

### Stack

swatimali@somaiya.edu





#### **Outline**

- Stack concept
- Stack ADT
- Stack operations
- Stack implementations
- Stack applications
- Summary
- Queries?





#### Stack

- Last In First Out
- Elements can be added or removed only from one end
- Gives access only to element at the top of data structure





#### What is this good for ?

- To store history in a Web browser
- Undo sequence in a any application software or text editor
- Saving local variables during function calls
- Recursions
- Watchlists?



#### A Stack

- Definition:
  - An ordered collection of homogenous data items
  - Can be accessed at only one end (the top)
- Operations:
  - Create an empty stack
  - check if it is empty
  - Push: add an element to the top
  - Pop: remove the top element
  - Peek: retrieve the top element(Not the deletion)
  - Destroy: remove all the elements one by one and destroy the data structure





#### The Stack ADT: Value definition

Abstract typedef StackType(ElementType ele)

Condition: none





Abstract StackType CreateEmptyStack()

Precondition: none

Postcondition: CreateEmptyStack is created

2. Abstract StackType PushStack(StackType Stack, ElementType Element)

Precondition: Stack not full or NotFull(Stack)= True

Postcondition: stack= stack + Element at the top

Or Stack= original stack with new Element at the top





#### Abstract ElementType PopStack(StackType stack)

Precondition: Stack not empty <u>or</u> NotEmpty(Stack)= True

Postcondition: PopStack= element at the top,

Stack = stack - Element at the top

Or Stack= original stack without top Element

#### 4. Abstract DestroyStack(StackType Stack)

Precondition: Stack not empty <u>or</u> NotEmpty(Stack)= True

Postcondition: Element from the stack are removed one by

one starting from top to bottom.

Empty(Stack)= True



#### Abstract Boolean NotFull(StackType stack)

Precondition: none

Postcondition: NotFull(Stack)= true if Stack is not full

NotFull(Stack)= False if Stack is full.

#### 6. Abstract Boolean NotEmpty(StackType stack)

Precondition: none

Postcondition: NotEmpty(Stack)= true if Stack is not empty

~Empty(Stack)= False if Stack is empty.





7. Abstract ElementType Peep(StackType stack)

Precondition: Stack not empty or NotEmpty(Stack)= True

Postcondition: PeepStack= element at the top,

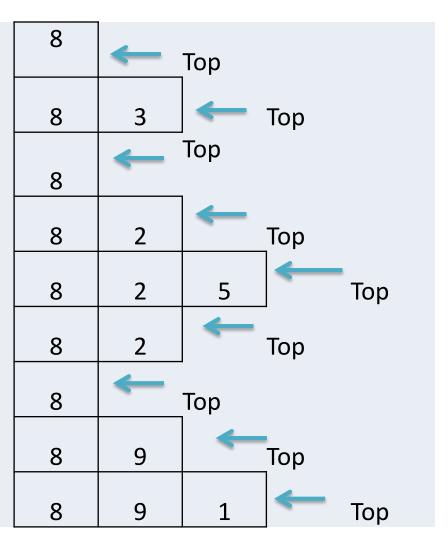
Stack = original stack





#### **Exercise: Stacks**

- -Push(8)
- -Push(3)
- -Pop()
- -Push(2)
- -Push(5)
- -Pop()
- -Pop()
- -Push(9)
- -Push(1)







#### Implementing a Stack

- At least three different ways to implement a stack
  - array
  - vector
  - linked list
- Which method to use depends on the application
  - what advantages and disadvantages does each implementation have?





#### Implementing Stacks: Array

- Advantages -best performance
- Disadvantage fixed size
- Basic implementation
  - initially empty array
  - field to record where the next data gets placed into
  - if array is full, push() returns false
    - otherwise adds it into the correct spot
  - if array is empty, pop() returns null
    - otherwise removes the next item in the stack





#### Implementing a Stack: Vector

- Advantages
  - grows to accommodate any amount of data
  - second fastest implementation when data size is less than vector size
- Disadvantage
  - slowest method if data size exceeds current vector size
    - have to copy everything over and then add data
  - wasted space if anomalous growth
    - vectors only grow in size they don't shrink
  - can grow to an unlimited size
    - I thought this was an advantage?
- Basic implementation
  - virtually identical to array based version



- Advantages:
  - always constant time to push or pop an element
  - can grow to an infinite size
- Disadvantages
  - the common case is the slowest of all the implementations
- Basic implementation
  - list is initially empty
  - push() method adds a new item to the head of the list
  - pop() method removes the head of the list



