- Prob Archana Sharma

- #. Waves are barically of 2 types.
- (i) Longitudinal waves: A wave ni which particles of the medium oscillate to 4 fro along the direction of propagation.
- particle of the medium oscillates up 4 down at right angles to the direction of wave propagation.
- # Unpolarised light: The ordinary light consists of very large number of vibrations in all planes with equal probability at eight angles to the direction of propagation.
- # Plane Polarised light: In plane polarized light the vibrations are along a straight line in a plane I to the direction of propagation.

 If the direction of vibration is parallel to the plane of paper, it is represented by a straight line arrow. Fig 1.(a).

 If the direction of vibration is perpendicular to the plane of the paper, it is represented by a dot. Fig. 1(b)
 - (i). Unpolarized light:

1-a(ii) Plane polarized light

1.6(111) Plane polarized light:

(Vib" 11 to the plane of paper)

(Vib" I to the plane of paper)

Unpolarized light

- 1. Consists of waves with planes of vibrations equally distributed in all directions about the ray direction.
- 2. Symmetrical about the ray dir.
- 3. Produced by conventional light
 sources
- 4. May be regarded as the result.

 ant of 2 incoherent waves of

 equal intensity but polarized in
 mutually \perp planes.

++++

THE STATE STATE OF THE STATE OF

the Plane Phlatical Capit Ina Plane potential to the

by the chiestons of the orbitalism of perpendicular

Polarized light.

- 1. Consists of waves having their electric field vactor vibrating in a single plane normal to ray direction.
- 2. Asymmetrical about the ray direction.
- 3. Is to be obtained from unpolarized light with the help of polarizers:
- 4. May be regarded as H. resultant of two mutually.

 L coherent waves having zero phase difference.

(4) 1 . FT . . the a

place planesian Ip

PRODUCTION OF PLANE POLARIZED LIGHT

Plane polarized light may be produced from unpolarized light using the following optical phenomena.

(i) Polarization by reflection

(ii). By double repraction

Polarization.

Method 1: Polarization by reflection (Brewestern law).

The simplest way of producing a plane polarized light is by reflection.

When ordinary light is reflected from the surface of a transparent medium like glass or water it becomes partially polarized. The degree of polarization changes with the angle of incidence. At a particular angle of merdence the reflected light has the greatest percentage of polarised light, whereas the angle depends upon the nature of the reflecting surface.

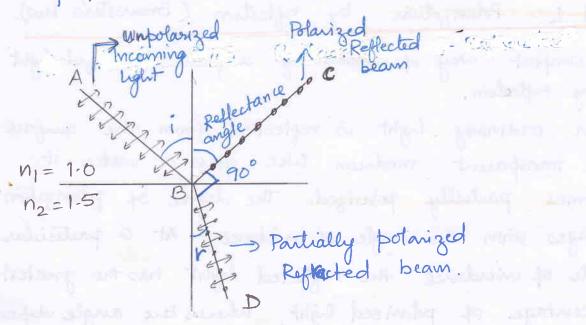
The angle of incidence is known as angle of

Brewester observed that for a particular angle of incidence known as angle of polarization, the reflected light is completely polarized in the in the plane of incidence. I've having plane of vibration peopendicular to the plane of incidence.

Brewester proved that the tangent of the angle of polarization (P) is numerically equal to the refractive index (µ) of the medium.

i.e M = tan p.

This is known as Brewester's law. He also proved that the reflected of prefracted rays are performancellar to each other.



If a natural light is incident on a smooth surface at the polarizing angle, it is reflected along BC that the differented along BD. Brewester found that the maximum polarization of reflected vary occurs when it is at eight angles to the refracted rays. i.e. i+r=90°.

