 1, 2, \ldots, m$, are independently distributed, (iii) the rejection region A is data-independent and fixed in advance.