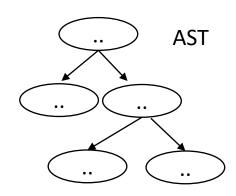
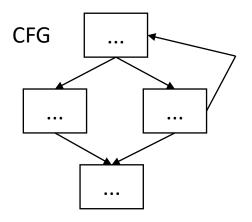
# CSE110A: Compilers

May 3, 2024

#### **Topics**:

- Module 3: Intermediate representations
  - ASTs





#### 3 address code

```
store i32 0, ptr %2
%3 = load i32, ptr %1
%4 = add nsw i32 %3, 1,
store i32 %4, ptr %1
%5 = load i32, ptr %2
```

#### Announcements

- Homeworks
  - HW 1 grades are coming
    - Aiming for Monday
  - HW 3 is out now, along with the grammar
    - Due on May 9
    - Time to study for the midterm
- Midterm will be given on Monday: May 6
  - Taken during class
  - 3 pages of notes are allowed
  - Study:
    - Slides
    - Homeworks
    - book readings

#### Midterm

- Given on Monday
- ~3 questions with multiple parts
- I will not be there
  - Proctored by Rithik and Sakshi and some tutors
- Split between 2 rooms
  - This room + Oakes 106
  - Will get an email about which room you should go to. Based on last name

## Midterm study guide (so far)

Any of the following are fair game. Anything not listed below but in the lectures are fair game. Any combination of topics is fair game. This is only meant to be an overview of what we have discussed so far.

## Midterm study guide (so far)

- Regular expressions
  - Operators, how to specify, how match vs full match works
- Scanners
  - What the API is, how strings are tokenized, how to specify tokens, token actions
- Grammars
  - How to specify a grammar, how to identify/avoid ambiguous grammars, how to show a derivation for match, parse trees
  - How to re-write grammars not to be left recursive, how to identify first+ sets
  - How the top down parsing algorithm works, how a recursive decent parser works
- Symbol tables
  - How scope can be tracked and manage during parse time, symbol table specification and implementation
- No material from Module 3

# Quiz

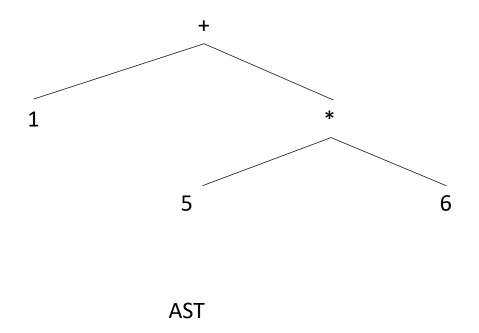
# Quiz

A parse tree is an abstract syntax tree

O True

False

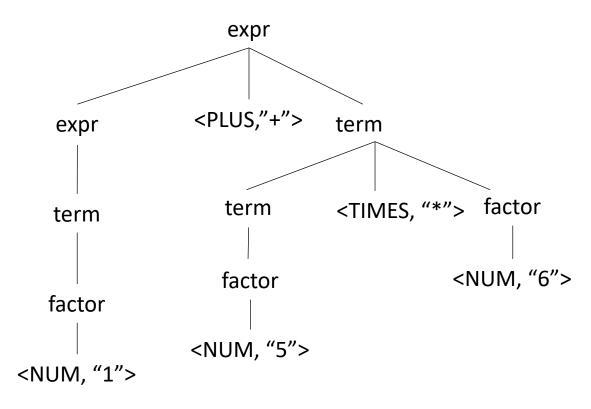
#### What is an AST?



What are some differences?

- disjoint from the grammar
- leaves are data, not lexemes
- nodes are operators, not non-terminals

input: 1+5\*6

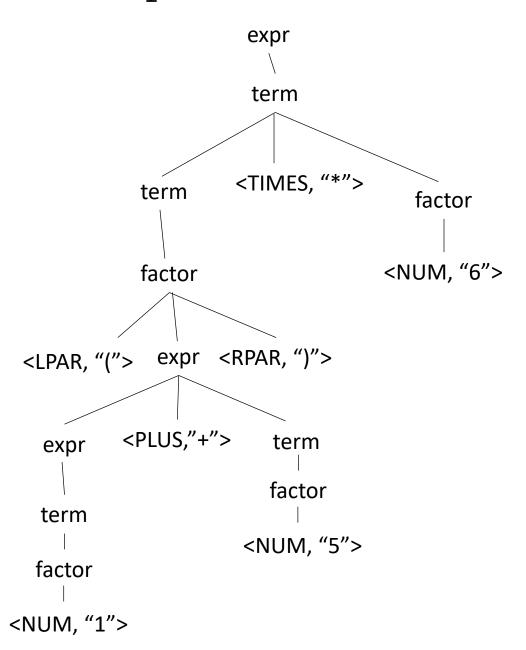


# Example

what happens to ()s in an AST?