#### Writing an algorithm

- Specify algorithm name, list of inputs, data types of the inputs and return data types clearly
- Specify purpose of the algorithm
- Algo should produce at least one Output
- Definiteness: Each step must be clear and unambiguous.
- Should react correctly to all valid and invalid inputs
- Finiteness: If we trace the steps of an algorithm, then for all cases, the algorithm must terminate after a finite number of steps.
- Effectiveness:
- Comment Session: Comment is additional info of program for easily modification. In algorithm comment would be appear between two square bracket []. For example: [ this is a comment of an algorithm ].



```
Algorithm StackType CreateStack()
//This Algorithm returns an empty stack- stack
{ integer StackTop =-1;
Return stack;
2. Algorithm StackType PushStack(StackType Stack, ElementType
Element)
// This algorithm accepts a StackType stack and ElementType Element as
input and adds 'Element' at the top of 'stack'. StackTop is an integer index
that holds current value of StackTop position.
        if NotFull(Stack)= True
        stack[++StackTop]= Element
        Else "Error Message"
```





```
Algorithm ElementType PopStack(StackType stack)
// This algorithm accepts a stack as input and returns 'Element' at the
top of 'stack'.
{ if NotEmpty(Stack)= True
Return Stack[StackTop--]
Else print "Error Message"
4. Abstract DestroyStack(StackType Stack)
//This algorithm returns all the elements from Stack in LIFO order and
destroys the data structure
{ if NotEmpty(Stack) = true
   while(NotEmpty(Stack))
      print PopStack(Stack)
  else print "Error Message"
```





```
Abstract Boolean NotFull(StackType stack)
// This algorithm returns true if the stack is not full, false otherwise.
{ if NotFull(Stack)
        retrun True
 else
        return False
Abstract Boolean NotEmpty(StackType stack)
// This algorithm returns true if the stack is not empty, false otherwise.
{ if NotEmpty(Stack)
        retrun True
 else
        return False
```





7. Abstract ElementType Peek(StackType stack)
//// This algorithm accepts a stack as input and returns
'Element' at the top of 'stack'.
{ if NotEmpty(Stack)= True
Return Stack[StackTop]
Else print "Error Message"
}





```
Struct NodeType{
                 ElementType Element;
                 NodeType Next;
    Algorithm StackType CreateStack()
//This Algorithm creates and returns an empty stack- pointed by a pointer-Top
{ createNode(Top);
Top =NULL;
                                    Top
```





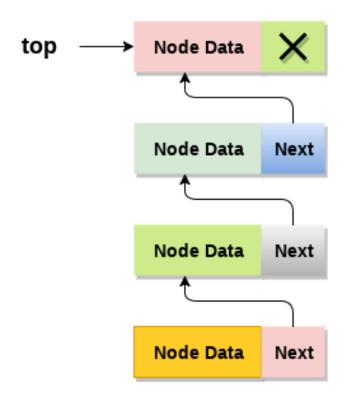




Image Courtesy: https://www.javatpoint.com/ds-linked-list-implementation-of-stack



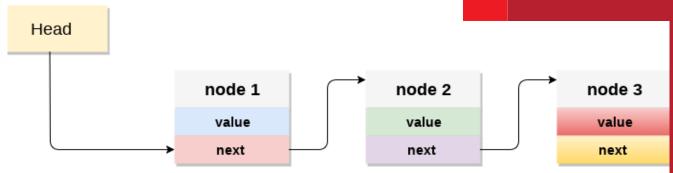
# 2. StackType PushStack(StackType Stack, NodeType NewNode)

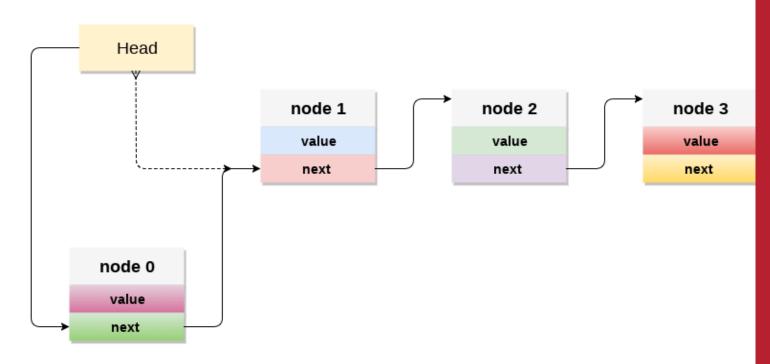
// This Algorithm adds a NewNode at the top of 'stack'. Top is an pointer that points to the topmost Stack node.

```
{ if Top ==NULL // first element in stack
          NewNode->Next = NULL;
          Top=NewNode;
Else NewNode->Next=Top;// General case
          Top=NewNode;
```









New Node

TRUST Image Courtesy: https://www.javatpoint.com/ds-linked-list-implementation-of-stack



#### 3. Algorithm ElementType PopStack(StackType stack)

//This algorithm returns value of ElementType stored in topmost node of stack. Temp is a temproary node used in pop process.





