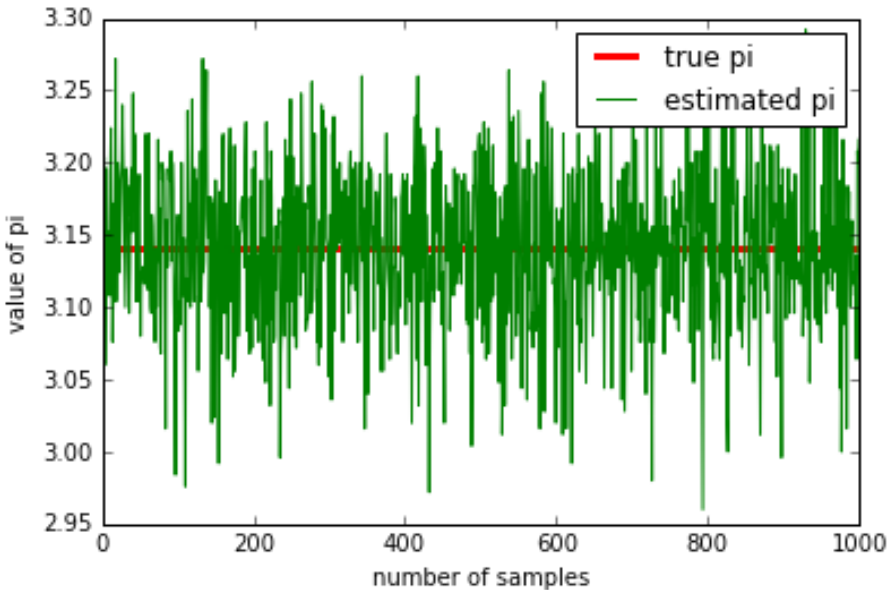


## Assignment 2

```
import random
import numpy as np
import math
import matplotlib.pyplot as plt
%matplotlib inline
def pi_calc(n):
    radius = 1
    length = float(radius * 2)
    holder_list = []
    #Assuming length of rectangle is 2. The center of circle is at
    (1,1)
    # The vertex of rectangles are at (1,1), (1,-1), (-1,1), (-1,-1)
    for i in range(1000):
        land_in_count = 0
        for i in range(n):
            x = random.uniform(-1,1)
            y = random.uniform(-1,1)
            if (x**2 + y**2) <= 1.0:
                land_in_count += 1
        rectangle_area = length ** 2
        #Circle area would be 'pi'
        probab_land_in = land_in_count / float(n)
        pi = probab_land_in * rectangle_area
        holder_list.append(pi)
    plt.plot([math.pi for i in range(n)], color = "red",linewidth=3,
label = "true pi")
    plt.plot(holder_list, color = "green", label = "estimated pi")
    plt.legend()
    plt.xlabel("number of samples")
    plt.ylabel("value of pi")
    plt.show()

pi_calc(1000)
```



1. Error bars as a function of N
  - a. The error bars in big Oh notation are  $O(1/\sqrt{N})$ . Looking at the standard error formula, we get  $SE = (\text{height} \times \text{width} \times \sqrt{(\text{ratio}(1-\text{ratio}))/N})/\text{radius}^2$ . So, we see that the error reduces as  $2\sqrt{N}$  increases.
2. Instead of putting the circle in any-sized rectangle, specifically put the circle in a square and make sure that the diameter of the circle = width of the square. If we do this, we only need ONE input i.e. the diameter = width, and we can find pi more easily because the area ratio we obtain will simply =  $(\pi \times (\text{diameter}/2)^2)/(\text{diameter}^2) = ((\pi \times \text{diameter}^2)/4)/(\text{diameter}^2) = (\pi \times \text{diameter}^2)/(4 \times \text{diameter}^2) = \pi/4$ . So,  $\pi = 4 \times \text{ratio}$ . We will not have to deal with the different heights and widths.
3. You cannot keep the estimate accurate within a given number of samples. This is because you randomly throw darts at the dartboard-- whether or not your ratio of area of circle to area of rectangle is accurate depends totally on chance. You CAN however, repeat the simulation multiple times and obtain a mean-- which will almost definitely be more accurate than single samples