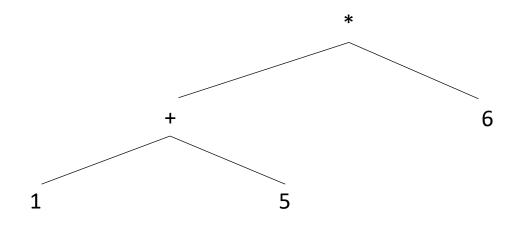
Operator	Name	Productions
+	expr	: expr PLUS term   term
*	term	: term TIMES factor   factor
()	factor	: LPAR expr RPAR   NUM

input: (1+5)\*6



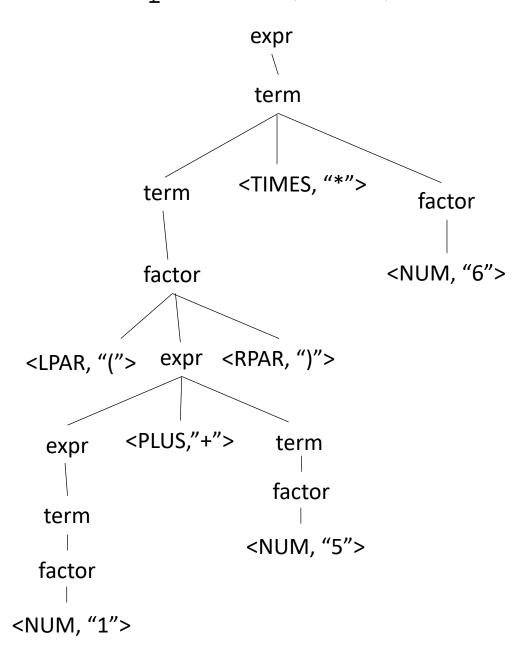
#### Example

what happens to ()s in an AST?



No need for (), they simply encode precedence. And now we have precedence in the AST tree structure

input: (1+5)\*6



#### Quiz

If you are writing a compiler on M languages for N target architectures. How many components (front end or backend) will you need to write with the help of an IR? How about without an IR

_		
	Μ,	N
	1 7 1 ,	IΝ

- MN, M+N
- M+N, MN
- MN, NM
- O M, NM
- $\bigcirc$  M, N + M

# Quiz

Loop unrolling will loop overhead and program code size	
○ increase, increase	
○ increase, reduce	
○ reduce, increase	
○ reduce, reduce	

# Example: loop unrolling

```
for (i = 0; i < 102; i = i++) {
   x = x + 1;
}</pre>
```

#### Quiz

Name and discuss few Intermediate Representations you have seen in real life. If you have not used or seen any, then describe some that you might have been using without knowing.

# **ASTs**

```
class ASTNode():
    def __init__(self):
        pass
```

```
class ASTLeafNode(ASTNode):
    def __init__(self, value):
        self. value = value
class ASTNumNode(ASTLeafNode):
    def __init__(self, value):
        super().__init__(value)
class ASTIDNode(ASTLeafNode):
    def __init__(self, value):
        super().__init__(value)
```

```
class ASTBinOpNode(ASTNode):
    def __init__(self, l_child, r_child):
        self.l_child = l_child
        self.r child = r child
class ASTPlusNode(ASTBinOpNode):
    def __init__(self, l_child, r_child):
        super().__init__(l_child,r_child)
class ASTMultNode(ASTBinOpNode):
    def __init__(self, l_child, r_child):
        super().__init__(l_child,r_child)
```

# Creating an AST from a parser

```
class ASTNode():
    def __init__(self):
        pass
```

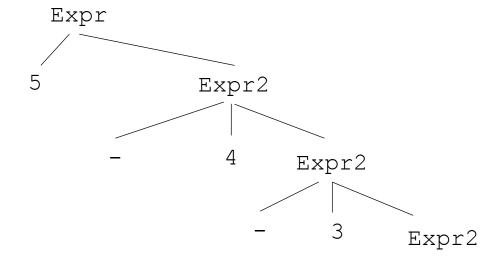
```
class ASTLeafNode(ASTNode):
    def __init__(self, value):
        self. value = value
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```

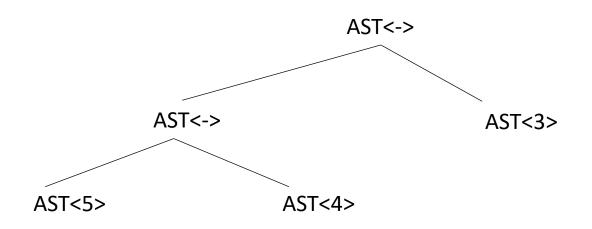
```
class ASTBinOpNode(ASTNode):
    def __init__(self, l_child, r_child):
        self.l_child = l_child
        self.r child = r child
class ASTPlusNode(ASTBinOpNode):
    def __init__(self, l_child, r_child):
        super().__init__(l_child,r_child)
class ASTMultNode(ASTBinOpNode):
    def __init__(self, l_child, r_child):
        super().__init__(l_child,r_child)
```

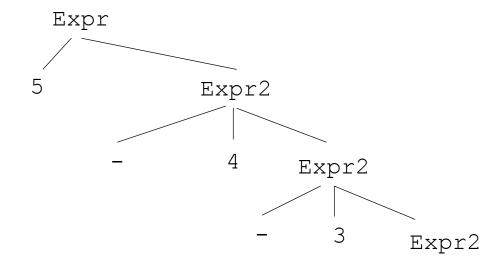
# Creating an AST from production rules

Operator	Name	Productions	Production action
+	expr	: expr PLUS term   term	<pre>{return ASTAddNode(\$1,\$3)} {return \$1}</pre>
*	term	: term TIMES factor   factor	<pre>{return ASTMultNode(\$1,\$3)} {return \$1}</pre>
()	factor	: LPAR expr RPAR   NUM   ID	<pre>{return \$2} {return ASTNumNode(\$1)} {return ASTIDNode(\$1)}</pre>

