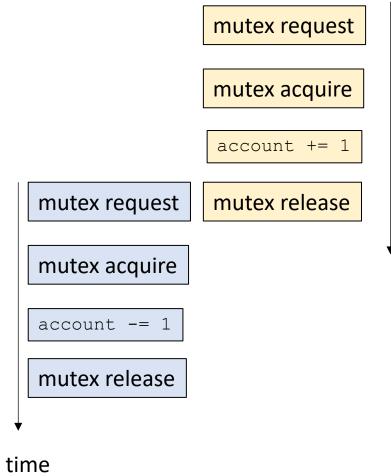
CSE113: Parallel Programming

Jan. 29, 2024

• Topics:

- Intro to mutual exclusion
 - Different types of parallelism
 - Data conflicts
 - Protecting shared data



time

Second lecture in Module 2: mutexes!

Last chance to turn in HW 1 is tomorrow at midnight

 HW 2 will be assigned by tomorrow at midnight. You'll have what you need to complete part 1 by end of today.

No guarantee of homework help after 5 PM

- Homework 1 notes:
 - No assigned speedup required. However, you should get a noticeable speedup from ILP
 - You can start to share timing results on your personal machines. Everyone's results will be slightly different
 - Sometimes you cannot account for small differences
 - Run your code for more iterations and take an average
 - Part 1 and Part 2 notes

• As always, we have regularly scheduled office hours and piazza

- Midterm is in 2 weeks
 - In-person test
 - 3 pages of notes front and back (but no memorization questions)
 - 10% of your grade

Previous quiz

Previous quiz

It is possible to interleave the load and store operations of RMW atomic operations; however, it is so rare that it does not matter in practice.

Mutex alternatives?

Other ways to implement accounts?

Atomic Read-modify-write (RMWs): primitive instructions that implement a read event, modify event, and write event indivisibly, i.e. it cannot be interleaved.

```
atomic_fetch_add(atomic_int * addr, int value) {
  int tmp = *addr; // read
  tmp += value; // modify
  *addr = tmp; // write
}
```

other operations: max, min, etc.

Modify these programs to use atomic RMWs

Tyler's coffee addiction:

<u>Tyler's employer</u>

atomic_fetch_add(&tylers_account, -1);

atomic_fetch_add(&tylers_account, 1);

time

time

Modify these programs to use atomic RMWs

Tyler's coffee addiction:

Tyler's employer

atomic_fetch_add(&tylers_account, -1);

```
atomic_fetch_add(&tylers_account, 1);
```

```
atomic_fetch_add(&tylers_account, -1);
```

time

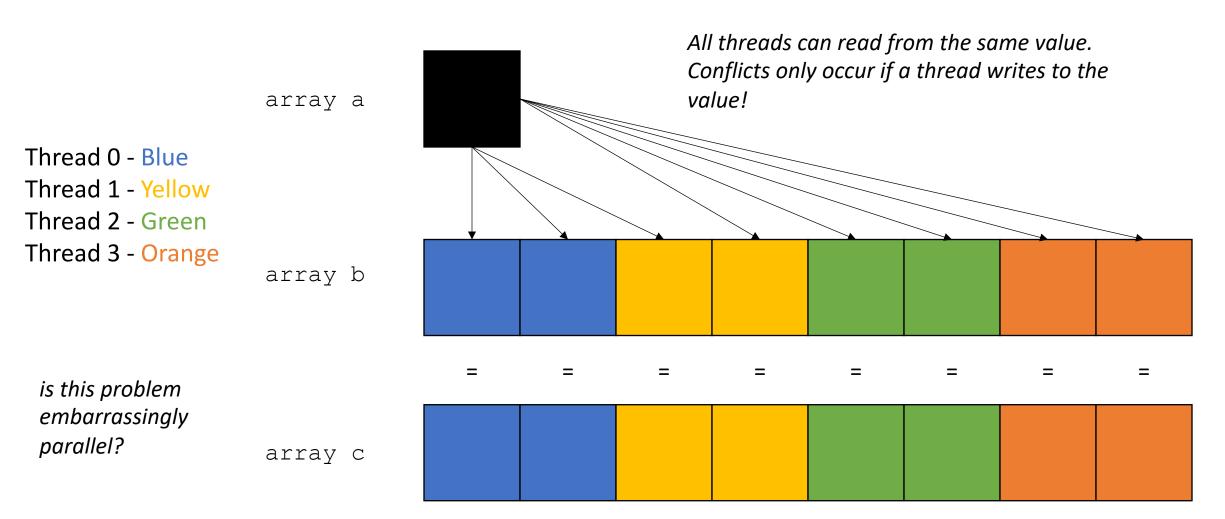
```
atomic_fetch_add(&tylers_account, 1);
```

time

Previous quiz

A data conflict is when two threads access the same memory location.

Embarrassingly parallel



Embarrassingly parallel

Note: Reductions have some parallelism in them, as seen in your homework.

Thread 0 - Blue

Thread 1 - Yellow

n

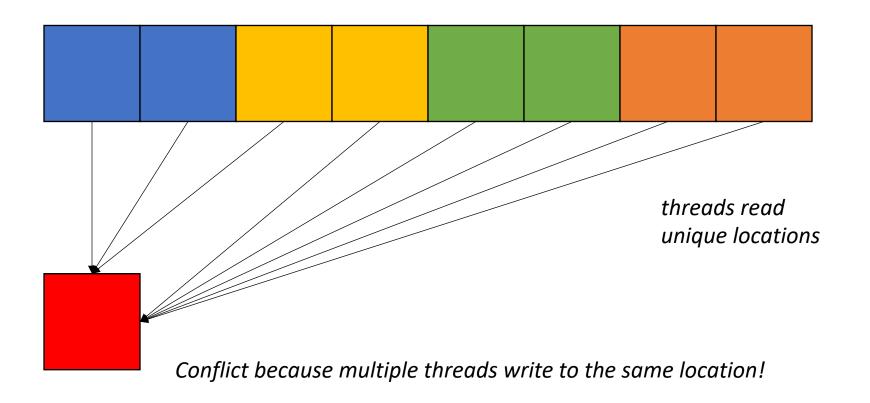
Thread 2 - Green

Thread 3 - Orange

is this problem embarrassingly parallel?

array c

array b



Previous quiz

How many interleavings are possible with 3 threads, each them executing 1 event?

 \bigcirc 1

○ 3

 \bigcirc 6

O 12

Previous quiz

How many extra arguments are required to turn a function into an SPMD function?

- \bigcirc 0
- \bigcirc 1
- \bigcirc 2
- 3

```
void increment_array(int *a, int a_size, int tid, int num_threads) {
    for (int i = tid; i < a_size; i+=num_threads) {
        a[i]++;
    }
}</pre>
```

iterations computed by thread 1



array a

switch to thread 1

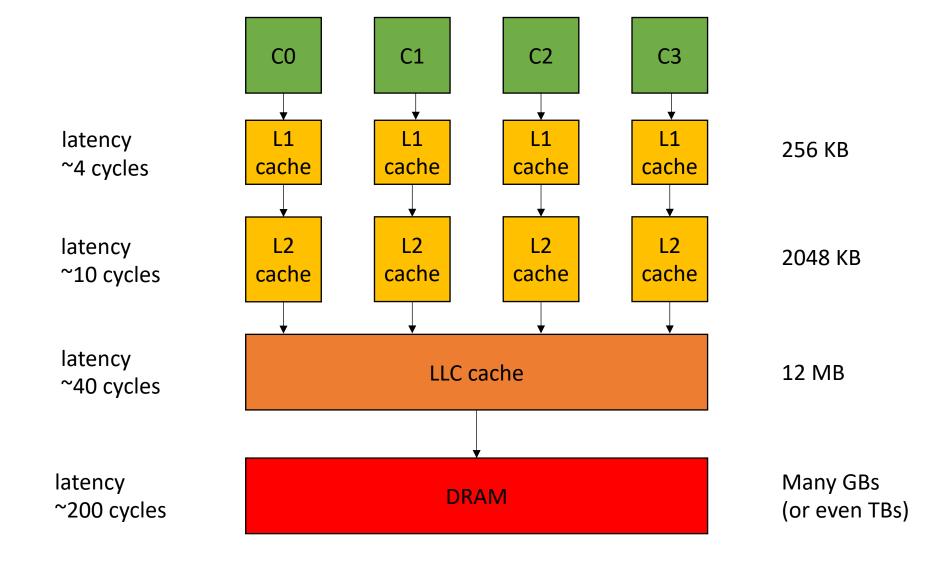
```
Assume 2 threads
lets step through thread 1
i.e.
tid = 1
num_threads = 2
```

Previous quiz

Write a few sentences about how you can remove data-conflicts from your program. We have mentioned a few ways in class, but feel free to mention other ways you can think of!

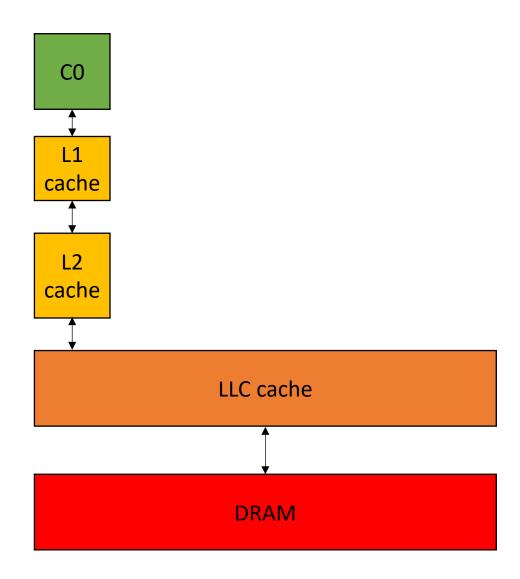
Review

Caches

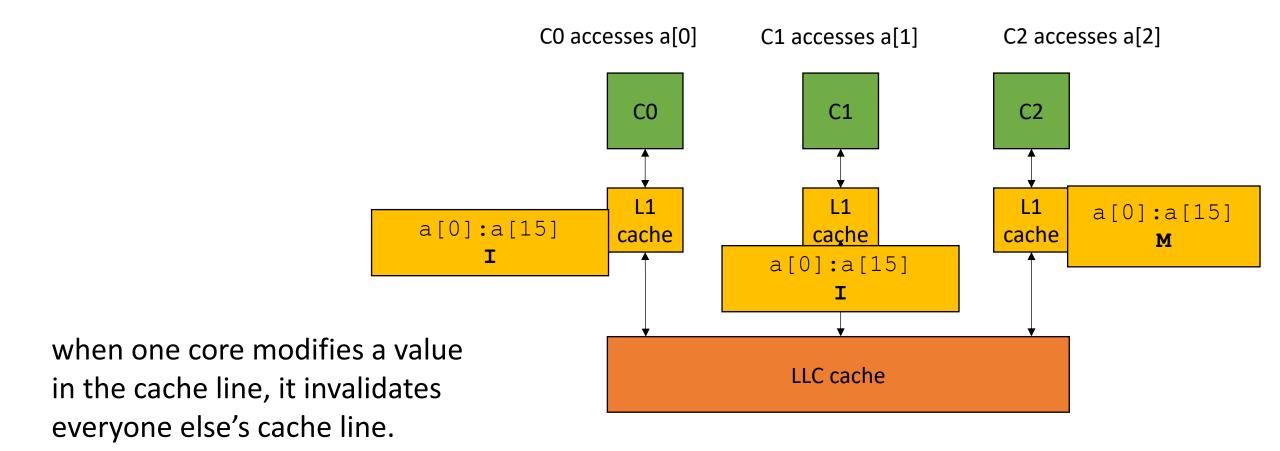


Caches

```
int increment(int *a) {
   a[0]++;
%5 = load i32, i32* %4
                             4 cycles
\%6 = add nsw i32 \%5, 1
                             1 cycles
store i32 %6, i32* %4
                             4 cycles
                             9 cycles!
```



Cache Coherence and False Sharing

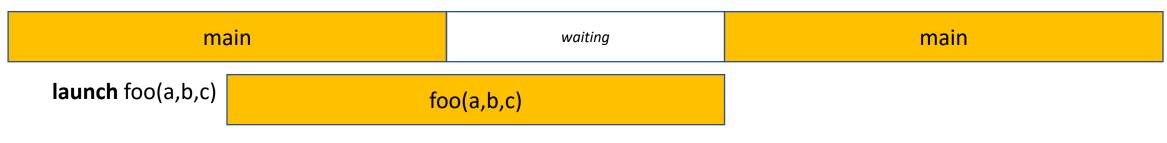


This is called *False Sharing*

```
#include <thread>
using namespace std;
void foo(int a, int b, int c) {
 // some foo code
int main() {
  // some main code
  thread thread handle (foo, 1, 2, 3);
  // code here runs concurrently with foo
  thread handle.join();
  return 0;
```

main waits for foo. called **join()**

join() returns in main



foo finishes

```
#include <thread>
#include <iostream>
using namespace std;
void foo(int a, int b, int *c) {
  // return a + b;
  *c = a + b;
int main() {
  // some main code
  int ret = 0;
  thread thread handle (foo, 1, 2, &ret);
  // code here runs concurrently with foo
  cout << ret << endl;</pre>
  thread handle.join();
  return 0;
```

What if....

• Same program, multiple data

 Main idea: many threads execute the same function, but they operate on different data.

- How do they get different data?
 - each thread can access their own thread id, a contiguous integer starting at 0 up to the number of threads

```
void increment_array(int *a, int a_size, int tid, int num_threads) {
    for (int i = tid; i < a_size; i+=num_threads) {
        a[i]++;
    }
}</pre>
```

iterations computed by thread 1



array a

switch to thread 1

```
Assume 2 threads
lets step through thread 1
i.e.
tid = 1
num_threads = 2
```

```
void increment array(int *a, int a size, int tid, int num threads);
#define THREADS 8
#define A SIZE 1024
int main() {
  int *a = new int[A SIZE];
 // initialize a
 thread thread ar[THREADS];
  for (int i = 0; i < THREADS; i++) {
   thread ar[i] = thread(increment array, a, A SIZE, i, THREADS);
  for (int i = 0; i < THREADS; i++) {
   thread ar[i].join();
  delete[] a;
  return 0;
```

New material

Three properties

Mutual exclusion - Only 1 thread can hold the mutex at a time.
 Critical sections cannot interleave

Other threads are allowed to request, but not acquire until the thread that has acquired the mutex releases it.

concurrent execution



mutex request

mutex acquire

Three properties

Mutual exclusion - Only 1 thread can hold the mutex at a time.
 Critical sections cannot interleave

Other threads are allowed to request, but not acquire until the thread that has acquired the mutex releases it.



Three properties

 Deadlock Freedom - If a thread has requested the mutex, and no thread currently holds the mutex, the mutex must be acquired by one of the requesting threads



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> Program cannot hang here Either thread 0 or thread 1 must acquire the mutex



Three properties

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Three properties

 Deadlock Freedom - If a thread has requested the mutex, and no thread currently holds the mutex, the mutex must be acquired by one of the requesting threads

> Program cannot hang here Either thread 0 or thread 1 must acquire the mutex



Three properties

• **Starvation Freedom** (*Optional*) - A thread that requests the mutex must eventually obtain the mutex.

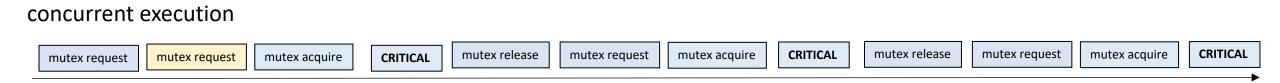
Thread 1 (yellow) requests the mutex but never gets it

Concurrent execution mutex request mutex request mutex acquire critical mutex release mutex request mutex acquire critical mutex request mute

Three properties

• Starvation Freedom (Optional) - A thread that requests the mutex must eventually obtain the mutex.

Thread 1 (yellow) requests the mutex but never gets it



Recap: three properties

 Mutual Exclusion: Two threads cannot be in the critical section at the same time

- Deadlock Freedom: If a thread has requested the mutex, and no thread currently holds the mutex, the mutex must be acquired by one of the requesting threads
- Starvation Freedom (optional): A thread that requests the mutex must eventually obtain the mutex.

Building blocks

- Memory reads and memory writes
 - later: read-modify-writes
- We need to guarantee that our reads and writes actually go to memory.
 - And other properties we will see soon
- To do this, we will use C++ atomic operations

A historical perspective

- Adding concurrency support to a programming language is hard!
- The memory model defines how threads can safely share memory
- Java tried to do this,

wikipedia

The original Java memory model, developed in 1995, was widely perceived as broken, preventing many runtime optimizations and not providing strong enough guarantees for code safety. It was updated through the Java Community Process, as Java Specification Request 133 (JSR-133), which took effect in 2004, for Tiger (Java 5.0).^{[1][2]}

Brian Goetz (2019)

It is worth noting that broken techniques like double-checked locking are still broken under the new memory model, a

A historical perspective

• How is C++?

