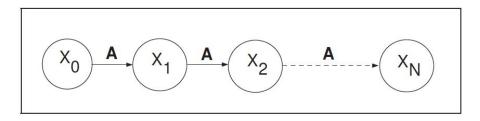
# Introducing Hidden Markov Models First – a Markov Model

A Markov Model is a chain-structured process where future states depend only on the present state, not on the sequence of events that preceded it.

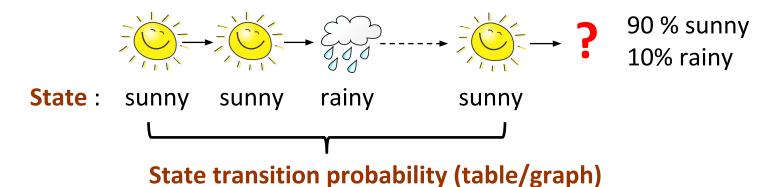


The X at a given time is called the **state**. The value of Xn depends only on Xn-1.



**State**: sunny cloudy rainy sunny?

## The Markov Model



(The probability of tomorrow's weather given today's weather)

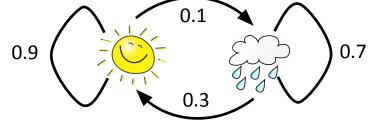
#### **Output format 1:**

Today	Tomorrow	Probability
sunny	sunny	0.9
sunny	rainy	0.1
rainy	sunny	0.3
rainy	rainy	0.7

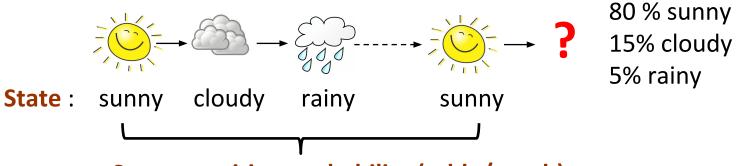
#### **Output format 2:**

	sunny	rainy
sunny	0.9	0.1
rainy	0.3	0.7

**Output format 3:** 



## The Markov Model

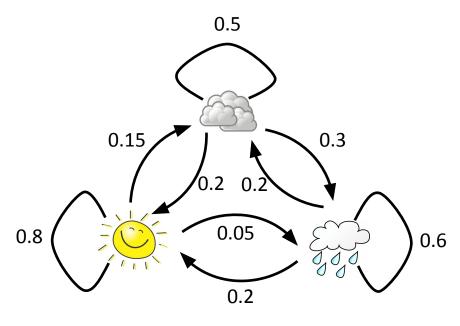


### State transition probability (table/graph)

#### **Output format 1:**

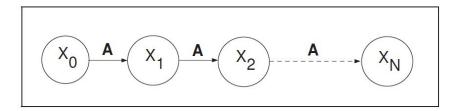
Today	Tomorrow	Probability
sunny	sunny	0.8
sunny	rainy	0.05
sunny	cloudy	0.15
rainy	sunny	0.2
rainy	rainy	0.6
rainy	cloudy	0.2
cloudy	sunny	0.2
cloudy	rainy	0.3
cloudy	cloudy	0.5

#### **Output format 3:**

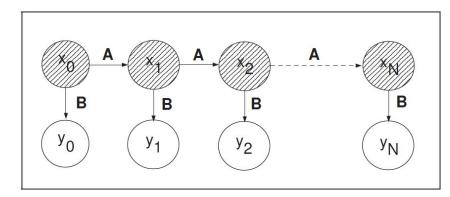


A Hidden Markov Model is a Markov chain for which the state is only partially observable.

**A Markov Model** 



A Hidden Markov Model



**Hidden states**: the (TRUE) states of a system that can be described by a Markov process (e.g., the weather).

**Observed states**: the states of the process that are 'visible' (e.g., umbrella).

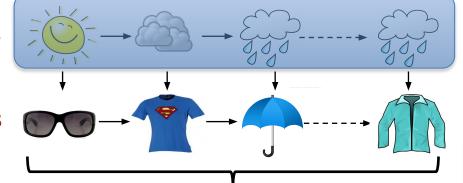
	sunny	rainy	cloudy
sunny	0.8	0.05	0.15
rainy	0.2	0.6	0.2
cloudy	0.2	0.3	0.5



#### **State transition probability table**

**Hidden States** 

**Observed States** 



State emission probability table

	sunglasses	T-shirt	umbrella	Jacket
sunny	0.4	0.4	0.1	0.1
rainy	0.1	0.1	0.5	0.3
cloudy	0.2	0.3	0.1	0.4

The probability of observing a particular observable state given a particular hidden state



The probability of switching from one state type to another (ex. Exon - Intron).