```
Expr ::= NUM Expr2
Expr2 ::= MINUS NUM Expr2
```



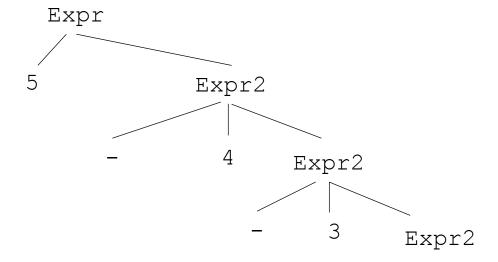




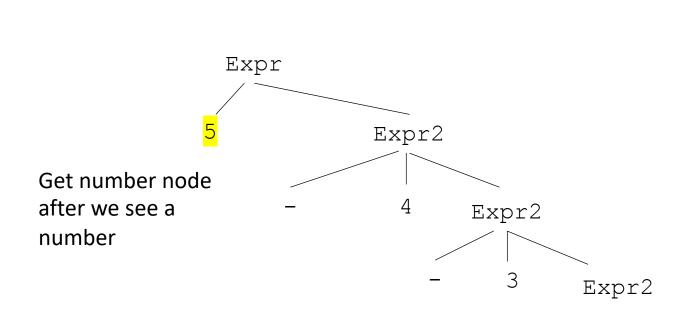
How do we get to the desired parse tree?

```
Expr ::= NUM Expr2
Expr2 ::= MINUS NUM Expr2
```

Keep in mind that because we wrote our own parser, we can inject code at any point during the parse.



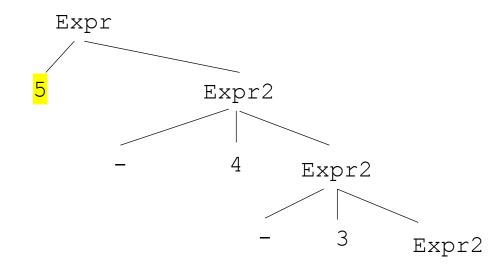
```
Expr ::= NUM Expr2
Expr2 ::= MINUS NUM Expr2
| ""
```



5 - 4 - 3



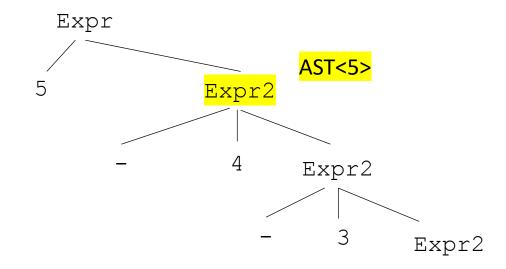
5 - 4 - 3



Pass the node down

```
Expr ::= NUM Expr2
Expr2 ::= MINUS NUM Expr2
```

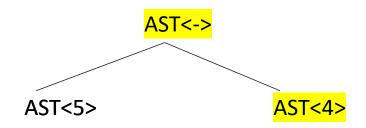
5 - 4 - 3



Pass the node down



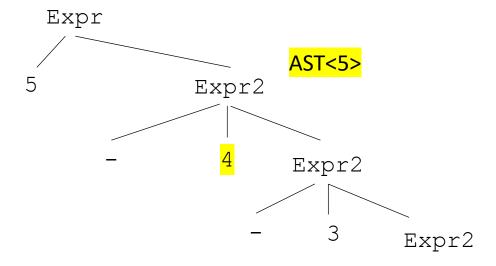
```
Expr ::= NUM Expr2
Expr2 ::= MINUS NUM Expr2
```



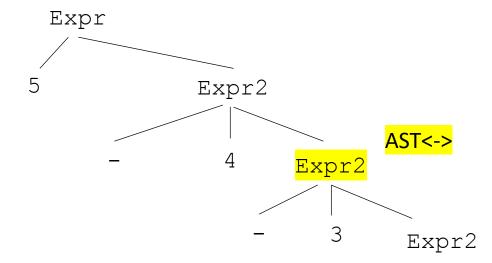
In Expr2, after 4 is parsed, create a number node and

a minus node

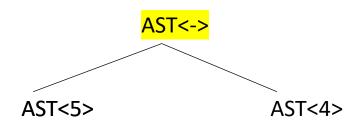




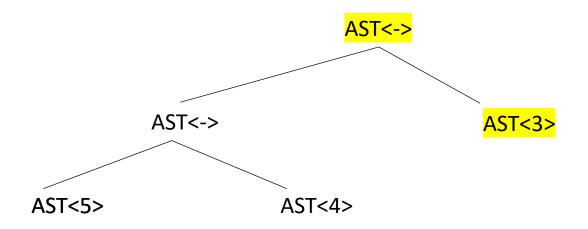
5 - 4 - 3

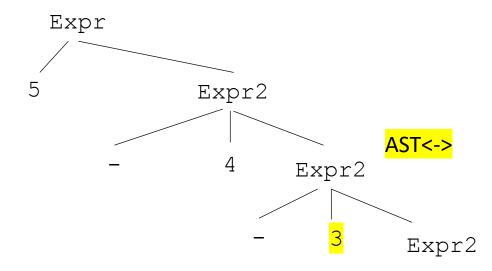


pass the new node down



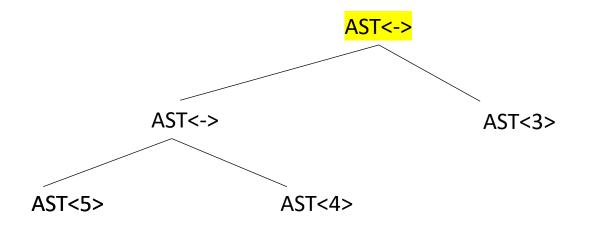
```
Expr ::= NUM Expr2
Expr2 ::= MINUS NUM Expr2
```

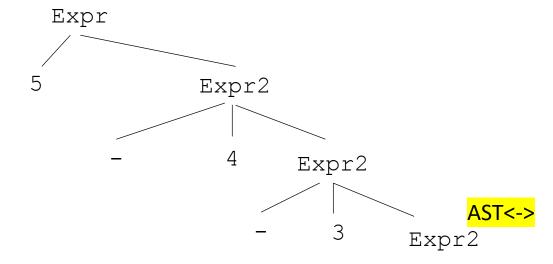




In Expr2, after 3 is parsed, create a number node and a minus node

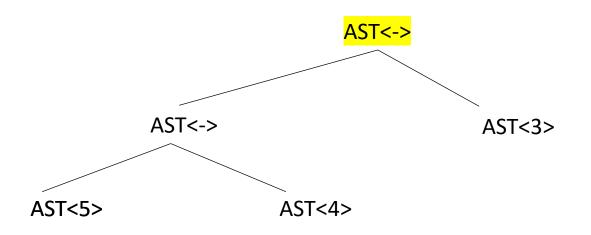
```
Expr ::= NUM Expr2
Expr2 ::= MINUS NUM Expr2
```

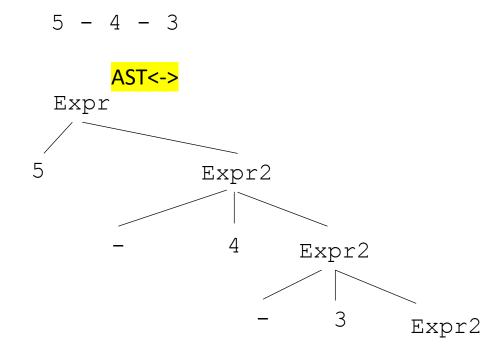




pass down the new node