- Has issues (imprecise, not modular)
 - but at least considered safe
 - Specification makes it difficult to reason about all programs
 - Open problem!
- Luckily mutexes (and their implementations) avoid the problematic areas of the language!

Our primitive instructions

Types: atomic_int

- Interface (C++ provides overloaded operators):
 - load
 - store

- Properties:
 - loads and stores will always go to memory.
 - compiler memory fence
 - hardware memory fence

loads and stores will always go to memory

• Compiler example, performance difference

loads and stores will always go to memory

• Compiler example, performance difference

```
int foo(int x) {
    x = 0;
    for (int i = 0; i < 2048; i++) {
        x++;
    }
    return x;
}</pre>
```

```
int foo(atomic x) {
    x.store(0);
    for (int i = 0; i < 2048; i++) {
        int tmp = x.load();
        tmp++;
        x.store(tmp);
    }
    return x.load();
}</pre>
```

loads and stores will always go to memory

• Compiler example, performance difference

- Compiler makes reasoning about parallel code hard, but big performance improvements for sequential code:
 - O(ITERS) vs. O(1)

Compiler Fence

- Compiler can be aggressive with memory operations:
 - For non-atomic memory locations, the following optimizations are valid

Compiler Fence

- Compiler can be aggressive with memory operations:
 - For non-atomic memory locations, the following optimizations are valid

```
a[i] = 0;
a[i] = 1;
```

can be optimized to:

```
a[i] = 1;
```

Compiler Fence

a[i] = 1;

- Compiler can be aggressive with memory operations:
 - For non-atomic memory locations, the following optimizations are valid

x = a[i];

x2 = x;

```
a[i] = 0; x = a[i]; x2 = a[i]; can be optimized to: can be optimized to:
```

Compiler Fence

- Compiler can be aggressive with memory operations:
 - For non-atomic memory locations, the following optimizations are valid

```
a[i] = 0;
a[i] = 1;
```

can be optimized to:

```
a[i] = 1;
```

$$x = a[i];$$

 $x2 = a[i];$

can be optimized to:

$$x = a[i];$$

 $x2 = x;$

$$a[i] = 6;$$

 $x = a[i];$

can be optimized to:

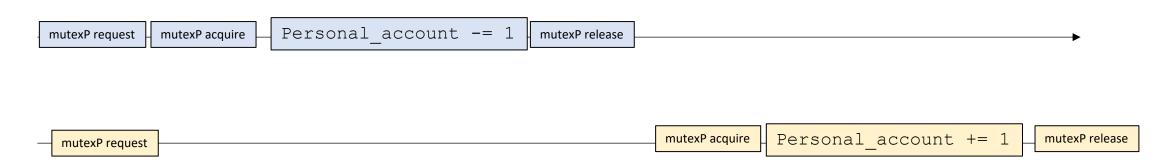
$$x = 6;$$

Compiler Fence

- Compiler can be aggressive with memory operations:
 - For non-atomic memory locations, the following optimizations are valid
- And many others... especially when you consider mixing with other optimizations
 - Very difficult to understand when/where memory accesses will actually occur in your code

Compiler Fence

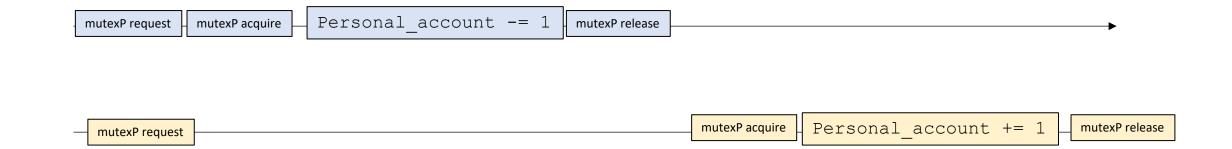
Compiler cannot keep personal_account in a register past the mutex



because this thread needs to see the updated view

Compiler Fence

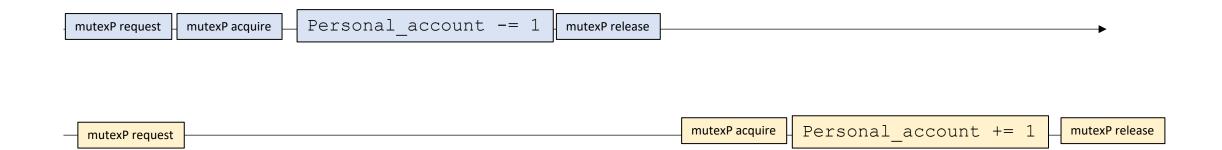
what can go wrong if the compiler doesn't write values to memory?



Compiler Fence

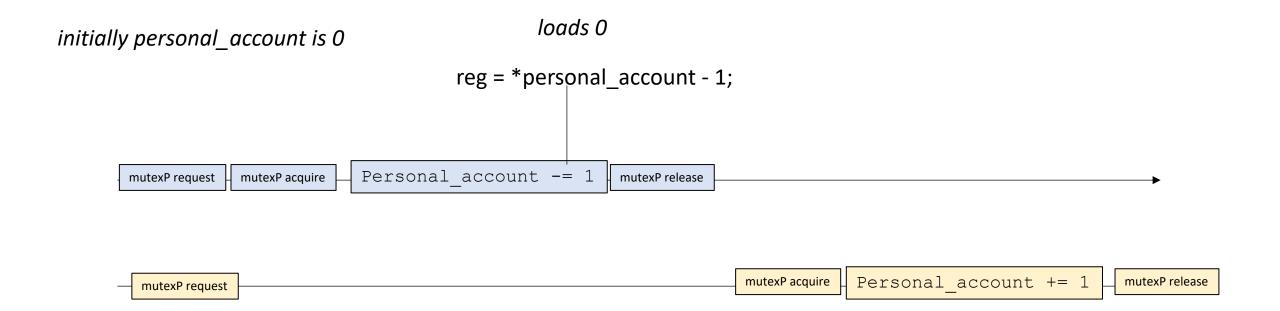
what can go wrong if the compiler doesn't write values to memory?

initially personal_account is 0



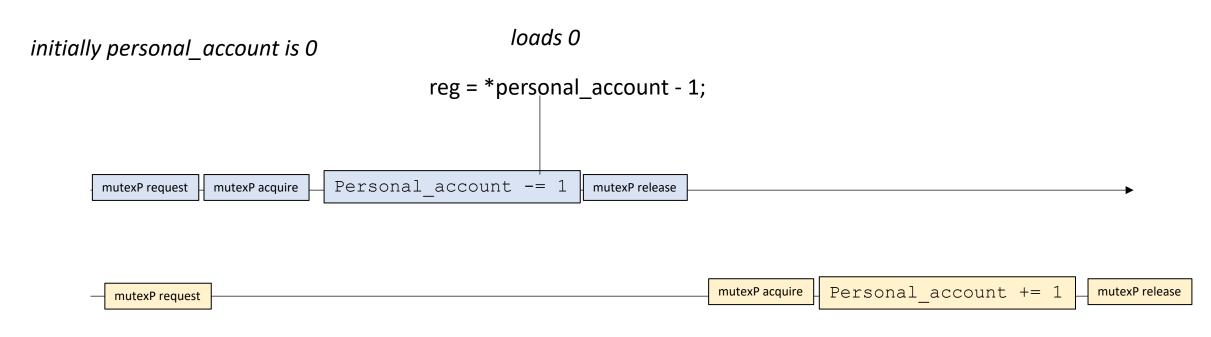
Compiler Fence

what can go wrong if the compiler doesn't write values to memory?



Compiler Fence

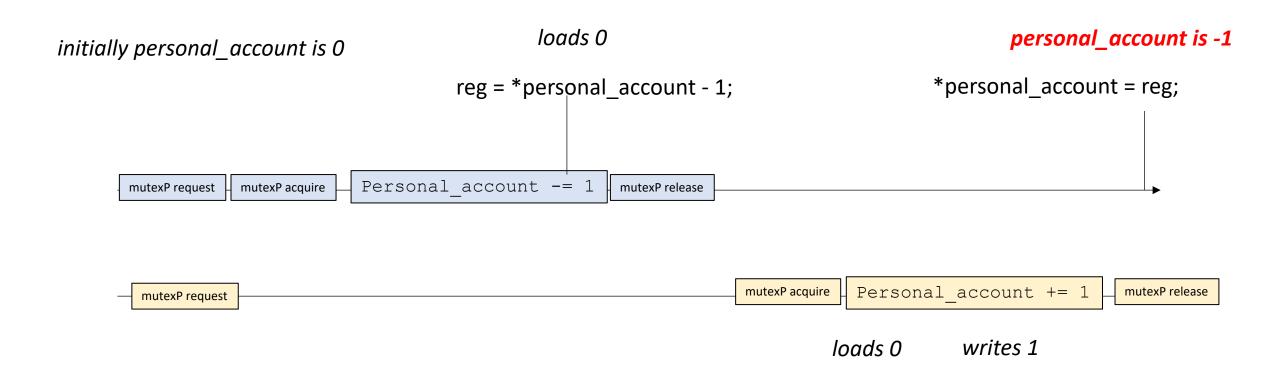
what can go wrong if the compiler doesn't write values to memory?



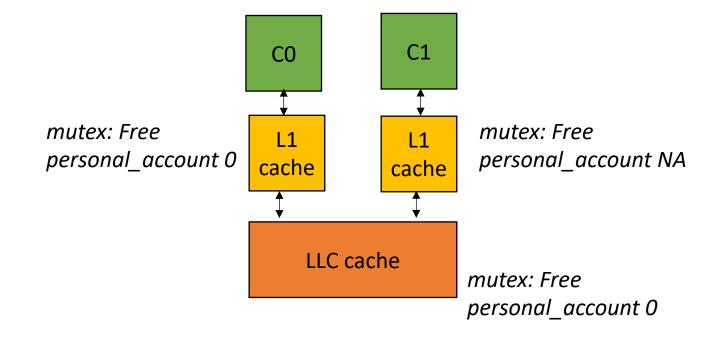
loads 0 writes 1

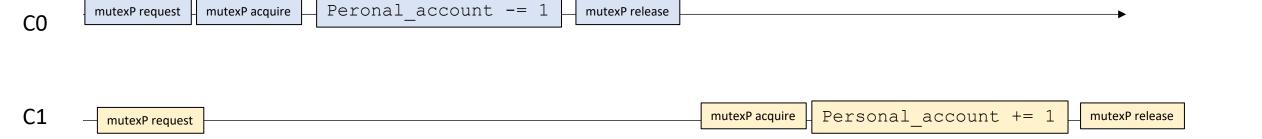
Compiler Fence

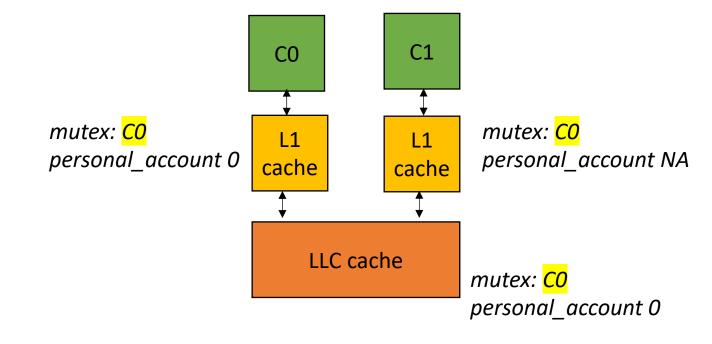
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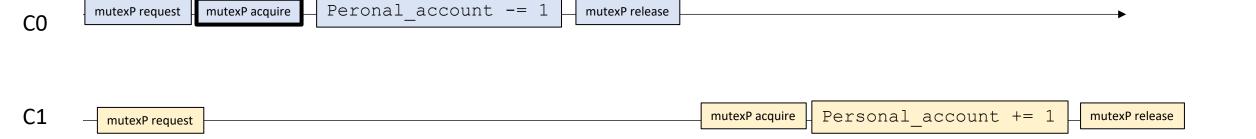


