CSE110A: Compilers

April 26, 2024

Topics:

- Syntactic Analysis continued
 - First and follow sets
 - Recursive decent parsing

```
int main() {
  printf("");
  return 0;
}
```

Announcements

- HW 2 is due on **Monday** by midnight
 - Please get started earlier!
 - You have everything you need

- For help
 - Several office hours before due date
 - Ask on Piazza
 - No guaranteed help over the weekend or off business hours
- You do not have to return anything from your parser. Right now it is all about specification. You either match the string or you don't

Announcements

- Autograder should be working well now
 - Thanks to those who have worked with us

- We've added a few test cases to grade scope
 - However designing test cases, asking questions about the grammar is part of compilers
 - Design your own test cases and try them out
 - Fine to discuss individual test cases on piazza or with classmates

Midterm study guide (so far)

Any of the following are fair game. Anything not listed below but in the lectures are fair game. Any combination of topics is fair game. This is only meant to be an overview of what we have discussed so far.

Midterm study guide (so far)

- Regular expressions
 - Operators, how to specify, how match vs full match works
- Scanners
 - What the API is, how strings are tokenized, how to specify tokens, token actions
- Grammars
 - How to specify a grammar, how to identify/avoid ambiguous grammars, how to show a derivation for match, parse trees
 - How to re-write grammars not to be left recursive, how to identify first+ sets
 - How the top down parsing algorithm works, how a recursive decent parser works
- Symbol tables
 - How scope can be tracked and manage during parse time, symbol table specification and implementation
- First 2 classes of module 3

Homework questions?

Quiz

To prepare a grammar for a top-down parser, you must ensure that there is no recursion, except in the right-most element of any production rule.

○ True

○ False

```
root = start symbol;
focus = root;
push (None);
                                  What can go wrong
to match = s.token();
while (true):
  if (focus is a nonterminal)
    pick next rule (A ::= B1,B2,B3...BN);
    push (BN... B3, B2);
    focus = B1
  else if (focus == to match)
    to match = s.token()
    focus = pop()
  else if (to match == None and focus == None)
    Accept
```

Variable	Value
focus	
to_match	
s.istring	
stack	

Can we derive the string (a+b) *c

Expanded Rule	Sentential Form
start	Expr
2	Expr Op Unit
2	Expr Op Unit Op Unit
2	Expr Op Unit Op Unit
2	Expr Op Unit

Infinite recursion!

```
Fee ::= Fee "a"
| "b"
```

What does this grammar describe?

The grammar can be rewritten as

```
Fee ::= Fee "a" Fee2
| "b" Fee2
| Fee2 ::= "a" Fee2
| """
```

In general, A and B can be any sequence of non-terminals and terminals

```
Fee ::= Fee A

| B

Fee ::= B Fee2

| Fee2 ::= A Fee2

| ""
```

Lets do this one as an example:

```
Fee ::= B Fee2

| Fee ::= B Fee2
| Fee2 ::= A Fee2
| ""
```

```
A = ??

B = ??
```

Lets do this one as an example:

Quiz

It is only possible to write a top-down parser if you can determine exactly which production rule to apply at each step.

○ True

○ False

```
root = start symbol;
focus = root;
push (None);
to match = s.token();
                                        Keep track of what
while (true):
                                        choices we've done
  if (focus is a nonterminal)
    cache state();
   pick next rule (A ::= B1,B2,B3...BN);
    if B1 == "": focus=pop(); continue;
    push (BN... B3, B2);
    focus = B1
 else if (to match == None and focus == None)
    Accept
  else if (focus == to match)
    to match = s.token()
    focus = pop()
  else if (we have a cached state)
    backtrack();
  else
    parser error()
```

1:	Expr	::=	ID	Expr2
2:	Expr2	::=	\ +'	Expr2
			// //	

Can we match: "a"?

Expanded Rule	Sentential Form
start	Expr
1	ID Expr2

Quiz

In many cases, a top-down parser requires the grammar to be re-written. Write a few sentences about why this might be an issue when developing a compiler and how the issues might be addressed.

```
A = OP Unit
B = Unit
```

Lets do this one as an example:

Making a backtrack free parser

```
root = start symbol;
focus = root;
push (None);
to match = s.token();
while (true):
  if (focus is a nonterminal)
   pick next rule (A ::= B1,B2,B3...BN);
    if B1 == "": focus=pop(); continue;
    push (BN... B3, B2);
    focus = B1
  else if (focus == to match)
    to match = s.token()
    focus = pop()
  else if (to match == None and focus == None)
    Accept
 Variable
                      Value
 focus
                      Expr2
                      None
 to_match
                      w
 s.istring
```

None

stack

1:	Expr	::=	ID 1	Expr2
2:	Expr2	::=	\+'	Expr2
3:			// //	

Could we make a smarter choice here?