```
Expr ::= NUM Expr2
Expr2 ::= MINUS NUM Expr2
```





return the node when there is nothing left to parse

```
def parse_expr(self):
    #get the value from the lexeme
    value = self.to_match.value
    node = ASTNumNode(value)
    self.eat("NUM")
    return self.parse_expr2(node)
```

```
def parse_expr(self):
    #get the value from the lexeme
    value = self.to_match.value
    node = ASTNumNode(value)
    self.eat("NUM")
    return self.parse_expr2(node)
```

```
def parse_expr2(self, lhs_node):
    # ... for applying the first production rule
    self.eat("MINUS")
    value = self.to_match.value
    rhs_node = ASTNumNode(value)
    self.eat("NUM")
    node = ASTMinusNode(lhs_node, rhs_node)
    return self.parse_expr2(node)
```

```
def parse_expr(self):
    #get the value from the lexeme
    value = self.to_match.value
    node = ASTNumNode(value)
    self.eat("NUM")
    return self.parse_expr2(node)
```

```
def parse_expr2(self, lhs_node):
    # ... for applying the second production rule
    return lhs_node
```

```
Expr ::= Term Expr2
Expr2 ::= MINUS Term Expr2
| ""
```

In a more realistic grammar, you might have more layers: e.g. a Term

how to adapt?

```
def parse_expr(self):
    #get the value from the lexeme
    value = self.to_match.value
    node = ASTNumNode(value)
    self.eat("NUM")
    return self.parse_expr2(node)
```

```
def parse_expr2(self, lhs_node):
    # ... for applying the first production rule
    self.eat("MINUS")
    value = self.to_match.value
    rhs_node = ASTNumNode(value)
    self.eat("NUM")
    node = ASTMinusNode(lhs_node, rhs_node)
    return self.parse_expr2(node)
```

```
Expr ::= Term Expr2
Expr2 ::= MINUS Term Expr2
| ""
```

```
def parse_expr(self):
    node = self.parse_term()
    return self.parse_expr2(node)
```

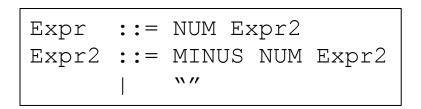
In a more realistic grammar, you might have more layers: e.g. a Term

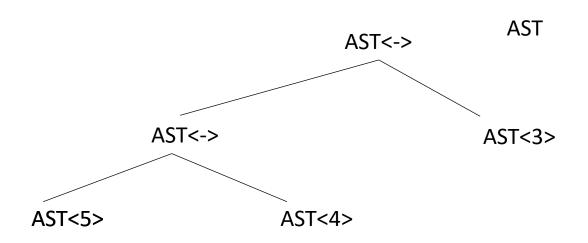
how to adapt?

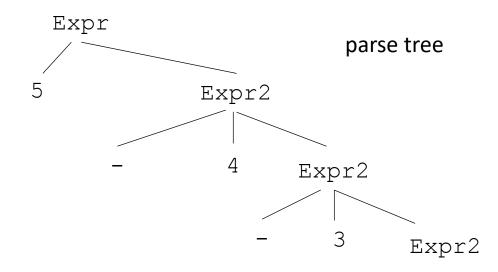
```
def parse_expr2(self, lhs_node):
    # ... for applying the first production rule
    self.eat("MINUS")
    rhs_node = self.parse_term()
    node = ASTMinusNode(lhs_node, rhs_node)
    return self.parse_expr2(node)
```

The parse\_term will figure out how to get you an AST node for that term.

# Evaluate an AST by doing a post order traversal







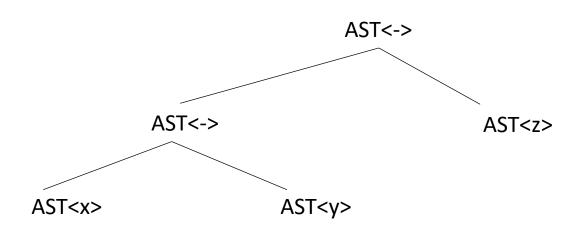
Parse trees cannot always be evaluated in post-order. An AST should always be

## Example

Python AST

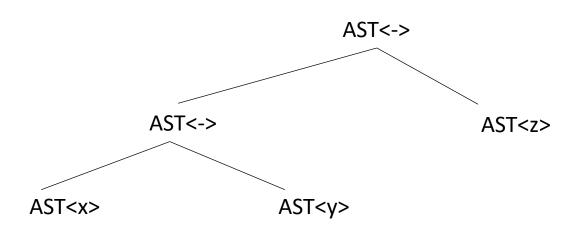
```
import ast
print(ast.dump(ast.parse('5-4-2')))
```

```
Expr(value=BinOp(left=BinOp(left=Num(n=5), op=Sub(), right=Num(n=4)), op=Sub(), right=Num(n=2)))
```



What if you cannot evaluate it? What else might you do?

