1. Jacobi.cpp

```
#include<iostream>
#include<stdio.h>
#include<conio.h>
#include<math.h>
using namespace std;
int main()
{
        int ans = 1;
        while (ans != 0)
        {
                int i, j;
                double I = 0;
                const int n = 3;
                double a[n][n], b[n][1], x[n][1], T[n][1], e, k;
                cout << "[a].[x]=[b]" << endl;
                cout << "Enter Matrix a:" << endl;</pre>
                for (i = 0; i < n; i++)
                        for (j = 0; j < n; j++)
                                 cout << "a[" << i << "," << j << "] = ";
                                 cin >> a[i][j];
                        }
                cout << "Enter Matrix b:" << endl;
                for (i = 0; i < n; i++)
                {
                        cout << "b[" << i << "][0] = ";
                        cin >> b[i][0];
                }
                cout << "Enter the Accuracy = ";</pre>
                cin >> e;
                for (i = 0; i < n; i++)
                        T[i][0] = 0;
                I = 0;
                while (1)
                {
                        cout << "\nIteration no: " << I << "\n";
```

```
for (i = 0; i < n; i++)
        {
                x[i][0] = (1 / a[i][i])*(b[i][0]);
                //cout << x[i][0] << " ";
                for (j = 0; j < n; j++)
                         if (j != i)
                                 x[i][0] = x[i][0] - (1 / a[i][i])*(a[i][i] * T[i][0]);
                         //cout << x[i][0] << " ";
                //cout << "\n";
        }
        k = 0;
        for (i = 0; i < n; i++)
        {
                k += pow(fabs(x[i][0] - T[i][0]), 2);
        if (k \le e)
        {
                break;
        }
        |++;
        for (i = 0; i < n; i++)
                T[i][0] = x[i][0];
        /*for (i = 0; i < n; i++)
                cout << "x" << i + 1 << "=" << x[i][0] << endl;*/
};
for (i = 0; i < n; i++)
        cout << "x" << i + 1 << "=" << x[i][0] << endl;
//trying spectral radius calculation
double p_G = 0, sum1 = 0, sum2 = 0, base = 0, expo = 0;
for (i = 0; i < n; i++)
{
        sum1 += (x[i][0] - T[i][0])*(x[i][0] - T[i][0]);
cout << sum1 << "\n";
for (i = 0; i < n; i++)
{
        sum2 += x[i][0] * x[i][0];
cout << sum2 << "\n";
base = sum1 / sum2;
cout << " base = " << base;
expo = 1 / I;
```

```
cout << "expo = " << expo;
p_G = pow(base, expo);
cout << "\nspectral radius of G matrix = " << p_G;
cout << "\ncontinue (1 or 0)?";
cin >> ans;
};
_getch();
return 0;
}
```

Please ignore the spectral radius calculation.

```
soumick@soumick-HP-Pavilion-Laptop-15-cclxx:~/hpsc_old_codes$ g++ jacobi.cpp
soumick@soumick-HP-Pavilion-Laptop-15-cc1xx:~/hpsc_old_codes$ ./a.out
[a].[x]=[b]
Enter Matrix a:
a[0,0] = 6
a[0,1] = 2
a[0,2] = 0
a[1,0] = 0
a[1,1] = 12
a[1,2] = 2
a[2,0] = 0
a[2,1] = 0
a[2,2] = 4
Enter Matrix b:
b[0][0] = 4
b[1][0] = 7
b[2][0] = 2
Enter the Accuracy = 0.00001
Iteration no: 0
Iteration no: 1
Iteration no: 2
Iteration no: 3
x1=0.5
x2=0.5
x3=0.5
```

The code with IOFF provision was used in midsem but I didn't upload the code to my drive after the exam.