Can we match: "a"?

Expanded Rule	Sentential Form
start	Expr
1	ID <mark>Expr2</mark>

The First Set

For each production choice, find the set of tokens that each production can start with

```
First sets:
                                      1: {}
1: Expr ::= Unit Expr2
2: Expr2 ::= Op Unit Expr2
                                      2: {}
3:
           \\ //
                                      3: {}
4: Unit ::= '(' Expr ')'
5:
                                       5: {}
               ID
                                       6: {}
6: Op ::= '+'
7:
              1 * /
                                      7: {}
```

The First Set

```
For each production choice, find the set of tokens that each production can start with
```

```
First sets:
1: {'(', ID}
2: {'+', '*'}
3: {""}
4: {'(')
5: {ID}
6: {'+'}
7: {'*'}
```

We can use first sets to decide which rule to pick!

```
root = start symbol;
focus = root;
push (None);
to match = s.token();
while (true):
  if (focus is a nonterminal)
    pick next rule (A ::= B1, B2, B3...BN);
    push (BN... B3, B2);
    focus = B1
  else if (focus == to match)
    to match = s.token()
    focus = pop()
  else if (to match == None and focus == None)
   Accept
```

Variable

Value

focus	
to_match	
s.istring	
stack	

```
1: Expr ::= Unit Expr2
2: Expr2 ::= Op Unit Expr2
3:
4: Unit ::= '(' Expr ')'
5: I
            ΙD
6: Op ::= '+'
7: | \*/
First sets:
1: { '(', ID}
2: { '+', '*'}
3: {\"\"}
4: { '(')
5: {ID}
6: { '+' }
7: { \*'}
```

We simply use to_match and compare it to the first sets for each choice

For example, Op and Unit

The Follow Set

Rules with "" in their First set need special attention

We need to find the tokens that any string that follows the production can start with.

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Rules with "" in their First set need special attention

We need to find the tokens that any string that follows the production can start with.

The First+ Set

The First+ set is the combination of First and Follow sets

Do we need backtracking?

The First+ set is the combination of First and Follow sets

For each non-terminal: if every production has a disjoint First+ set then we do not need any backtracking!

Do we need backtracking?

The First+ set is the combination of First and Follow sets

For each non-terminal: if every production has a disjoint First+ set then we do not need any backtracking!

Do we need backtracking?

The First+ set is the combination of First and Follow sets

```
First+ sets:

1: {'(', ID}

2: {'+', '*'}

3: {None, ')'}

4: {'(')}

5: {ID}

6: {'+'}

7: {'*'}
```

These grammars are called LL(1)

- L scanning the input left to right
- L left derivation
- 1 how many look ahead symbols

They are also called predictive grammars

Many programming languages are LL(1)

For each non-terminal: if every production has a disjoint First+ set then we do not need any backtracking!

We cannot select the next rule based on a single look ahead token!

We can refactor

We can refactor

// We will need to compute the follow set

It is not always possible to rewrite grammars into a predictive form, but many programming languages can be.

We can refactor

// We will need to compute the follow set

We now have a full top-down parsing algorithm!

```
root = start symbol;
focus = root;
push (None);
to match = s.token();
while (true):
  if (focus is a nonterminal)
    pick next rule (A ::= B1, B2, B3...BN);
    push (BN... B3, B2);
    focus = B1
  else if (focus == to match)
    to match = s.token()
    focus = pop()
```

```
First+ sets:
1: {'(', ID}
2: {'+', '*'}
3: {None, ')'}
4: {'('}
5: {ID}
6: {'+'}
7: {'*'}
```

First+ sets for each production rule

input grammar, refactored to remove left recursion

```
else if (to_match == None and focus == None)
   Accept
```

To pick the next rule, compare to _match with the possible first+ sets. Pick the rule whose first+ set contains to _match.

If there is no such rule then it is a parsing error.

Moving on to a simpler implementation:

Recursive Descent Parser

How do we parse an Expr?