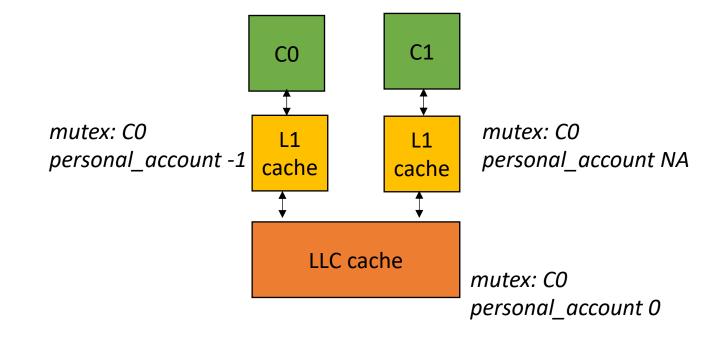
Also provides a memory barrier

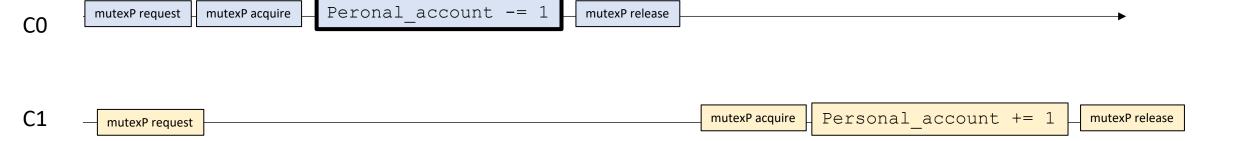


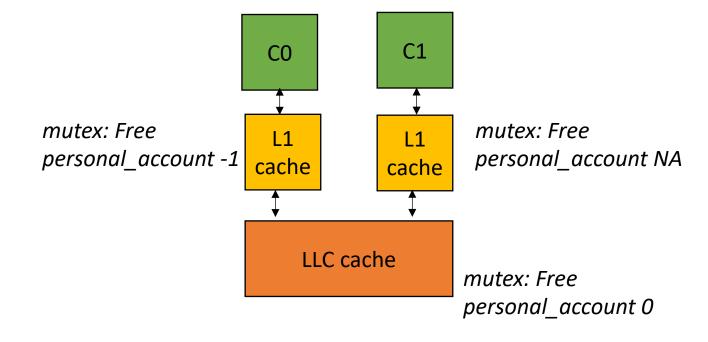


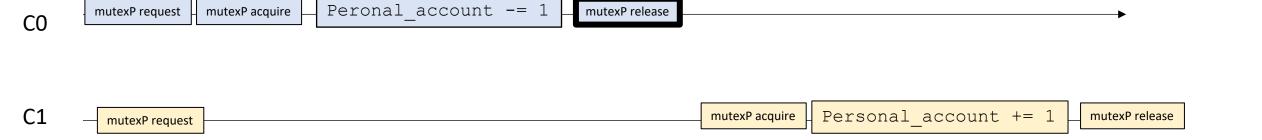


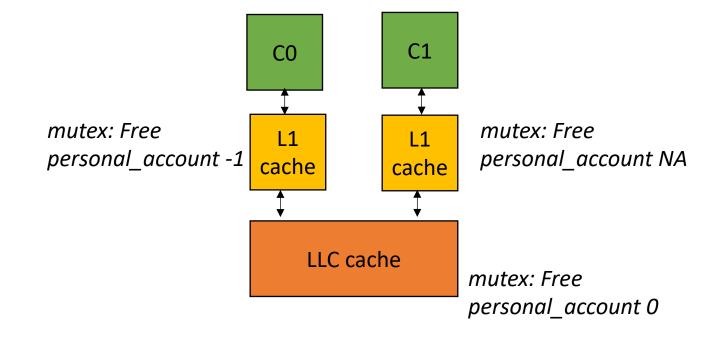


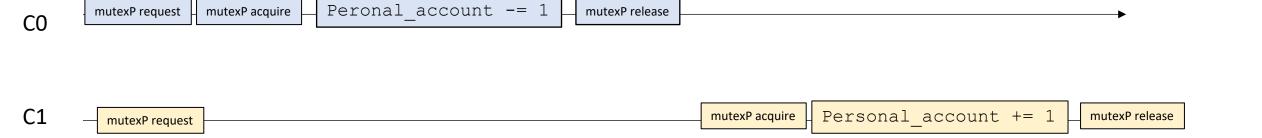






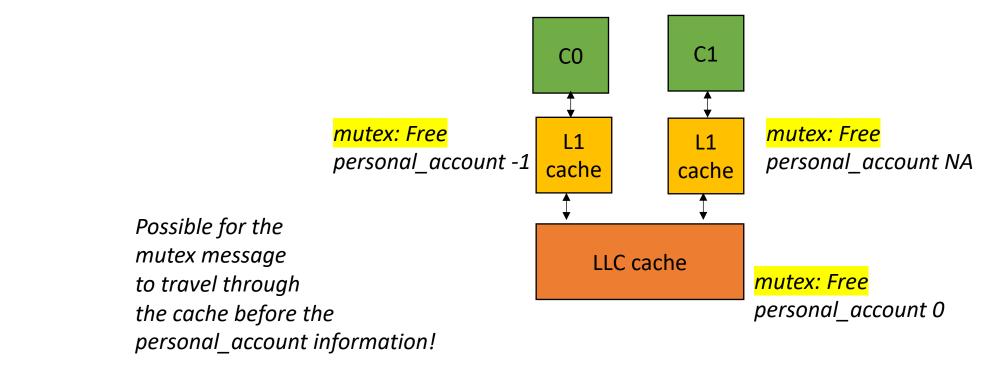






mutexP request

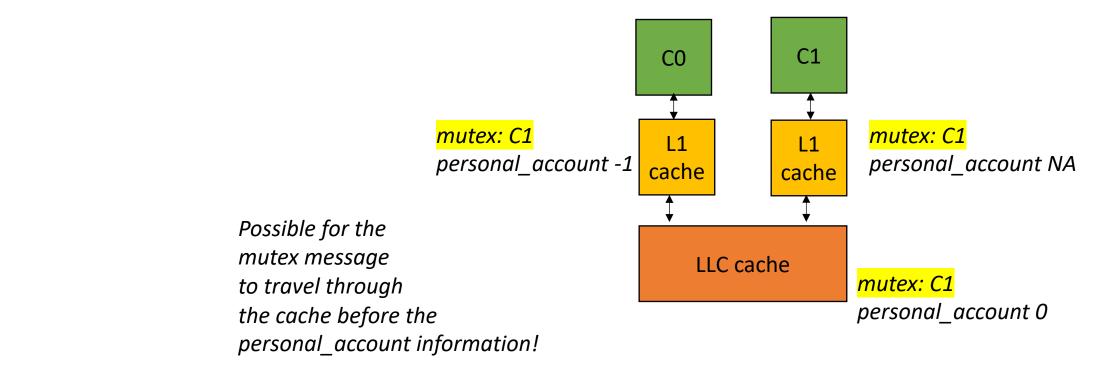
mutexP acquire

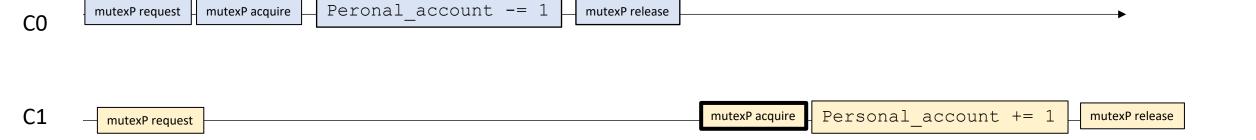




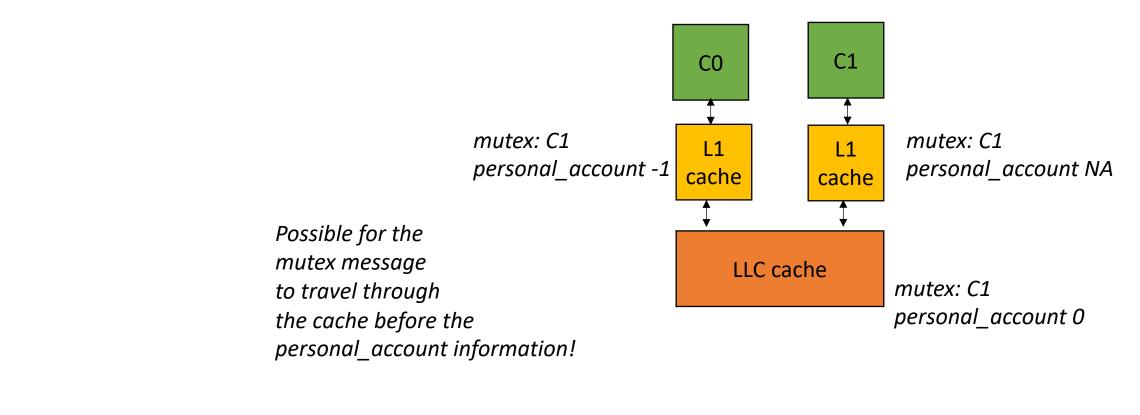
mutexP release

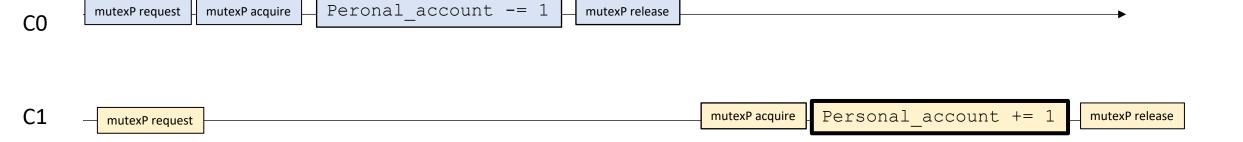
Peronal account -= 1



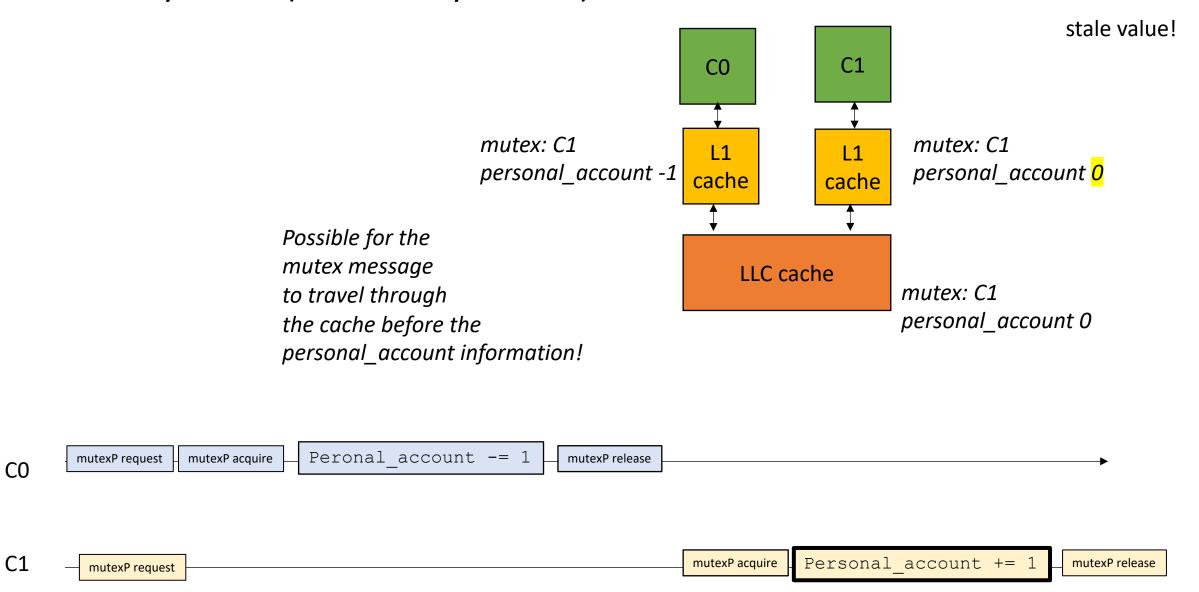


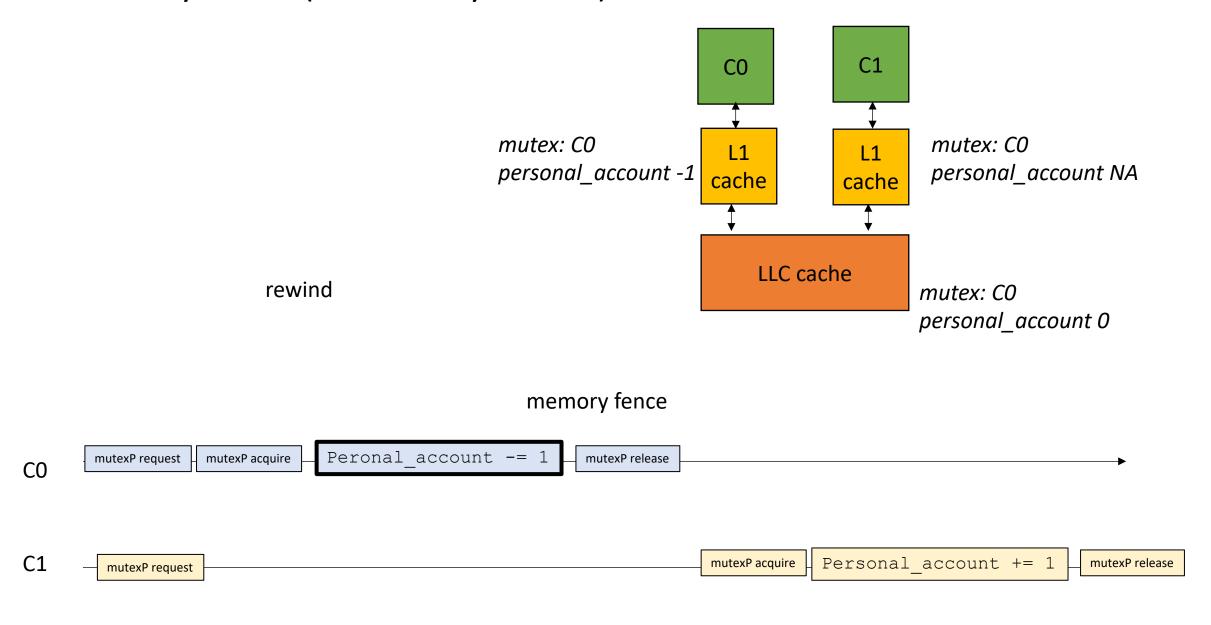
mutexP acquire

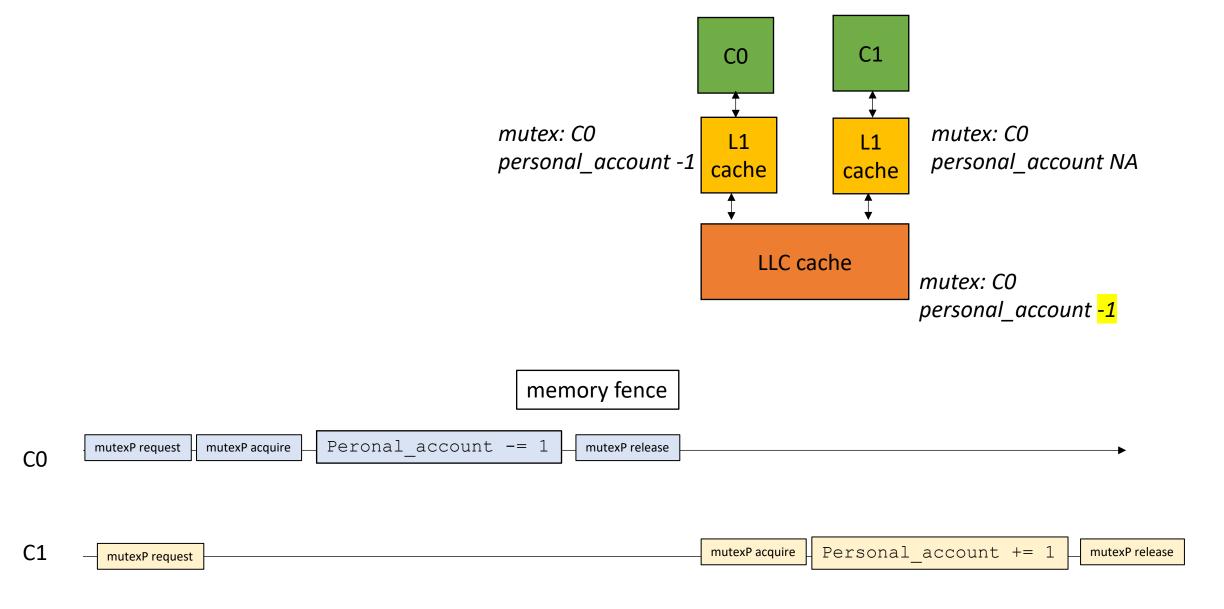


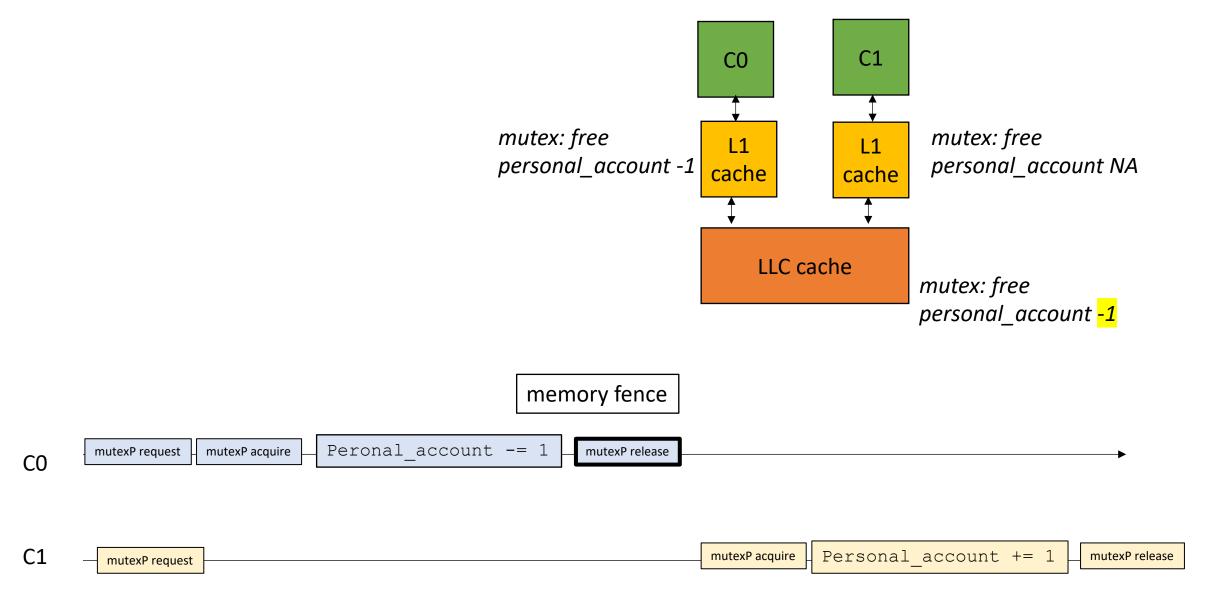


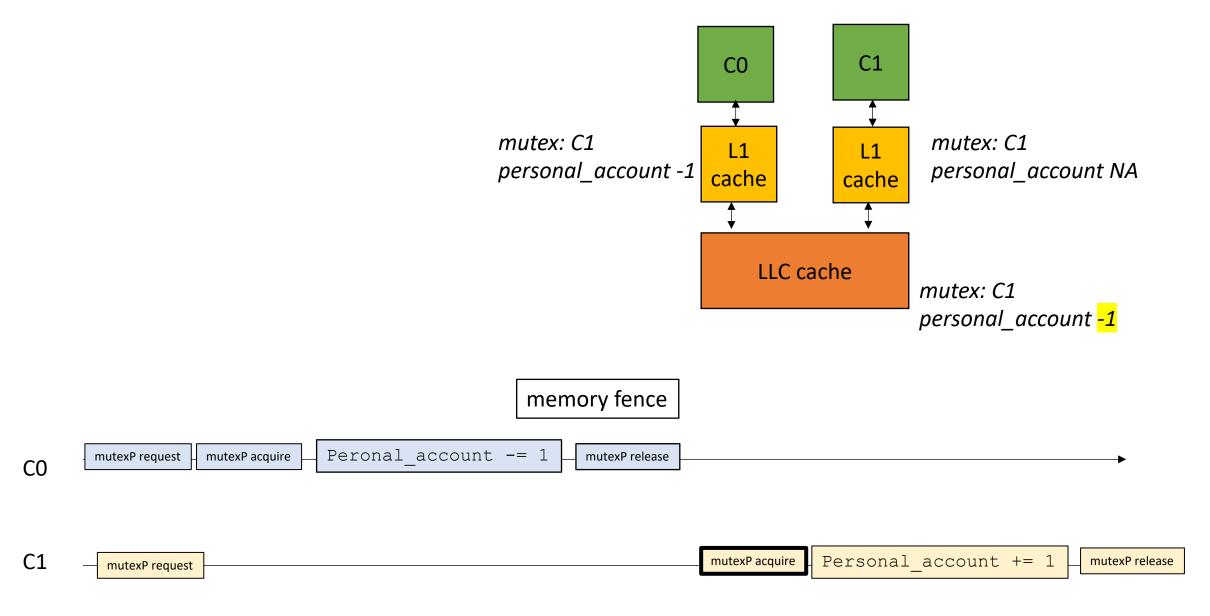
mutexP release

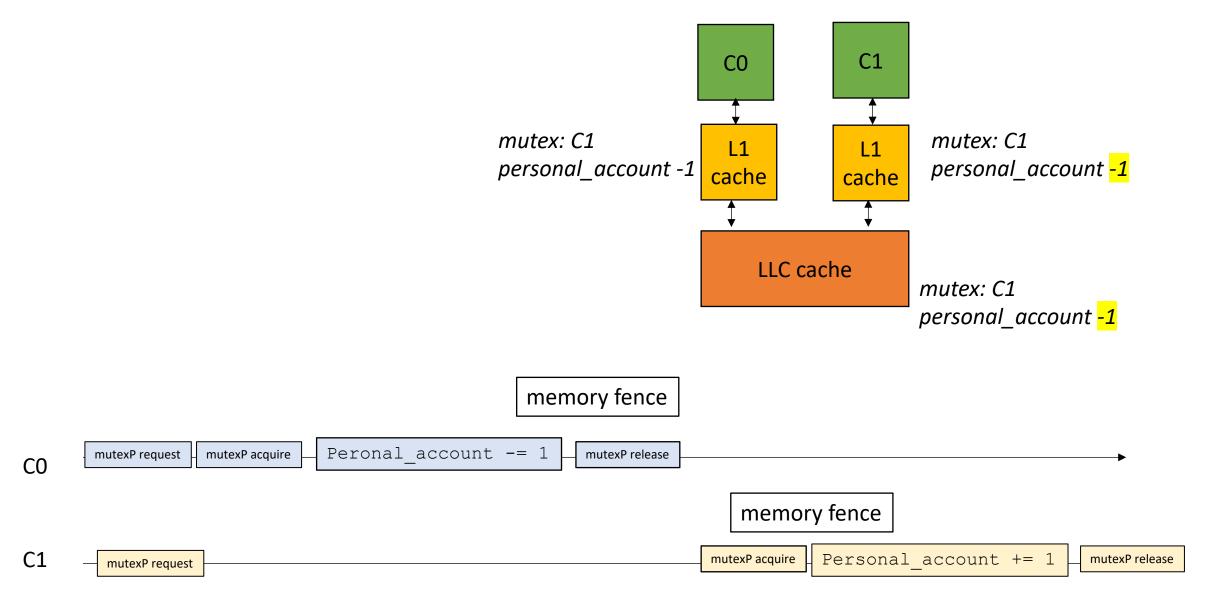


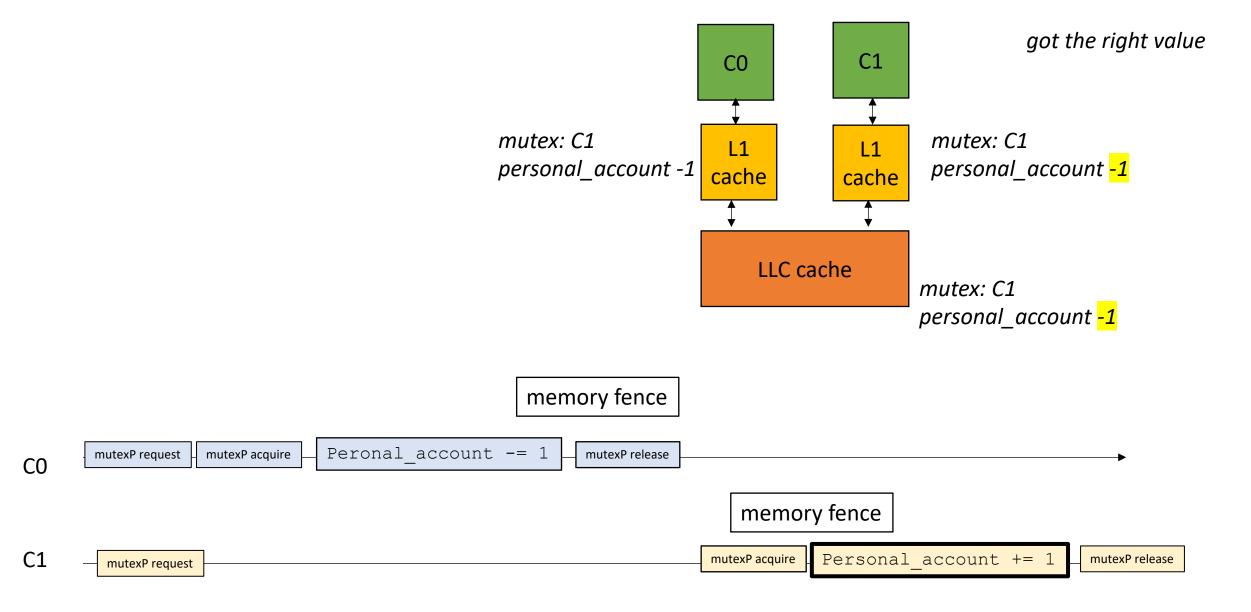












different architectures have different memory barriers

Intel X86 naturally manages caches in order

ARM and PowerPC let cache values flow out-of-order GPUs let caches flow out-of-order

RISC-V has two models:

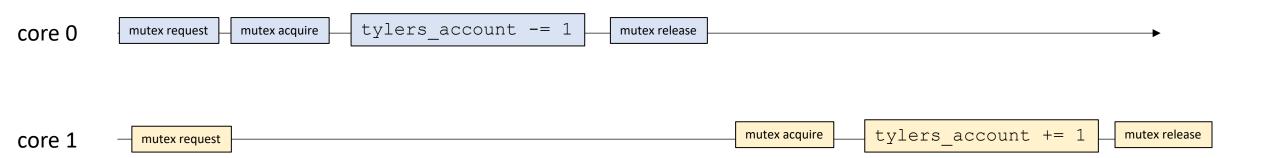
more like x86: easier to program

more like ARM: faster and more energy efficient

For mutexes, atomics will naturally handle the memory fences for us!

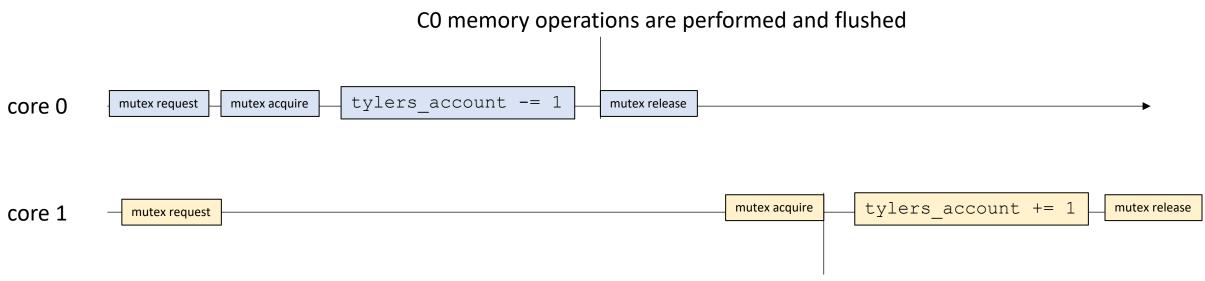
Atomics

- What do those fences (compiler and memory) give us?
- Atomics were designed so that we can implement things like mutexes!



Atomics

- What do those fences (compiler and memory) give us?
- Atomics were designed so that we can implement things like mutexes!



C1 memory operations have **not** yet been performed and cache is invalidated

• We will just consider two threads for now, with thread ids 0, 1

- A first attempt:
 - A mutex contains a boolean.
 - The mutex value set to 0 means that it is free. 1 means that some thread is holding it.
 - To aquire the mutex, you wait until it is set to 0, then you store 1 in the flag.
 - To release the mutex, you set the mutex back to 0.

```
#include <atomic>
using namespace std;
class Mutex {
public:
  Mutex() {
    flag = 0;
  void lock();
  void unlock();
private:
  atomic_bool flag;
```

mutex is initialized to "free"

atomic_bool for our memory location

```
void lock() {
  while (flag.load() == 1);
  flag.store(1);
}
```

While the mutex is not available (i.e. another thread has it)

Once the mutex is available, we will claim it

```
void lock() {
  while (flag.load() == 1);
  flag.store(1);
}
```

While the mutex is not available (i.e. another thread has it)

Once the mutex is available, we will claim it

Whats up with this while loop?

```
void unlock() {
  flag.store(0);
}
```

To release the mutex, we just set it back to 0 (available)

```
void lock() {
  while (flag.load() == 1);
  flag.store(1);
}
```

```
void unlock() {
  flag.store(0);
}
```

```
Thread 0: Thread 1:
m.lock(); m.lock();
m.unlock(); m.unlock();
```

```
core 0
```

```
core 1
```

```
void lock() {
  while (flag.load() == 1);
  flag.store(1);
}
```

```
void unlock() {
  flag.store(0);
}
```

```
Thread 0: Thread 1:
m.lock(); m.lock();
m.unlock();
```

```
void lock() {
  while (flag.load() == 1);
  flag.store(1);
}
```

```
void unlock() {
  flag.store(0);
}
```

```
Thread 0: Thread 1:
m.lock();
m.unlock();
m.unlock();
```

```
Mutex request

core 0

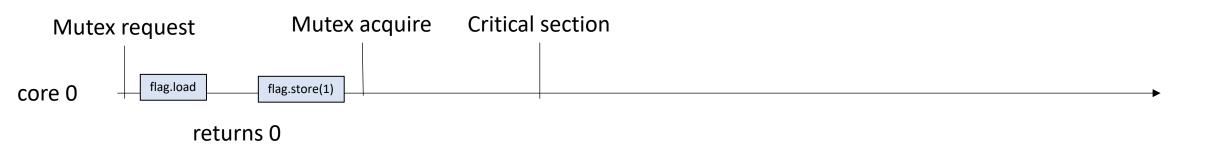
flag.load

returns 0
```

```
void lock() {
  while (flag.load() == 1);
  flag.store(1);
}
```

```
void unlock() {
  flag.store(0);
}
```

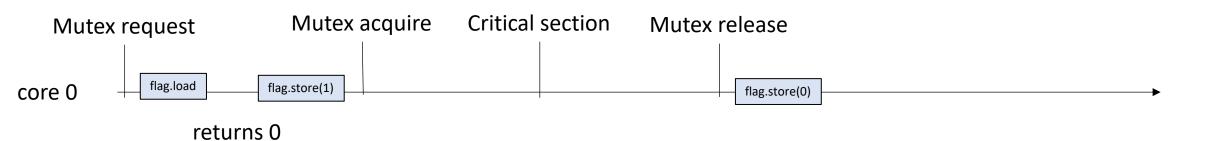
```
Thread 0: Thread 1:
m.lock(); m.lock();
m.unlock();
```



```
void lock() {