2. Seidel.cpp

```
#include<iostream>
#include<stdio.h>
#include<conio.h>
#include<math.h>
using namespace std;
int main()
{
        int ans = 1;
        while (ans != 0)
        {
                int i, j;
                double I = 0, k = 0;
                //const int n = 200;
                const int n = 3;
                double a[n][n], b[n][1], x[n][1], T[n][1], T_dash[n][1], e;
                cout << "[a].[x]=[b]" << endl;
                cout << "Enter Matrix a:" << endl;</pre>
                for (i = 0; i < n; i++)
                        for (j = 0; j < n; j++)
                        {
                                 cout << "a[" << i << "," << j << "] = ";
                                 cin >> a[i][j];
                        }
                cout << "Enter Matrix b:" << endl;
                for (i = 0; i < n; i++)
                {
                        cout << "b[" << i << "][0] = ";
                        cin >> b[i][0];
                }
                /*for (i = 0; i < n; i++)
                        for (j = 0; j < n; j++)
                        {
                                 if (i == j)
                                         a[i][j] = 200;
                                 else
                                         a[i][j] = 1;
                for (i = 0; i < n; i++)
                {
                        b[i][0] = 299;
                }*/
                e = 0.000001;
```

```
for (i = 0; i < n; i++)
        T[i][0] = 0;
        T_dash[i][0] = 0;
I = 0;
while (1)
{
        cout << "\nIteration no: " << I << "\n";
        for (i = 0; i < n; i++)
        {
                x[i][0] = (1 / a[i][i])*(b[i][0]);
                //cout << x[i][0] << " ";
                for (j = 0; j < n; j++)
                         if (j != i)
                                 x[i][0] = x[i][0] - (1 / a[i][i])*(a[i][j] * T[j][0]);
                         //cout << x[i][0] << " ";
                }
                //cout << "\n";
                T_dash[i][0] = T[i][0];
                T[i][0] = x[i][0];
        }
        k = 0;
        for (i = 0; i < n; i++)
        {
                 k += pow(fabs(x[i][0] - T_dash[i][0]), 2);
        }
        if (k \le e)
                 break;
        |++;
};
for (i = 0; i < n; i++)
        cout << "x" << i + 1 << "=" << x[i][0] << endl;
//trying spectral radius calculation
double p_G = 0, sum1 = 0, sum2 = 0, base = 0, expo = 0;
for (i = 0; i < n; i++)
{
        sum1 += (x[i][0] - T_dash[i][0])*(x[i][0] - T_dash[i][0]);
cout << sum1 << "\n";
for (i = 0; i < n; i++)
```

```
{
                      sum2 += x[i][0] * x[i][0];
               cout << sum2 << "\n";
               base = sum1 / sum2;
               cout << " base = " << base;
               expo = 1 / I;
               cout << "expo = " << expo;
               p_G = pow(base, expo);
               cout << "\nspectral radius of G matrix = " << p_G;
               cout << "\nconvergence rate = " << -1 * log(p G);
               cout << "\ncontinue (1 or 0)?";
               cin >> ans;
       };
       _getch();
       return 0;
}
```

```
soumick@soumick-HP-Pavilion-Laptop-15-cclxx:~/hpsc_old_codes$ g++ seidel.cpp
soumick@soumick-HP-Pavilion-Laptop-15-cclxx:~/hpsc_old_codes$ ./a.out
[a].[x]=[b]
Enter Matrix a:
a[0,0] = 6
a[0,1] = 2
a[0,2] = 0
a[1,0] = 0
a[1,1] = 12
a[1,2] = 2
a[2,0] = 0
a[2,1] = 0
a[2,2] = 4
Enter Matrix b:
b[0][0] = 4
b[1][0] = 7
b[2][0] = 2
Iteration no: 0
Iteration no: 1
Iteration no: 2
Iteration no: 3
x1=0.5
x2=0.5
x3=0.5
```

```
3. Jacobi_openmp.c
```

```
# include <math.h>
# include <stdio.h>
# include <stdlib.h>
int main ();
int main ()
Purpose:
     MAIN is the main program for JACOBI_OPENMP.
 Discussion:
     JACOBI_OPENMP carries out a Jacobi iteration with OpenMP.
Licensing:
     This code is distributed under the GNU LGPL license.
 Modified:
     31 January 2017
Author:
     John Burkardt
*/
double *b;
double d;
int i;
int it;
int m;
int n;
 double r;
 double t;
double *x;
 double *xnew;
```

```
m = 5000;
 n = 50000;
 b = ( double * ) malloc ( n * sizeof ( double ) );
 x = ( double * ) malloc ( n * sizeof ( double ) );
 xnew = ( double * ) malloc ( n * sizeof ( double ) );
 printf ( "\n" );
 printf ( "JACOBI_OPENMP:\n" );
 printf ( " C/OpenMP version\n" );
 printf ( " Jacobi iteration to solve A*x=b.\n" );
 printf ( "\n" );
 printf ( " Number of variables N = %d\n", n );
 printf ( " Number of iterations M = %d\n", m );
 printf ( "\n" );
 printf ( " IT I2(dX) I2(resid)\n" );
 printf ( "\n" );
 /*
 Each thread in the loop inside the block below will have it's own copy of i
 All other variables in the loops will be shared by default because of the type
 of abstaction on which OpenMP is buit.
 */
# pragma omp parallel private ( i )
 {
 Set up the right hand side for Ax=b
*/
# pragma omp for
       for (i = 0; i < n; i++)
       b[i] = 0.0;
       b[n-1] = (double)(n+1);
 Initialize the solution estimate to 0.
 Exact solution is (1,2,3,...,N).
*/
# pragma omp for
       for (i = 0; i < n; i++)
       x[i] = 0.0;
       }
```

```
}
*
```

