

Introduction to Deep Learning for Computer Vision

Adhyayan '23 - ACA Summer School
Department of Computer Science and Engineering
Indian Institute of Technology Kanpur

Lecture 1

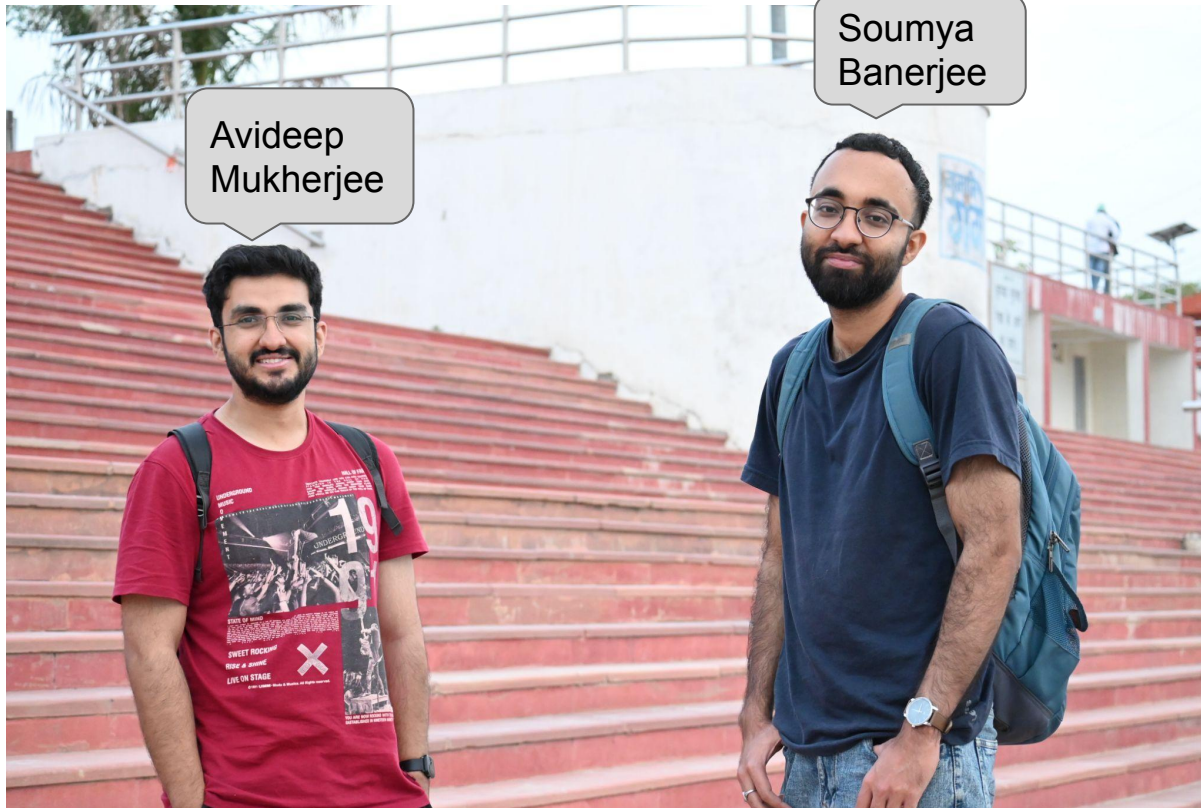
Instructors



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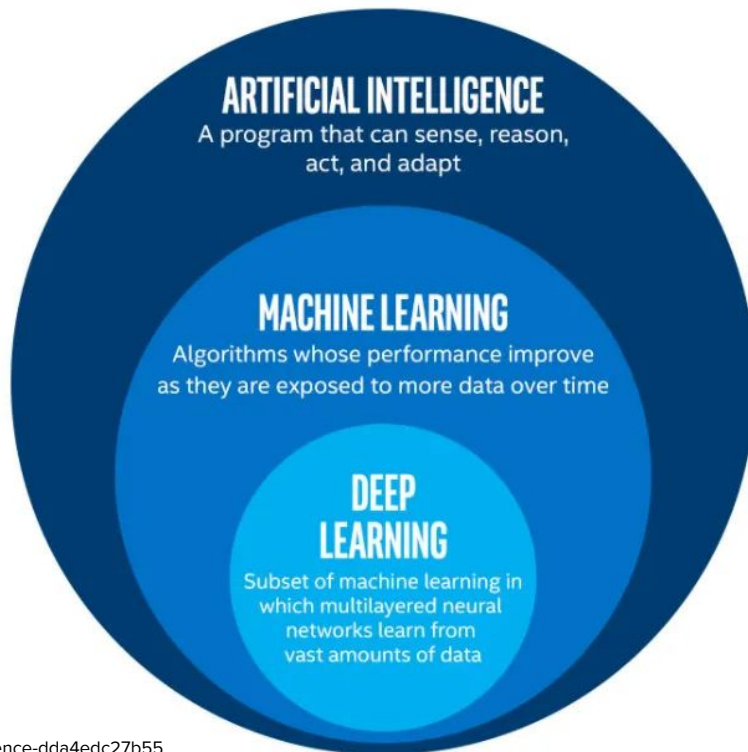
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Credits:

- <http://introtodeeplearning.com/>
- <https://towardsdatascience.com/cousins-of-artificial-intelligence-dda4edc27b55>
- <https://0space.org/c/2098-machine-learning-vs-deep-learning-examples-and-use-case>
- http://beamlab.org/deeplearning/2017/02/23/deep_learning_101_part1.html
- <https://anjali-dl.blogspot.com/2020/03/importance-of-activation-functions.html>

What is Deep Learning?



Lecture Schedule

- Week 1:
 - Perceptron, Multi-layer Perceptron, Activation and Loss Functions. Python and Numpy hands-on demo.
 - Backpropagation, Batch Gradient Descent, SGD, Mini-batch SGD. Regularisation and Optimization. Introduction to PyTorch hands-on demo.
 - Convolutional Neural Networks
 - Popular CNN architectures. CNN Hands-on demo with PyTorch.
 - Training NNs: Weight Init, Dropout, Learning Rate Scheduling, Early Stopping, Weight Decay, Data Augmentation and Normalization, Batch Norm.

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- Week 2:
 - Object Detection (R-CNN, Yolov3), Image Segmentation (FCN, U-Net)
 - Unsupervised Learning and Generative Modelling: Autoencoder, VAE
 - Self-Attention & ViT
 - Adversarial Autoencoders, GANs, Diffusion (very brief overview)
 - Assorted Topics: Self Supervised Learning (SimSiam, Contrastive Learning, Rotation Loss), Active learning

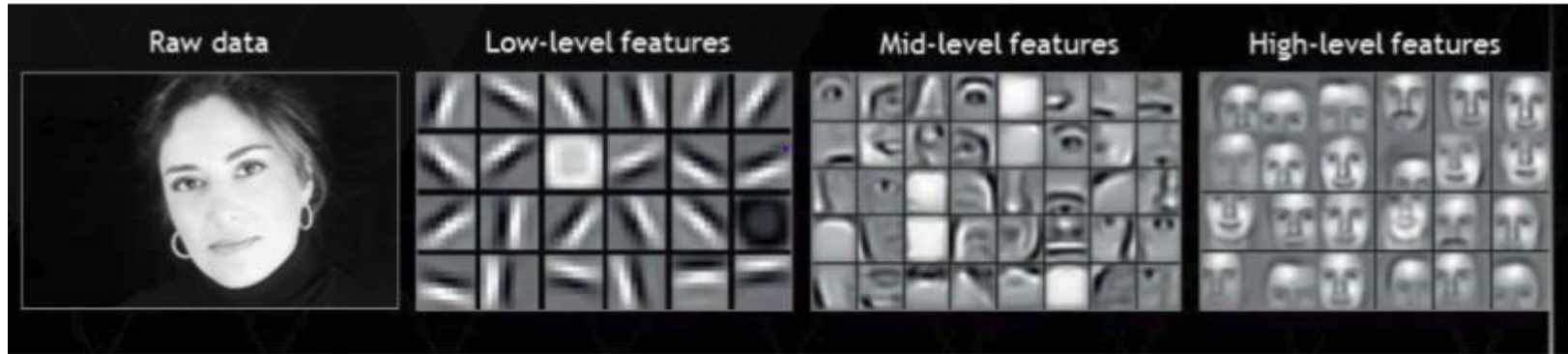
Grading Policy

- 1 Quiz after Week 1 (comprising of Week 1 syllabus) - 50% weight.
- 1 Quiz after Week 2 (comprising of whole syllabus) - 50% weight.