  while (flag.load() == 1);
  flag.store(1);
}
```

```
void unlock() {
  flag.store(0);
}
```

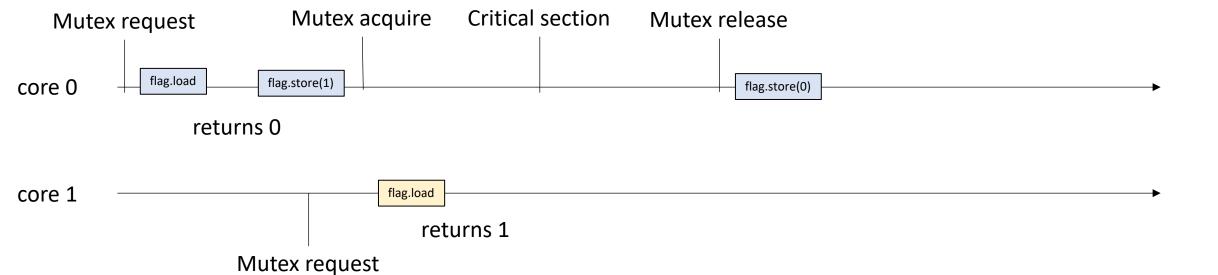
```
Thread 0: Thread 1:
m.lock(); m.lock();
m.unlock();
```



```
void lock() {
  while (flag.load() == 1);
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}
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void unlock() {
  flag.store(0);
}
```

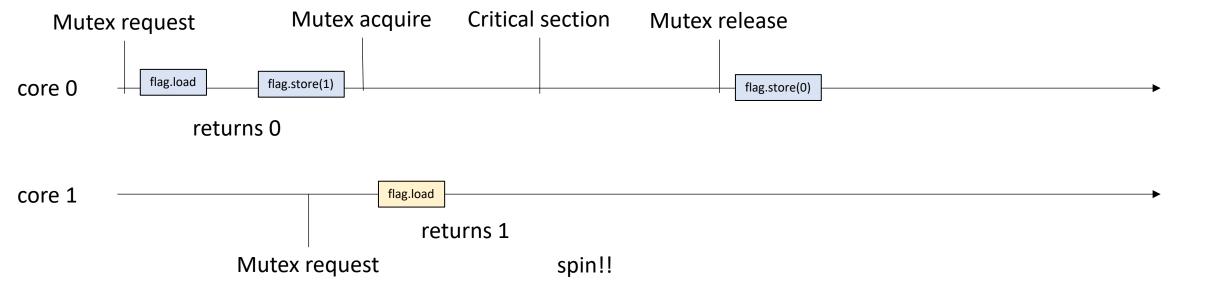
```
Thread 0: Thread 1:
m.lock();
m.unlock();
m.unlock();
```



```
void lock() {
  while (flag.load() == 1);
  flag.store(1);
}
```

```
void unlock() {
  flag.store(0);
}
```

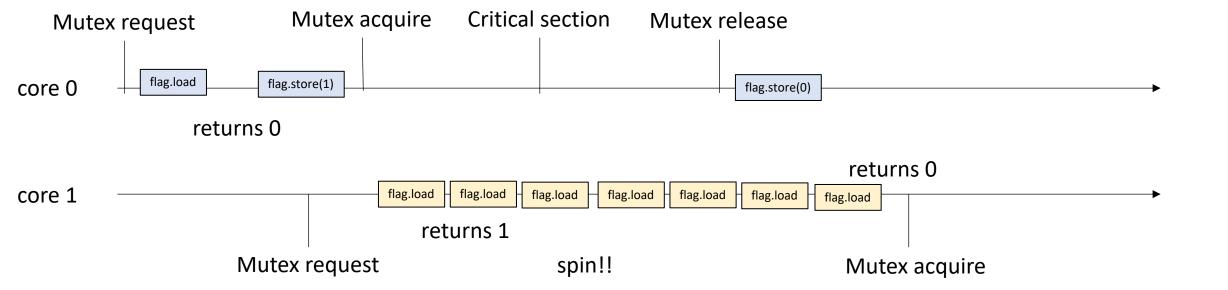
```
Thread 0: Thread 1:
m.lock();
m.unlock();
m.unlock();
```



```
void lock() {
  while (flag.load() == 1);
  flag.store(1);
}
```

```
void unlock() {
  flag.store(0);
}
```

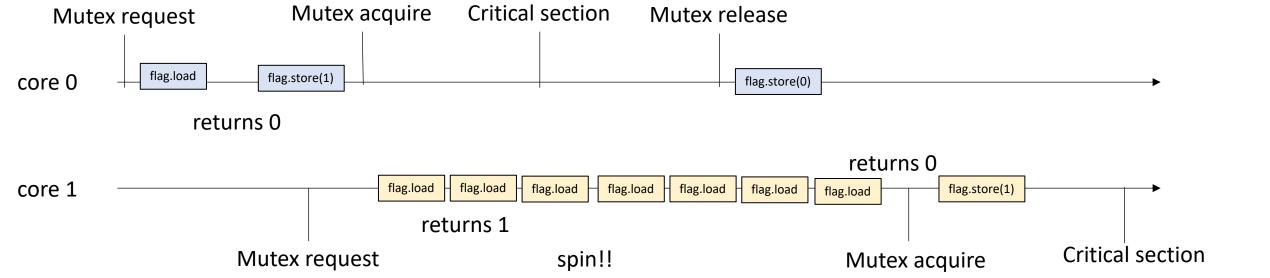
```
Thread 0: Thread 1:
m.lock(); m.lock();
m.unlock();
```



```
void lock() {
  while (flag.load() == 1);
  flag.store(1);
}
```

```
void unlock() {
  flag.store(0);
}
```

```
Thread 0: Thread 1:
m.lock(); m.lock();
m.unlock();
```



Thread 0:

Thread 1:

Mutex request

```
void lock() {
  while (flag.load() == 1);
  flag.store(1);
}
```

```
void unlock() {
  flag.store(0);
}
```

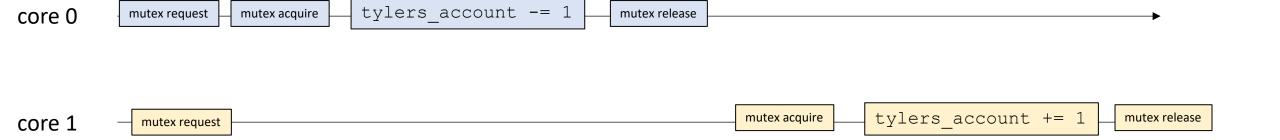
Critical section

Mutex acquire

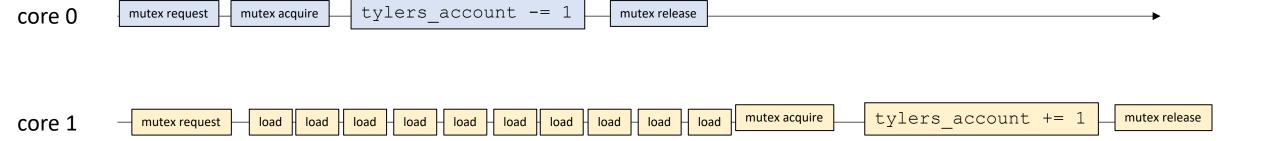
```
m.lock();
                              m.lock();
                                                                                     Mutual Exclusion property!
    m.unlock();
                              m.unlock();
                                                                                     critical sections do not overlap!
   m.lock();
    m.unlock();
                               Mutex acquire
                                                   Critical section
                                                                        Mutex release
    Mutex request
                                                                                                           Mutex request
                                                                                                                              returns 1
               flag.load
                                                                                                                                        flag.load
                            flag.store(1)
                                                                                                                      flag.load
                                                                                                                               flag.load
core 0
                                                                                   flag.store(0)
                    returns 0
                                                                                               returns 0
core 1
                                                  flag.load
                                                          flag.load
                                          flag.load
                                                                   flag.load
                                                                           flag.load
                                                                                   flag.load
                                                                                            flag.load
                                                                                                          flag.store(1)
                                              returns 1
```

spin!!

