PRACTICE PROBLEMS ON MAXIMA AND MINIMA

Find the extreme values of the following functions:

1.
$$x^2y^3(1-x-y)$$

3.
$$xy(3a - x - y)$$

5.
$$x^2y - 3x^2 - 2y^2 - 4y + 3$$

7.
$$y^2 + 4xy + 3x^2 + x^3$$

2.
$$x^3y^2(1-x-y)$$

4.
$$xy(3 - x - y)$$

6.
$$x^3 + 3xy^2 - 3x^2 + 3y^2 + 4$$

8.
$$2(x^2-y^2)-x^4+y^4$$

9. Find the maximum value of
$$\cos A \cos B \cos C$$
, where A, B, C are angles of a triangle.

10. Find the maximum volume of a parallelepiped inscribed in a sphere
$$x^2 + y^2 + z^2 = a^2$$

11. A rectangular box with open top has volume V. Find the dimensions of the box requiring least material.

ANSWERS

1. Max. value
$$1/432$$
 at $(1/3, 1/2)$.

3. Max. value
$$a^3$$
 at (a,a).

5. Max. value 5 at
$$(0, -1)$$
.

7. Min. at
$$\left(\frac{2}{3}, \frac{-4}{3}\right)$$

9. Max. value
$$\frac{1}{8}$$
 at $\left(\frac{\pi}{3}, \frac{\pi}{3}\right)$

11.
$$x = y = 2z$$

2. Max. value
$$1/432$$
 at $(1/2, 1/3)$.

10.
$$8a^3/3\sqrt{3}$$
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