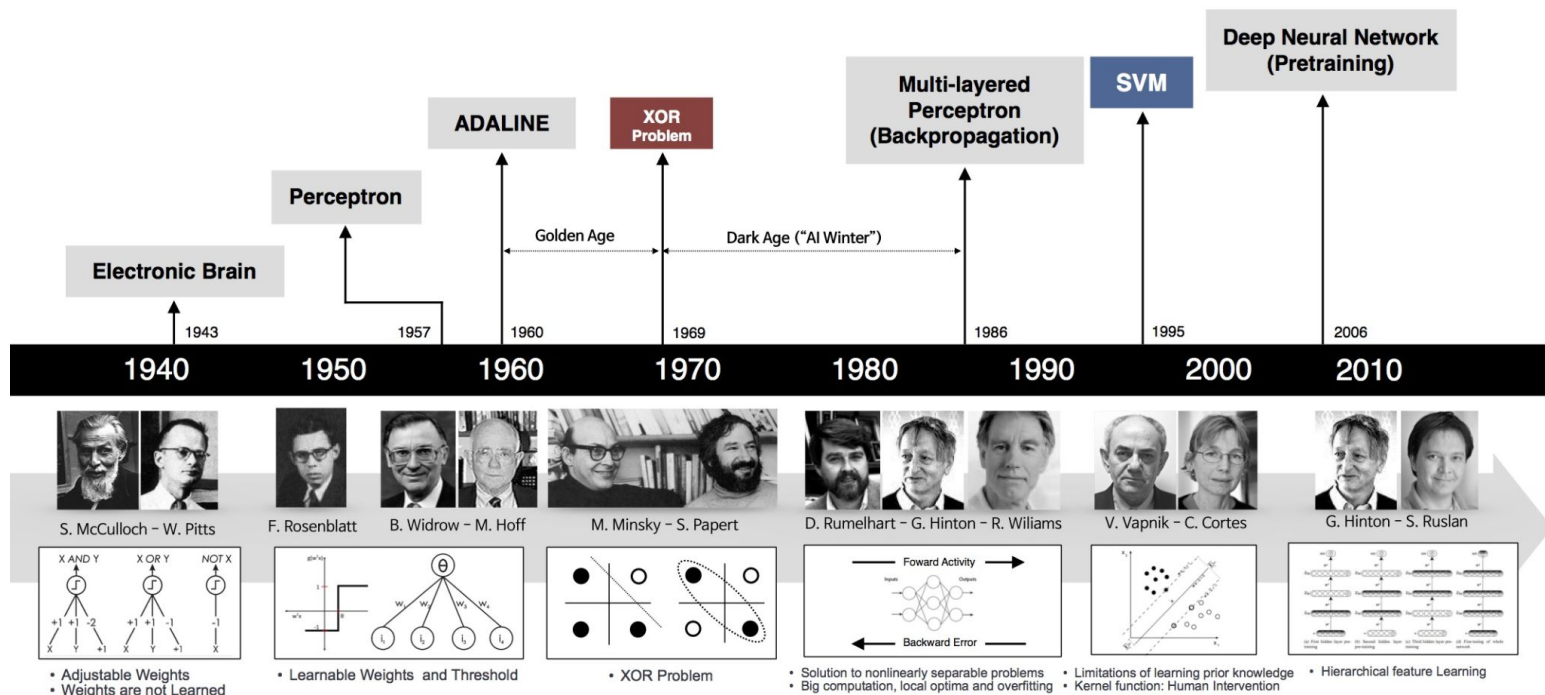
Why Deep Learning? And Why Now?

Why Deep Learning?

- Handcrafted features are expensive to engineer, delicate and unsuitable for scaling.
- Deep Learning attempts to *learn* the fundamental features directly from data.



Why Now?



Why Now?

- Big Data:
 - Larger datasets.
 - Easier storage facility.

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- Big Data:
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- Hardware:
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- Software:
 - Improved Techniques
 - Better Models
 - Better Frameworks

Perceptrons

The Perceptron

- Structural building block of deep learning.

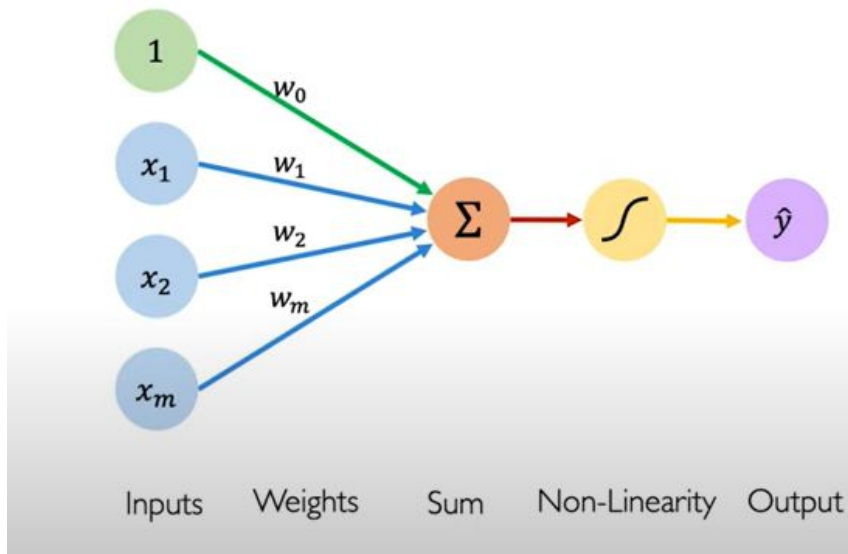


Diagram illustrating the mathematical representation of the perceptron output:

$$\hat{y} = g \left(w_0 + \sum_{i=1}^m x_i w_i \right)$$

Labels and arrows in the diagram:

- Output:** Points to \hat{y} (purple arrow).
- Linear combination of inputs:** Points to the summation term $w_0 + \sum_{i=1}^m x_i w_i$ (red arrow).
- Non-linear activation function:** Points to g (yellow arrow).
- Bias:** Points to w_0 (green arrow).

The Perceptron

- Structural building block of deep learning.