According to Snell's law,

Sm i = 1/2 Sm r = 1/41

where μ_2 : Refractive index of the reflecting surface and μ_1 : refractive index of the surrounding medium.

$$\frac{\sin i}{\sin (90-i)} = \frac{\mu_2}{\mu_1} = \frac{\sin i}{\cos i} = \frac{\mu_2}{\mu_1}$$

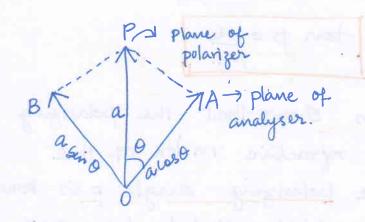
$$\frac{\tan i}{\mu_1} = \frac{\mu_2}{\mu_1} = \frac{\tan p}{\mu_1} = \frac{\mu_2}{\mu_1}$$

in the above equation shows that the polarizing angle depends on the refractive index of the reflecting surface. The polarizing angle p is known as Brewester's angle. Light reflected from any angle other than Brewester angle is partially polarized.

MALUS'S LAW

According to Malus, when a completely plane polarised light beam is incident on the analyser, the intensity of the polarized light transmitted. Through the analyser varies as the square of the cosine of the angle byw the plane of transmission of the analyser of the plane of polariser.

Proof: Let OP = a be the amplitude of the vicident plane polarized light from a polarizer and 0, the angle byw the planes of polarizer & analyser. The amplitude of vicident plane polarized light can be resolved in two components, one parallel to the plane of transmission of analyser (a cos 0) and the other perpendicular to it (a snio). The component a cor 0 is transmitted through the analyser.



Intensity of the transmitted light through the analyser $I_0 = (a\cos \theta)^2 = a^2\cos^2\theta$.

If I be the intensity of incident polarized light, then $I = a^2$ $I_0 = I \cos^2 \theta \qquad \qquad I_0 \ll \cos^2 \theta.$

- (i) When 0=0, i.e the two planes are parallel $I_0=1$ as $\cos 0=1$.
- (ii) when $0 = \frac{\pi}{2}$, i.e. the two planes are perpendicular $\Gamma_0 = 0$.
- (iii) when $O=\Pi$, the axes are parallel. $I_o=\frac{I_o}{2}$
- (iV) when $0=270^{\circ}$: the axes one perpendicular I=0.

Thus, we obtain two positions of maximum intensity and two positions of zero intensity when we notate the axis of the analyzer with respect to that of the polarizer.

DOUBLE REFRACTION

Evasmus (1869) discovered that when a beam of ordinary unpolarised light is parsed through a calcite crystal, the refracted light is split up into two refracted rays. The one which always obeys the ordinary laws of refraction thaving vibrations I to the principal section is known as ordinary rays. The other ray in general doesn't obey the laws of refraction and having vibrations in the principal areas. Section is called as extraordinary rays.

Both the rays are plane-polarized. This phenomenon is known as Double Refraction OR.

BIREFRINGENCE.

The crystal showing this phenomenon is known as Doubly refracting crystal. There are 2 types of doubly refracting crystals.

i) Unioxial: In unioxial crystals, there is only one direction Coptic axes) along which the two reported mys travel with the same relocity.

Eq: Townshire, Carite & Quartz crystal

(ii) Biaxial: In Bravial crystals, there are two such directions along which the velocities are same.

Eg: Topaz & Aragonite etc.

Description of a standard and a standard of the standard of th

** Polarizer: It is an optical instrument, which utilizes the phenomenon of selective absorption or double refraction and transforms impolarized light into polarized light. Plane polarized light is obtained by eliminating one of the two components in the impolarized light.

When natural light is meident on a polarizer, the E-fild component that is parallel to the chains of Todnie atoms induces current in the conducting chains

Tooline atoms induces current in the conducting chains and is therefore Strongly absorbed. Hence, the light transmitted contains only the component that is perpendicular to the direction of motecular chains.

