

		Surname		Type
Group Number		Name		A
List Number		e-mail		
Student ID		Signature		

**ATTENTION:** Each question has only one correct answer and is worth one point. Be sure to fill in completely the circle that corresponds to your answer on the answer sheet. Use a pencil (not a pen). Only the answers on your answer sheet will be taken into account.

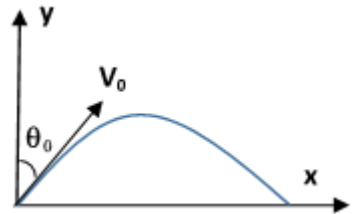
### Questions 1-3

Two vectors are given as  $\vec{A} = a\hat{i} - 2\hat{k}$  and  $\vec{B} = b\hat{j} - 2\hat{k}$  where a and b are positive real numbers.

- If the magnitudes of vectors are  $A = 3$  and  $B = 4$ , find magnitude of the vector  $\vec{A} - \vec{B}$ .  
(a) -4 (b)  $\sqrt{17}$  (c) 12 (d) 5 (e)  $-\sqrt{17}$
- Angle between the vectors  $\vec{A}$  and  $\vec{B}$  is  
(a)  $\arctan \sqrt{5/12}$  (b)  $\arccos 1/3$  (c)  $\arctan \sqrt{12/5}$  (d)  $37^\circ$  (e)  $53^\circ$
- Find a unit vector which is perpendicular to both vectors  $\vec{A}$  and  $\vec{B}$ .  
(a)  $(\sqrt{12}\hat{i} + \sqrt{5}\hat{j} + \sqrt{15}\hat{k})/\sqrt{32}$  (b)  $(3\hat{i} + 4\hat{j})/5$  (c)  $2(\hat{i} + \hat{j} - \hat{k})$  (d)  $-\sqrt{5}\hat{i} + \sqrt{12}\hat{j}$  (e)  $(-\sqrt{5}\hat{i} + \sqrt{12}\hat{j})/\sqrt{17}$

### Questions 4-9

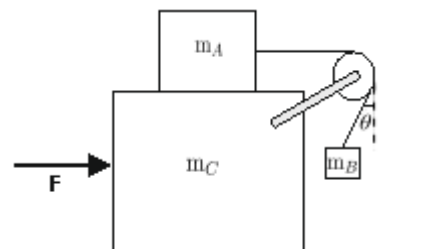
An object is thrown from ground with initial speed  $V_0 = 10$  m/s at an angle  $\theta_0 = 30^\circ$  with the vertical axis as shown in the figure. (Ignore air resistance and take,  $g \approx 10$  m/s<sup>2</sup>,  $\sin 30^\circ = 1/2$ )



- What is the acceleration of the object at the highest point?  
(a)  $\vec{a} = g\hat{j}$  (b)  $\vec{a} = g\hat{i}$  (c)  $\vec{a} = -g\hat{j}$  (d)  $\vec{a} = 0$  (e)  $\vec{a} = 2g\hat{j}$
- What is the maximum height that the object can reach?  
(a) 15m (b)  $5/4$ m (c)  $1/2$ m (d)  $15/4$ m (e) 5m
- What is the time for the object to reach the maximum height?  
(a)  $15/4$ s (b)  $5/4$ s (c)  $1/2$ s (d) 2s (e)  $\sqrt{3}/2$ s
- What is the horizontal range that the object can reach?  
(a) 10m (b)  $20\sqrt{3}$ m (c)  $10\sqrt{3}$ m (d) 5m (e)  $5\sqrt{3}$ m
- A little time after the take-off, the object passes from point  $(x=\sqrt{3}\text{m}, y)$ . What is y?  
(a)  $3\sqrt{3}$ m (b)  $(\sqrt{3} - 1)$ m (c)  $\sqrt{3}/2$ m (d)  $12/5$ m (e) 1m
- What is the velocity (in m/s) of the object when it hits the ground?  
(a)  $-5\hat{i} + 5\sqrt{3}\hat{j}$  (b)  $5\sqrt{3}\hat{i} + 5\hat{j}$  (c)  $5\hat{i} + 5\sqrt{3}\hat{j}$  (d)  $5\hat{i} - 5\sqrt{3}\hat{j}$  (e)  $-5\hat{i} - 5\sqrt{3}\hat{j}$