Iterate M times.

This outermost loop cannot be parallelised in a true sense since each iteration is dependent upon values from the previous iteration so threads corresponding to differnt iterations cannot run concurrently.

```
*/
for ( it = 0; it < m; it++ )
{
```

/*The private directive declares data to have a separate copy in the memory of each thread.

Such private variables are initialized as they would be in a main program.

Any computed value goes away at the end of the parallel region

```
# pragma omp parallel private ( i, t )
{
/*
```

Jacobi update.

_ A matrix : The main diagonal elements are all 2.

The elements of the diagonals adjacent to the main diagonal on either side are all -1.

Rest all elements are zero

The for loop below has a cannonical shape so it can be multithreaded by the complier.

Each thread in the loop below modifies a different index of the array xnew[] so there is no requirement of snooping of any kind.

Difference.

d below is the reduction variable that will hold the result of the summation

```
of values across threads.
*/
       d = 0.0;
# pragma omp for reduction (+:d)
       for (i = 0; i < n; i++)
       d = d + pow (x[i] - xnew[i], 2);
 Overwrite old solution.
 This is an "embarassingly parallel" block
*/
# pragma omp for
       for (i = 0; i < n; i++)
       x[i] = xnew[i];
 Residual.
 r below is the reduction variable that will hold the result of the summation
 of values across threads. OpenMP will take care of details like storing partial
 sums in private variables and then adding the partial sums to the shared variable.
*/
       r = 0.0;
# pragma omp for reduction (+:r)
       for (i = 0; i < n; i++)
       t = b[i] - 2.0 * x[i];
       if (0 < i)
       t = t + x[i-1];
       if (i < n - 1)
       t = t + x[i+1];
       r = r + t * t;
/*This just prints the iteration no. and L2 norm values
The omp master directive means that the section of code that follows
must be run only by the master thread
*/
# pragma omp master
       if ( it < 10 \parallel m - 10 < it )
```

```
printf ( " \%8d \%14.6g \%14.6g\n", it, sqrt ( d ), sqrt ( r ) );
        if ( it == 9 )
        printf ( " Omitting intermediate results.\n" );
        }
        }
 }
 Write part of final estimate.
 No parallel directive below
*/
 printf ( "\n" );
 printf ( " Part of final solution estimate:\n" );
 printf ( "\n" );
 for (i = 0; i < 10; i++)
        printf ( " %8d %14.6g\n", i, x[i] );
 printf ( "...\n" );
 for (i = n - 11; i < n; i++)
        printf ( " %8d %14.6g\n", i, x[i] );
 }
 Free memory to avoid creating orphaned blocks in memory created by dynamic
allocation.
 free (b);
 free (x);
 free ( xnew );
 Terminate.
 printf ( "\n" );
 printf ( "JACOBI_OPENMP:\n" );
 printf ( " Normal end of execution.\n" );
 return 0;
}
```

```
soumick@soumick-HP-Pavilion-Laptop-15-cclxx:~/MPI_codes$ gcc -o jacobi_openmp jacobi_openmp.c
soumick@soumick-HP-Pavilion-Laptop-15-cclxx:~/MPI_codes$ ./jacobi_openmp
JACOBI OPENMP:
   C/OpenMP version
   Jacobi iteration to solve A*x=b.
  Number of variables N = 50000
Number of iterations M = 5000
             12(dX)
                           l2(resid)
                           25000.5
12500.2
8839.01
6987.85
5846.46
                                                  25000.5
                                                     17678
             1
2
3
4
                                                  13975.7
11692.9
                                                  10126.4
                           5063.18
4488.03
                                                  8976.06
8090.91
                           4045.45
3692.98
                                                  7385.96
6809.52
             8
                           3404.76
                                                  6328.22
   Omitting intermediate results.
4991 31.6207
                                                  63.2319
63.2224
                           31.616
31.6112
31.6065
31.6017
         4992
                                                  63.2129
63.2034
63.194
         4993
        4994
        4995
                           31.597
31.5922
        4996
                                                  63.1845
        4997
                                                   63.175
                           31.5875
31.5828
        4998
                                                  63.1655
        4999
                                                    63.156
   Part of final solution estimate:
                                    Θ
             12345678
                                    Θ
                                    Θ
                                    Θ
                                    Θ
                                    Θ
                                    Θ
                                    Θ
                           43819.8
       49989
       49990
                           44378.4
       49991
                             44937
                           45497.5
       49992
                           46058.1
       49993
       49994
                           46620.2
                           47182.4
       49995
                           47745.7
48308.9
       49996
       49997
       49998
                           48872.9
       49999
                           49436.8
JACOBI OPENMP:
  Normal end of execution.
```