```
Expr ::= NUM Expr2
Expr2 ::= MINUS NUM Expr2
```



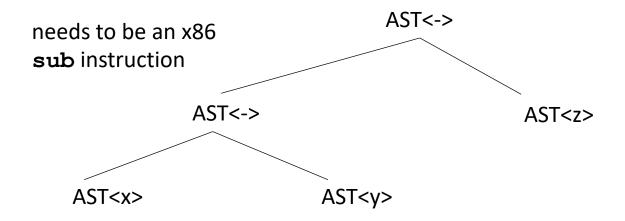
What if you cannot evaluate it? What else might you do?

```
int x;
int y;
float z;
float w;
w = x - y - z
```

How does this change things?

```
Expr ::= NUM Expr2
Expr2 ::= MINUS NUM Expr2
| ""
```

needs to be an x86 **subss** instruction



What if you cannot evaluate it? What else might you do?

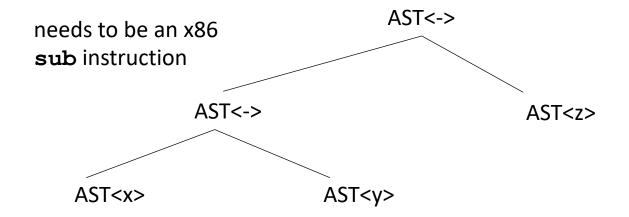
```
int x;
int y;
float z;
float w;
w = x - y - z
```

How does this change things?

Is this all?

```
Expr ::= NUM Expr2
Expr2 ::= MINUS NUM Expr2
```

needs to be an x86 **subss** instruction



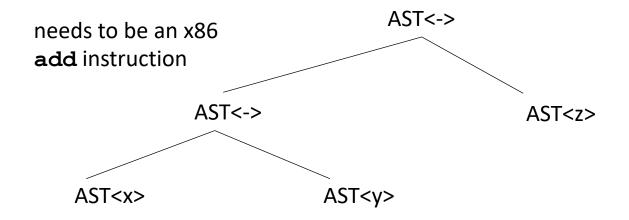
```
int x;
int y;
float z;
float w;
w = x - y - z
```

Lets do some experiments.

What should 5 - 5.0 be?

```
Expr ::= NUM Expr2
Expr2 ::= MINUS NUM Expr2
```

needs to be an x86 addss instruction



Is this all?

```
int x;
int y;
float z;
float w;
w = x - y - z
```

Lets do some experiments.

What should 5 - 5.0 be?

but

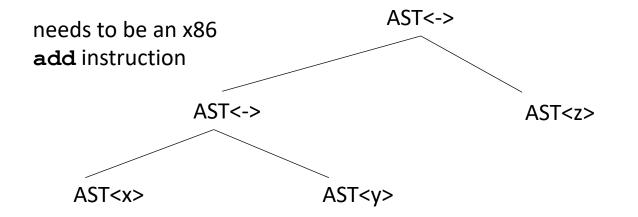
addss r1 r2

interprets both registers as floats

```
Expr ::= NUM Expr2
Expr2 ::= MINUS NUM Expr2
```

```
int x;
int y;
float z;
float w;
w = x - y - z
```

needs to be an x86 addss instruction



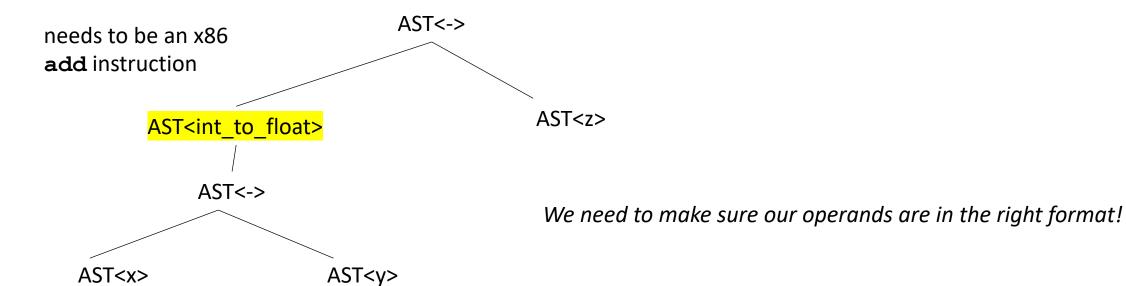
But the binary of 5 is 0b101 the float value of 0b101 is 7.00649232162e-45

We cannot just subtract them!

