

		Surname		Type
Group Number		Name		A
List Number		e-mail		
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**ATTENTION:** Each question has only one correct answer and is worth one point. Be sure to fill in completely the circle that corresponds to your answer on the answer sheet. Use a pencil (not a pen). Only the answers on your answer sheet will be taken into account.

### Questions 1-5

A scale is adjusted so that when a large, shallow pan is placed on it, it reads zero Newton. There is a water faucet 1.6 m above the pan. When the faucet is turned on, water leaves the faucet with a speed of 2 m/s and falls into the pan at a rate  $R = 0.14 \text{ kg/s}$ . Take  $g = 10 \text{ m/s}^2$ .

- What is the magnitude of the velocity of water as it strikes the pan in m/s?  
(a) 3 (b)  $4\sqrt{2}$  (c) 5 (d) 4 (e) 6
- Just after water strikes the pan what is the momentum change per unit time in  $\text{kgm/s}^2$ ?  
(a) 0.14 (b) 0.56 (c) 0.84 (d) 0.42 (e) 0.28
- What is the scale reading at  $t = 0 \text{ s}$  (Water just strikes to the pan initially)  
(a) 0.84 N (b) 1 N (c) 10 N (d) 1.4 N (e) 0.64 N
- What is the mass of water in the pan at  $t = 4 \text{ s}$  in kg?  
(a) 0.56 kg (b) 1.5 kg (c) 2 kg (d) 1 kg (e) 3 kg
- What is the scale reading at  $t = 4 \text{ s}$ ? (Assume that the increase in water level is negligible)  
(a) 10.2 N (b) 15.6 N (c) 6.44 N (d) 21 N (e) 16 N

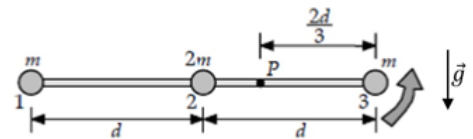
### Questions 6-8

Two objects, A ( $m_A = 1.0 \text{ kg}$ ) and B ( $m_B = 2.0 \text{ kg}$ ), collide. The velocities before the collision are  $\vec{v}_A = 2\hat{i} \text{ m/s}$  and  $\vec{v}_B = 4\hat{j} \text{ m/s}$ . The velocity of object A after the collision is given by  $\vec{v}_A' = -0.4\hat{i} + 2\hat{j} \text{ m/s}$ .

- What is the speed of object B just after the collision ( $v_B'$ )?  
(a)  $\sqrt{8.76} \text{ m/s}$  (b)  $\sqrt{10.44} \text{ m/s}$  (c)  $\sqrt{8.44} \text{ m/s}$  (d)  $\sqrt{9.36} \text{ m/s}$  (e)  $\sqrt{9.64} \text{ m/s}$
- What is  $\tan \theta$ , where  $\theta$  is the angle between the velocity of B ( $v_B'$ ) and the x-axis?  
(a) 1.5 (b) 5 (c) 2 (d) 2.5 (e) 3
- What is the energy lost due to the collision?  
(a) 7.16 J (b) 7.48 J (c) 5.48 J (d) 6.56 J (e) 6.38 J

### Questions 9-15

A rigid, massless rod has three masses attached to it. The rod is free to rotate in a vertical plane about a frictionless axle perpendicular to the rod through the point P, and it is released from rest in the horizontal position at  $t=0\text{s}$ .



- Find the moment of inertia of the system about the point P.  
(a)  $7md^2$  (b)  $4md^2$  (c)  $\frac{7md^2}{3}$  (d)  $\frac{22md^2}{9}$  (e)  $\frac{4md^2}{9}$
- Find the magnitude of the torque about point P at  $t=0\text{s}$ .  
(a) 0 (b)  $mgd$  (c)  $\frac{3}{4}mgd$  (d)  $\frac{7mgd}{9}$  (e)  $\frac{4}{3}mgd$
- Find the angular acceleration of the system at  $t=0\text{s}$ .  
(a)  $\frac{6g}{11d}$  counter clockwise (b)  $\frac{3g}{7d}$  counter clockwise (c)  $\frac{3g}{7d}$  clockwise (d)  $\frac{6d}{11g}$  counter clockwise (e)  $\frac{6g}{11d}$  clockwise
- Find the linear acceleration of the mass labelled as “3” at  $t=0\text{s}$ .  
(a)  $\frac{4g}{11}$  down (b) 0 (c)  $\frac{2g}{7}$  up (d)  $\frac{2g}{7}$  down (e)  $\frac{4g}{11}$  up
- Find the maximum kinetic energy of the system.  
(a)  $\frac{4}{5}mgd$  (b)  $\frac{4}{3}mgd$  (c)  $\frac{5}{4}mgd$  (d)  $\frac{3}{4}mgd$  (e)  $mgd$
- Find the maximum angular speed attained by the rod.  
(a)  $\sqrt{\frac{7g}{6d}}$  (b)  $\sqrt{\frac{4g}{3d}}$  (c)  $\sqrt{\frac{12g}{11d}}$  (d)  $\sqrt{\frac{6g}{7d}}$  (e)  $\sqrt{\frac{11g}{12d}}$