Recall our previous analysis. What was core 1 probably doing?



Recall our previous analysis. What was core 1 probably doing?

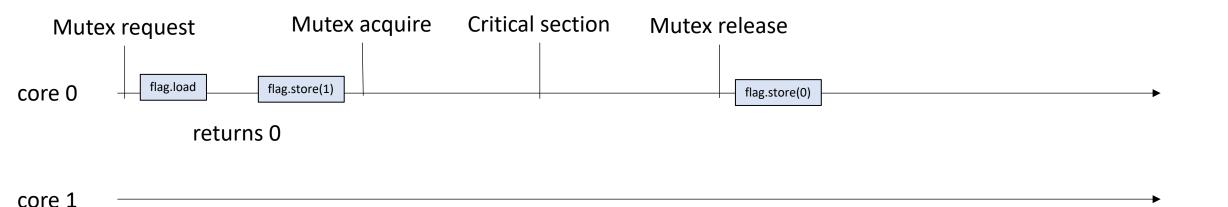


```
void lock() {
  while (flag.load() == 1);
  flag.store(1);
}
```

```
void unlock() {
  flag.store(0);
}
```

```
Thread 0: Thread 1:
m.lock(); m.lock();
m.unlock();
```

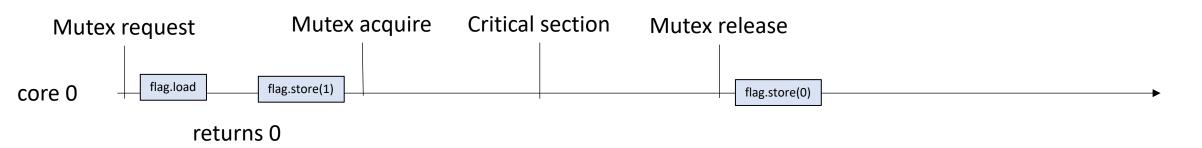
Lets try another interleaving



```
void lock() {
  while (flag.load() == 1);
  flag.store(1);
}
```

```
void unlock() {
  flag.store(0);
}
```

```
Thread 0: Thread 1:
m.lock(); m.lock();
m.unlock();
```



```
returns 0

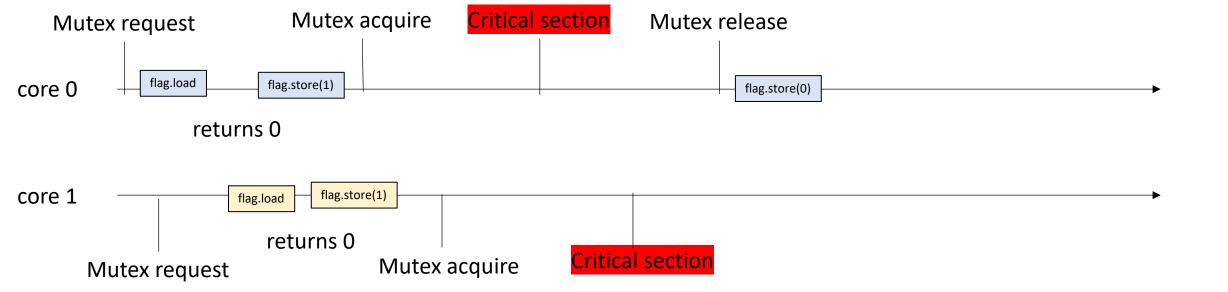
Mutex request
```

```
void lock() {
  while (flag.load() == 1);
  flag.store(1);
}
```

```
void unlock() {
  flag.store(0);
}
```

```
Thread 0: Thread 1:
m.lock(); m.lock();
m.unlock();
```

Critical sections overlap! This mutex implementation is not correct!



- Second attempt:
 - A flag for each thread (2 flags)
 - If you want the mutex, set your flag to 1.
 - Spin while the other flag is 1 (the other thread has the mutex)
 - To release the mutex, set your flag to 0

```
#include <atomic>
using namespace std;
class Mutex {
public:
  Mutex() {
    flag[0] = flag[1] = 0;
  void lock();
  void unlock();
private:
  atomic_bool flag[2];
```

both initialized to 0

two flags this time

```
void lock() {
  int i = thread_id;
  flag[i].store(1);
  int j = i == 0 ? 1 : 0;
  while (flag[j].load() == 1);
}
```

Thread id (0, or 1)

Mark your intention to take the lock

Wait for other thread to leave the critical section

```
void unlock() {
  int i = thread_id;
  flag[i].store(0);
}
```

Thread id (0, or 1)

Mark your flag to say you have left the critical section.

```
void lock() {
   int i = thread_id;
   flag[i].store(1);
   int j = i == 0 ? 1 : 0;
   while (flag[j].load() == 1);
}
```

```
void unlock() {
  int i = thread_id;
  flag[i].store(0);
}
```

```
Thread 0: Thread 1:
m.lock(); m.lock();
m.unlock();
```

```
core 0 —
```

```
core 1 -
```

```
void lock() {
   int i = thread_id;
   flag[i].store(1);
   int j = i == 0 ? 1 : 0;
   while (flag[j].load() == 1);
}
```

```
void unlock() {
  int i = thread_id;
  flag[i].store(0);
}
```

```
Thread 0: Thread 1:
m.lock(); m.lock();
m.unlock();
```

```
Mutex request

core 0

flag[0].store(1)

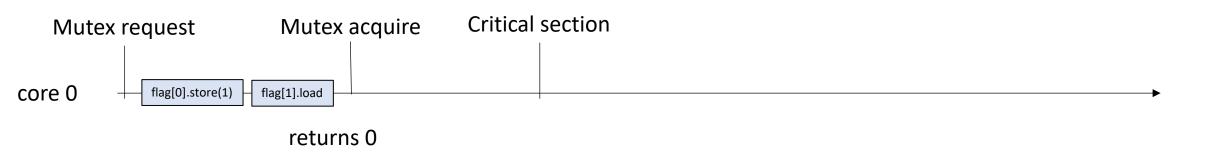
flag[1].load

returns 0
```

```
void lock() {
   int i = thread_id;
   flag[i].store(1);
   int j = i == 0 ? 1 : 0;
   while (flag[j].load() == 1);
}
```

```
void unlock() {
  int i = thread_id;
  flag[i].store(0);
}
```

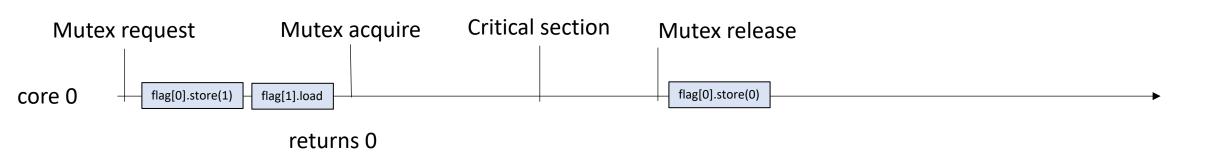
```
Thread 0: Thread 1:
m.lock(); m.lock();
m.unlock();
```



```
void lock() {
  int i = thread_id;
  flag[i].store(1);
  int j = i == 0 ? 1 : 0;
  while (flag[j].load() == 1);
}
```

```
void unlock() {
  int i = thread_id;
  flag[i].store(0);
}
```

```
Thread 0: Thread 1:
m.lock(); m.lock();
m.unlock();
```

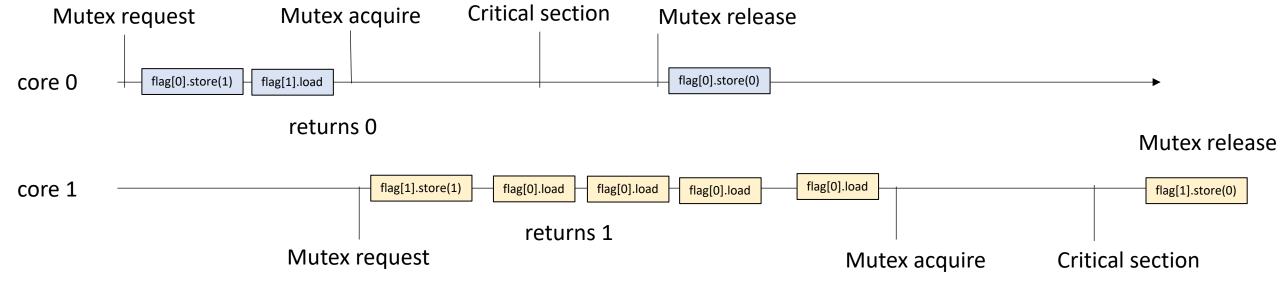


```
void lock() {
  int i = thread_id;
  flag[i].store(1);
  int j = i == 0 ? 1 : 0;
  while (flag[j].load() == 1);
}
```

```
void unlock() {
  int i = thread_id;
  flag[i].store(0);
}
```

```
Thread 0: Thread 1:
m.lock(); m.lock();
m.unlock(); m.unlock();
```

critical sections do not overlap!



```
void lock() {
  int i = thread_id;
  flag[i].store(1);
  int j = i == 0 ? 1 : 0;
  while (flag[j].load() == 1);
}
```

```
void unlock() {
  int i = thread_id;
  flag[i].store(0);
}
```

```
Thread 0: Thread 1:
m.lock();
m.unlock();
m.unlock();
```

```
Mutex request

core 0

flag[0].store(1)
```

```
core 1 
flag[1].store(1)
```

Mutex request

Mutex request

```
void lock() {
  int i = thread_id;
  flag[i].store(1);
  int j = i == 0 ? 1 : 0;
  while (flag[j].load() == 1);
}
```

```
void unlock() {
  int i = thread_id;
  flag[i].store(0);
}
```

```
Thread 0: Thread 1:
m.lock();
m.unlock();
m.unlock();
```

```
core 0

flag[0].store(1)

flag[1].load

core 1

flag[1].store(1)

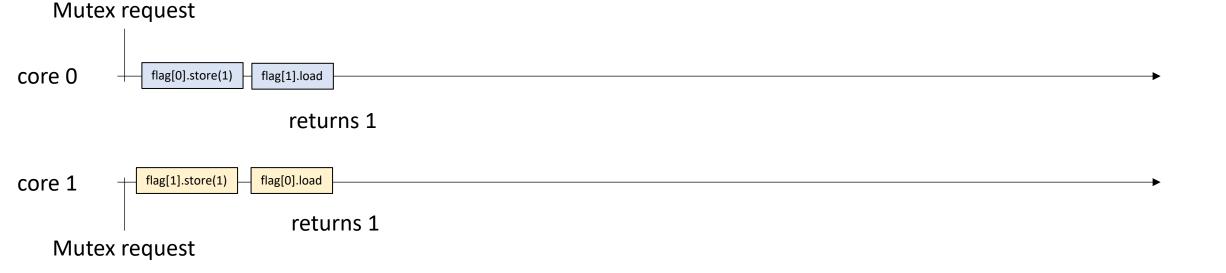
flag[0].load

Mutex request
```

```
void lock() {
  int i = thread_id;
  flag[i].store(1);
  int j = i == 0 ? 1 : 0;
  while (flag[j].load() == 1);
}
```

```
void unlock() {
  int i = thread_id;
  flag[i].store(0);
}
```

```
Thread 0: Thread 1:
m.lock();
m.unlock();
m.unlock();
```

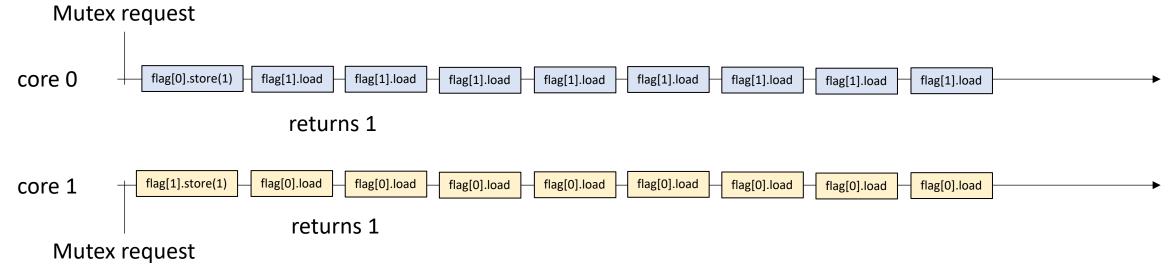


```
void lock() {
  int i = thread_id;
  flag[i].store(1);
  int j = i == 0 ? 1 : 0;
  while (flag[j].load() == 1);
}
```

```
void unlock() {
  int i = thread_id;
  flag[i].store(0);
}
```

```
Thread 0: Thread 1:
m.lock();
m.unlock();
m.unlock();
```

Both will spin forever!



Properties of mutexes

Three properties

 Deadlock Freedom - If a thread has requested the mutex, and no thread currently holds the mutex, the mutex must be acquired by one of the requesting threads

> Program cannot hang here Either thread 0 or thread 1 must acquire the mutex

concurrent execution



Third attempt:

```
class Mutex {
public:
  Mutex() {
    victim = -1;
  void lock();
  void unlock();
private:
  atomic_int victim;
```

initialized to -1

back to a single variable

```
void lock() {
  victim.store(thread_id);
  while (victim.load() == thread_id);
}
```

Volunteer to be the victim

Victims only job is to spin



No unlock!

```
void lock() {
  victim.store(thread_id);
  while (victim.load() == thread_id);
}
```

```
void unlock() {}
```

```
Thread 0:
```

```
m.lock();
m.unlock();
```

```
Mutex request
```

core 0

```
void lock() {
  victim.store(thread_id);
  while (victim.load() == thread_id);
}
```

```
void unlock() {}
```

```
Thread 0:
```

```
m.lock();
m.unlock();
```

Mutex request

core 0

victim.store(0)

victim.load

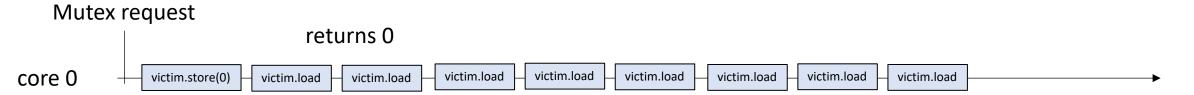
```
void lock() {
  victim.store(thread_id);
  while (victim.load() == thread_id);
}
```

```
void unlock() {}
```

```
Thread 0:
```

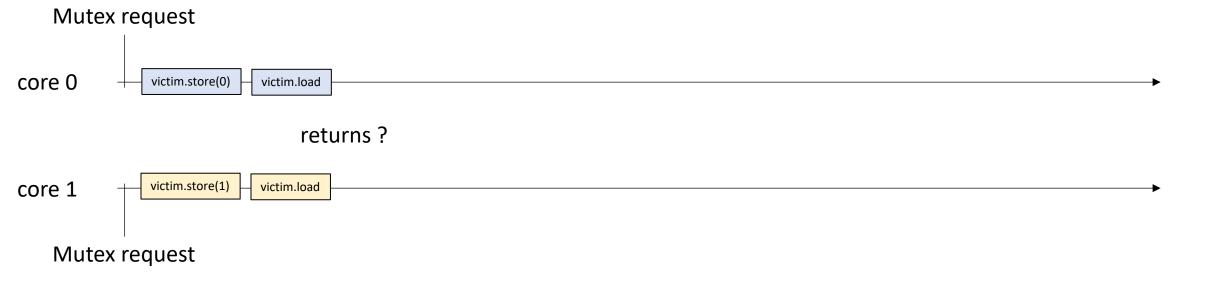
```
m.lock();
m.unlock();
```

spins forever if the second thread never tries to take the mutex!



```
void lock() {
  victim.store(thread_id);
  while (victim.load() == thread_id);
}
```