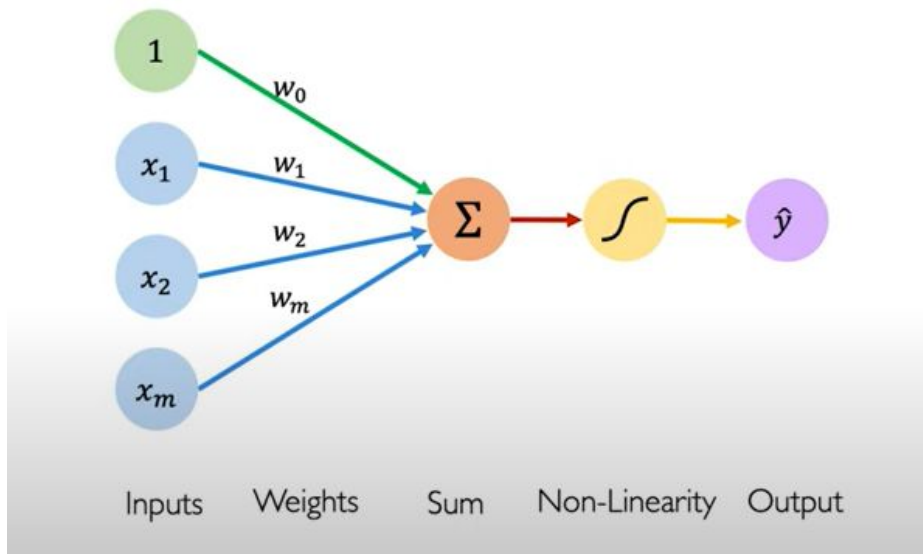


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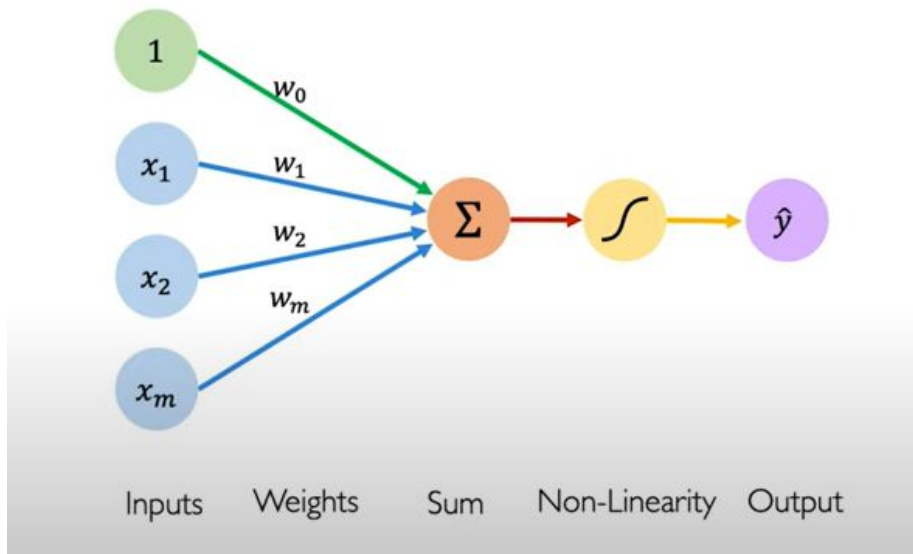
- Output: \hat{y}
- Linear combination of inputs: $w_0 + \sum_{i=1}^m x_i w_i$
- Non-linear activation function: g
- Bias: w_0

$$\hat{y} = g (w_0 + \mathbf{X}^T \mathbf{W})$$

where: $\mathbf{X} = \begin{bmatrix} x_1 \\ \vdots \\ x_m \end{bmatrix}$ and $\mathbf{W} = \begin{bmatrix} w_1 \\ \vdots \\ w_m \end{bmatrix}$

The Perceptron

- Structural building block of deep learning.

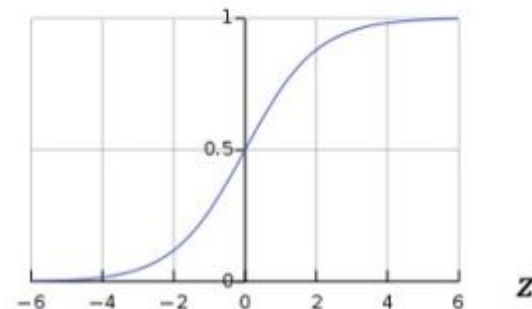


Activation Functions

$$\hat{y} = g(w_0 + \mathbf{X}^T \mathbf{W})$$

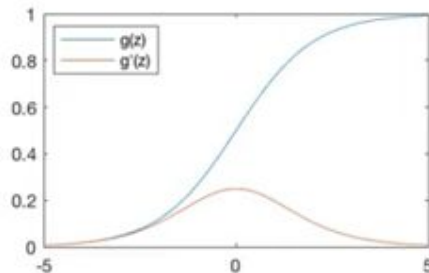
- Example: sigmoid function

$$g(z) = \sigma(z) = \frac{1}{1 + e^{-z}}$$



Common Activation Functions

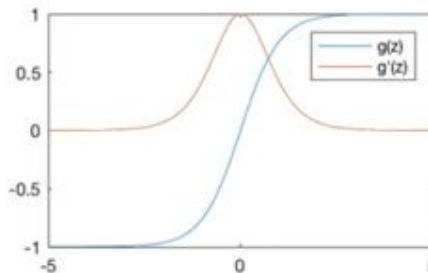
Sigmoid Function



$$g(z) = \frac{1}{1 + e^{-z}}$$

$$g'(z) = g(z)(1 - g(z))$$

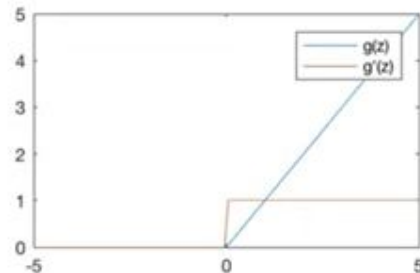
Hyperbolic Tangent



$$g(z) = \frac{e^z - e^{-z}}{e^z + e^{-z}}$$

$$g'(z) = 1 - g(z)^2$$

Rectified Linear Unit (ReLU)

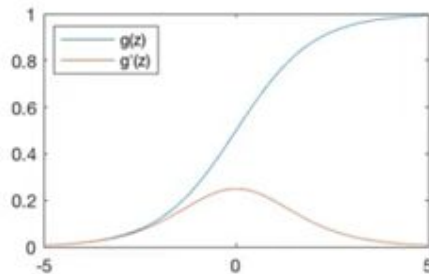


$$g(z) = \max(0, z)$$

$$g'(z) = \begin{cases} 1, & z > 0 \\ 0, & \text{otherwise} \end{cases}$$

Common Activation Functions

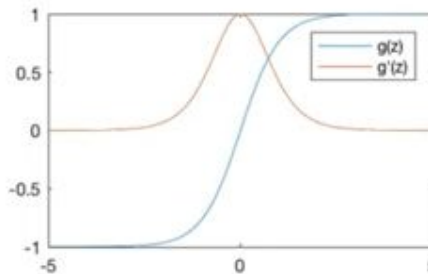
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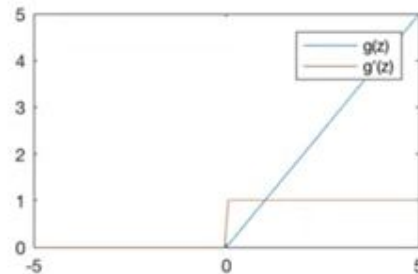
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Rectified Linear Unit (ReLU)



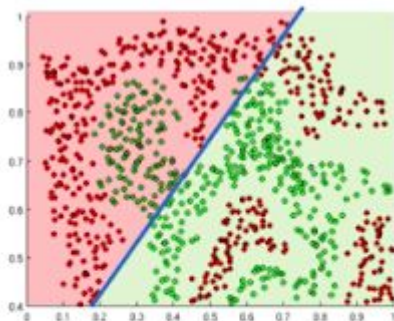
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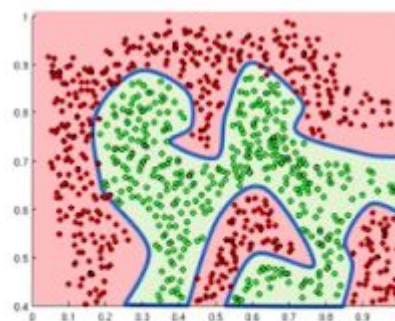
Note: All Activation functions are non-linear.

Importance of Activation Functions

- The purpose of Activation Functions is to introduce non-linearities in the network.