#### Abstract DestroyStack(StackType Stack)

//This algorithm returns values stored in data structure and free the memory used in data structure implementation.





5. Abstract ElementType Peep(StackType stack)
//This algorithm returns value of ElementType stored in topmost node of stack.
{ if Top==NULL Print "Error Message"

Else

Return(Top->Data);



```
Abstract DisplayStack(StackType stack)
//This algorithm Prints all the Elements stored in stack. Temp purpose?
{ if Top==NULL
       Print "Error Message"
Else {createNode(Temp)
       Temp=Top;
       While(Temp!=Null)
              Print(Temp->Data);
              Temp= Temp->next;
```



- Push(8)
- Push(3)
- Pop()
- Push(2)
- Push(5)
- Pop()
- Peek()
- Peek()
- Pop()
- Push(9)
- Push(1)





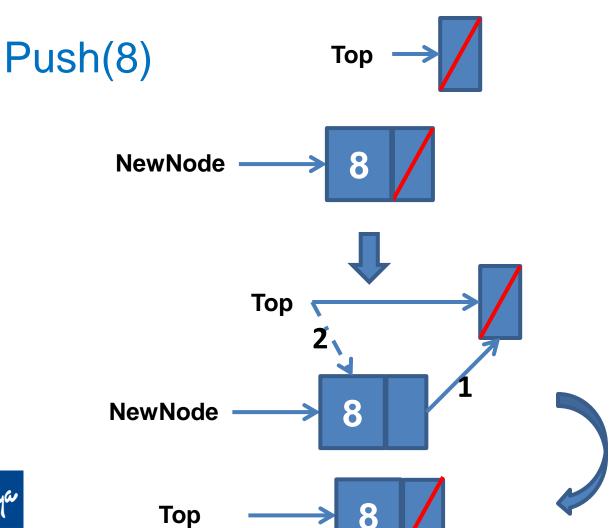
Create empty stack



Push(8)









#### **Stack Applications**

- Stacks are a very common data structure
  - Compilers(parsing data between delimiters/ brackets)
  - operating systems (program stack)
  - virtual machines
    - manipulating numbers
      - pop 2 numbers off stack, do work (such as add)
      - push result back on stack and repeat
  - Algorithms
    - backtracking
  - artificial intelligence
    - finding a path

### Stack applications



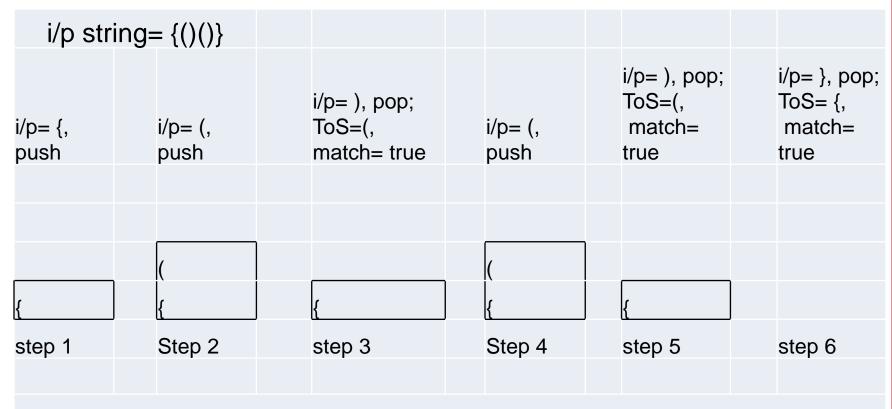
#### 1. Parentheses Matching Algorithm

```
Algorithm Boolean ParenMatch(X,n):
Input: An array X of n tokens, each of which is either a grouping symbol, a
variable, an arithmetic operator, or a number
Output: true if and only if all the grouping symbols in X match
Let S be an empty stack
for i=0 to n-1 do
    if X[i] is an opening grouping symbol then
          S.push(X[i])
    else if X[i] is a closing grouping symbol then
          if S.isEmpty() then
                     return false {nothing to match with}
          if S.pop() does not match the type of X[i] then
                     return false {wrong type}
if S.isEmpty() then
    return true {every symbol matched}
else
    return false {some symbols were never matched}
```