How do we parse an Expr?
We parse a Unit followed by an Expr2

How do we parse an Expr?
We parse a Unit followed by an Expr2

We can just write exactly that!

```
def parse_Expr(self):
          self.parse_Unit();
          self.parse_Expr2();
          return
```

How do we parse an Expr2?

```
3: ""
4: Unit ::= '(' Expr ')'
5:
              ID
6: Op ::= '+'
First+ sets:
1: {'(', ID}
2: { '+', '*'}
3: {None, ')'}
4: { '(')
5: {ID}
6: { '+'}
7: { '*'}
```

1: Expr ::= Unit Expr2

2: Expr2 ::= Op Unit Expr2

How do we parse an Expr2?

```
1: Expr ::= Unit Expr2
                                                         How do we parse an Expr2?
2: Expr2 ::= Op Unit Expr2
            | \\ //
3:
4: Unit ::= '(' Expr ')'
5:
                  ID
6: Op ::= '+'
                              def parse Expr2(self):
7:
                 \ * /
                                  token id = get token id(self.to match)
                                  # Expr2 ::= Op Unit Expr2
                                  if token id in ["PLUS", "MULT"]:
                                     self.parse Op()
First+ sets:
                                     self.parse Unit()
1: { '(', ID}
                                     self.parse_Expr2()
                                     return
2: { '+', '*'}
                                     # Expr2 ::= ""
3: {None, ')'}
                                  if token_id in [None, "RPAR"]:
4: { '(')
                                     return
5: {ID}
                                  raise ParserException(-1,
                                                                              # line number (for you to do)
6: { \+'}
                                                     self.to_match,
                                                                              # observed token
                                                      ["PLUS", "MULT", "RPAR"])
7: { \*/ }
                                                                              # expected token
```

How do we parse a Unit?

```
First+ sets:
1: {'(', ID}
2: {'+', '*'}
3: {None, ')'}
4: {'(')}
5: {ID}
6: {'+'}
7: {'*'}
```

```
1: Expr ::= Unit Expr2
                                                         How do we parse a Unit?
2: Expr2 ::= Op Unit Expr2
3:
              \\ //
4: Unit ::= '(' Expr ')'
5:
                                     def parse Unit(self):
6: Op
7:
                 1 * /
                                         token id = get token id(self.to match)
                                         # Unit ::= '(' Expr ')'
                                         if token id == "LPAR":
                                            self.eat("LPAR")
                                            self.parse Expr()
First+ sets:
                                            self.eat("RPAR")
1: { '(', ID}
                                            return
2: { '+', '*'}
                                        # Unit :: = ID
                                         if token id == "ID":
3: {None, ')'}
                                            self.eat("ID")
4: { '(')
                                            return
5: {ID}
                                         raise ParserException(-1,
                                                                            # line number (for you to do)
6: { \+'}
                                                            self.to_match,
                                                                            # observed token
7: { \*/ }
                                                            ["LPAR", "ID"])
                                                                            # expected token
```

```
1: Expr ::= Unit Expr2
                                                           How do we parse a Unit?
2: Expr2 ::= Op Unit Expr2
3:
               \\ //
4: Unit ::= '(' Expr ')'
5:
                                     def parse Unit(self):
6: Op
7:
                  1 * /
                                         token id = get token id(self.to match)
                                         # Unit ::= '(' Expr ')'
                                                                         ensure that to_match has token ID of "LPAREN"
                                         if token id == "LPAR":
                                                                         and get the next token
                                            self.eat("LPAR")
                                             self.parse Expr()
First+ sets:
                                            self.eat("RPAR")
1: { '(', ID}
                                            return
2: { '+', '*'}
                                         # Unit :: = ID
                                         if token id == "ID":
3: {None, ')'}
                                             self.eat("ID")
4: { '(')
                                            return
5: {ID}
                                         raise ParserException(-1,
                                                                      # line number (for you to do)
6: { \+'}
                                                             self.to match, # observed token
7: { \*/ }
                                                              ["LPAR", "ID"])
                                                                             # expected token
```

How do we parse an Op?

```
First+ sets:
1: {'(', ID}
2: {'+', '*'}
3: {None, ')'}
4: {'(')}
5: {ID}
6: {'+'}
7: {'*'}
```

```
1: Expr ::= Unit Expr2
                                                       How do we parse an Op?
2: Expr2 ::= Op Unit Expr2
              \\ //
3:
4: Unit ::= '(' Expr ')'
5:
                  ID
6: Op ::= '+'
                                def parse_Op(self):
                                     token id = get token id(self.to match)
                                     # Op ::= '+'
                                     if token id == "PLUS":
First+ sets:
                                        self.eat("PLUS")
                                        return
1: { '(', ID}
2: { '+', '*'}
                                     # Op ::= '*'
                                     if token id == "MULT":
3: {None, ')'}
                                        self.eat("MULT")
4: { '(')
                                        return
5: {ID}
6: { '+'}
                                     raise ParserException(-1, # line number (for you to do)
                                                        self.to_match, # observed token
7: { \*/ }
                                                        ["MULT", "PLUS"]) # expected token
```

Moving on: Scope

Scope

What is scope?

 Can it be determined at compile time? Can it be determined at runtime?

• C vs. Python

Anyone have any interesting scoping rules they know of?