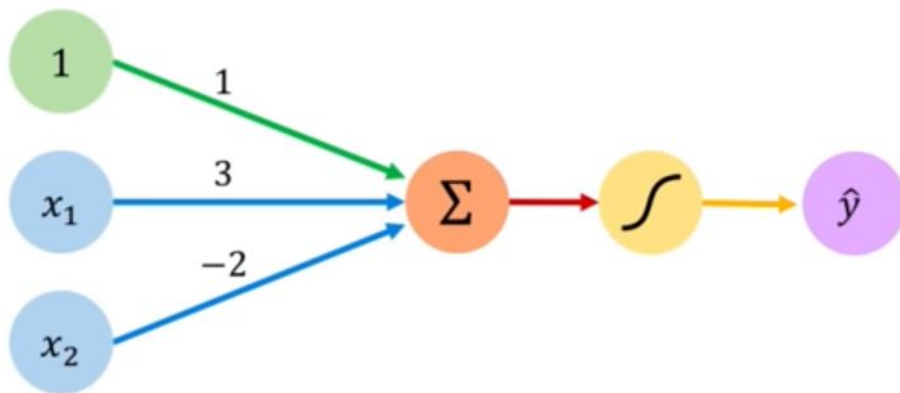


Linear activation functions produce linear decisions no matter the network size



Non-linearities allow us to approximate arbitrarily complex functions

Perceptron: Example

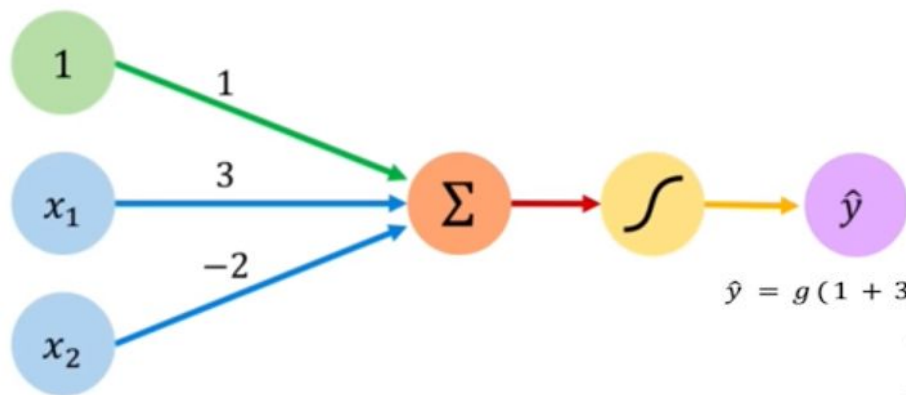


We have: $w_0 = 1$ and $\mathbf{W} = \begin{bmatrix} 3 \\ -2 \end{bmatrix}$

$$\begin{aligned}\hat{y} &= g(w_0 + \mathbf{X}^T \mathbf{W}) \\ &= g\left(1 + \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}^T \begin{bmatrix} 3 \\ -2 \end{bmatrix}\right) \\ \hat{y} &= g(1 + 3x_1 - 2x_2)\end{aligned}$$

This is just a line in 2D!

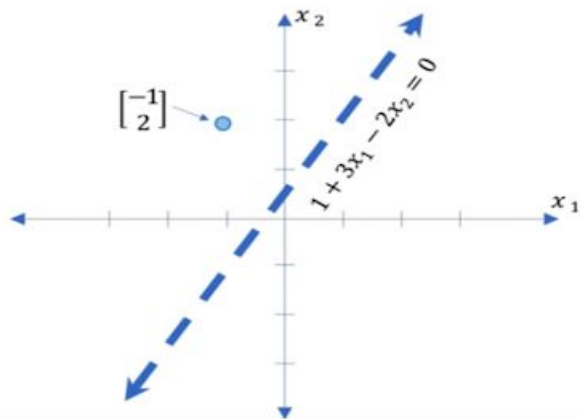
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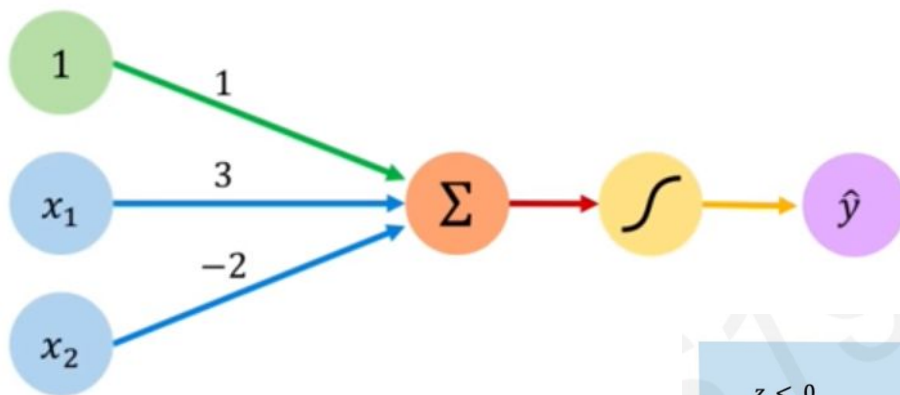
$$\hat{y} = g(1 + 3x_1 - 2x_2)$$



Assume we have input: $\mathbf{X} = \begin{bmatrix} -1 \\ 2 \end{bmatrix}$

$$\begin{aligned}\hat{y} &= g(1 + (3 * -1) - (2 * 2)) \\ &= g(-6) \approx 0.002\end{aligned}$$

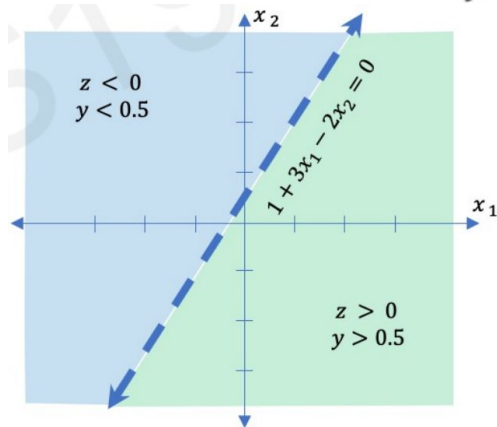
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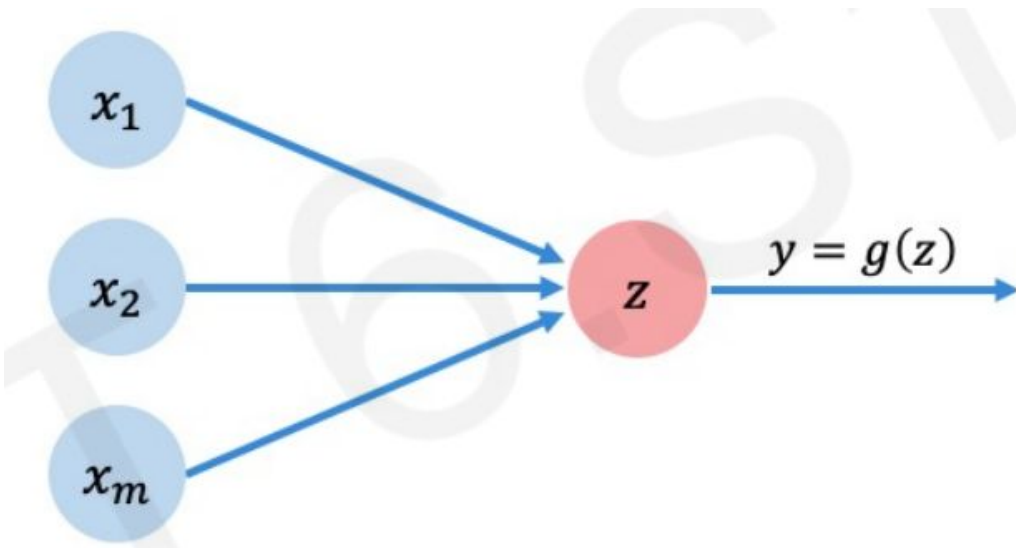
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Building Neural Networks with Perceptrons!

