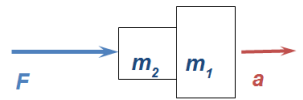


		Surname		Type
Group Number		Name		A
List Number		e-mail		
Student ID		Signature		

**ATTENTION:** Each question has only one correct answer and is worth one point. Be sure to fill in completely the circle that corresponds to your answer on the answer sheet. Use a pencil (not a pen). Only the answers on your answer sheet will be taken into account.

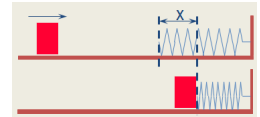
1. A force  $F$  acts on mass  $m_1$  giving acceleration  $a_1$ . The same force acts on a different mass  $m_2$  giving acceleration  $a_2 = 2a_1$ . If  $m_1$  and  $m_2$  are glued together and the same force  $F$  acts on this combination, what is the resulting acceleration?

(a)  $4/3 a_1$  (b)  $3/4 a_1$  (c)  $2/3 a_1$  (d)  $1/2 a_1$  (e)  $3/2 a_1$



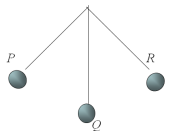
2. A box sliding on a frictionless flat surface runs into a fixed spring, which is compressed a distance  $x$  until the box stops. If the initial speed of the box were doubled, how much would the spring compress in this case?

(a)  $\sqrt{2}$  times as much (b) The same amount (c) Half as much (d) Four times as much  
(e) Twice as much



3. A pendulum of length  $L$  with a bob of mass  $m$  swings back and forth. At the low point of its motion (point Q), the tension in the string is  $(3/2)mg$ . What is the speed of the bob at this point?

(a)  $\sqrt{gL}$  (b)  $2\sqrt{gL}$  (c)  $\sqrt{gL}$  (d)  $\sqrt{2gL}$  (e)  $\sqrt{\frac{gL}{2}}$



4. One car has twice the mass of a second car, but only half as much kinetic energy. When both cars increase their speed by 7 m/s, they then have the same kinetic energy. What were the original speeds of two cars?

(a)  $v_1 = \frac{7.0}{\sqrt{2}}$  m/s;  $v_2 = v_1$  (b)  $v_1 = 7\sqrt{2}$  m/s;  $v_2 = v_1$  (c)  $v_1 = 7\sqrt{2}$  m/s;  $v_2 = 2v_1$  (d)  $v_1 = 7\sqrt{2}$  m/s;  $2v_2 = v_1$   
(e)  $v_1 = \frac{7.0}{\sqrt{2}}$  m/s;  $v_2 = 2v_1$

5. A particle is moving along the  $x$ -axis subject to the potential energy function  $U(x) = \frac{a}{x} + bx^2 + cx - d$ , where  $a = 3.00$  J m,  $b = 12.0$  J/m<sup>2</sup>,  $c = 7.00$  J/m, and  $d = 20.0$  J. Determine the  $x$ -component of the net force on the particle at the coordinate  $x = 1$  m.

(a)  $-2.8 \cdot 10^6$  g.cm/s<sup>2</sup> (b)  $2.8 \cdot 10^6$  N (c)  $-2.8 \cdot 10^6$  N (d) 0 (e)  $2.8 \cdot 10^6$  g.cm/s<sup>2</sup>

### Questions 6-9

Two blocks shown in the figure are of mass "m" and rest on a flat frictionless air track. A spring of force constant "k" is attached to block (2). Block (1) has initial velocity in the +x direction. Block (2) is initially at rest. Block (1) also becomes attached when it hits the spring.



