

Group Number		Name		Type
List Number		Surname		A
Student ID		Signature		
E-mail				

ATTENTION: Each question has only one correct answer and is worth one point. Be sure to fill in completely the circle that corresponds to your answer on the answer sheet. Use a pencil (not a pen). Only the answers on your answer sheet will be taken into account.

Questions 1-5

An object of mass m is thrown from point A at $t = 0$ with an initial speed $v_0 = 10 \text{ m/s}$ from a height $h = 1 \text{ m}$ over the ground making an angle $\theta = 53^\circ$ with the horizontal, and following the trajectory shown in the figure, it hits the point D which is at height $H = 7/4 \text{ m}$ over the ground.

Take $g = 10 \text{ m/s}^2$ and $\sin 53^\circ = \cos 37^\circ = 4/5$.

1. In the given Cartesian coordinate system, which of the followings is the $y(t)$ of the object in meters?

(a) $1 + 8t + 5t^2$ (b) $1 + 6t - 5t^2$ (c) $1 - 8t - 5t^2$ (d) $1 + 8t - 5t^2$ (e) $1 - 6t + 5t^2$

2. What is the time to reach point D in seconds?

(a) 2 (b) $5/3$ (c) $4/3$ (d) 1 (e) $3/2$

3. If C is the highest point of the trajectory over the ground, what is the ratio R/d ?

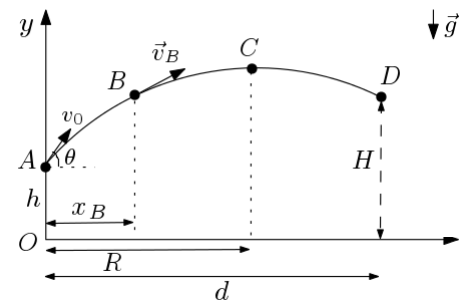
(a) $4/5$ (b) $3/5$ (c) $7/15$ (d) $8/15$ (e) $11/15$

4. Assuming that B and D are at the same height, what is x_B in meters?

(a) $3/5$ (b) $4/3$ (c) $2/5$ (d) 1 (e) $3/4$

5. What is the velocity \vec{v}_B at point B in units of m/s ?

(a) $6\hat{i} - 6\hat{j}$ (b) $6\hat{i} + 7\hat{j}$ (c) $8\hat{i} + 7\hat{j}$ (d) $6\hat{i} - 7\hat{j}$ (e) $8\hat{i} + 6\hat{j}$



Questions 6-8

Consider a particle moving in the xy -plane with a constant acceleration. At $t = 0$ the particle's initial position is $(2 \text{ m})\hat{i} - (3 \text{ m})\hat{j}$ and at that instant its initial velocity is $(10 \text{ m/s})\hat{i}$. At $t = 3 \text{ s}$ its velocity is $(4 \text{ m/s})\hat{i} + (3 \text{ m/s})\hat{j}$.

6. What is the acceleration of this particle?

(a) $(2 \text{ m/s}^2)\hat{i} - (1 \text{ m/s}^2)\hat{j}$ (b) $(3 \text{ m/s}^2)\hat{i} + (2 \text{ m/s}^2)\hat{j}$ (c) $(-2 \text{ m/s}^2)\hat{i} + (3 \text{ m/s}^2)\hat{j}$ (d) $(-3 \text{ m/s}^2)\hat{i} + (2 \text{ m/s}^2)\hat{j}$
(e) $(-2 \text{ m/s}^2)\hat{i} + (1 \text{ m/s}^2)\hat{j}$

7. What is the position vector of the particle at $t = 3 \text{ s}$?

(a) $(5 \text{ m})\hat{i} + (2 \text{ m})\hat{j}$ (b) $(17 \text{ m})\hat{i} + (5/2 \text{ m})\hat{j}$ (c) $(23 \text{ m})\hat{i} + (3/2 \text{ m})\hat{j}$ (d) $(13 \text{ m})\hat{i} + (5/2 \text{ m})\hat{j}$
(e) $(3 \text{ m})\hat{i} + (4 \text{ m})\hat{j}$

8. During the time interval $t_i = 0$ and $t_f = 3 \text{ s}$ what is the average velocity of the particle?

(a) $(4 \text{ m})\hat{i} + (5/2 \text{ m})\hat{j}$ (b) $(7 \text{ m})\hat{i} + (3/2 \text{ m})\hat{j}$ (c) $(5 \text{ m})\hat{i} + (5/2 \text{ m})\hat{j}$ (d) $(4 \text{ m})\hat{i} + (7/2 \text{ m})\hat{j}$ (e) $(5 \text{ m})\hat{i} + (3 \text{ m})\hat{j}$

Questions 9-10

A block of mass m is at rest at the origin at $t = 0$. It is pushed with constant force F_0 from $x = 0$ to $x = L$ across a horizontal surface whose coefficient of kinetic friction is $\mu_k = \mu_0(1 - x/L)$, that is, the coefficient of friction decreases from μ_0 at $x = 0$ to zero at $x = L$.