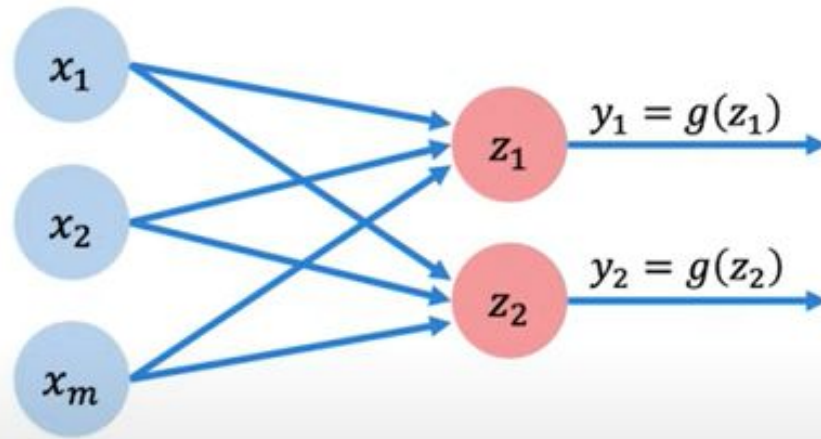
Perceptron: Simplified



$$z = w_0 + \sum_{j=1}^m x_j w_j$$

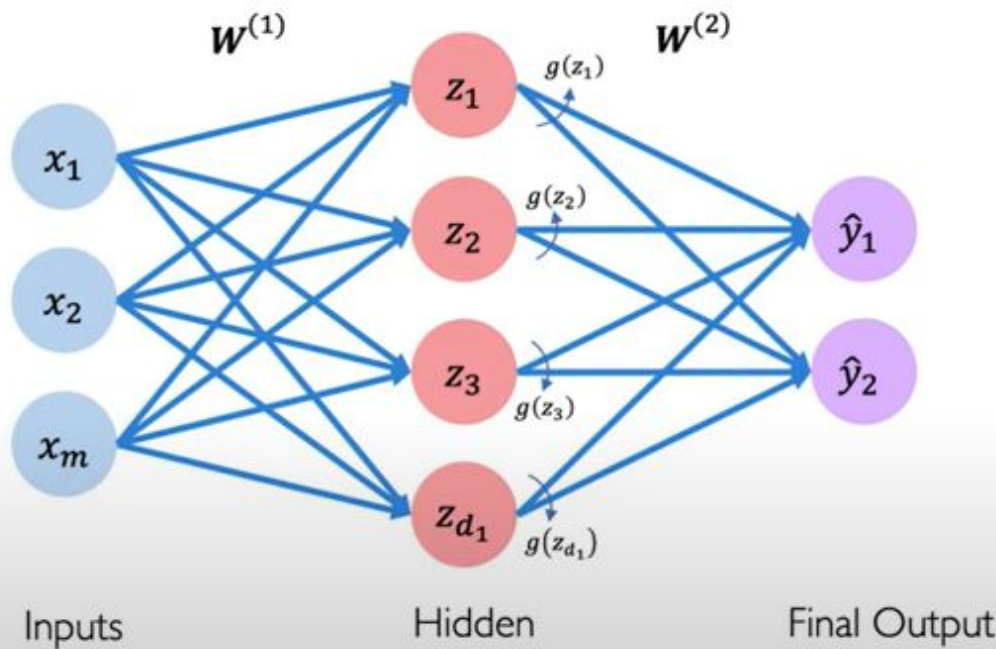
Multi Output Perceptron

Because all inputs are densely connected to all outputs, these layers are called **Dense** Layers.



$$z_i = w_{0,i} + \sum_{j=1}^m x_j w_{j,i}$$

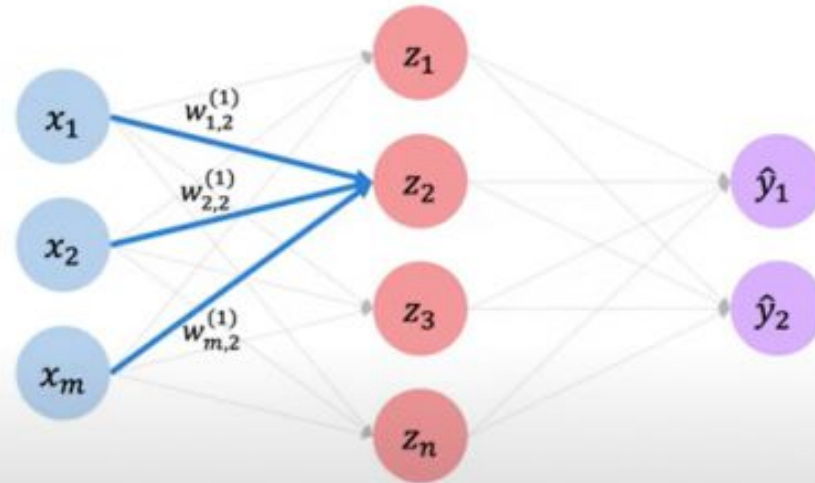
Single Layer Neural Network



$$z_i = w_{0,i}^{(1)} + \sum_{j=1}^m x_j w_{j,i}^{(1)}$$

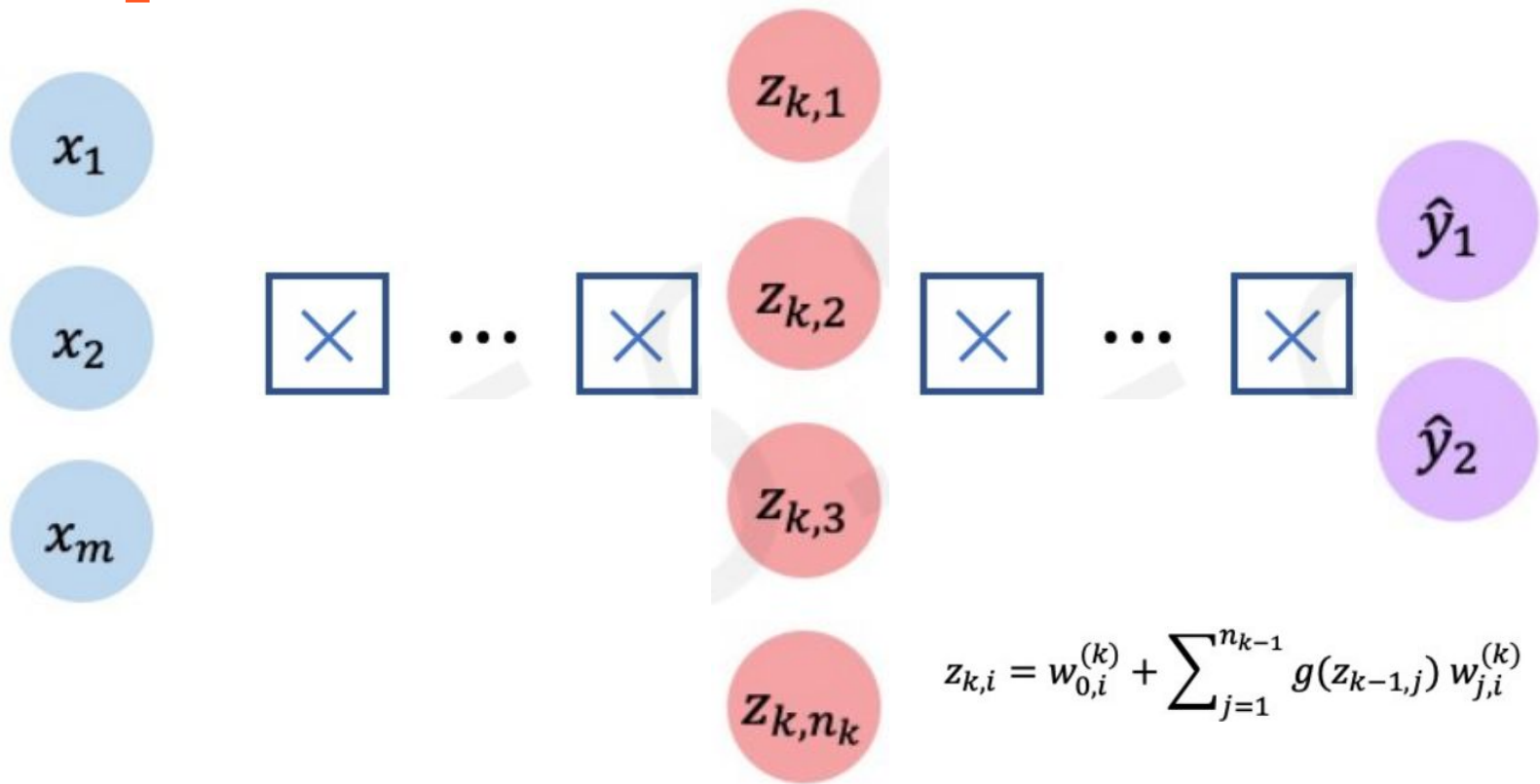
$$\hat{y}_i = g \left(w_{0,i}^{(2)} + \sum_{j=1}^{d_1} g(z_j) w_{j,i}^{(2)} \right)$$