4. mxm_openmp.c

```
# include <stdlib.h>
# include <stdio.h>
# include <math.h>
# include <time.h>
# include <omp.h>
```

```
int main (void);
void timestamp (void);
int main (void)
Purpose:
     MAIN is the main program for MXM_OPENMP.
Licensing:
     This code is distributed under the GNU LGPL license.
 Modified:
     13 October 2011
 Author:
     John Burkardt
*/
The code below solves matrix matrix multiplication problem using
OpenMP for parallel execution
*/
 double a[500][500];
 double angle;
 double b[500][500];
 double c[500][500];
 int i;
int j;
int k;
 int n = 500;
 double pi = 3.141592653589793;
 double s;
 int thread_num;
 double wtime;
 timestamp ();
 printf ( "\n" );
```

```
printf ( "MXM_OPENMP:\n" );
 printf ( " C/OpenMP version\n" );
 printf ( " Compute matrix product C = A * B.\n" );
 //assigning thread number to be the maximum possible during runtime
 //More threads means less iterations per thread => lower runtime
 thread_num = omp_get_max_threads ( );
 printf ( "\n" );
 //The integer returned by this function may be less than the total no. of
 //physical processors in the multiprocessor depending on how the run-tme system
 //gives access to processors
 printf ( " The number of processors available = %d\n", omp_get_num_procs ( ) );
 printf ( " The number of threads available = %d\n", thread num );
 printf ( " The matrix order N
                                            = %d\n", n);
 s = 1.0 / sqrt ((double)(n));
 //The omp get wtime routine returns elapsed wall clock time in seconds
 wtime = omp_get_wtime ( );
//inside this block every time the program forks all threads will have their own copy
//of variables declared private by the directive below. Rest of the shared variables
//accessible by all threads at a common memory address.
# pragma omp parallel shared (a, b, c, n, pi, s) private (angle, i, j, k)
{
 Loop 1: Assign value to matrix A.
*/
 Here we parallelize the outer loop and not the inner loop.
 Reason: If we parallelize the inner loop, then the program will fork
 and join threads for every iteration of the outer
 loop. The fork/join overhead may very well be greater than the time saved by
 dividing the execution of the n iterations of the inner loop among multiple threads.
 On the other hand, if we parallelize the outer loop, the program only incurs the
 fork/join overhead once
 */
 # pragma omp for
 for (i = 0; i < n; i++)
 {
       for (j = 0; j < n; j++)
       angle = 2.0 * pi * i * j / ( double ) n;
       a[i][j] = s * (sin (angle) + cos (angle));
```

```
}
}
 Loop 2: Copy A into B.
 Here we parallelize the outer loop and not the inner loop.
 Reason mentioned in Loop 1 comment.
 # pragma omp for
 for (i = 0; i < n; i++)
       for (j = 0; j < n; j++)
       b[i][j] = a[i][j];
 }
 Loop 3: Compute C = A * B.
 Here we parallelize the outer loop and not the inner loops.
 Reason mentioned in Loop 1 comment.
*/
 Here by structure no 2 threads accesses the same index of the 3 matrices