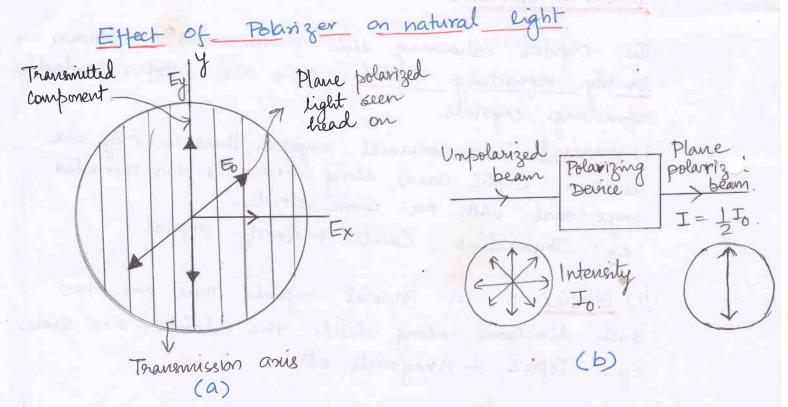


Figure: (a) Action of polarizer on linearly polarized wave.

(b) The intensity of an unpolarized beam reduces to half after passing through a polarizer.

* Action of polarizer on the incident upolarized light.

If an unpolarized light is merdent on a polarizer with electric field vector E_0 making an arighe θ w.r.t the transmission axis of the polarizer. Then, E_0 may be revolved into its component vectors lying II and \bot to the transmission axis. Of the polarizer, i.e. Ey II to the axis and $E_{\infty} \bot$ to the transmission axis. The polarizer transmits the parallel component while blocking the perpendicular Component. As $E_{\gamma} = E_0 \cos \theta$ Hence, intensity of the transmitted components is given by

Hence, Intensity of the transmitted components is given by $I \propto E_y^2 = E_0^2 \cos^2 \theta$

In unpolarized light all the values of 0 are equally probable. Therefore, the fraction of light transmitted through the polarizer equals the average value of $\cos^2 0$, which is equal to 1/2.

Thus, $I = E_0^2/2 = I_0/2$.

** Analyser: — It is an optical element, which is used to identify the plane of vibration of plane polarized light.

It is not different in structure from the polarizer.

Only its working differs.

of all sould seek with our that he had dispute till

NICOL'S PRISM . THE MAN THE RESIDENCE OF THE PRISM .

Principle:— It's a device to produce plane polarized light.

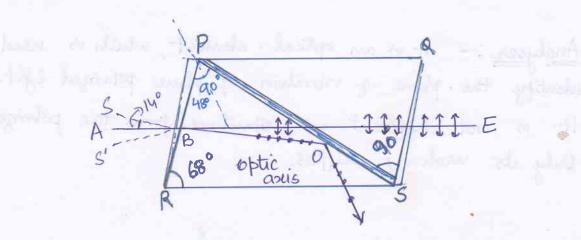
It is known that when an ordinary line passe is toamsinstead through a calcula crystal, it splits no o-ray and
e-ray which are completely plane polarized with vibrations
in two mutually I planes.

If one beam is eliminated then the emergent beam from
the calcula crystal will be plane-polarized light.

In 1828, Nicol eliminated the ordinary beams by utilizing the phenomenon of total reflection at thin film of
canada balsam separating the two pieces of calcula.

The device is known as Nicol's prism.

Construction! A calcule crystal with length 3 times its windth is taken. The end taces are grounded such that the angles in the principal Section becomes 68° and 112° instead of 71° and 109°.



The crystal is cut into two pieces by a plane I to the principal section as well as the end faces PR and QS. The two cut surfaces are grounded and polished optically flat and then, cemented together by Canada Balsam.

The refractive indexes for the ordinary and extraordinary rays for calcite. For soduin Differences, the values are given below:

Refractive index for ordinary $\mu_0 = 1.6588$ Refractive videx for canada balsam $\mu = 1.55$ Refractive index for extraordinary $\mu = 1.486$.

Action: when a beam of light A+3 extens the faces PIR wi direction parallel to the long side, it is doubly refracted into ordinary plane polarised beam BE. It is clear that canada balsam layer acts a a reser medium for an o-ray and denser medium for e-ray. The dimensions of the crystal are chosen such that the angle of incidence for o-ray at the CB surface becomes greater than the corresponding critical angle 69°.