Stacks 34



## Parentheses Matching Algorithm

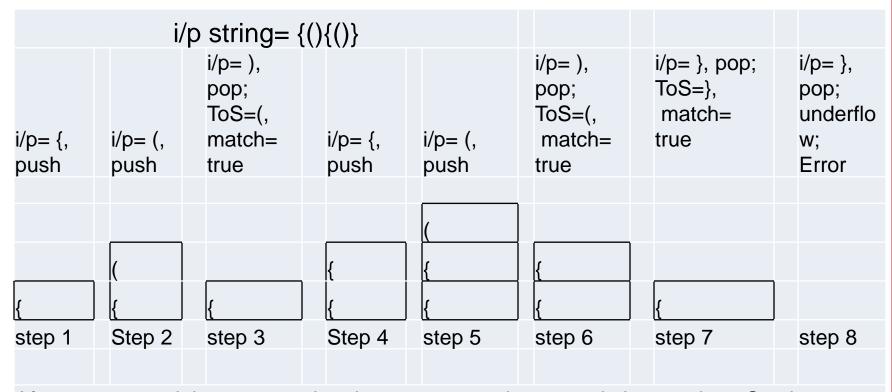


After step 6, stack is empty. So given string of parenthesis is balanced





### Parentheses Matching Algorithm



After step 8, stack is nonempty but there are more characters in input string. So given string of parenthesis is not balanced





# 2. Infix to postfix

- Infix: operand operator operand
  - E.g a+b
- Postfix: operand operand operator
  - E.g. a b +
- Operator Precedence
  - ^ exponential operator
  - **-\***, /
  - -+, -
- Infix to postfix expression with parenthesis



Stacks 37



# 2. Infix to postfix

 Infix to postfix expression with parenthesis



Stacks 38



# 2. Infix to postfix

 Infix to postfix expression with parenthesis

AB+C\*DE-FG+\*-

$$(((A + B) * C) - ((D - E) * (F + G)))$$



39



# Infix to postfix

Infix to postfix expression without parenthesis

$$A + BC^* - D - EF^* + G$$

$$ABC*+D--EF*+G$$

$$ABC*+D-EF*-+G$$





### Infix to postfix process without parenthesis

- Create an empty stack called opstack for keeping operators. Create an empty list for output.
- Scan the input string from left to right.
  - If the input is an operand, append it to the end of the output list.
  - If the token is an operator, \*, /, +, or -, push it on the opstack. However, first remove any operators already on the opstack that have higher or equal precedence and append them to the output list.
- When the input expression has been completely processed, check the opstack. Any operators still on the stack can be removed and appended to the end of the output list.



# A + B \* C - D - E \* F + G

Input char	Opstack	Output
A		A
+	+	A
В	+	AB
*	+*	AB
С	+*	ABC
_	-	ABC*+
D	-	ABC*+D
_	-	ABC*+D-
E	-	ABC*+D-E
*	-*	ABC*+D-E
F	-*	ABC*+D-EF
+	+	ABC*+D-EF*-
G	+	ABC*+D-EF*-G
NULL	<b>EMPTYSTACK</b>	ABC*+D-EF*-G+



SOLVE : M\*N+T^Q/F\*A+B

 $MN*TQ^F/A*+B+$ 



## Infix to postfix process with parenthesis

Let, X is an arithmetic expression written in infix notation. This algorithm finds the equivalent postfix expression Y.

- Scan X from left to right and repeat Step 2 to 5 for each element of X until the Stack is empty.
- 2. If an operand is encountered, add it to Y
- 3. If a left parenthesis is encountered, push it onto Stack.
- 4. If an operator is encountered, then:
  - Repeatedly pop from Stack and add to Y each operator (on the top of Stack) which has the same precedence as or higher precedence than operator until an opening parenthesis is encountered.
  - Add operator to Stack.
- 5. If a right parenthesis is encountered ,then:
  - Repeatedly pop from Stack and add to Y each operator (on the top of Stack) until a left parenthesis is encountered.
  - Remove the left Parenthesis.
- 6. END.



```
Input: input expression: (((A + B) * C) - ((D - E) * (F + G)))
Input char
                         stack
                                                                    Output
                         ((
                         (((
                         (((
                                                                    Α
           Α
                         (((+
                                                                    Α
            +
           В
                         (((+
                                                                    AB
                                                                    AB+
                         ((
                         ((*
                                                                    AB+
                         ((*
           C
                                                                    AB+C
                                                                    AB+C*
                                                                    AB+C*
                                                                    AB+C*
                         (-(
                                                                    AB+C*
                         (-((
                                                                    AB+C*D
           D
                         (-((
                         (-((-
                                                                    AB+C*D
           Ε
                         (-((-
                                                                    AB+C*DE
                                                                    AB+C*DE-
                         (-(
                         (-(*
                                                                    AB+C*DE-
                                                                    AB+C*DE-
                         (-(*(
                                                                    AB+C*DE-F
                         (-(*(
                                                                    AB+C*DE-F
                         (-(*(+
           +
           G
                                                                    AB+C*DE-FG
                         (-(*(+
                                                                    AB+C*DE-FG+
                         (-(*
                                                                    AB+C*DE-FG+*
                         EMPTY
                                                                    AB+C*DE-FG+*-
```