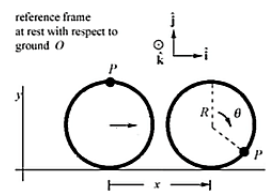
6. What is the center of mass velocity of the system?  
(a)  $v_0/2$  (b) 0 (c)  $v_0$  (d)  $2v_0$  (e)  $v_0/4$
7. What is the minimum total kinetic energy consistent with the conservation laws?  
(a) 0 (b)  $mv_0^2/4$  (c)  $2mv_0^2$  (d)  $mv_0^2$  (e)  $mv_0^2/2$

8. What is the maximum compression of the spring?  
(a)  $(m/2k)v_0$  (b) 0 (c)  $(2k/m)v_0^2$  (d)  $(m/2k)^{1/2}v_0$  (e)  $(k/m)^{1/2}v_0$

9. What is the maximum velocity of block (1) after the collision?  
(a)  $v_0/\sqrt{2}$  (b)  $v_0$  (c)  $v_0/2$  (d)  $2v_0$  (e) 0

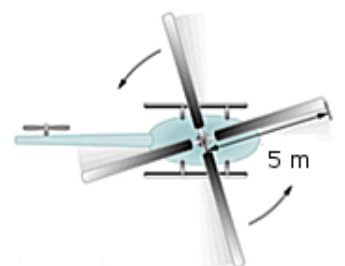
10. If a wheel of radius  $R$  rolls without slipping through an angle  $\theta$ , what is the relationship between the distance the wheel rolls,  $x$ , and the product  $R\theta$ ?

(a)  $R < x\theta$  (b)  $x < R\theta$  (c)  $x > R\theta$  (d)  $x = R\theta$  (e)  $R > x\theta$



### Questions 11-13

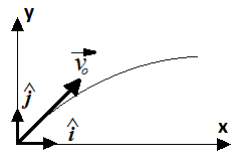
A typical small rescue helicopter has four blades as shown in the figure on right. Each is 5.00 m long and has a mass of 60.0 kg. The blades can be approximated as thin rods that rotate about one end of an axis perpendicular to their length. The helicopter has a total loaded mass of 2000 kg.



11. Calculate the rotational kinetic energy in the blades when they rotate at 300 rpm.  
(a)  $1.00 \times 10^6$  J (b)  $2.00 \times 10^5$  J (c)  $1.00 \times 10^5$  J (d)  $4.00 \times 10^6$  J (e)  $2.00 \times 10^6$  J
12. When the helicopter flies at 20.0 m/s, what is the ratio of the translational kinetic energy of the helicopter with respect to the rotational energy in the blades?  
(a) 5.0 (b) 0.8 (c) 2.5 (d) 0.4 (e) 1
13. To what height could the helicopter be raised if all of the rotational kinetic energy could be used to lift it?  
(a) 500.0 m (b) 50.0 m (c) 5.0 m (d) 25.0 m (e) 100.0 m

## Questions 14-17

A projectile of mass  $m = 1 \text{ kg}$  is fired from the ground with an initial position  $\vec{r}_o = \vec{0}$  and initial velocity of  $\vec{v}_o = 8 \text{ (m/s)}\hat{i} + 15 \text{ (m/s)}\hat{j}$ . Acceleration due to gravity is  $\vec{g} = -10 \text{ (m/s}^2)\hat{j}$ . Answer the following for  $t = 2 \text{ s}$ .

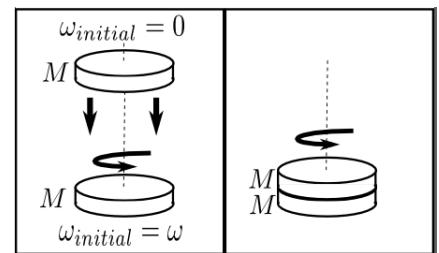


14. Which of the following is the linear momentum of the particle in  $\text{kg m/s}$ ?
- (a)  $5\hat{i} + 8\hat{j}$  (b)  $8\hat{i} - 10\hat{j}$  (c)  $5\hat{i} - 8\hat{j}$  (d)  $8\hat{i} + 5\hat{j}$  (e)  $8\hat{i} - 5\hat{j}$
15. Which of the following is the angular momentum of the particle in  $\text{kg m}^2/\text{s}$ ?
- (a)  $160\hat{k}$  (b)  $-80\hat{k}$  (c)  $-160\hat{k}$  (d)  $80\hat{i} - 80\hat{j}$  (e)  $-80\hat{j}$
16. Which of the following is the rate of change of angular momentum of the particle in  $\text{kg m}^2/\text{s}^2$ ?
- (a)  $-160\hat{k}$  (b)  $-80\hat{k}$  (c)  $-80\hat{j}$  (d)  $80\hat{i} - 80\hat{j}$  (e)  $160\hat{k}$
17. Which of the following is the net torque acting on the particle in  $\text{N m}$ ?
- (a)  $-80\hat{k}$  (b)  $160\hat{k}$  (c)  $-160\hat{k}$  (d)  $-80\hat{j}$  (e)  $80\hat{i} - 80\hat{j}$

