

University of Tehran College of Engineering School of Electrical and Computer Engineering



Digital Communications Lab

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Prelab 3 - Part II

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Abstract

In this prelab we shall study the conversion of lowpass and bandpass signals to eachother, we shall study a realistic model of this conversion which has amplitude and phase errors.

1 Conversion of Lowpass Equivalent of Bandpass signals

1.1 Unideal conversion to lowpass equivalent

As we know the lowpass equivalent of a bandpass signal is extracted from the following equation.

$$x_{lp}(t) = x_i(t) + jx_q(t)$$

Now, we shall review the ideal conversion to freshen our minds.

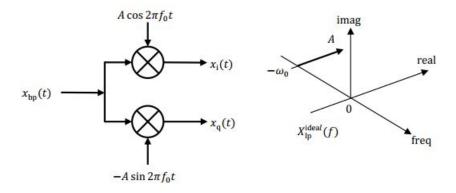


Figure 1: Ideal Structure

In this structure we can easily deduce:

$$x_{lp}(t) = Ax_{bp}(t)\cos(2\pi f_0 t) - jAx_{bp}(t)\sin(2\pi f_0 t) = Ax_{bp}(t)e^{-j2\pi f_0 t}$$

In the unideal realization of our structure, the quadrature part of the signal consists of two errors, amplitude (α) and phase (φ) .

For this case we have the following.

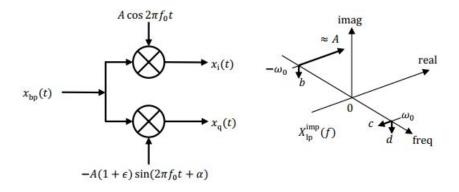


Figure 2: Unideal Structure

In this structure we can deduce:

$$x_{lp}(t) = Ax_{bp}(t)\cos(2\pi f_0 t) - jA(1+\varepsilon)x_{bp}(t)\sin(2\pi f_0 t + \alpha)$$

From trigonometry, we can rewrite the above term as:

$$x_{lp}(t) = Ax_{bp}(t)\cos(2\pi f_0 t) - jA(1+\varepsilon)x_{bp}(t)\left(\sin(2\pi f_0 t)\cos(\alpha) + \cos(2\pi f_0 t)\sin(\alpha)\right)$$

Now we use the exponential terms of the $\sin(.)$ and $\cos(.)$ function.

$$x_{lp}(t) = \frac{A}{2} x_{bp}(t) \left(e^{j2\pi f_0 t} + e^{-j2\pi f_0 t} \right)$$
$$- j \frac{A}{2} x_{bp}(t) \left(\frac{(\varepsilon + 1)\cos(\alpha)}{j} \left(e^{j2\pi f_0 t} - e^{-j2\pi f_0 t} \right) + (\varepsilon + 1)\sin(\alpha) \left(e^{j2\pi f_0 t} + e^{-j2\pi f_0 t} \right) \right)$$

Now we use the Fourier transform to go into the frequency domain, hence we have:

$$\mathscr{X}_{lp}(f) = \frac{A}{2} \left[\left(1 - e^{j\alpha} (\varepsilon + 1) \right) \mathscr{X}_{bp}(f - f_0) + \left(1 + e^{-j\alpha} (\varepsilon + 1) \right) \mathscr{X}_{bp}(f + f_0) \right]$$

It is obvious to us that $(1 - e^{j\alpha}(\varepsilon + 1))$ is undesirable and $(1 + e^{-j\alpha}(\varepsilon + 1))$ is desirable, so to find the range of ε and α we set one of them to zero and find the range of the other respectively, so we shall have:

$$P = \frac{1 - (1 + \varepsilon)e^{j\alpha}}{1 + (1 + \varepsilon)e^{-j\alpha}}$$

$$if \ \varepsilon = 0 \longrightarrow P = \left| \frac{1 - e^{j\alpha}}{1 + e^{j\alpha}} \right| \le 0.001 \longrightarrow 0.0006\pi \le \alpha \le 1.999\pi$$
$$if \alpha = 0 \longrightarrow P = \left| \frac{\varepsilon}{2 + \varepsilon} \right| \le 0.001 \longrightarrow |\varepsilon| \le 0.002$$