```
Expr ::= NUM Expr2
Expr2 ::= MINUS NUM Expr2
```

```
int x;
int y;
float z;
float w;
w = x - y - z
```

needs to be an x86 addss instruction



- Given a language a type system defines:
  - The primitive (base) types in the language
  - How the types can be converted to other types
    - implicitly or explicitly
  - How the user can define new types

## Type checking and inference

Check a program to ensure that it adheres to the type system

Especially interesting for compilers as a program given in the type system for the input language must be translated to a type system for lower-level program

- Different types of Type Systems for languages:
  - statically typed: types can be determined at compile time
  - dynamically typed: types are determined at runtime
  - untyped: the language has no types
- What are examples of each?
- What are pros and cons of each?

- Different types of Type Systems for languages:
  - statically typed: types can be determined at compile time
  - dynamically typed: types are determined at runtime
  - untyped: the language has no types
- What are examples of each?
- What are pros and cons of each?

do type conversion at compile time otherwise you have to check without static types, this would need to be translated to:

x + y

```
if type(x) == int and type(y) == int:
   add(x,y)

if type(x) == int and type(y) == float:
   addss(int_to_float(x), y)

if ...
```

- Different types of Type Systems for languages:
  - statically typed: types can be determined at compile time
  - **dynamically typed**: types are determined at runtime
  - untyped: the language has no types
- What are examples of each?
- What are pros and cons of each?

Can write more generic code

```
def add(x,y):
    return x + y
```

You would need to write many different functions for each type

- Different types of Type Systems for languages:
  - statically typed: types can be determined at compile time
  - dynamically typed: types are determined at runtime
  - untyped: the language has no types
- What are examples of each?
- What are pros and cons of each?

Very close to assembly. You can write really optimized code. But very painful

**Considerations:** 

#### **Considerations:**

- Base types:
  - ints
  - chars
  - strings
  - floats
  - bool
- How to combine types in expressions:
  - int and float?
  - int and char?
  - int and bool?

#### **Considerations:**

- Base types:
  - ints
  - chars
  - strings
  - floats
  - bool
- How to combine types in expressions:
  - int and float?
  - int and char?
  - int and bool?

#### **Considerations:**

- Base types:
  - ints
  - chars
  - strings
  - floats
  - bool
- How to combine types in expressions:
  - int and float?
  - int and char?
  - int and bool?

What do each of these do if they are +'ed together?

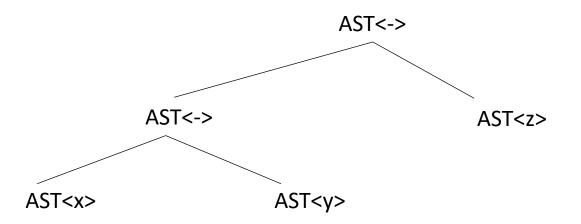
# Type checking

#### Two components

- Type inference
  - Determines a type for each AST node
  - Modifies the AST into a type-safe form
- Catches type-related errors

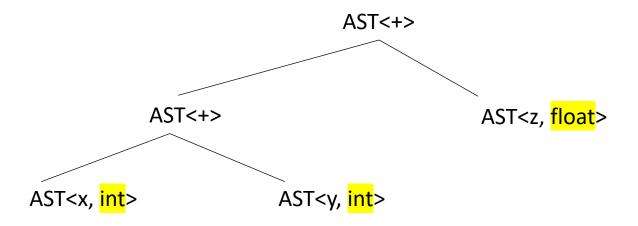
```
int x;
int y;
float z;
float w;
w = x + y + z
```

each node additionally gets a type



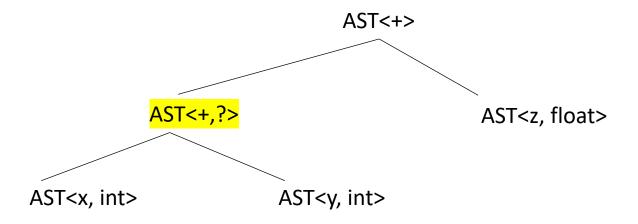
```
int x;
int y;
float z;
float w;
w = x + y + z
```

each node additionally gets a type we can get this from the symbol table for the leaves or based on the input (e.g. 5 vs 5.0)



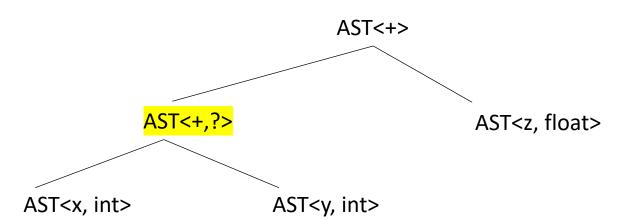
```
int x;
int y;
float z;
float w;
w = x + y + z
```

How do we get the type for this one?



```
int x;
int y;
float z;
float w;
w = x + y + z
```

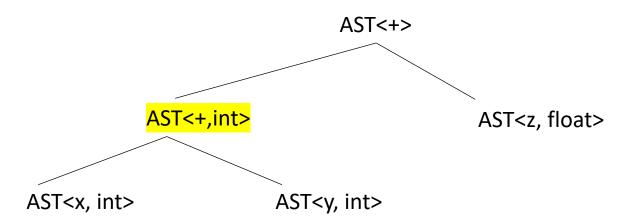
How do we get the type for this one?



first	second	result
int	int	int
int	float	float
float	int	float
float	float	float

```
int x;
int y;
float z;
float w;
w = x + y + z
```

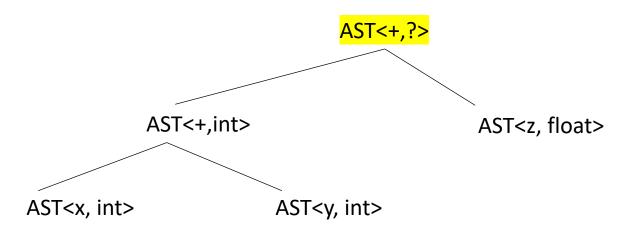
How do we get the type for this one?



first	second	result
int	int	<mark>int</mark>
int	float	float
float	int	float
float	float	float