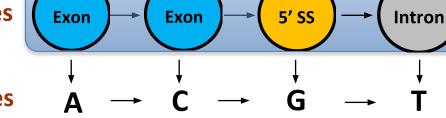
	exon	<b>5'SS</b>	intron
exon	0.9	0.1	0
<b>5'SS</b>	0	0	1
intron	0	0	0.9



**State transition probability table** 



**Observed States** 

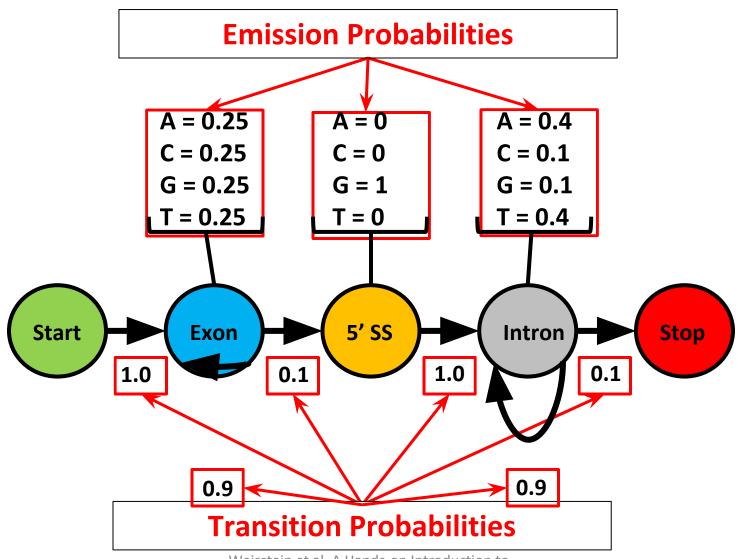


### State emission probability table

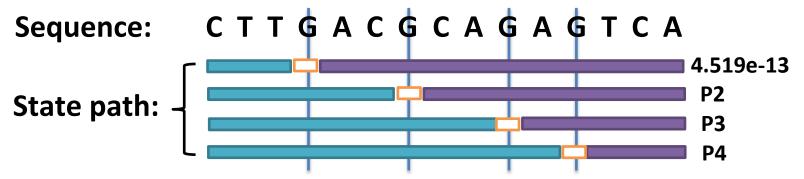
	Α	С	G	T
exon	0.25	0.25	0.25	0.25
<b>5'SS</b>	0	0	1	0
intron	0.4	0.1	0.1	0.4

The probability of observing a nucleotide (A, T, C, G) that is of a certain state (exon, intron, splice site)





## Splicing Site Prediction Using HMMs



To calculate the *probability* of each state path, multiply all transition and emission probabilities in the state path.

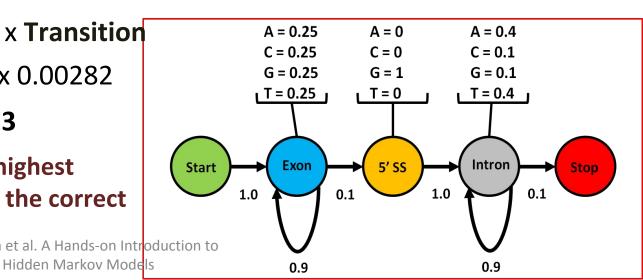
Emission =  $(0.25^3) \times 1 \times (0.4 \times 0.1 \times 0.1 \times 0.4 \times 0.1 \times 0.1 \times 0.4 \times 0.1 \times 0$ 

Transition =  $1.0 \times (0.9^2) \times 0.1 \times 1 \times (0.9^{10}) \times 0.1$ 