## 3. Evaluation of postfix expression

- Create a stack for storing operands
- Scan the input expression from left to right
  - If the element is operand, push it onto the stack
  - If the element is operator, pop two operands, evaluate and push the result onto the stack
- If the expression is over, the stack contains the final answer



```
Input: input expression: AB+C*DE-FG+*-
      e.g. A=2, B=3,C=1,D=4,E=5, F=7, G=8
Input char
                stack
                2, 3
                (2+3)=5
                5, 1
                (5*1)=5
                5,4
                5,4,5
                5,-1
                5,-1,7
                5,-1,7,8
                5,-1,15
                5,-15
                20
```



## 4. Reverse a string using Stack

- 1) Create an empty stack.
- 2) One by one push all characters of string to stack.
- 3) One by one pop all characters from stack and put them back to string.





## 5. Check if a string is palindrome

- 1) Push the input string onto the stack
- 2) POP characters ONE by one from stack and compare with string characters from left to right
- 3) If all comparisons are true, the string is palindrome





#### 6. Recursion

- Definition: calling the same function again directly or indirectly
- Concept: represent a problem in terms of one or more smaller problems, and add one or more base conditions that stop the recursion.
- The maximal number of nested calls (including the first one) is called recursion depth.





#### 4. Recursion

## Self study:

Recursive Vs iterative implementation



# SOMATYA VIDYAVIHAR UNIVERSITY K J Somaiya College of Engine Cursive function call

- The current function is paused.
- The execution context associated with it is remembered in a special data structure called execution context stack.
- The nested call executes.
- After it ends, the old execution context is retrieved from the stack, and the outer function is resumed from where it stopped.



# SOMATYA VIDYAVIHAR UNIVERSITY K J Somaiya College of Engine Cursive function call

- In each recursive call, there is need to save the
  - current values of parameters,
  - local variables and
  - the return address (the address where the control has to return from the call).
- Also, as a function calls to another function, first its arguments, then the return address and finally space for local variables is pushed onto the stack.





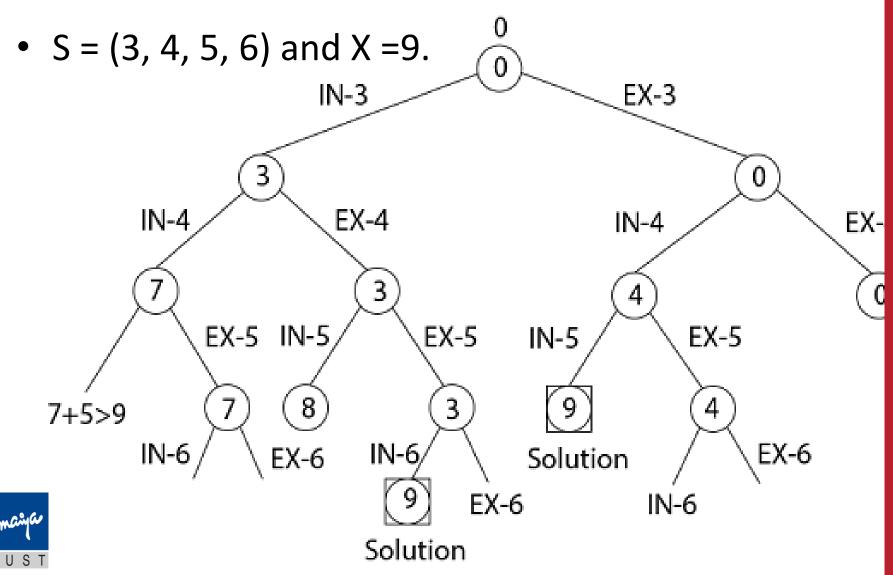
# Backtracking

- Backtracking is an algorithmic-technique for solving problems recursively by trying to build a solution incrementally, one piece at a time, removing those solutions that fail to satisfy the constraints of the problem at any point of time.
- Uses stack for storing solution path





# Summer of subsets Backtracking



# Queries?

# Thank you!