```
int x;
int y;
float z;
float w;
w = x + y + z
```

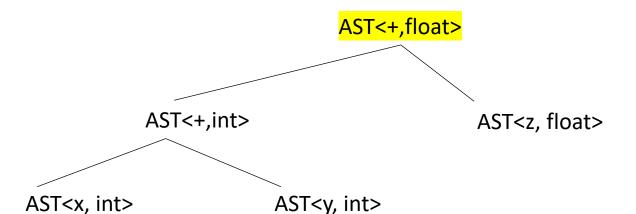
How do we get the type for this one?



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int	int	int
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float	int	float
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int x;
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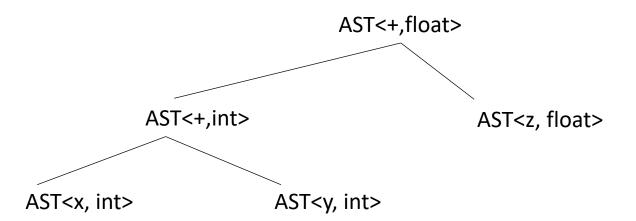
How do we get the type for this one?



first	second	result
int	int	int
int	float	float
float	int	float
float	float	float

```
int x;
int y;
float z;
float w;
w = x + y + z
```

How do we get the type for this one?



inference rules for addition:

first	second	result
int	int	int
int	float	float
float	int	float
float	float	float

what else?

```
int x;
int y;
float z;
float w;
w = x + y + z
```

How do we get the type for this one?

# AST<+,float> AST<int\_to\_float,?> AST<+,int> AST<y, int> AST<+,float>

inference rules for addition:

first	second	result
int	int	int
int	float	float
float	int	float
float	float	float

what else? need to convert the int to a float

```
class ASTNode():
    def __init__(self):
        pass
```

```
class ASTLeafNode(ASTNode):
    def __init__(self, value):
        self. value = value
class ASTNumNode(ASTLeafNode):
    def __init__(self, value):
        super().__init__(value)
class ASTIDNode(ASTLeafNode):
    def __init__(self, value):
        super().__init__(value)
```

```
class ASTBinOpNode(ASTNode):
    def __init__(self, l_child, r_child):
        self.l_child = l_child
        self.r child = r child
class ASTPlusNode(ASTBinOpNode):
    def __init__(self, l_child, r_child):
        super().__init__(l_child,r_child)
class ASTMultNode(ASTBinOpNode):
    def __init__(self, l_child, r_child):
        super().__init__(l_child,r_child)
```

```
from enum import Enum

class Types(Enum):
    INT = 1
    FLOAT = 2
```

#### Our base AST Node needs a type

```
class ASTNode():
    def __init__(self):
        self.node_type = None
    pass

def set_type(self, t):
        self.node_type = t

def get_type(self):
    return self.node_type
```

Now we need to set the types for the leaf nodes

```
from enum import Enum

class Types(Enum):
    INT = 1
    FLOAT = 2
```

#### Our base AST Node needs a type

```
class ASTNode():
    def __init__(self):
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    pass

def set_type(self, t):
        self.node_type = t

def get_type(self):
    return self.node_type
```

#### Now we need to set the types for the leaf nodes

```
class ASTNumNode(ASTLeafNode):
    def __init__(self, value):
        super().__init__(value)
        if is_int(value):
            self.set_type(Types.INT)
        else:
        self.set_type(Types.FLOAT)
```

```
from enum import Enum

class Types(Enum):
    INT = 1
    FLOAT = 2
```

#### Our base AST Node needs a type

```
class ASTNode():
    def __init__(self):
        self.node_type = None
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```

Now we need to set the types for the leaf nodes

```
class ASTNumNode(ASTLeafNode):
    def __init__(self, value):
        super().__init__(value)
    if is_int(value):
        self.set_type(Types.INT)
    else:
        self.set_type(Types.FLOAT)
```

```
class ASTIDNode(ASTLeafNode):
    def __init__(self, value, value_type):
        super().__init__(value)
        self.set_type(value_type)
```

Where can we get the value type for an ID?

## Symbol Table

Say we are matched the statement: int x;

```
• SymbolTable ST;
              (TYPE, 'int') (ID, 'x')
declare statement ::= TYPE ID SEMI
  eat (TYPE)
  id name = self.to match.value
  eat(ID)
  ST.insert(id name, None)
  eat (SEMI)
```

in homework 2 and 3 we didn't record any information in the symbol table

# Symbol Table

Say we are matched the statement: int x;

```
• SymbolTable ST;
                (TYPE, 'int') (ID, 'x')
declare statement ::= TYPE ID SEMI
                                                   previously we weren't saving any
  value type = self.to match.value
                                                   information about the ID
  eat (TYPE)
  id name = self.to match.value
  eat(ID)
                                                   record the type in the symbol table
  ST.insert(id name, value type)
  eat (SEMI)
```

```
from enum import Enum

class Types(Enum):
    INT = 1
    FLOAT = 2
```

#### Our base AST Node needs a type

```
class ASTNode():
    def __init__(self):
        self.node_type = None
    pass

def set_type(self, t):
        self.node_type = t

def get_type(self):
    return self.node_type
```

Now we need to set the types for the leaf nodes

```
class ASTNumNode(ASTLeafNode):
    def __init__(self, value):
        super().__init__(value)
    if is_int(value):
        self.set_type(Types.INT)
    else:
        self.set_type(Types.FLOAT)
```

```
class ASTIDNode(ASTLeafNode):
    def __init__(self, value, value_type):
        super().__init__(value)
        self.set_type(value_type)
```

Where can we get the value type for an ID?

But that doesn't get us here yet...