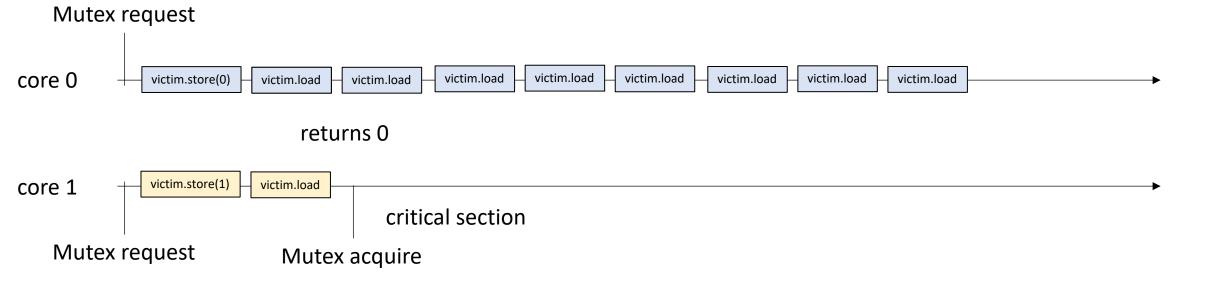
```
void unlock() {}
```



```
void lock() {
  victim.store(thread_id);
  while (victim.load() == thread_id);
}
```

```
void unlock() {}
```

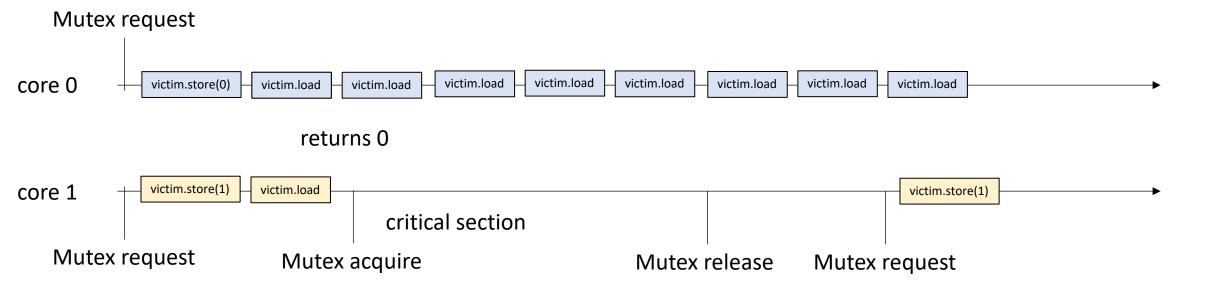
```
Thread 0: Thread 1:
m.lock();
m.unlock();
m.unlock();
```



```
void lock() {
  victim.store(thread_id);
  while (victim.load() == thread_id);
}
```

```
void unlock() {}
```

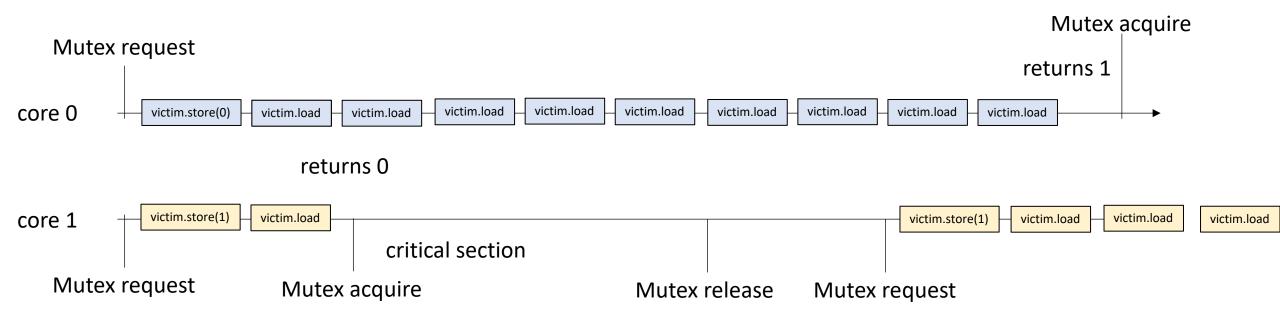
```
Thread 0: Thread 1:
m.lock();
m.unlock();
m.unlock();
```



```
void lock() {
  victim.store(thread_id);
  while (victim.load() == thread_id);
}
```

```
void unlock() {}
```

```
Thread 0: Thread 1:
m.lock();
m.unlock();
m.unlock();
```



Not deadlock free for one thread, but for two infinite threads it seems to work.

Finally, we can can make a mutex that works:

Use flags to mark interest Use victim to break ties

Called the **Peterson Lock**

```
class Mutex {
public:
  Mutex() {
    victim = -1;
    flag[0] = flag[1] = 0;
  void lock();
  void unlock();
private:
  atomic_int victim;
  atomic_bool flag[2];
```

Initially:

No victim and no threads are interested in the critical section

flags and victim

```
void lock() {
  int j = thread_id == 0 ? 1 : 0;
  flag[thread_id].store(1);
  victim.store(thread_id);
  while (victim.load() == thread_id
         && flag[j] == 1);
}
```

j is the other thread

Mark ourself as interested

volunteer to be the victim in case of a tie

Spin only if:
 there was a tie in wanting the lock,
 and I won the volunteer raffle to spin

```
void unlock() {
  int i = thread_id;
  flag[i].store(0);
}
```

mark ourselves as uninterested

previous flag issue

```
void lock() {
   int i = thread_id;
   flag[i].store(1);
   int j = i == 0 ? 1 : 0;
   while (flag[j].load() == 1);
}
```

```
void unlock() {
  int i = thread_id;
  flag[i].store(0);
}
```

```
Thread 0: Thread 1:
m.lock();
m.unlock();
m.unlock();
```

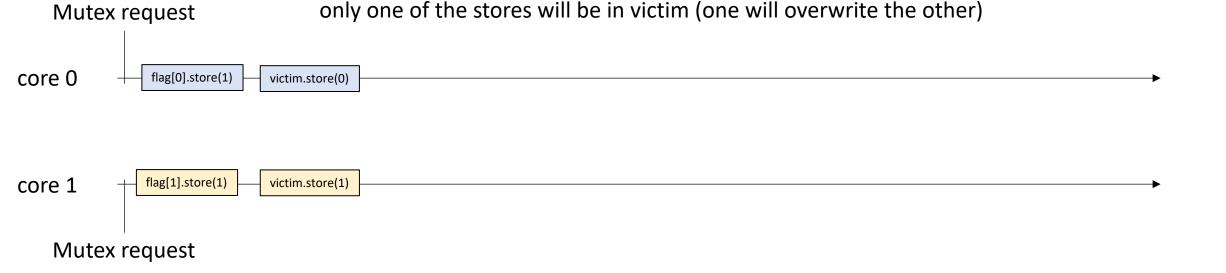
how does petersons solve this?

Both will spin forever! Mutex request core 0 flag[0].store(1) flag[1].load flag[1].load flag[1].load flag[1].load flag[1].load flag[1].load flag[1].load flag[1].load returns 1 flag[1].store(1) flag[0].load flag[0].load flag[0].load flag[0].load core 1 flag[0].load flag[0].load flag[0].load flag[0].load Mutex request

```
void lock() {
  int j = thread_id == 0 ? 1 : 0;
  flag[thread_id].store(1);
  victim.store(thread_id);
  while (victim.load() == thread_id
         && flag[j] == 1);
}
```

```
void unlock() {
  int i = thread_id;
  flag[i].store(0);
}
```

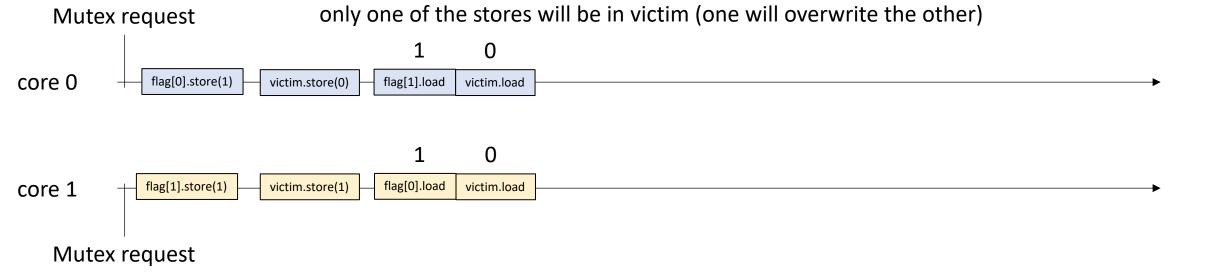
```
Thread 0: Thread 1:
m.lock();
m.unlock();
m.unlock();
```



```
void lock() {
  int j = thread_id == 0 ? 1 : 0;
  flag[thread_id].store(1);
  victim.store(thread_id);
  while (victim.load() == thread_id
         && flag[j] == 1);
}
```

```
void unlock() {
  int i = thread_id;
  flag[i].store(0);
}
```

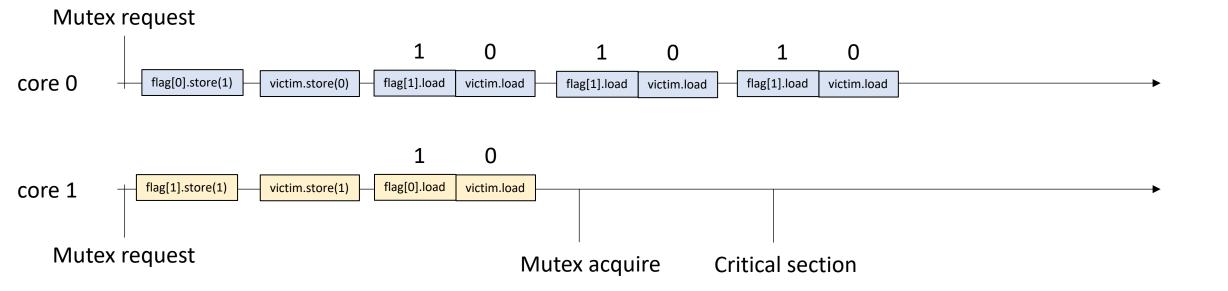
```
Thread 0: Thread 1:
m.lock();
m.unlock();
m.unlock();
```



```
void lock() {
  int j = thread_id == 0 ? 1 : 0;
  flag[thread_id].store(1);
  victim.store(thread_id);
  while (victim.load() == thread_id
         && flag[j] == 1);
}
```

```
void unlock() {
  int i = thread_id;
  flag[i].store(0);
}
```

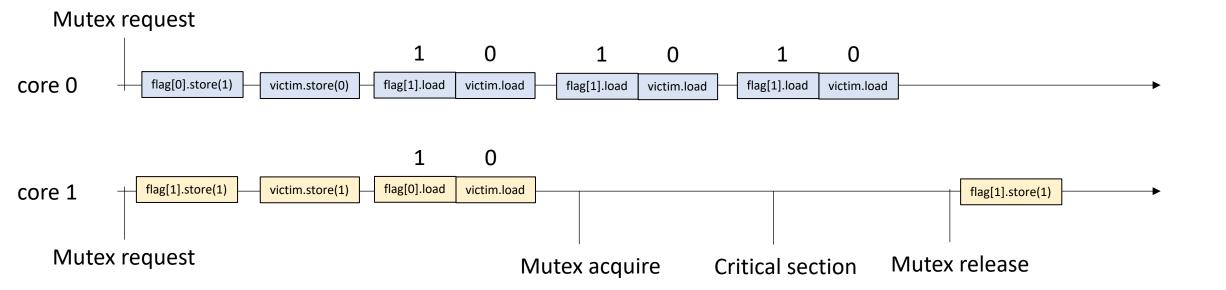
```
Thread 0: Thread 1:
m.lock();
m.unlock();
m.unlock();
```



```
void lock() {
  int j = thread_id == 0 ? 1 : 0;
  flag[thread_id].store(1);
  victim.store(thread_id);
  while (victim.load() == thread_id
         && flag[j] == 1);
}
```

```
void unlock() {
  int i = thread_id;
  flag[i].store(0);
}
```

```
Thread 0: Thread 1:
m.lock(); m.lock();
m.unlock();
m.unlock();
```

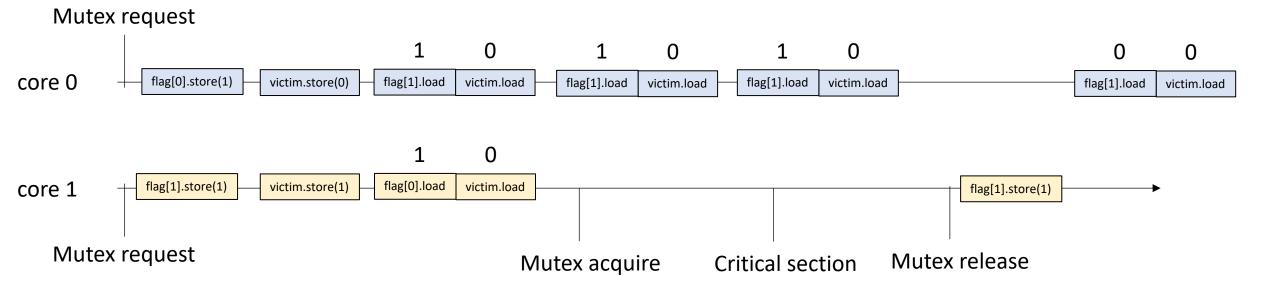


```
void lock() {
  int j = thread_id == 0 ? 1 : 0;
  flag[thread_id].store(1);
  victim.store(thread_id);
  while (victim.load() == thread_id
         && flag[j] == 1);
}
```

```
void unlock() {
  int i = thread_id;
  flag[i].store(0);
}
```

```
Thread 0: Thread 1:
m.lock(); m.lock();
m.unlock();
```

Mutex acquire



previous victim issue

```
void lock() {
  victim.store(thread_id);
  while (victim.load() == thread_id);
}
```

```
void unlock() {}
```

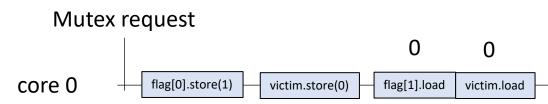
```
Thread 0:
m.lock();
m.unlock();
```

previous flag issue

```
void lock() {
  int j = thread_id == 0 ? 1 : 0;
  flag[thread_id].store(1);
  victim.store(thread_id);
  while (victim.load() == thread_id
         && flag[j] == 1);
}
```

```
void unlock() {
  int i = thread_id;
  flag[i].store(0);
}
```

```
Thread 0:
m.lock();
m.unlock();
```



previous flag issue

```
void lock() {
  int j = thread_id == 0 ? 1 : 0;
  flag[thread_id].store(1);
  victim.store(thread_id);
  while (victim.load() == thread_id
          && flag[j] == 1);
}
```

```
void unlock() {
  int i = thread_id;
  flag[i].store(0);
}
```

```
Thread 0:
m.lock();
m.unlock();
```

```
Mutex request

O

O

flag[0].store(1)  victim.store(0)  flag[1].load  victim.load
```

we can enter critical section because the other thread isn't interested

This lock satisfies the two critical properties

Mutual exclusion

Deadlock freedom

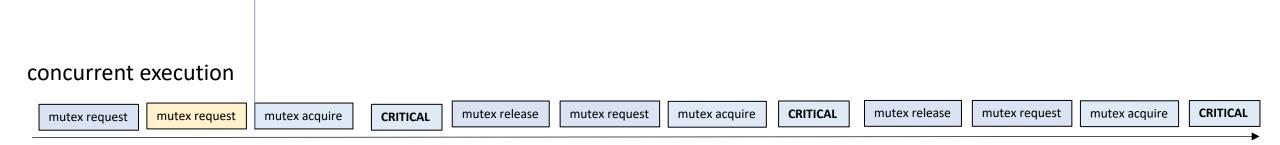
More formal proof given in the textbook

recall the starvation property:

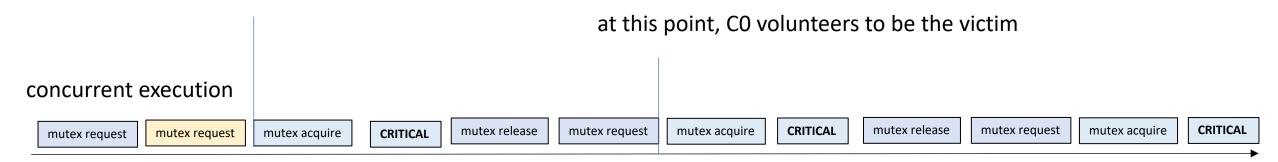
Thread 1 (yellow) requests the mutex but never gets it

