## Problem Set I

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Alon Filler<sup>1</sup>

## 1 Automatas

Given the automata  $D = (Q^D, \{a, b\}, \delta^D, q_0^D, F^D)$ 

## Problem 1.1.

Imagine a new automata  $E = (Q^E, \{a, b\}, \delta^E, q_0^E, F^E)$  s.t:

- $\bullet \ Q^E = Q^D \cup \{q_0^E\}$
- $\bullet \ F^E = F^D$

$$\bullet \ \delta^E(q,\sigma) = \begin{cases} \delta^D(q,\sigma) & q \in Q^D \\ q_0^D & q = q_0^E, \sigma = a \\ q_0^E & q = q_0^E, \sigma = b \end{cases}$$

Define:

• *L(A)* 

## Solution.

It would be non but rational to divide this construction into three divisions, each corresponding to a different set of circumstances recognised by the trasitions function.

One of those aforementioned circumstances is  $q = q_0^E$ ,  $\sigma = b$ , the study of such case lead me to determine that for the character input of b, under the assumption that the current state is  $q_0^E$ , the state would lead back to itself, meaning that that an instance of  $\{b\}^*$  at the beginning of the input would not affect the output of the automata. And hence  $\{b\}^*$  should be imbued to the language L(A).

Another set of circumstances is  $q = q_0^E$ ,  $\sigma = a$ , which implies the current state to be the one added to  $Q^D$  in order to craft  $Q^E$ , and that the input chracter is 'a'. Such circumstances appear to be digested by the automata to return  $q_0^D$ , the first state of the previous automata D. Accordingly, it would only be after the appearance of an 'a' character in the input that the

 $<sup>^{1}</sup>$ With  $\Sigma$ orer

state would be changed. And hence,  $\{a\}$  must be added to the language L(A).

The last of such circumstances addressed in  $\delta^E$  appears to be  $q \in Q^D$ . For such case, the function would make the transition from the current state to the one returned by  $\delta^D$ , accordingly, L(D) must be concatenated at the end of L(E)

Hence - I may declare that 
$$L(A) = \{b\}^* \cdot \{a\} \cdot L(D)$$