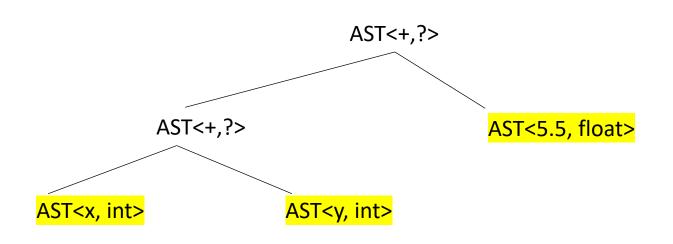
## add the type at parse time

```
Unit ::= ID | NUM
```

```
def parse_unit(self, lhs_node):
    # ... for applying the first production rule (ID)
    value = self.next_word.value
    # ... Check that value is in the symbol table
    node = ASTIDNode(value, ST[value])
    return node
```

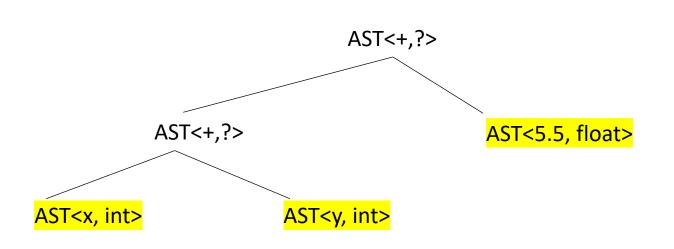
# Type inference

We now have the types for the leaf nodes



```
int x;
int y;
float w;
w = x + y + 5.5
```

We now have the types for the leaf nodes



Next steps:

we do a post order traversal on the AST and do a type inference

def type\_inference(n): Given a node n: find its type and the types of any of its children

```
def type_inference(n):
   case split on n:
   if n is a leaf node:
     return n.get_type()
   if n is a plus node:
     ...
```

Given a node n: find its type and the types of any of its children

```
def type_inference(n):
                                 Given a node n: find its type and the types of any of its children
 case split on n:
 if n is a leaf node:
   return n.get_type()
                              lookup the rule for plus
 if n is a plus node:
    return lookup type from table
```

#### inference rules for plus

left	right	result
int	int	int
int	float	float
float	int	float
float	float	float

```
def type_inference(n):
                                 Given a node n: find its type and the types of any of its children
 case split on n:
 if n is a leaf node:
   return n.get_type()
                              lookup the rule for plus
 if n is a plus node:
    return lookup type from table
```

#### inference rules for plus

left	right	result
int	int	int
int	float	float
float	int	float
float	float	float

but we're missing a few things

```
def type_inference(n):
                                 Given a node n: find its type and the types of any of its children
 case split on n:
 if n is a leaf node:
                                we need to make sure the
   return n.get_type()
                                children have types!
 if n is a plus node:
     do type inference on children
     return lookup type from table
```

#### inference rules for plus

left	right	result
int	int	int
int	float	float
float	int	float
float	float	float

```
def type_inference(n):
                                Given a node n: find its type and the types of any of its children
 case split on n:
 if n is a leaf node:
                                we should record our type
   return n.get type()
 if n is a plus node:
    do type inference on children
    t = lookup type from table
    set n type to t
    return t
```

#### inference rules for plus

left	right	result
int	int	int
int	float	float
float	int	float
float	float	float

```
def type_inference(n):
                               Given a node n: find its type and the types of any of its children
 case split on n:
 if n is a leaf node:
   return n.get type()
 do type inference on children
 if n is a plus node:
    t = lookup type from table
    set n type to t
    return t
```

is this just for plus?

left	right	result
int	int	int
int	float	float
float	int	float
float	float	float

```
def type_inference(n):
                                Given a node n: find its type and the types of any of its children
 case split on n:
                                      is this just for plus?
 if n is a leaf node:
   return n.get type()
 if n is a plus node:
    do type inference on children
    t = lookup type from table
    set n type to t
    return t
```

most language promote types, e.g. ints to float for expression operators

left	right	result
int	int	int
int	float	float
float	int	float
float	float	float

```
def type_inference(n):
                                Given a node n: find its type and the types of any of its children
 case split on n:
                                      is this just for plus?
 if n is a leaf node:
   return n.get type()
 if n is a bin op node:
    do type inference on children
    t = lookup type from table
    set n type to t
    return t
```

most language promote types, e.g. ints to float for expression operators

left	right	result
int	int	int
int	float	float
float	int	float
float	float	float

```
def type_inference(n):
    case split on n:
    if n is a leaf node:
        return n.get_type()

    if n is a bin op node:
        do type inference on children
        t = lookup type from table
        set n type to t
        return t
```

#### What about for assignments?

```
int x; cout << (x = 5.5) << endl;
```

#### What does this return?

left	right	result
int	int	int
int	float	float
float	int	float
float	float	float

```
def type_inference(n):
 case split on n:
 if n is a leaf node:
   return n.get type()
 if n is a bin op node:
    do type inference on children
    t = lookup type from table
    set n type to t
    return t
```

#### What about for assignments?

```
int x; cout << (x = 5.5) << endl;
```

#### What does this return?

left	right	result
int	int	<mark>int</mark>
int	float	<mark>int</mark>
float	int	float
float	float	float

#### whatever the left is

```
def type_inference(n):
 case split on n:
 if n is a leaf node:
   return n.get_type()
 if n is an assignment:
   . . . .
 if n is a bin op node:
    . . .
```

#### What about for assignments?

```
int x; cout << (x = 5.5) << endl;
```

#### What does this return?

left	right	result
int	int	<mark>int</mark>
int	float	<mark>int</mark>
float	int	float
float	float	float

#### whatever the left is

#### Good luck with the test!

• Study for the test!