Concurrent execution mutex request mutex re

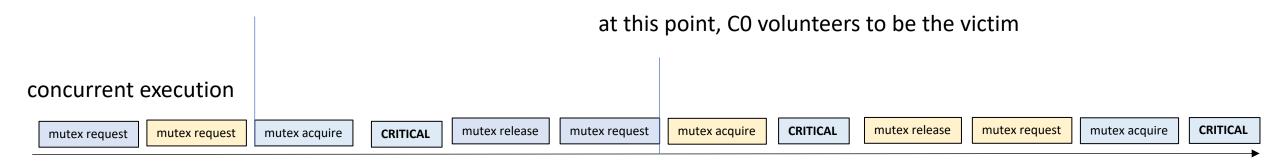
```
void lock() {
  int j = thread_id == 0 ? 1 : 0;
  flag[thread_id].store(1);
  victim.store(thread_id);
  while (victim.load() == thread_id
         && flag[j] == 1);
}
```



```
void lock() {
  int j = thread_id == 0 ? 1 : 0;
  flag[thread_id].store(1);
  victim.store(thread_id);
  while (victim.load() == thread_id
         && flag[j] == 1);
}
```

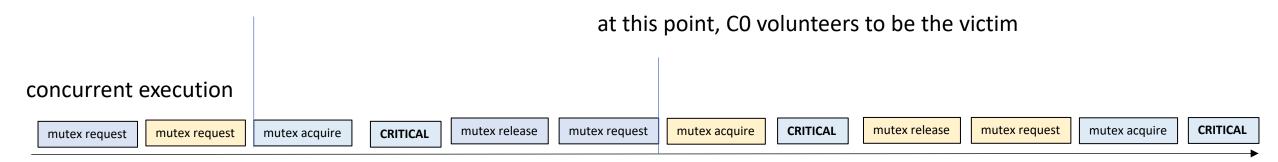


```
void lock() {
  int j = thread_id == 0 ? 1 : 0;
  flag[thread_id].store(1);
  victim.store(thread_id);
  while (victim.load() == thread_id
         && flag[j] == 1);
}
```



Threads take turns in petersons algorithm. It is starvation free

```
void lock() {
  int j = thread_id == 0 ? 1 : 0;
  flag[thread_id].store(1);
  victim.store(thread_id);
  while (victim.load() == thread_id
         && flag[j] == 1);
}
```



Peterson only works with 2 threads.

Generalizes to the Filter Lock (Read chapter 2 in the book, part 1 of your homework!)

Check implementations

- Thread sanitizer provided in Clang
- Checks for "data races"
 - Generally can help you check if you've used mutexes correctly (protecting all shared memory accesses).
 - Also: If you don't implement your mutexes correctly, you will probably have data races
 - This should hold for your next assignments too
 - Can also check for deadlock based on lock inversion
- Checking tool: if you pass, it doesn't mean your code is correct

Check implementations

Why not run all the time with thread sanitizer?

Back to Mutex Implementations

Peterson only works with 2 threads.

Generalizes to the Filter Lock (Read chapter 2 in the book, part 1 of your homework!)

Historical perspective

- These locks are not very performant compared to modern solutions
 - Your HW will show this
- However, they are academically interesting: they can be implemented with plain loads and stores

 We will now turn our attention to more performant implementations that use RMWs

Start by revisiting our first mutex implementation

- A first attempt:
 - A mutex contains a boolean.
 - The mutex value set to 0 means that it is free. 1 means that some thread is holding it.
 - To lock the mutex, you wait until it is set to 0, then you store 1 in the flag.
 - To unlock the mutex, you set the mutex back to 0.
- Let's remember why it was buggy

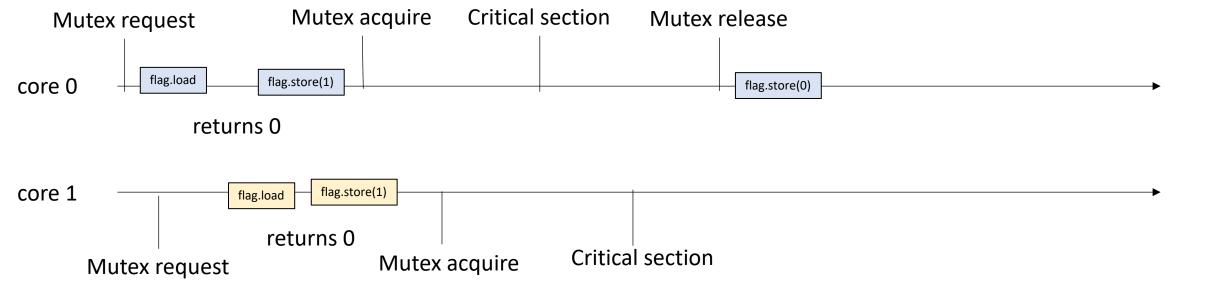
```
Buggy Mutex implementation: Analysis
```

```
void lock() {
  while (flag.load() == 1);
  flag.store(1);
}
```

```
void unlock() {
  flag.store(0);
}
```

```
Thread 0: Thread 1:
m.lock();
m.unlock();
m.unlock();
```

Critical sections overlap! This mutex implementation is not correct!



What went wrong?

- The load and stores from two threads interleaved
 - What if there was a way to prevent this?

What went wrong?

- The load and stores from two threads interleaved
 - What if there was a way to prevent this?

- Atomic RMWs
 - operate on atomic types (we already have atomic types)
 - recall the non-locking bank accounts:
 atomic fetch add(atomic *a, value v);

What is a RMW

A read-modify-write consists of:

- read
- modify
- write

done atomically, i.e. they cannot interleave.

Typically returns the value (in some way) from the read.

atomic_fetch_add

Recall the lock free account

Atomic Read-modify-write (RMWs): primitive instructions that implement a read event, modify event, and write event indivisibly, i.e. it cannot be interleaved.

```
atomic_fetch_add(atomic_int * addr, int value) {
   int tmp = *addr; // read
   tmp += value; // modify
   *addr = tmp; // write
}
```

atomic_fetch_add

Recall the lock free account

Atomic Read-modify-write (RMWs): primitive instructions that implement a read event, modify event, and write event indivisibly, i.e. it cannot be interleaved.

```
int atomic_fetch_add(atomic_int * addr, int value) {
   int stash = *addr; // read
   int new_value = value + stash; // modify
   *addr = new_value; // write
   return stash; // return previous value in the memory location
}
```

Tyler's coffee addiction:

<u>Tyler's employer</u>

atomic_fetch_add(&tylers_account, -1);

atomic_fetch_add(&tylers_account, 1);

time

Tyler's coffee addiction:

Tyler's employer

atomic_fetch_add(&tylers_account, -1);

atomic_fetch_add(&tylers_account, 1);

```
atomic fetch add(&tylers account, -1);
```

time

atomic_fetch_add(&tylers_account, 1);

Tyler's coffee addiction:

Tyler's employer

```
atomic_fetch_add(&tylers_account, -1); at
```

```
atomic_fetch_add(&tylers_account, 1);
```

time

```
tmp = tylers_account.load();
tmp -= 1;
tylers_account.store(tmp);
```

```
tmp = tylers_account.load();
tmp += 1;
tylers_account.store(tmp);
```

Tyler's coffee addiction:

Tyler's employer

```
atomic_fetch_add(&tylers_account, -1); atomic_fetch_add(&tylers_account, 1);
```

time

```
tmp = tylers_account.load();
tmp -= 1;
tylers_account.store(tmp);
```

cannot interleave!

```
tmp = tylers_account.load();
tmp += 1;
tylers_account.store(tmp);
```

Tyler's coffee addiction:

Tyler's employer

```
atomic_fetch_add(&tylers_account, -1);
```

```
atomic_fetch_add(&tylers_account, 1);
```

time

```
cannot interleave!
```

```
tmp = tylers_account.load();
tmp += 1;
tylers_account.store(tmp);
```

time

```
tmp = tylers_account.load();
tmp -= 1;
tylers_account.store(tmp);
```

either way, account breaks even at the end!

RMW-based locks

A few simple RMWs enable lots of interesting mutex implementations

 When we have simpler implementations, we can focus on performance

• Simplest atomic RMW will allow us to implement an:

N-threaded mutex with 1 bit!

```
value atomic_exchange(atomic *a, value v);
```

Loads the value at a and stores the value in v at a. Returns the value that was loaded.

```
value atomic_exchange(atomic *a, value v);
```

Loads the value at a and stores the value in \forall at a. Returns the value that was loaded.

```
value atomic_exchange(atomic *a, value v) {
  value tmp = a.load();
  a.store(v);
  return tmp;
}
```

```
#include <atomic>
using namespace std;
class Mutex {
public:
  Mutex() {
    flag = false;
  void lock();
  void unlock();
private:
  atomic_bool flag;
```

Lets make a mutex with just one atomic bool!

```
#include <atomic>
using namespace std;
class Mutex {
public:
  Mutex() {
    flag = false;
  void lock();
  void unlock();
private:
  atomic_bool flag;
```

Lets make a mutex with just one atomic bool!

initialized to false

one atomic flag

```
#include <atomic>
using namespace std;
class Mutex {
public:
  Mutex() {
    flag = false;
  void lock();
  void unlock();
private:
  atomic_bool flag;
```

Lets make a mutex with just one atomic bool!

initialized to false

main idea:

The flag is false when the mutex is free.

The flag is true when some thread has the mutex.

one atomic flag

```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

So what's going on?

```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

Two cases:

So what's going on?

mutex is free: the value loaded is false. We store true. The value returned is False, so we don't spin

mutex is taken: the value loaded is true, we put the SAME value back (true). The returned value is true, so we spin.

```
void unlock() {
  flag.store(false);
}
```

Unlock is simple: just store false to the flag, marking the mutex as available.

core 1

```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
Thread 0: Thread 1:
m.lock(); m.lock();
m.unlock();
```

```
void unlock() {
  flag.store(false);
}
```

```
core 0
```

```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
Thread 0: Thread 1:
m.lock();
m.unlock();
m.unlock();
```

```
void unlock() {
  flag.store(false);
}
```

```
Mutex request

core 0

EXCH()

returns false
```

core 1

```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
Thread 0: Thread 1:
m.lock(); m.lock();
m.unlock();
```

```
void unlock() {
  flag.store(false);
}
```

```
Mutex request Mutex acquire

core 0

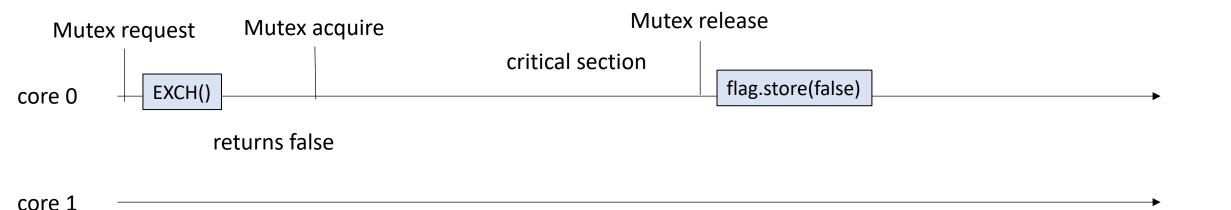
EXCH()

returns false
```

```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
Thread 0: Thread 1:
m.lock(); m.lock();
m.unlock();
```

```
void unlock() {
  flag.store(false);
}
```



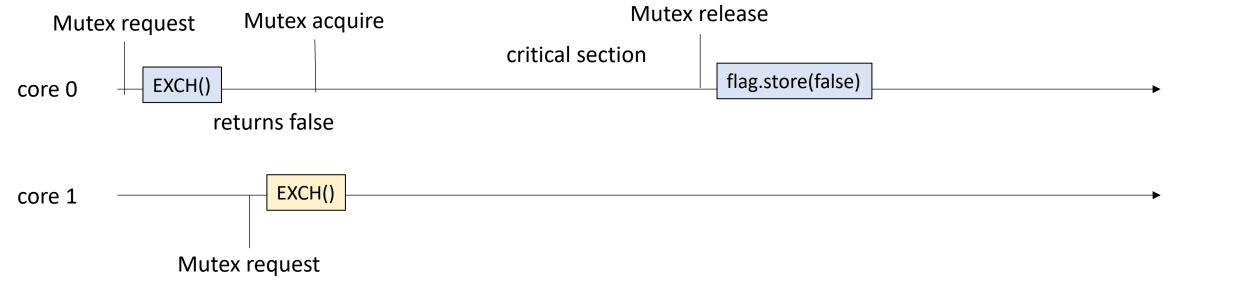
```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
void unlock() {
                                                                     flag.store(false);
  Thread 0:
                      Thread 1:
  m.lock();
                      m.lock();
  m.unlock();
                 m.unlock();
                                                                                     mutex works
                                                                                     with one thread
                                                   Mutex release
                  Mutex acquire
   Mutex request
                                        critical section
                                                           flag.store(false)
           EXCH()
core 0
                returns false
core 1
```

```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
Thread 0: Thread 1:
m.lock();
m.unlock();
m.unlock();
```

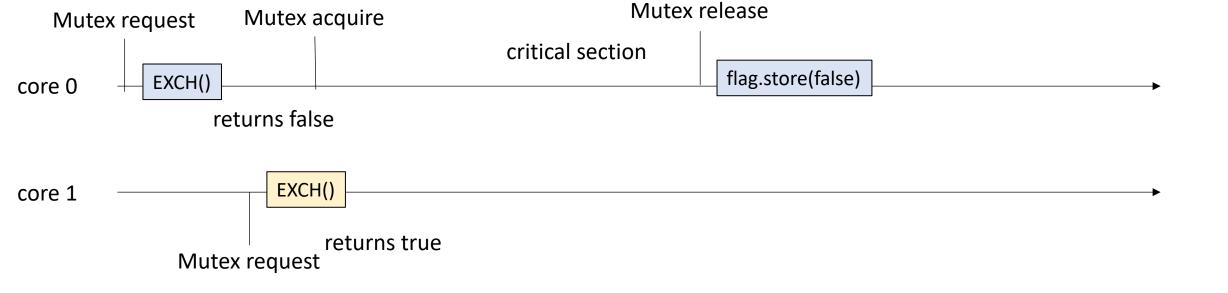
```
void unlock() {
  flag.store(false);
}
```



```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
Thread 0: Thread 1:
m.lock();
m.unlock();
m.unlock();
```

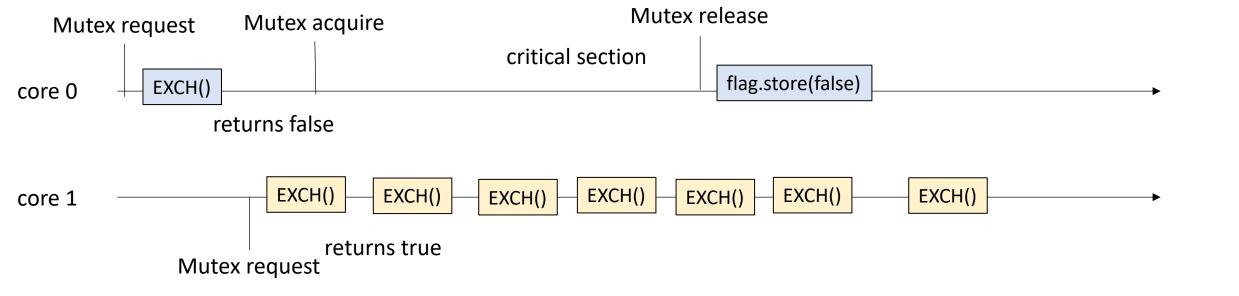
```
void unlock() {
  flag.store(false);
}
```



```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
Thread 0: Thread 1:
m.lock();
m.unlock();
m.unlock();
```

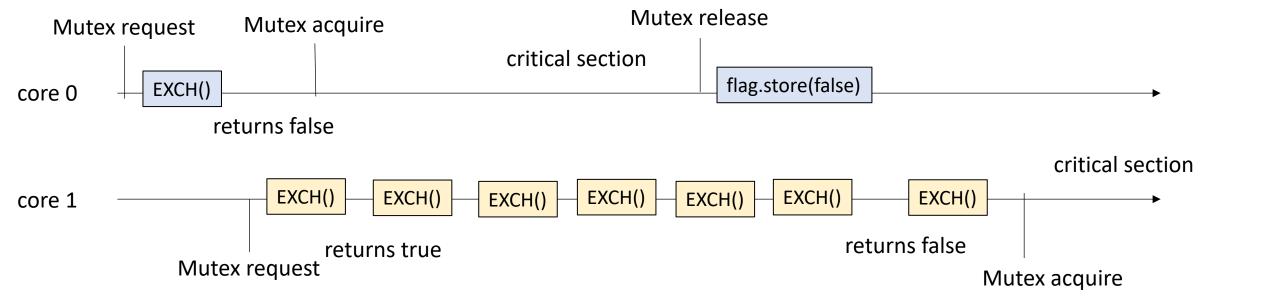
```
void unlock() {
  flag.store(false);
}
```



```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
Thread 0: Thread 1:
m.lock(); m.lock();
m.unlock();
```

```
void unlock() {
  flag.store(false);
}
```

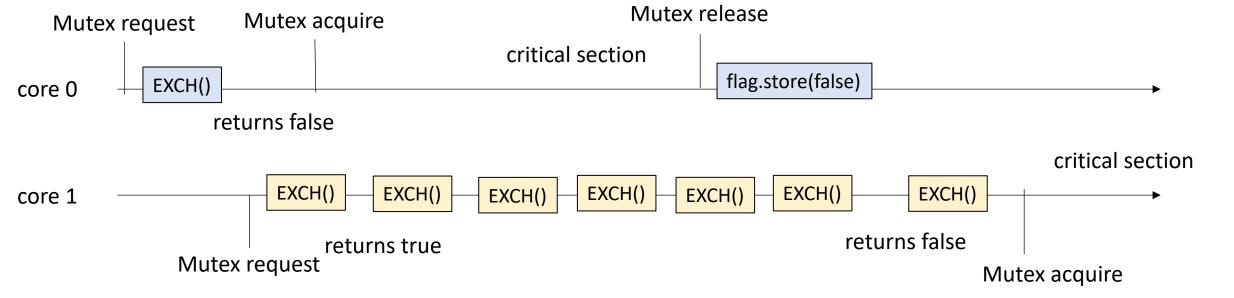


```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
Thread 0: Thread 1:
m.lock(); m.lock();
m.unlock();
```

```
void unlock() {
  flag.store(false);
}
```

what about interleavings?



```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

what about 4 threads?