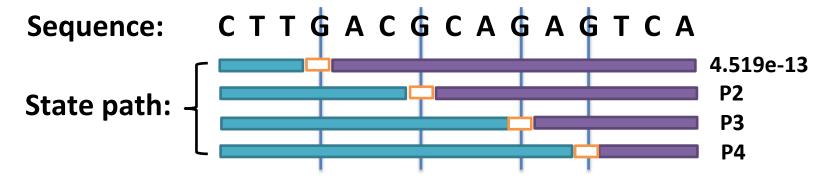
State path = **Emission** x **Transition**= 1.6e-10 x 0.00282
= **4.519e-13** 

The state path with the highest probability is most likely the correct state path.

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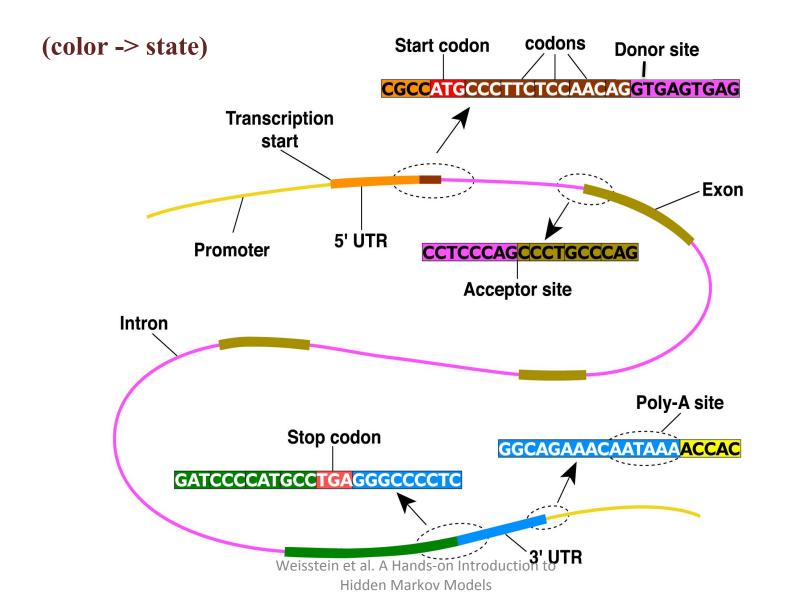
# Identification of the Most Likely Splice Site



The *likelihood* of a splice site at a particular position can be calculated by taking the probability of a state path and dividing it by the sum of the probabilities of all state paths.

likelihood of a splice site in state path #1

## **HMMs** and Gene Prediction

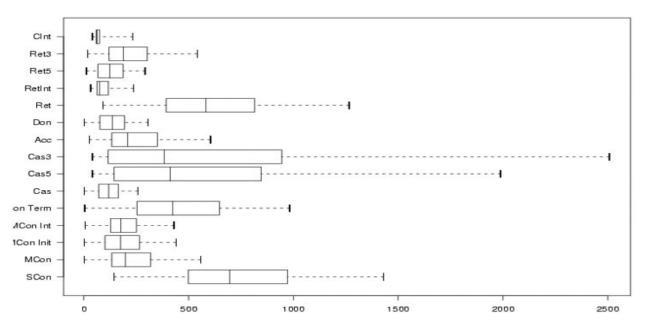


## **HMMs and Gene Prediction**

The accuracy of HMM gene prediction depends on emission probabilities and transition probabilities.

**Emission probabilities** are calculated based on the base composition in that particular state in the training data.

**Transition probabilities** are calculated based on the average lengths of that particular state in the training data.



Exon length boxplots (DEDB, Drosophila melanogaster Exon Database)

Homework Question: How do transition probabilities affect the length of predicted ORFs?

## Conclusions

- Hidden Markov Models have proven to be useful for finding genes in unlabeled genomic sequence. HMMs are the core of a number of gene prediction algorithms (such as Genscan, Genemark, Twinscan).
- Hidden Markov Models are machine learning algorithms that use transition probabilities and emission probabilities.
- Hidden Markov Models label a series of observations with a state path, and they can create multiple state paths.
- It is mathematically possible to determine which state path is most likely to be correct.