Under these conditions, the o-ray is completely reflected at calcite-balsam surface and is absorbed by the two containing the Nicol's Prism. The e-ray is not totally reflected because it is travelling from a rarer to a denser medium and it thus transmitted with no-appreciable loss in intensity. It is slightly displaced laterally but emerges out of prism parallel to its original direction. Thus, only e-ray is transmitted. Since, e-ray is plane polarised having vibrations parallel to principal plane, the light emerging from the Nicol's prism is plane polarised.

Uses: <u>Nicol's priem</u> can be used as both polasiser and an analyser.

- when two Nicols are arranged co-axially, then the first Nicol which produces plane polarised light is known as polariser while the second which analyses the polarised light is known as analyser.
- when the Nicols are placed with their principal sections parallel to each other as shown in Fig (a) then the e-ray transmitted by one is freely transmitted by the other. If the second prism is gradually rotated, then the intensity of e-ray gradually decreases.
 - -) when the two Nicol's are at englit angle to each other (Fig. b) i.e, they are in a crossed position, no light comes from second prism.

This is due to the fact that when the polarised e-rays enters the Second Nicol's prism, it acts as 0-ray t is totally internally reflected. Therefore, the first Nicol's prism N, produces plane polarised light the second Nicol's prism N2 detects it.

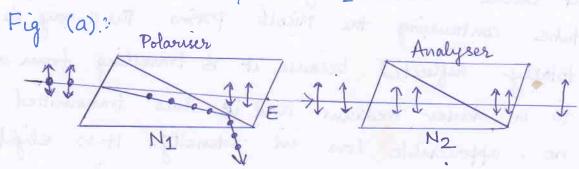
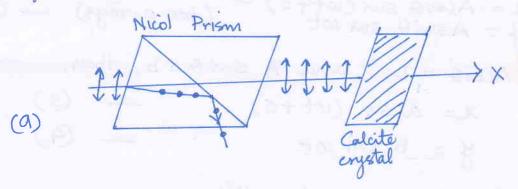


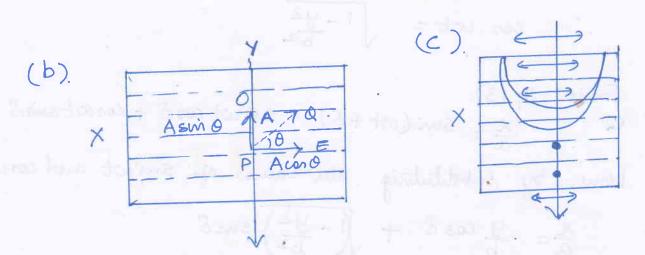
Fig (b):

ELLIPTICALLY AND CIRCULARLY POLARISED LIGHT.

Consider a beam of plane polarized light falling normally on a calcute crystal cut with its optic axis parallel to its faces. Fig (a).

Let A=PQ(b) be the maximum amplitude of incident light which makes angle of with optic axis. The plane polarized light on entering the crystal is split up in two components. O-ray and e-ray i.e., the amplitude A of incident plane polarized light is divided into two parts.





(i) The amplitude of 0-rays (vib" I to optic axis) as Asmio along PO.

ii) The amplitude of e-rays (vib" along optic axis) as Acoso along PE.