Single Layer Neural Network



$$\begin{aligned} z_2 &= w_{0,2}^{(1)} + \sum_{j=1}^m x_j w_{j,2}^{(1)} \\ &= w_{0,2}^{(1)} + x_1 w_{1,2}^{(1)} + x_2 w_{2,2}^{(1)} + x_m w_{m,2}^{(1)} \end{aligned}$$

Deep Neural Network



Applying Neural Networks

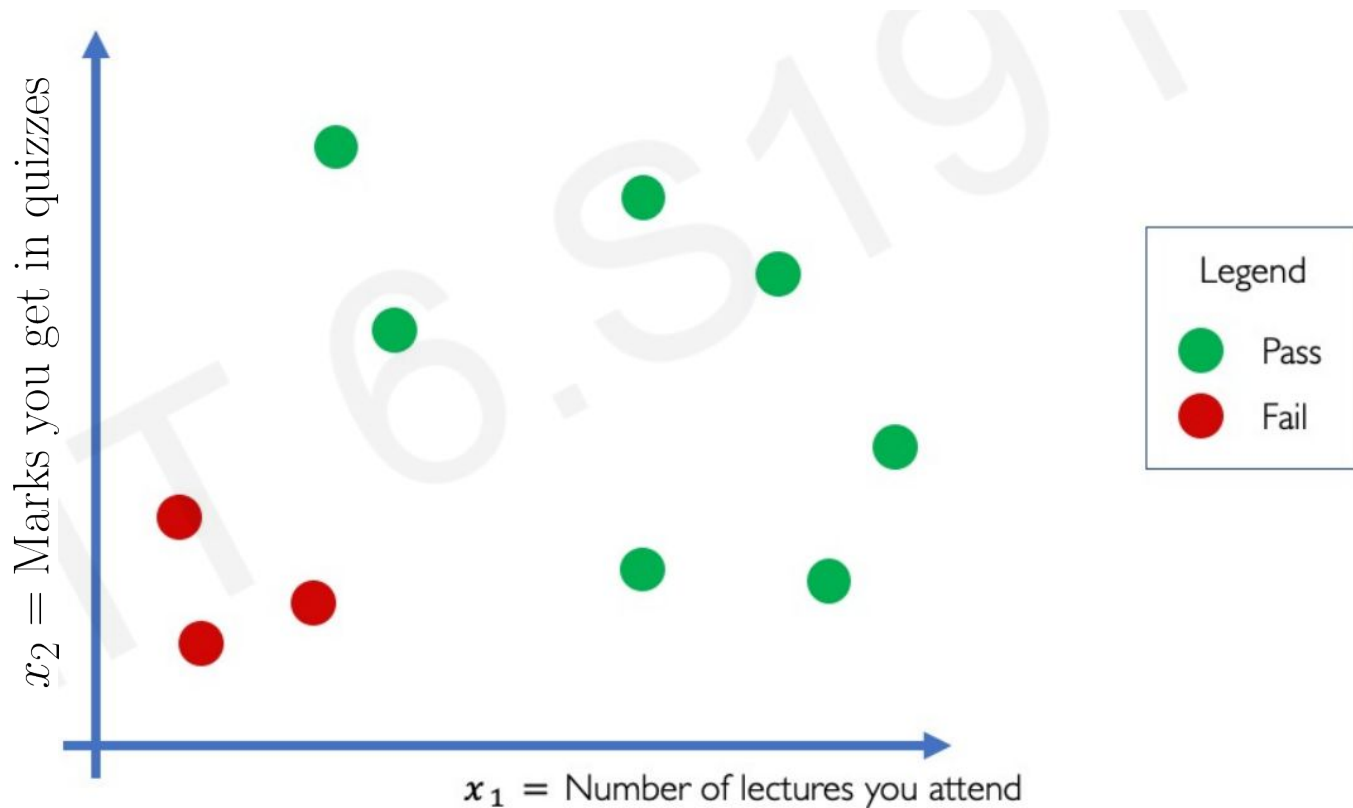
Example Problem

- Will I pass this course?
- Let us start with a simple two-feature model.