### Questions 10-14

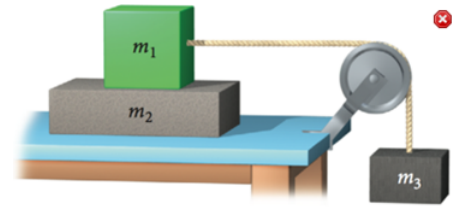
A block of mass  $m_A = 3$  kg rests on another block of mass  $m_C = 5$  kg. Block  $m_A$  is connected by a thin string that passes over a pulley to a third block of mass  $m_B = 1$  kg. A force  $\vec{F}$  is exerted on the large block  $m_C$  so that the mass  $m_A$  does not move relative to  $m_C$ . Ignore all friction. Assume  $m_B$  does not make contact with  $m_C$ .  $g = 10$  m/s<sup>2</sup>.



- What is the tension (in units of N) in the string in terms of the acceleration (a) of the system?  
(a) 3a (b) 2a (c) 4a (d) a (e) 5a
- What is the tension (in units of N) in the string?  
(a)  $\frac{10}{\cos \theta}$  (b) 40 (c) 20 (d) 10 (e)  $\frac{10}{\sin \theta}$
- What is the value of  $\sin \theta$ ?  
(a)  $3/5$  (b)  $1/3$  (c) 0.5 (d)  $\frac{\sqrt{3}}{2}$  (e)  $2/5$
- What is the magnitude of  $\vec{F}$  in units of N?  
(a) 120 (b) 30 (c)  $\frac{90}{\sqrt{8}}$  (d) 50 (e) 60
- What is the acceleration (in m/s<sup>2</sup>) of the block of mass  $m_B$ ?  
(a)  $\frac{10}{3}$  (b)  $\frac{20}{3}$  (c)  $\frac{10}{\sqrt{8}}$  (d)  $\frac{40}{3}$  (e)  $\frac{50}{\sqrt{8}}$

## Questions 15-19

Two blocks with masses  $m_1$  and  $m_2$  ( $m_1\mu_s < m_2$ ) are on a frictionless table, and the blocks with masses,  $m_1$  and  $m_3$  are connected by a string as shown in the figure. The coefficients of static and kinetic friction between  $m_1$  and  $m_2$  are  $\mu_s$  and  $\mu_k$ , respectively. The three blocks are initially at rest and then left free to move.



15. If block  $m_1$  slips on block  $m_2$  what is the force of kinetic friction?

- (a)  $\frac{(-\mu_k m_1 - m_3)g}{m_1 - m_3}$  (b)  $\frac{(-\mu_k m_1 - \mu_k m_2 + m_3)g}{m_1 + m_2 + m_3}$  (c)  $\frac{\mu_k m_1 g}{m_1 + m_2 + m_3}$  (d)  $\mu_k m_1 g$   
 (e)  $\frac{(-\mu_k m_1 - \mu_k m_2 + m_3)g}{m_1 + m_2 - m_3}$

16. If block  $m_1$  slips on block  $m_2$  what is the acceleration of  $m_2$ ?

- (a)  $\mu_k g \frac{m_1 - m_2}{m_2}$  (b)  $\mu_k g \frac{m_1}{m_2}$  (c)  $\mu_k g \frac{m_2}{m_1 + m_2}$  (d)  $\mu_k g \frac{m_1 + m_2}{m_2}$  (e)  $\mu_k g \frac{m_1}{m_1 + m_2}$