From the theory of double referaction, the o-ray and e-rays thus produced, traverses in the crystal in the same direction but with different velocities as mi Fig. (c). On emerging from the crystal their have a phase difference (8) depending upon the thickness of crystal. Thus, we have 2 waves / 2 harmonic motions having amplitudes A cord and A soil, vibrating along I directions. (along and I to optic axis) and having a phase difference 8, depending upon the truckness of the crystal. The equations for such waves can be written as $\chi = A\cos\theta \sin(\omega t + \delta)$ (for 0-rays) — (1) $\chi = A\sin\theta \sin\omega t$ (for 0-rays) — (2). Smid = b, then, Let Acoro = a and A $x = a \leq m (\omega t + \delta) \qquad - \qquad (4)$ y = b swi wt From eq. 4; Sm: wt = 9/6 $cos wt = \sqrt{1 - \frac{y^2}{b^2}}$ From eq.(3). $\frac{x}{a} = \sin(\omega t + \delta) = \sin \omega t \cos \delta + \cos \omega t \sin \delta$

Now, by substituting the values of smiwt and concet. $\frac{\chi}{a} = \frac{y}{b} \cos \delta + \sqrt{1 - \frac{y^2}{b^2}} \sin \delta$ $\frac{\chi}{a} - \frac{y \cos \delta}{b} = \sqrt{1 - \frac{y^2}{b^2}} \sin \delta.$

Now, squering both the sides, we get,
$$\frac{x^2}{a^2} - 2 \frac{xy}{ab} \cos \delta + \frac{y^2 \cos^2 \delta}{b^2} = \left(1 - \frac{y^2}{b^2}\right) \sin^2 \delta$$

or
$$\frac{x^2}{a^2} = \frac{2\pi y \cos \delta}{ab} + \frac{y^2(\cos^2 \delta + \sin^2 \delta)}{b^2} = \sin^2 \delta$$

or
$$\frac{x^2}{a^2} + \frac{y^2}{b^2} - \frac{2xy}{ab} \cos \delta = \sin^2 \delta$$
. - (5)

This is the general equation of ellipse.

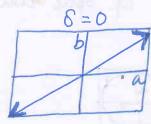
Special Cases:

1.) When
$$\delta = 0^{\circ}$$
, $\sin \delta = 0$ and $\cos \delta = 1$.

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} - \frac{2\pi y}{ab} = 0$$

$$\left(\frac{x}{a} - \frac{y}{b}\right)^2 = 0 \Rightarrow \frac{x}{a} = \frac{y}{b}$$
and
$$y = \frac{bx}{a} \qquad (6)$$

This is the equ of Storight line. Therefore, the light will be plane polarised light with vibrations mi the same plane as ni incident light. as nis Fig 1. (a) H Alfar 24



2) When
$$\delta = (2n+1)\frac{11}{2}$$
 where $n = (0,1,2,3,...)$
 $\delta = \frac{\pi}{2}, \frac{3\pi}{2}, \frac{5\pi}{2}, ...$

Here, eqn (5) reduces to
$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1. \qquad \qquad (7.).$$
(as Sin $\delta = 1$; cos $\delta = 0$.).

This represents the equation of a symmetrical ellipse.

Thus, the energent light in this case will be elliptically polarised as in Fig 1(b) and (d)

Fig
$$1(d)$$
.
$$8 = 3\pi/2$$

3) When
$$\delta = \frac{\pi}{2}$$
 and $a = b$, then eq^h 5 becomes $\pi^2 + y^2 = a^2$. (8).

this prepresents the equation of a circle. Thus, the emergent light will be circularly polarised.

This happens when 0=45°, i.e., the micident plane polarised light on the crystal makes an angle of 45° with the direction of offic axis. Fig 1 (+) and(g)

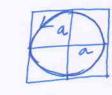


Fig 1.(f)

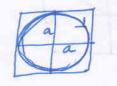


Fig. 1 (g).