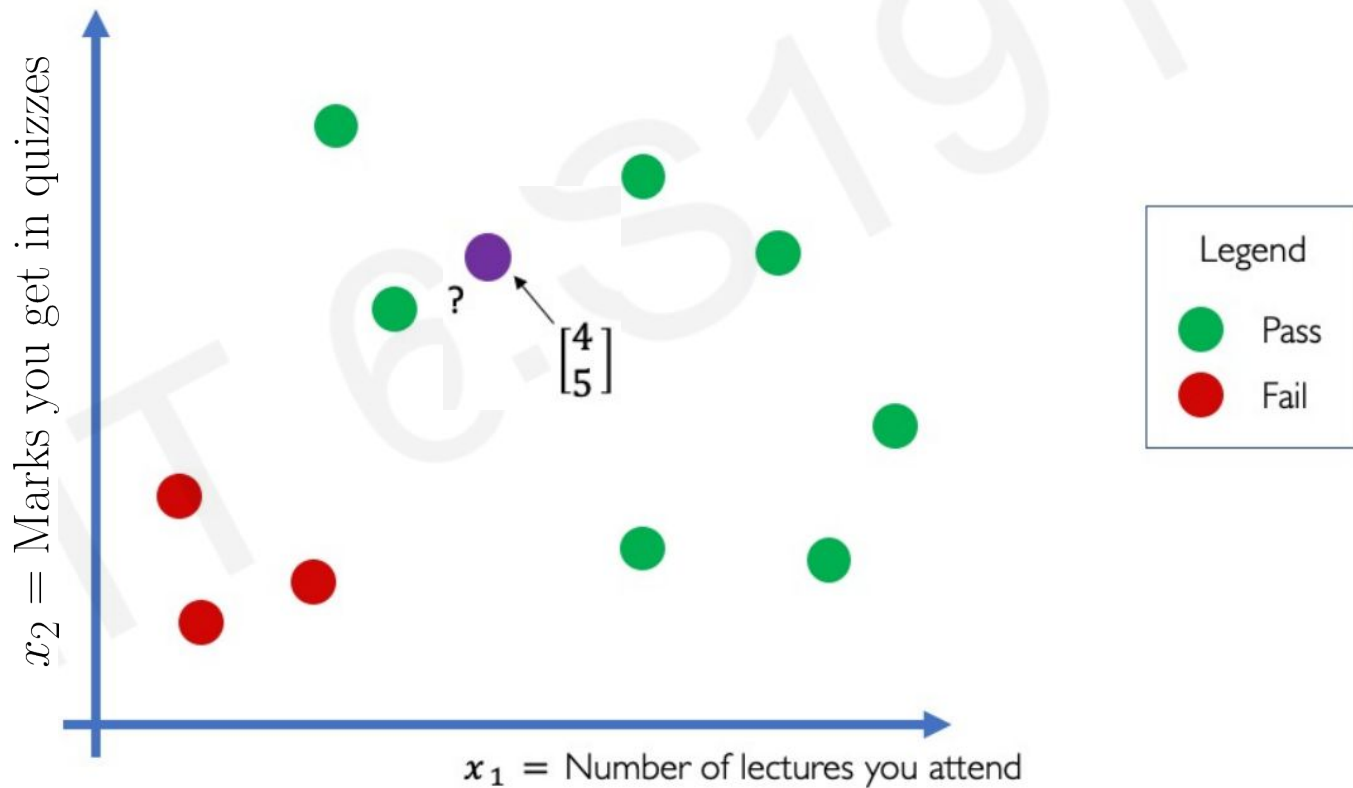
x_1 = Number of Lectures you attend

x_2 = Marks you get in quizzes

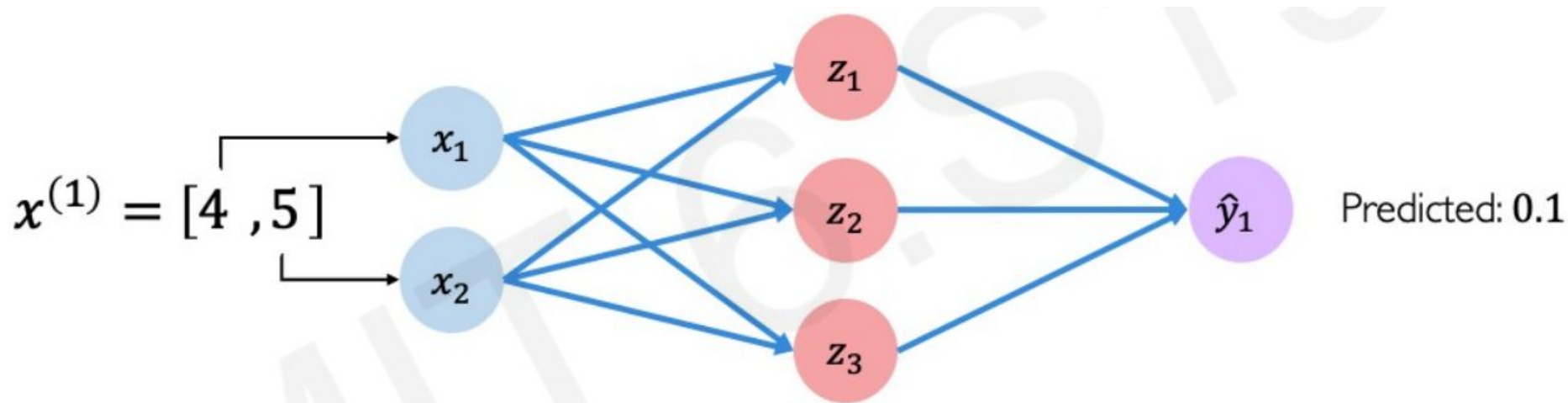
Example Problem: Will I pass this course?



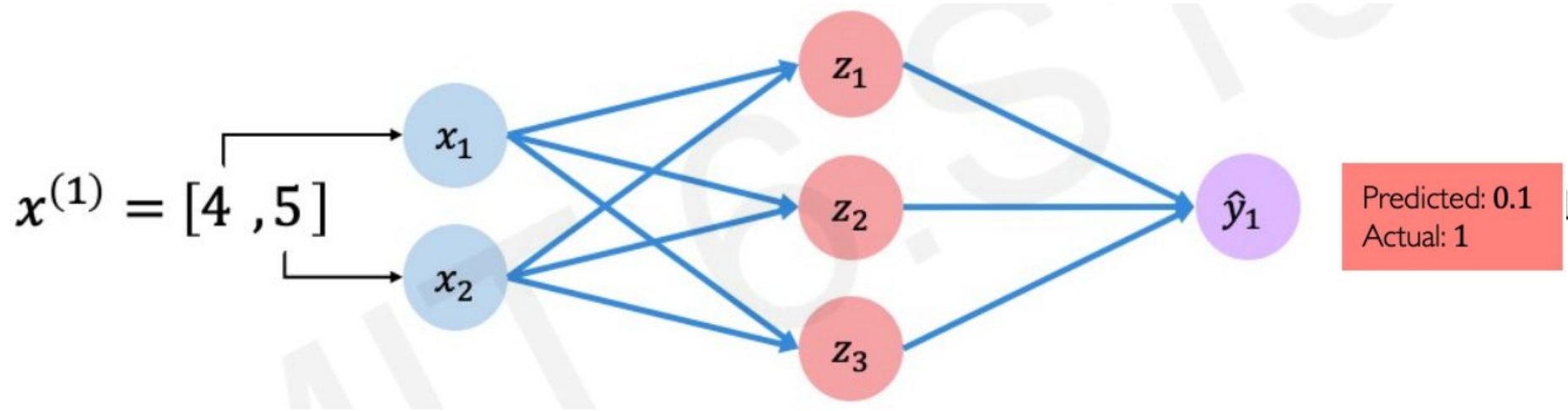
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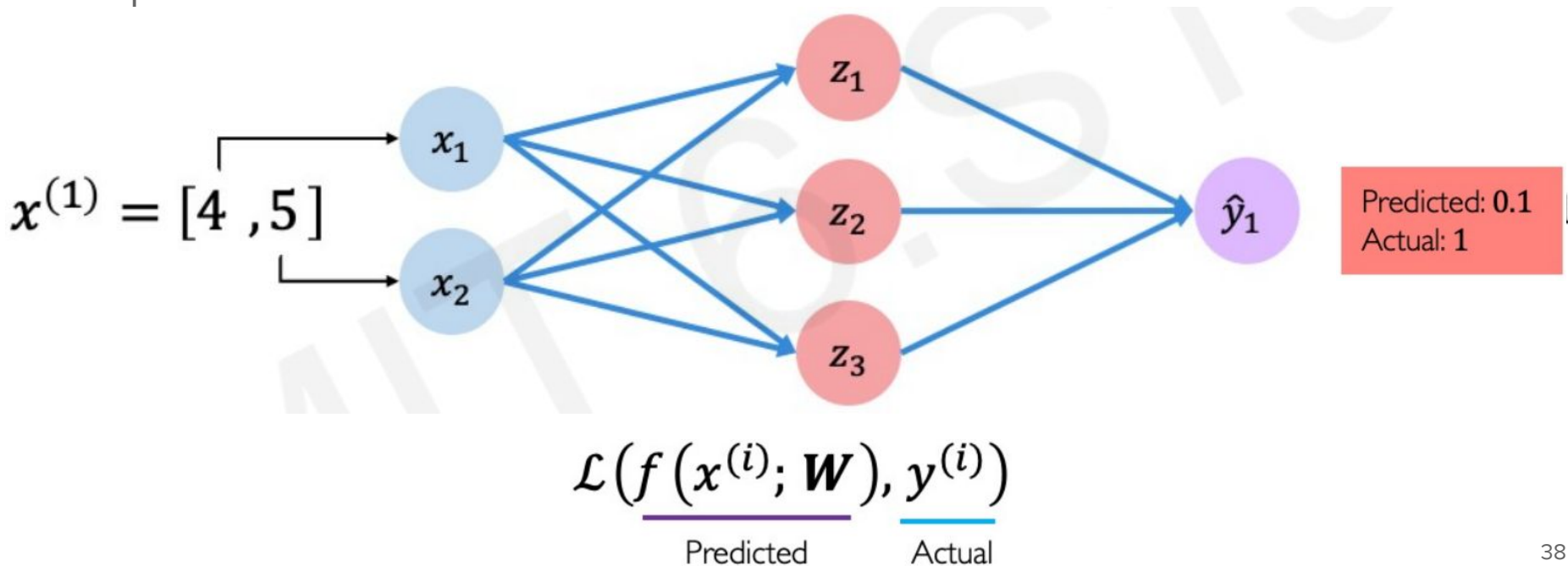