15. Find the maximum value of the magnitude of the angular momentum of the system about point P.

- (a)  $md^{\frac{3}{2}}\sqrt{(\frac{14g}{3})}$  (b)  $\frac{44}{9}md^{\frac{3}{2}}\sqrt{\frac{3g}{11}}$  (c)  $md^{\frac{3}{2}}\sqrt{(\frac{5g}{14})}$  (d)  $22md^{\frac{3}{2}}\sqrt{(\frac{14g}{3})}$  (e)  $\frac{44}{9}md^{\frac{3}{2}}\sqrt{\frac{5g}{21}}$

### Questions 16-20

The turbine and associated rotating parts of a jet engine have a total moment of inertia of  $10 \text{ kgm}^2$ . The turbine is accelerated uniformly from rest to an angular speed of  $100 \text{ rad/s}$  in a time of  $25 \text{ s}$ . Find

16. the angular acceleration,

- (a)  $1/4 \text{ rad/s}^2$  (b)  $4 \text{ rad/s}^2$  (c)  $1/2 \text{ rad/s}^2$  (d)  $2 \text{ rad/s}^2$  (e)  $5 \text{ rad/s}^2$

17. the net torque required,

- (a)  $20 \text{ Nm}$  (b)  $5 \text{ Nm}$  (c)  $50 \text{ Nm}$  (d)  $40 \text{ Nm}$  (e)  $2 \text{ Nm}$

18. the angle turned through in  $25 \text{ s}$ ,

- (a)  $1750 \text{ rad}$  (b)  $1000 \text{ rad}$  (c)  $500 \text{ rad}$  (d)  $750 \text{ rad}$  (e)  $1250 \text{ rad}$

19. the work done by the net torque,

- (a)  $100000 \text{ J}$  (b)  $12500 \text{ J}$  (c)  $50000 \text{ J}$  (d)  $0$  (e)  $25000 \text{ J}$

20. the kinetic energy of the turbine at the end of the  $25 \text{ s}$ .

- (a)  $25000 \text{ J}$  (b)  $0$  (c)  $100000 \text{ J}$  (d)  $50000 \text{ J}$  (e)  $12500 \text{ J}$

### Questions 21-25

The potential energy between two identical point like objects of the same mass,  $m$ , is given by the relation,  $U(r) = m.A[(\frac{r_0}{r})^{12} - 2(\frac{r_0}{r})^6]$ . Here  $r$  is the distance between the objects,  $r_0$  is the equilibrium distance where the net force on the objects is zero, and  $A$  is a constant.

21. What is the unit of  $A$ ?

- (a)  $\text{N.kg/m}^9$  (b)  $\text{N.kg/m}^6$  (c)  $\text{N.m/kg}$  (d)  $\text{N.kg/m}^{12}$  (e)  $\text{N/m.kg}$

22. What is the minimum value of the potential energy?

- (a)  $-6mA$  (b)  $-mA$  (c)  $3mA$  (d)  $-2mA$  (e)  $-3mA$

23. What is the magnitude of the force applied by one of the objects on the other at the distance that the *potential energy becomes minimum*?

- (a)  $F = 3mA$  (b)  $F = mA[r_0^{11} - 2r_0^5]$  (c)  $F = mA[r_0^{12} - 2r_0^6]$  (d)  $F = 0$  (e)  $F = 2mA$

24. What is the magnitude of the force applied on each object as a function of the distance  $r$ ?

- (a)  $F = 12m.A[+\frac{r_0^{12}}{r^{13}} - \frac{r_0^6}{r^7}]$  (b)  $F = m.A[-\frac{r_0^{13}}{r^{11}} - \frac{r_0^7}{r^5}]$  (c)  $F = m.A[-\frac{r_0^{13}}{r^{11}} + \frac{r_0^7}{r^5}]$  (d)  $F = 12m.A[-\frac{r_0^{12}}{r^{13}} - \frac{r_0^6}{r^7}]$   
 (e)  $F = m.A[+\frac{r_0^{12}}{r^{13}} - \frac{r_0^6}{r^9}]$

25. Consider that one of the objects is fixed. What is the minimum work that must be done to bring the other object from a distance  $r_0$  to  $2r_0$ .

- (a)  $W = mA(1 - 2^{-12} - 2^{-7})$  (b)  $W = 12mA(1 + 2^{-11} - 2^{-6})$  (c)  $W = 12mA(-1 - 2^{-11} + 2^{-6})$  (d)  $W = mA(1 + 2^{-12} - 2^{-5})$  (e)  $W = mA(-1 - 2^{-12} + 2^{-7})$