17. If block  $m_1$  slips on block  $m_2$  what is the acceleration of  $m_3$ ?

- (a)  $\frac{(-\mu_k m_1 - \mu_s m_2 + m_3)g}{m_1 + m_2 + m_3}$  (b)  $\frac{(-\mu_k m_1 - \mu_k m_2 + m_3)g}{m_1 + m_2 + m_3}$  (c)  $\frac{(-\mu_k m_1 - m_3)g}{m_1 - m_3}$  (d)  $\frac{(-\mu_k m_1 + m_3)g}{m_1 + m_3}$  (e)  $\frac{(-\mu_k m_1 - \mu_k m_2 + m_3)g}{m_1 + m_2 - m_3}$

18. If block  $m_1$  slips on block  $m_2$  what is the tension in the string?

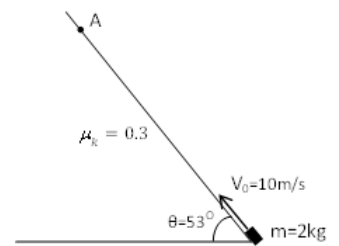
- (a)  $\frac{m_1 m_3 g}{m_1 + m_3} (1 + \mu_k)$  (b)  $\frac{m_1 m_3 g}{m_2} (1 + \mu_s)$  (c)  $\frac{m_3 g}{m_1 + m_3} (1 + \mu_s)$  (d)  $\frac{m_1 g}{m_1 + m_3} (1 + \mu_s)$  (e)  $\frac{m_1 m_2 m_3 g}{m_1 + m_2 + m_3} (1 + \mu_k)$

19. What is the condition to be satisfied for the blocks with masses  $m_1$  and  $m_2$  move together without slipping?

- (a)  $m_3 \leq \mu_s \frac{m_2}{m_1} (-m_1 + m_2)$  (b)  $m_3 \leq \frac{m_1(m_1 + m_2)\mu_s}{m_2 - m_1\mu_s}$  (c)  $m_3 \leq \mu_s(m_1 + m_2)$  (d)  $m_3 \leq \mu_k \frac{m_1}{m_2} (m_1 + m_2)$  (e)  $m_3 \leq \mu_k \frac{m_2}{m_1} (-m_1 + m_2)$

## Questions 20-25

An object of mass  $m=2\text{kg}$  is thrown up with the speed  $10\text{ m/s}$  on an inclined surface of angle  $53^\circ$  as shown in the figure. The kinetic friction coefficient between the object and the surface is  $0.3$ . (Take  $\cos 53^\circ = 0.6$ ,  $\sin 53^\circ = 0.8$  and gravitational acceleration  $g=10\text{ m/s}^2$ )



20. What is the work (in Joule, J) done by the friction when the object reaches the point A, at a distance of 2 m from its initial point?

- (a) +12 (b) +9.6 (c) -3.6 (d) 0 (e) -7.2

21. What is the work (in Joule) done by normal force up to the point A?

- (a) +12 (b) 0 (c) +7.2 (d) +3.6 (e) -3

22. What is the work (in Joule) done by the net force up to the point A?

- (a) -39.2 (b) -10.8 (c) +10.8 (d) +39.2 (e) -32

23. What is the speed (in m/s) of the object at the point A?

- (a)  $\sqrt{10.8}$  (b)  $\sqrt{39.2}$  (c)  $\sqrt{32}$  (d)  $\sqrt{60.8}$  (e)  $\sqrt{89.2}$

24. What is the approximate value of the distance (in m) that the object can travel on the inclined surface?

- (a) 5.1 (b) 10.2 (c) 4.0 (d) 3.6 (e) 7.2

25. When the object turns back to its shooting point what is the speed (in m/s) of the object approximately?

- (a) 5 (b) 6 (c)  $\sqrt{63.3}$  (d)  $\sqrt{36.7}$  (e)  $\sqrt{18.4}$