```
void unlock() {
  flag.store(false);
}
```

```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
void unlock() {
  what about 4 threads?
                                                                        flag.store(false);
                  atomic operations can't overlap
        Mutex request
                                EXCH()
core 0
         Mutex request
core 1
                                EXCH()
         Mutex request
core 2
                                EXCH()
         Mutex request
core 3
                                EXCH()
```

```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
void unlock() {
  what about 4 threads?
                                                                        flag.store(false);
                  atomic operations can't overlap
        Mutex request
                                        EXCH()
core 0
         Mutex request
core 1
                                EXCH()
         Mutex request
core 2
                                                   EXCH()
         Mutex request
core 3
                                                               EXCH()
```

```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
void unlock() {
  what about 4 threads?
                                                                         flag.store(false);
                   atomic operations can't overlap
         Mutex request
                                         EXCH()
core 0
         Mutex request
core 1
                                EXCH()
                             this one will win
         Mutex request
core 2
                                                    EXCH()
         Mutex request
core 3
                                                                EXCH()
```

```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
void unlock() {
  what about 4 threads?
                                                                          flag.store(false);
                   atomic operations can't overlap
         Mutex request
                                          EXCH()
core 0
                                                  spin
         Mutex request
core 1
                                 EXCH()
                             this one will win
         Mutex request
core 2
                                                     EXCH()
                                                  spin
         Mutex request
                                                                 EXCH()
core 3
                                                                        spin
```

```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
void unlock() {
  what about 4 threads?
                                                                          flag.store(false);
                   atomic operations can't overlap
         Mutex request
                           EXCH()
core 0
                                   spin
         Mutex acquired
                             Critical section
core 1
         Mutex request
core 2
                                      EXCH()
                                           spin
         Mutex request
core 3
                                                 EXCH()
                                                         spin
```

```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
void unlock() {
  what about 4 threads?
                                                                            flag.store(false);
                   atomic operations can't overlap
         Mutex request
                            EXCH()
core 0
                                    spin
                                                  mutex release
         Mutex acquired
                              Critical section
                                                                  flag.store(false)
core 1
         Mutex request
core 2
                                        EXCH()
                                            spin
          Mutex request
core 3
                                                   EXCH()
                                                          spin
```

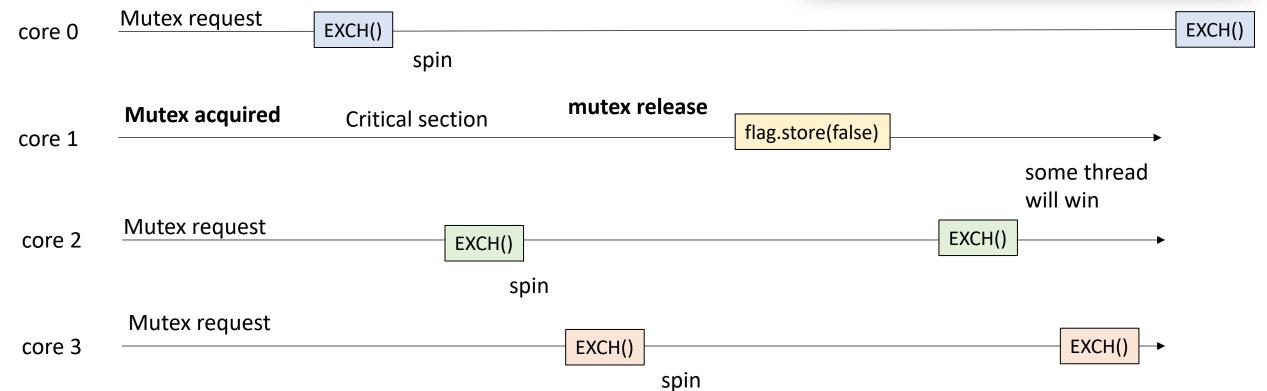
```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
void unlock() {
  what about 4 threads?
                                                                              flag.store(false);
                    atomic operations can't overlap
         Mutex request
                            EXCH()
                                                                                                             EXCH()
core 0
                                    spin
                                                   mutex release
         Mutex acquired
                              Critical section
                                                                   flag.store(false)
core 1
                                                                                              some thread
                                                                                              will win
         Mutex request
core 2
                                                                                       EXCH()
                                        EXCH()
                                             spin
          Mutex request
core 3
                                                                                                  EXCH()
                                                    EXCH()
                                                            spin
```

```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

what about 4 threads?

void unlock() {
 flag.store(false);
}



First example: Exchange Mutex

• Questions?

Exchange was the simplest RMW (no modify)

```
bool atomic compare exchange strong(atomic *a, value *expected, value replace);
```

Exchange was the simplest RMW (no modify)

Most versatile RMW: Compare-and-swap (CAS)

```
bool atomic_compare_exchange_strong(atomic *a, value *expected, value replace);
```

Checks if value at a is equal to the value at expected. If it is equal, swap with replace. returns True if the values were equal. False otherwise.

Exchange was the simplest RMW (no modify)

Most versatile RMW: Compare-and-swap (CAS)

```
bool atomic_compare_exchange_strong(atomic *a, value *expected, value replace);
```

Checks if value at a is equal to the value at expected. If it is equal, swap with replace. returns True if the values were equal. False otherwise.

expected is passed by reference: the previous value at a is returned

Exchange was the simplest RMW (no modify)

```
bool atomic_compare_exchange_strong(atomic *a, value *expected, value replace) {
    value tmp = a.load();
    if (tmp == *expected) {
        a.store(replace);
        return true;
    }
    *expected = tmp;
    return false;
}
```

Exchange was the simplest RMW (no modify)

we will discuss this soon!

```
bool atomic_compare_exchange_strong(atomic *a, value *expected, value replace) {
   value tmp = a.load();
   if (tmp == *expected) {
       a.store(replace);
       return true;
   }
   *expected = tmp;
   return false;
}
```

```
bool atomic compare exchange strong(atomic *a, value *expected, value replace) {
   value tmp = a.load();
   if (tmp == *expected) {
     a.store(replace);
     return true;
   *expected = tmp;
   return false;
   thread 0:
   // some atomic int address a
   int e = 0;
                                                             a:0
   bool s = atomic CAS(a, \&e, 6);
```

```
bool atomic compare exchange strong(atomic *a, value *expected, value replace) {
   value tmp = a.load();
   if (tmp == *expected) {
     a.store(replace);
     return true;
   *expected = tmp;
   return false;
   thread 0:
   // some atomic int address a
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                                                             a:0
   bool s = atomic CAS(a, \&e, 6);
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```
bool atomic compare exchange strong(atomic *a, value *expected, value replace) {
   value tmp = a.load();
   if (tmp == *expected) {
     a.store(replace);
     return true;
   *expected = tmp;
   return false;
   thread 0:
   // some atomic int address a
   int e = 0;
                                                             a:6
   bool s = atomic CAS(a, &e, 6);
```

```
bool atomic compare exchange strong(atomic *a, value *expected, value replace) {
   value tmp = a.load();
   if (tmp == *expected) {
     a.store(replace);
     return true;
   *expected = tmp;
   return false;
   thread 0:
   // some atomic int address a
   int e = 0;
                                                              a:6
   bool s = atomic CAS(a, \&e, 6);
       true
```

```
bool atomic compare exchange strong(atomic *a, value *expected, value replace) {
   value tmp = a.load();
   if (tmp == *expected) {
     a.store(replace);
     return true;
   *expected = tmp;
   return false;
                                       next example
   thread 0:
   // some atomic int address a
   int e = 0;
                                                             a:16
   bool s = atomic CAS(a, \&e, 6);
```

```
bool atomic compare exchange strong(atomic *a, value *expected, value replace) {
   value tmp = a.load();
   if (tmp == *expected) {
     a.store(replace);
     return true;
   *expected = tmp;
   return false;
   thread 0:
   // some atomic int address a
   int e = 0;
                                                             a:16
   bool s = atomic CAS(a, \&e, 6);
```

16

false

CAS lock

```
#include <atomic>
using namespace std;
class Mutex {
public:
  Mutex() {
    flag = false;
  void lock();
  void unlock();
private:
  atomic_bool flag;
```

Pretty intuitive: only 1 bit required again:

CAS lock

```
void lock() {
  bool e = false;
  int acquired = false;
  while (acquired == false) {
    acquired = atomic_compare_exchange_strong(&flag, &e, true);
    e = false;
  }
}
```

Check if the mutex is free, if so, take it.

compare the mutex to free (false), if so, replace it with taken (true). Spin while the thread isn't able to take the mutex.

CAS lock

```
void unlock() {
  flag.store(false);
}
```

Unlock is simple! Just store false back

Starvation

Are these RMW locks fair?

```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
void unlock() {
  flag.store(false);
}
```

```
mutex
request

core 0

mutex
request
core 1
```

```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
void unlock() {
  flag.store(false);
}
```

```
mutex request EXCH()

mutex request request

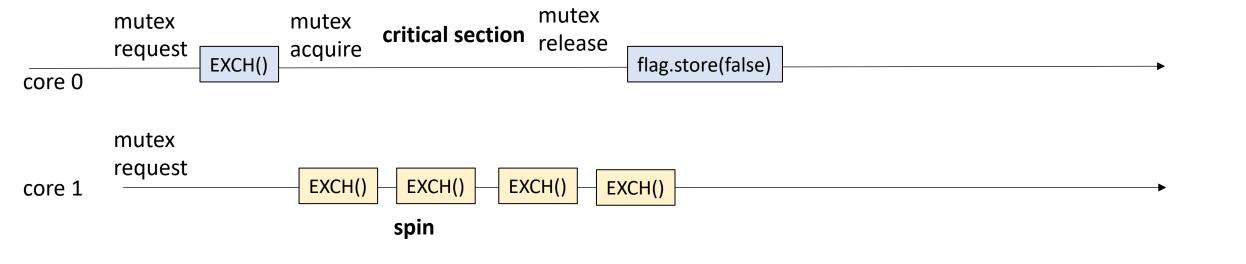
core 1

EXCH()

spin
```

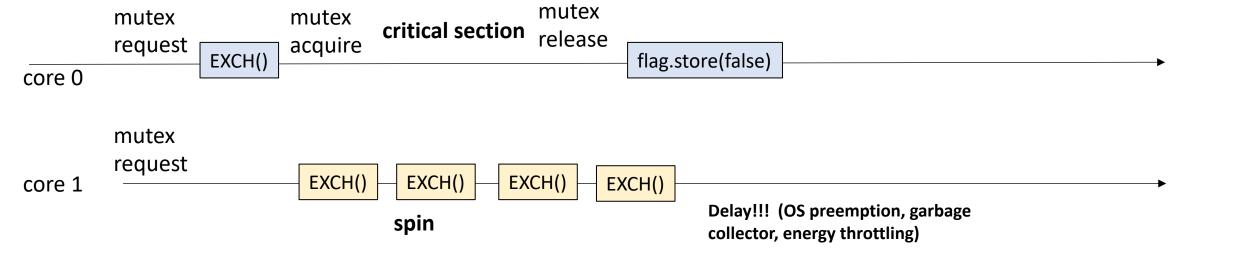
```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
void unlock() {
  flag.store(false);
}
```



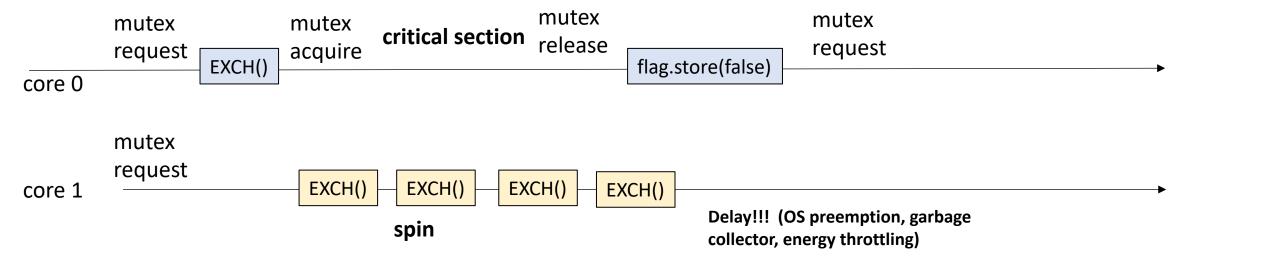
```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
void unlock() {
  flag.store(false);
}
```



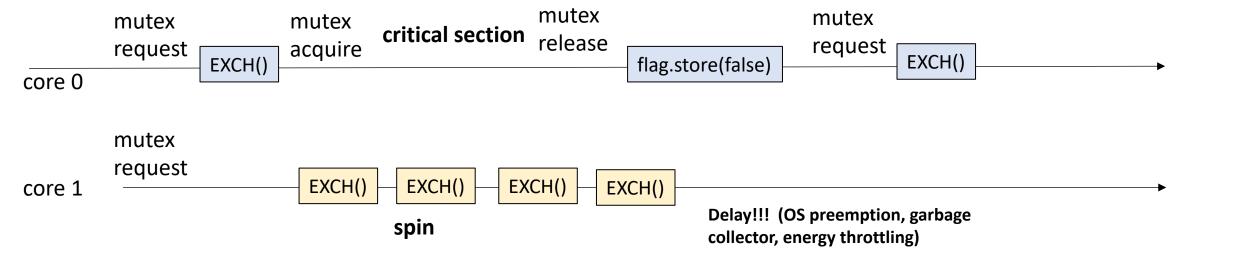
```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
void unlock() {
  flag.store(false);
}
```



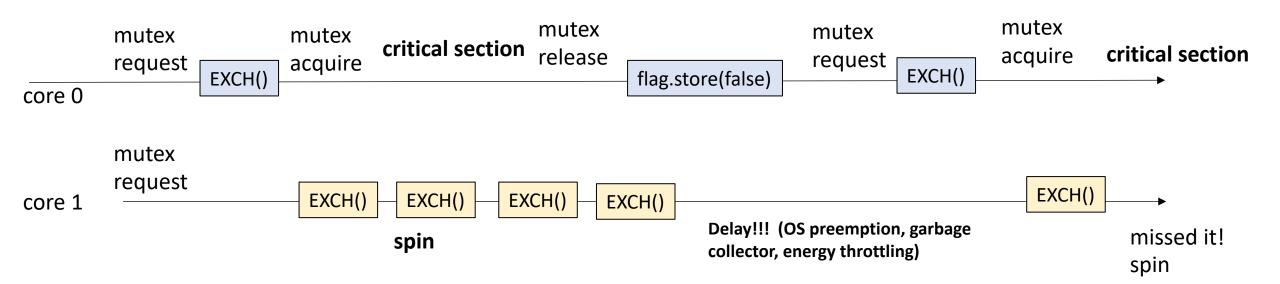
```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
void unlock() {
  flag.store(false);
}
```



```
void lock() {
  while (atomic_exchange(&flag, true) == true);
}
```

```
void unlock() {
  flag.store(false);
}
```



How about in practice?

• Code demo

Thanks!

- Next time:
 - practical mutual exclusion