- (i) If the light vector vibrates along a straight line, it will be a plane polarised light.
- (ii) If the light vector rotates along a circle i.e doesn't changes the magnitude, but traces a circular path while rotating (thus, circularly polarised).
- (111) If light vector sotates along allipse i.e. changes in magnitude while notating, it will be elliptically polarised. (i.e. the talls traversed by the light is an ellipse)

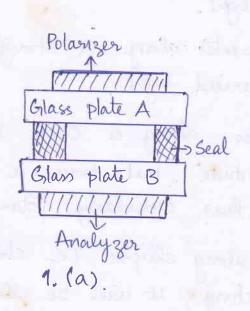
APPLICATIONS

1). LCD's : Liquid Crystal display's

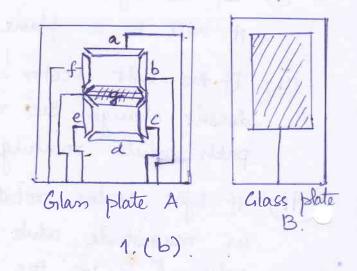
LCD applications is used no worist watches, computer screens, timers and clocks. These dences are based on the interaction of rod-like liquid crystalline molecules with an electric field and polarized light waves.

A LCD barically consists of a liquid crystal material, which is double suffracting, of about 10 mm thinks Suitably supported byw two their glass plates having transparent conducting coatings on their inner surfaces. (1a) The conducting coating is etched in the torm of a digit or character as shown in Fig 1(b).

The assembly of glass plates with liquid crystal material is sandwitched byw two crossed-polarizer sheets.



the front polarizer.



During the fabrication of LCD's, the liquid crystals molecules are aligned in such a way that their long axes undergo a 90° Autation as shown in Eig 2. It is called a twisted molecular assangement. When natural light is incident on the assembly, the front polarizer converts it into linearly polarized light propagates through the LCD, the optical vector is rotated through 90° by the twisted molecular arrangement. Therefore, it passes unhindered through the sear polarizer whose transmission axis is perfendicular to that of the front polarizer.

A reflecting coating at the back of the rear polarizer sends back the light, which emerges unobstructed by

Consequently, the display appears uniformly illuminated. When a voltage is applied to the device, the molecules blue the electrodes untwist and align along the field direction. As a result, the optical vector does not undergo rotation as it passes through that region. The rear polarizer blocks the light and therefore, a dark digit or character is seen in that region.

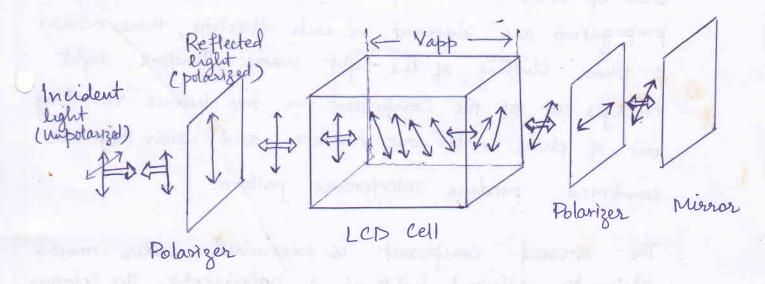


Fig 2.

2:) Photoelasticity

this is an experimental method to determine stress distribution in various engineering components. Its especially useful for the study of objects with virigular boundaries and stress concentrations, such as pieces of machinery with notches or curves, structural components with slits or holes, and materials with cracks.

Penniciple: The method is based on the property of double refraction, which is exhibited by photoelastic materialson the application of stress.

Birefringence is the property by virtue of which a may of light passing through a birefringent material splits into 2 beams (0-ray + e-rays). The path of the beams are same and their speed at each pt. is related to the state of stress at that point. As the relocation of light propagation are different in each direction, there occurs a phase shifting of the light waves. Therefore, light emerges out of the component as two beams vibrating out of phase with one another and when they are combined, produce interference pattern.

The stressed component is examined under monochromatic polarized light in a palariscope the polarizer in the polariscope produces polarized light. When the analyzer in the polariscope recombines with the waves, interference pattern is observed. Regions of stress where the wave phases cancel appears dark and regions of stress where the waves phases add appears bright.

Therefore, in models of complex stress distribution, bright & dark forige patterns (Isochromatic fringes) are projected from the model. As these fringes are related to the Stresses, the magnitude & direction of stresses at any point can be determined by examination of the fringe pattern. When the fringe component is unloaded, the photoelastic fringe pattern disappears.