## Questions 18-21

A uniform disk of mass “M”, radius “R” and moment of inertia  $I = MR^2/2$  is spinning around its axis with angular speed  $\omega$ . The system is frictionless.

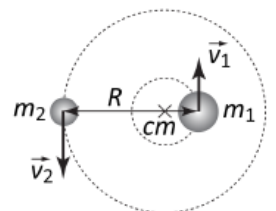
18. What is its angular momentum L?
- (a)  $MR^2\omega^2$  (b)  $MR^2\omega$  (c)  $2MR^2\omega$  (d)  $MR\omega^2/2$  (e)  $MR^2\omega/2$
- A second, identical disk is on the same axis, which is initially not spinning. It is allowed drop on the first disk. The two disks soon start turning together.
19. What quantity / quantities is /are conserved during the collision?
- (a) L only. (b) Mechanical energy only. (c) Kinetic energy only. (d) L and mechanical energy. (e) L and kinetic energy.



20. What is the angular momentum  $L_f$  after the collision?
- (a)  $MR\omega^2/2$  (b)  $MR^2\omega/2$  (c)  $MR^2\omega$  (d) 0 (e)  $2MR^2\omega$
21. What is the final kinetic energy  $KE_f$  after the collision?
- (a)  $MR^2\omega^2/2$  (b) 0 (c)  $MR^2\omega^2/4$  (d)  $MR^2\omega^2/8$  (e)  $MR^2\omega^2$
22. Using Kepler's laws of planetary motion, decide which of the following statements are correct:
- I) It takes the earth less time to complete one full revolution in its orbit around the sun than it takes Jupiter.
- II) A planet moving in an orbit around the sun experiences zero net external torque.
- III) Time needed by a planet to complete one full revolution around the sun increases with the mass of the planet.
- (a) Only II (b) I and II (c) I and III (d) II and III (e) I, II, and III
23. What is the magnitude of the angular momentum,  $L$ , of a satellite of mass  $m$  is in a circular orbit of radius  $R = 2R_E$ ? The mass and radius of Earth are  $M_E$  and  $R_E$ . The universal gravitational constant is  $G$  and the magnitude of the gravitational acceleration on the earth surface is  $g$ .
- (a)  $L = M_E\sqrt{2gR_E^3}$  (b)  $L = m\sqrt{GgR_E^3}$  (c)  $L = 0$  (d)  $L = (m + M_E)\sqrt{2gR_E^3}$  (e)  $L = m\sqrt{2gR_E^3}$

## Questions 24-25

Consider a binary star system with stars of masses  $m_1 = 3M$  and  $m_2 = M$ , separated by distance  $R$  (see figure). The stars are in circular orbits around the center of mass of the system labeled “cm”, with respective orbital speeds  $v_1$  and  $v_2$ .



24. What is the ratio of orbital speeds  $v_1/v_2$  of the two stars?
- (a) 1/3 (b) 1/9 (c) 3 (d) 9 (e) 1
25. What is the orbital period of each star (symbol  $G$  stands for the gravitational constant)?
- (a)  $\frac{1}{2\pi} \frac{GM^2}{R^2}$  (b)  $\frac{2\pi GM}{R}$  (c)  $\sqrt{\frac{\pi^2 R^3}{GM}}$  (d)  $3\sqrt{\frac{\pi^2 R^3}{GM}}$  (e)  $\frac{1}{3}\sqrt{\frac{\pi^2 R^3}{GM}}$