 so no cache coherence protocols required seperately
 */
 # pragma omp for
 for (i = 0; i < n; i++)
 {
       //Traversing along row i of A
       for (j = 0; j < n; j++)
       //Traversing along column j of B
       c[i][j] = 0.0;
       for (k = 0; k < n; k++)
       //updating value of 1 element of C
       c[i][j] = c[i][j] + a[i][k] * b[k][j];
       }
       }
 }
//Calculating time taken by the code from the point A was initialised to the point
//where C was calculated and all threads joined
 wtime = omp_get_wtime ( ) - wtime;
 printf ( " Elapsed seconds = %g\n", wtime );
 printf ( " C(100,100) = %g\n", c[99][99] );
```

```
/*
Terminate.
 printf ( "\n" );
 printf ( "MXM_OPENMP:\n" );
 printf ( " Normal end of execution.\n" );
 printf ( "\n" );
timestamp ();
return 0;
}
void timestamp (void)
/************************/
Purpose:
      TIMESTAMP prints the current YMDHMS date as a time stamp.
 Example:
      31 May 2001 09:45:54 AM
 Licensing:
      This code is distributed under the GNU LGPL license.
 Modified:
      24 September 2003
 Author:
      John Burkardt
 Parameters:
      None
*/
# define TIME_SIZE 40
static char time_buffer[TIME_SIZE];
```

```
const struct tm *tm;
           time_t now;
           now = time ( NULL );
           tm = localtime ( &now );
           strftime (time_buffer, TIME_SIZE, "%d %B %Y %I:%M:%S %p", tm );
           printf ( "%s\n", time_buffer );
           return;
         # undef TIME_SIZE
Result
soumick@soumick-HP-Pavilion-Laptop-15-cclxx:~/MPI_codes$ gcc -o mxm_openmp mxm_openmp.c -lm -fopenmp soumick@soumick-HP-Pavilion-Laptop-15-cclxx:~/MPI_codes$ ./mxm_openmp
15 June 2020 02:23:02 PM
MXM_OPENMP:
  C/OpenMP version
  Compute matrix product C = A * B.
  The number of processors available = 8
The number of threads available = 8
  The matrix order N
Elapsed seconds = 0.182224
                                            = 500
  C(100,100) = 1
 MXM OPENMP:
  Normal end of execution.
```

5. Mpi_hello.c

```
//HPSC MPI tut 1
#include <stdio.h>
#include <mpi.h>

int main (int argc, char *argv[])
{
  int rank, size;

MPI_Init (&argc, &argv); /* starts MPI */
  MPI_Comm_rank (MPI_COMM_WORLD, &rank); /* get current process id */
  MPI_Comm_size (MPI_COMM_WORLD, &size); /* get number of processes */
  if(rank == 0)
    printf( "Hello world from process %d of %d\n", rank, size );
  else
    printf( "Hello world from process %d\n", rank);
```

```
MPI_Finalize();
return 0;
}
```

```
soumick@soumick-HP-Pavilion-Laptop-15-cc1xx: ~/MPI_codes

soumick@soumick-HP-Pavilion-Laptop-15-cc1xx: ~/MPI_codes$ mpicc -o HPSC_tut1_hell

o HPSC_tut1_hello.c

soumick@soumick-HP-Pavilion-Laptop-15-cc1xx: ~/MPI_codes$ mpirun -np 6 HPSC_tut1_hello

hello

Hello world from process 3

Hello world from process 4

Hello world from process 5

Hello world from process 0 of 6

Hello world from process 1

Hello world from process 2

soumick@soumick-HP-Pavilion-Laptop-15-cc1xx: ~/MPI_codes$

■
```