One consideration: Scope

Lexical scope example

```
int x = 0;
int y = 0;
{
  int y = 0;
  x+=1;
  y+=1;
}
x+=1;
y+=1;
What are the final values in x and y?
```

Symbol table object

- two methods:
 - lookup(id): lookup an id in the symbol table.
 Returns None if the id is not in the symbol table.
 - insert(id,info): insert a new id (or overwrite an existing id) into the symbol table along with a set of information about the id.

a very simple programming language

```
ID = [a-z]+
INCREMENT = "\+\+"
INTYPE = "int"
LBRAC = "{"
RBRAC = "}"
SEMI = ";"
```

statements are either a declaration or an increment

a very simple programming language

```
ID = [a-z]+
INCREMENT = "\+\+"

TYPE = "int"

LBRAC = "{"

RBRAC = "}"

SEMI = ";"
int x;

int y;

int y;

x++;

y++;
```

statements are either a declaration or an increment

a very simple programming language

```
ID = [a-z]+
INCREMENT = "\+\+"

TYPE = "int"

LBRAC = "{"

RBRAC = "}"

SEMI = ";"

int x;

{
    int y;
    int y;
```

statements are either a declaration or an increment

• SymbolTable ST;

Say we are matched the statement: int x;

```
declare_statement ::= TYPE ID SEMI
{ }
```

lookup(id) : lookup an id in the symbol table. Returns None if the
id is not in the symbol table.

insert(id,info) : insert a new id (or overwrite an existing id) into
the symbol table along with a set of information about the id.

• SymbolTable ST;

Say we are matched the statement: int x;

```
declare statement ::= TYPE ID SEMI
  self.eat(TYPE)
  variable name = self.to match[1] # lexeme value
  self.eat(ID)
  ST.insert(variable name, None)
  self.eat(SEMI)
```

• SymbolTable ST;

Say we are matched string: x++;

```
inc_statement ::= ID INCREMENT SEMI
{ }
```

lookup(id) : lookup an id in the symbol table. Returns None if the
id is not in the symbol table.

insert(id,info) : insert a new id (or overwrite an existing id) into
the symbol table along with a set of information about the id.

```
• SymbolTable ST;
inc_statement ::= ID INCREMENT SEMI
  variable name = self.to match[1] # lexeme value
  if ST.lookup(variable name) is None:
      raise SymbolTableException(variable name)
  self.eat(ID)
  self.eat(INCREMENT)
  self.eat(SEMI)
```

Say we are matched string: x++;

• SymbolTable ST;

statement : LBRAC statement_list RBRAC

```
int x;
{
    int y;
    x++;
    y++;
}
```

• SymbolTable ST;

statement : LBRAC statement_list RBRAC

start a new scope S

remove the scope S

```
int x;
{
    int y;
    x++;
    y++;
}
```

- Symbol table
- four methods:
 - lookup(id) : lookup an id in the symbol table.

 Returns None if the id is not in the symbol table.
 - insert(id,info): insert a new id into the symbol table along with a set of information about the id.
 - push_scope() : push a new scope to the symbol table
 - pop_scope() : pop a scope from the symbol table

• SymbolTable ST;

statement : LBRAC statement_list RBRAC

You will be adding the functions to push and pop scopes in your homework

- Thoughts? What data structures are good at mapping strings?
- Symbol table
- four methods:
 - lookup(id): lookup an id in the symbol table.
 Returns None if the id is not in the symbol table.
 - insert(id,info): insert a new id into the symbol table along with a set of information about the id.
 - push scope() : push a new scope to the symbol table
 - pop_scope() : pop a scope from the symbol table

Many ways to implement:

A good way is a stack of hash tables:

base scope

HT 0

Many ways to implement:

A good way is a stack of hash tables:

push_scope()

HT 0

Many ways to implement:

A good way is a stack of hash tables:

adds a new Hash Table to the top of the stack

HT 1

push_scope()

HT 0

Many ways to implement:

A good way is a stack of hash tables:

HT 1

insert(id,data)

HT 0

Many ways to implement:

A good way is a stack of hash tables:

insert(id,data)

insert (id -> data) at
top hash table

HT 1

HT 0

Many ways to implement:

A good way is a stack of hash tables:

HT 1

lookup(id)

HT 0

Many ways to implement:

A good way is a stack of hash tables:

check here first

HT 1

lookup(id)

HT 0

Many ways to implement:

A good way is a stack of hash tables:

lookup (id)
then check here

HT 0

Stack of hash tables

Many ways to implement:

A good way is a stack of hash tables:

HT 1

pop_scope()

HT 0

Many ways to implement:

A good way is a stack of hash tables:

HT 0

• Example

```
int x = 0;
int y = 0;
{
  int y = 0;
  x++;
  y++;
}
x++;
y++;
```

HT 0

See you on Friday!

We will discuss parser generators