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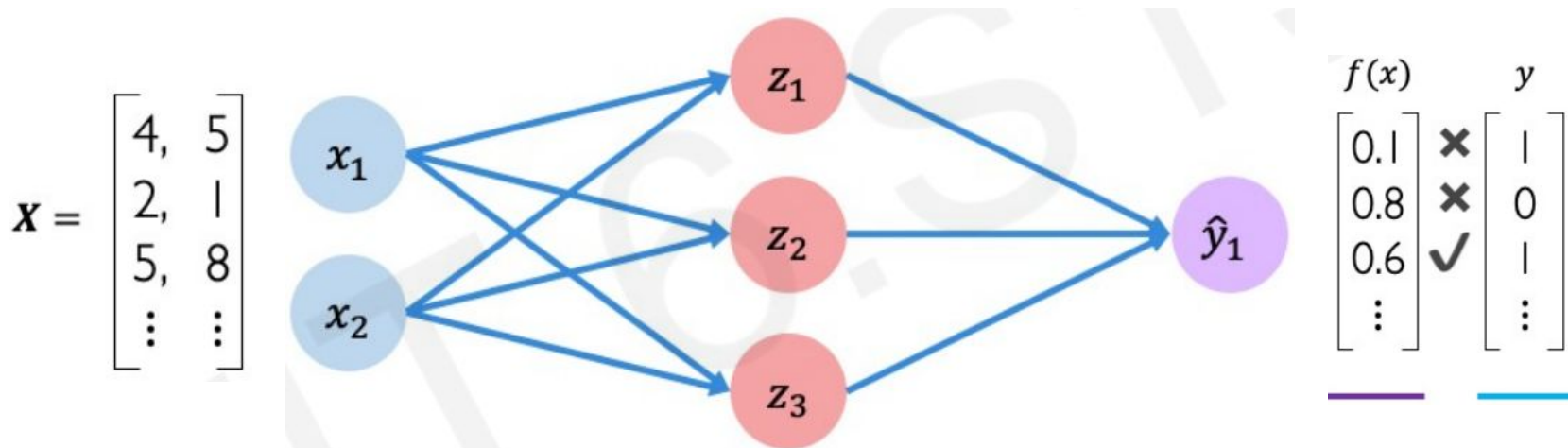
Quantifying the Loss

- The **Loss** of our Network measures the cost incurred from incorrect predictions.



Empirical Loss

- The **Empirical Loss** measures the total loss over our entire dataset.



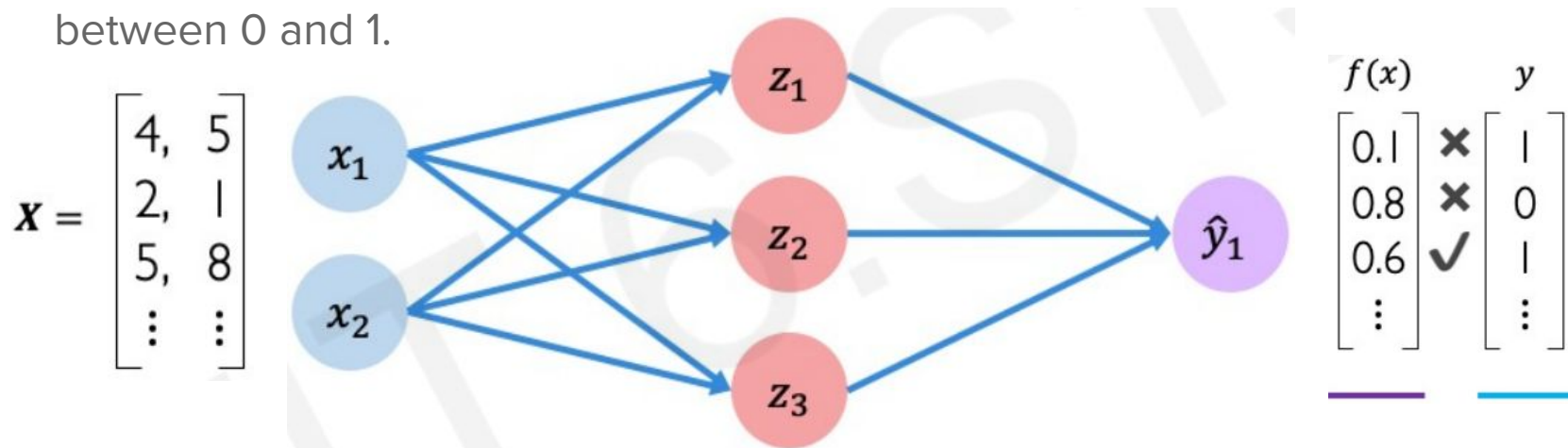
Also known as: ←

- Objective Function
- Cost Function
- Empirical Risk

$$J(W) = \frac{1}{n} \sum_{i=1}^n \underbrace{\mathcal{L}(f(x^{(i)}; W))}_{\text{Predicted}}, \underbrace{y^{(i)}}_{\text{Actual}}$$

Binary Cross Entropy Loss

- **Cross Entropy Loss** can be used with Models that output a probability between 0 and 1.

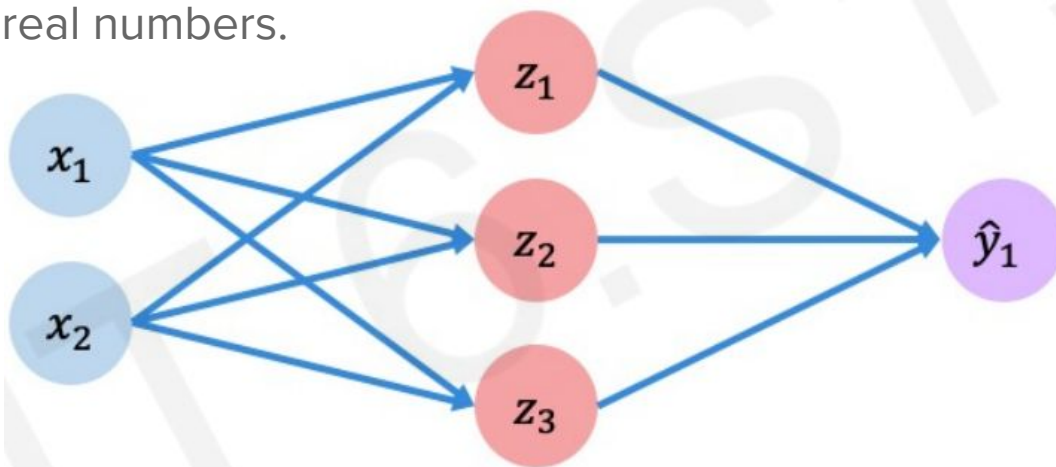


$$J(W) = -\frac{1}{n} \sum_{i=1}^n \underbrace{y^{(i)}}_{\text{Actual}} \log \left(\underbrace{f(x^{(i)}; W)}_{\text{Predicted}} \right) + (1 - \underbrace{y^{(i)}}_{\text{Actual}}) \log \left(1 - \underbrace{f(x^{(i)}; W)}_{\text{Predicted}} \right)$$

Mean Squared Error Loss

- **Mean squared error loss** can be used with regression models that output continuous real numbers.

$$\mathbf{x} = \begin{bmatrix} 4, & 5 \\ 2, & 1 \\ 5, & 8 \\ \vdots & \vdots \end{bmatrix}$$



$f(x)$		y
30	×	90
80	×	20
85	✓	95
⋮		⋮

Final Grades (percentage)

$$J(\mathbf{W}) = \frac{1}{n} \sum_{i=1}^n \left(\underbrace{y^{(i)}}_{\text{Actual}} - \underbrace{f(x^{(i)}; \mathbf{W})}_{\text{Predicted}} \right)^2$$

Next Lecture: Training Neural Networks!