6. mpi_send_receive.c

/*

*/

A simple MPI example program using standard mode send and receive

The program consists of two processes. Process 0 sends a large message to the receiver. This receives the message and sends it back. This program deadlocks if the the send and receive calls are in the wrong order, i.e. if both proceesses first try to send, because the message is large enough so that standard mode send does not use buffered communication.

Compile the program with 'mpicc -O3 send-standard-large.c -o send-standard-large' Run it on two processes.

```
#include <stdlib.h>
#include <stdlib.h>
#include "mpi.h"

int main(int argc, char* argv[]) {
  const int K = 1024;
  const int msgsize = 256*K; /* Messages will be of size 1 MB */
  int np, me, i;
  int *X, *Y;
  int tag = 42;
  MPI_Status status;

MPI_Init(&argc, &argv);
```

```
MPI_Comm_size(MPI_COMM_WORLD, &np);
 MPI_Comm_rank(MPI_COMM_WORLD, &me);
 /* Check that we run on exactly two processes */
 if (np!= 2) {
       if (me == 0) {
       printf("You have to use exactly 2 processes to run this program\n");
       MPI Finalize();
                          /* Quit if there is only one process */
       exit(0);
 }
 /* Allocate memory for large message buffers */
 X = (int *) malloc(msgsize*sizeof(int));
 Y = (int *) malloc(msgsize*sizeof(int));
 /* Initialize X and Y */
 for (i=0; i<msgsize; i++) {
       X[i] = 12345;
       Y[i] = me;
 }
 //if (me == 0) {
       printf("Message size is %d bytes\n", msgsize*sizeof(int));
       printf("Process %d sending to process 1\n", me);
       MPI Send(X, msgsize, MPI INT, 1, tag, MPI COMM WORLD); //send call a
       printf("Process %d receiving from process 1\n", me);
       MPI Recv (Y, msgsize, MPI INT, 1, tag, MPI COMM WORLD, &status); //recv call
b
       printf ("Y now has the value %d\n", Y[0]);
 //} else { /* me == 1 */
       MPI_Recv (Y, msgsize, MPI_INT, 0, tag, MPI_COMM_WORLD, &status); //recv call
а
       MPI Send (Y, msgsize, MPI INT, 0, tag, MPI COMM WORLD); //send call b
//}
       After removing the if-else condition the output was
       Message size is 1048576 bytes
       Process 0 sending to process 1
```

Message size is 1048576 bytes Process 1 sending to process 1 [hang/waiting]

Explanation:

The send and receive protocol used above is "blocking".

Both Process 0 and Process 1 (running parallely) execute send call a Then Both process wait for send call b from the other processor, but before the receiver sends the message back it has to receive first(recv call a) but here recv call b is called after sender's receive call (recv call b).

Thus we see that both process are waiting for their respective receivers to send back the message which will never happen because of the order conflict in the code.

```
*/
MPI_Finalize();
exit(0);
}
```

Result

a. With the if else construct

```
soumick@soumick-HP-Pavilion-Laptop-15-cclxx:~/MPI_codes$ mpirun -np 2 HPSC_tut1_
send_recv_original
Message size is 1048576 bytes
Process 0 sending to process 1
Process 0 receiving from process 1
Y now has the value 12345
```

b. Without the if else construct

```
soumick@soumick-HP-Pavilion-Laptop-15-cclxx:~/MPI_codes$ mpirun -np 2 HPSC_tut1_
send_recv
Message size is 1048576 bytes
Process 0 sending to process 1
Message size is 1048576 bytes
Process 1 sending to process 1
```