9. What is the net work done by the net force to bring the block from $x = 0$ to $x = L$?

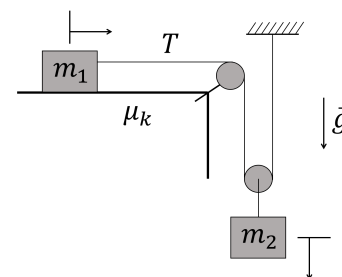
(a) $(F_0 - \frac{3}{2}mg\mu_0)L$ (b) $(2F_0 - \frac{1}{2}mg\mu_0)L$ (c) $(F_0 + \frac{3}{2}mg\mu_0)L$ (d) $(3F_0 + \frac{5}{2}mg\mu_0)L$ (e) $(F_0 - \frac{1}{2}mg\mu_0)L$

10. What is the block's speed as it reaches position L ?

(a) $\sqrt{(\frac{F_0}{m} - 4\mu_0g)L}$ (b) $\sqrt{(\frac{F_0}{m} - 3\mu_0g)L}$ (c) $\sqrt{(\frac{2F_0}{m} + 3\mu_0g)L}$ (d) $\sqrt{(\frac{2F_0}{m} - 3\mu_0g)L}$ (e) $\sqrt{(\frac{2F_0}{m} - \mu_0g)L}$

Questions 11-13

Consider the system shown in the figure. The pulleys are assumed to be frictionless and massless. The coefficient of kinetic friction between m_1 and the horizontal surface is $\mu_k = 0.25$. Take $m_1 = 2 \text{ kg}$ and $m_2 = 4 \text{ kg}$, $g = 10 \text{ m/s}^2$.



11. What is the relation between the magnitudes of the accelerations of the blocks?

- (a) $3a_1 = 2a_2$ (b) $a_1 = a_2$ (c) $a_1 = 3a_2$ (d) $a_1 = 2a_2$ (e) $2a_1 = a_2$

12. What is the acceleration of the block m_1 ?

- (a) 3 m/s^2 (b) 4.5 m/s^2 (c) 3.5 m/s^2 (d) 5 m/s^2 (e) 4 m/s^2

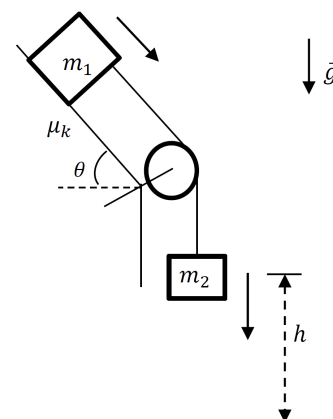
13. What is the tension T in the rope?

- (a) 13 N (b) 11 N (c) 19 N (d) 17 N (e) 15 N

Questions 14-16

Two blocks of masses $m_1 = 5 \text{ kg}$ and $m_2 = 10 \text{ kg}$ are connected by a string of negligible mass, as shown in the figure. The coefficient of kinetic friction between the block m_1 and the inclined plane is given by $\mu_k = 0.25$ and the angle of inclination is $\theta = 37^\circ$.

Take $g = 10 \text{ m/s}^2$ and $\sin 37^\circ = \cos 53^\circ = 3/5$.



14. What is the acceleration of the blocks?

- (a) 6.5 m/s^2 (b) 8 m/s^2 (c) 6 m/s^2 (d) 7 m/s^2 (e) 7.5 m/s^2

15. What is the tension in the string?

- (a) 25 N (b) 30 N (c) 15 N (d) 35 N (e) 20 N

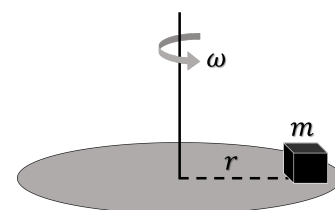
16. What is the work done by gravity when m_2 falls a distance $h = 0.5 \text{ m}$?

- (a) 55 J (b) 65 J (c) 60 J (d) 50 J (e) 45 J

Questions 17-18

A disk shaped platform of radius R is being rotated with a constant angular speed $\omega = 3 \text{ rad/s}$ about the axis passing through its center of mass, as shown in the figure. A block of mass $m = 500 \text{ g}$ is at rest relative to the platform at a distance $r = 25 \text{ cm}$ from the axis of rotation. The coefficient of static and kinetic frictions between the block and the platform are $\mu_s = 0.7$ and $\mu_k = 0.4$, respectively.

Take $g = 10 \text{ m/s}^2$.



17. What is the magnitude and direction of the friction force on m ?

- (a) $11/8 \text{ N}$, away from the rotation axis
(b) $9/5 \text{ N}$, towards the rotation axis
(c) $9/8 \text{ N}$, towards the rotation axis
(d) $11/8 \text{ N}$, towards the rotation axis
(e) $9/8 \text{ N}$, away from the rotation axis

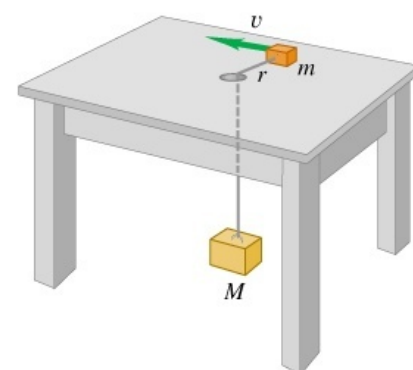
18. What is the maximum value of ω to keep the block at rest relative to the platform in units of rad/s ?

- (a) $3\sqrt{7}$ (b) $2\sqrt{7}$ (c) $4\sqrt{2}$ (d) $3\sqrt{5}$ (e) $2\sqrt{5}$

Questions 19-20

A small block of mass $m = 0.5 \text{ kg}$ is set into a uniform circular motion on a horizontal frictionless table at a distance $r = 50 \text{ cm}$ from a hole in the center of the table, as shown in the figure. A string tied to m passes down through the hole, and a larger block of mass M is suspended from the free end of the string. If the small block m makes 4 turns in a second, the height of M is not changing.

Take $g = 10 \text{ m/s}^2$, $\pi \approx 3$.



19. For this given configuration of the system, what is the magnitude of the acceleration of m ?

- (a) 328 m/s^2 (b) 148 m/s^2 (c) 288 m/s^2 (d) 178 m/s^2 (e) 258 m/s^2

20. What is the value of M ?

- (a) $72/5 \text{ kg}$ (b) 18 kg (c) 17 kg (d) $76/7 \text{ kg}$ (e) $72/7 \text{ kg}$