

# 01\_math\_module

October 27, 2019

```
[1]: import math
```

```
[2]: print(dir(math))
```

```
['__doc__', '__loader__', '__name__', '__package__', '__spec__', 'acos',  
'acosh', 'asin', 'asinh', 'atan', 'atan2', 'atanh', 'ceil', 'copysign', 'cos',  
'cosh', 'degrees', 'e', 'erf', 'erfc', 'exp', 'expm1', 'fabs', 'factorial',  
'floor', 'fmod', 'frexp', 'fsum', 'gamma', 'gcd', 'hypot', 'inf', 'isclose',  
'isfinite', 'isinf', 'isnan', 'ldexp', 'lgamma', 'log', 'log10', 'log1p',  
'log2', 'modf', 'nan', 'pi', 'pow', 'radians', 'remainder', 'sin', 'sinh',  
'sqrt', 'tan', 'tanh', 'tau', 'trunc']
```

```
[3]: help(math)
```

Help on built-in module math:

NAME

math

DESCRIPTION

This module provides access to the mathematical functions  
defined by the C standard.

FUNCTIONS

acos(x, /)

Return the arc cosine (measured in radians) of x.

acosh(x, /)

Return the inverse hyperbolic cosine of x.

asin(x, /)

Return the arc sine (measured in radians) of x.

asinh(x, /)

Return the inverse hyperbolic sine of x.

atan(x, /)

Return the arc tangent (measured in radians) of x.

`atan2(y, x, /)`

Return the arc tangent (measured in radians) of y/x.

Unlike `atan(y/x)`, the signs of both x and y are considered.

`atanh(x, /)`

Return the inverse hyperbolic tangent of x.

`ceil(x, /)`

Return the ceiling of x as an Integer.

This is the smallest integer  $\geq x$ .

`copysign(x, y, /)`

Return a float with the magnitude (absolute value) of x but the sign of y.

On platforms that support signed zeros, `copysign(1.0, -0.0)` returns -1.0.

`cos(x, /)`

Return the cosine of x (measured in radians).

`cosh(x, /)`

Return the hyperbolic cosine of x.

`degrees(x, /)`

Convert angle x from radians to degrees.

`erf(x, /)`

Error function at x.

`erfc(x, /)`

Complementary error function at x.

`exp(x, /)`

Return e raised to the power of x.

`expm1(x, /)`

Return  $\exp(x)-1$ .

This function avoids the loss of precision involved in the direct evaluation of  $\exp(x)-1$  for small x.

`fabs(x, /)`

Return the absolute value of the float x.

```

factorial(x, /)
    Find x!.

    Raise a ValueError if x is negative or non-integral.

floor(x, /)
    Return the floor of x as an Integral.

    This is the largest integer  $\leq x$ .

fmod(x, y, /)
    Return fmod(x, y), according to platform C.

     $x \% y$  may differ.

frexp(x, /)
    Return the mantissa and exponent of x, as pair (m, e).

    m is a float and e is an int, such that  $x = m * 2.^e$ .
    If x is 0, m and e are both 0. Else  $0.5 \leq \text{abs}(m) < 1.0$ .

fsum(seq, /)
    Return an accurate floating point sum of values in the iterable seq.

    Assumes IEEE-754 floating point arithmetic.

gamma(x, /)
    Gamma function at x.

gcd(x, y, /)
    greatest common divisor of x and y

hypot(x, y, /)
    Return the Euclidean distance,  $\sqrt{x^2 + y^2}$ .

isclose(a, b, *, rel_tol=1e-09, abs_tol=0.0)
    Determine whether two floating point numbers are close in value.

    rel_tol
        maximum difference for being considered "close", relative to the
        magnitude of the input values
    abs_tol
        maximum difference for being considered "close", regardless of the
        magnitude of the input values

    Return True if a is close in value to b, and False otherwise.

```

For the values to be considered close, the difference between them must be smaller than at least one of the tolerances.

-inf, inf and NaN behave similarly to the IEEE 754 Standard. That is, NaN is not close to anything, even itself. inf and -inf are only close to themselves.

isfinite(x, /)

Return True if x is neither an infinity nor a NaN, and False otherwise.

isinf(x, /)

Return True if x is a positive or negative infinity, and False otherwise.

isnan(x, /)

Return True if x is a NaN (not a number), and False otherwise.

ldexp(x, i, /)

Return  $x * (2^{**i})$ .

This is essentially the inverse of frexp().

lgamma(x, /)

Natural logarithm of absolute value of Gamma function at x.

log(...)

log(x, [base=math.e])

Return the logarithm of x to the given base.

If the base not specified, returns the natural logarithm (base e) of x.

log10(x, /)

Return the base 10 logarithm of x.

log1p(x, /)

Return the natural logarithm of 1+x (base e).

The result is computed in a way which is accurate for x near zero.

log2(x, /)

Return the base 2 logarithm of x.

modf(x, /)

Return the fractional and integer parts of x.

Both results carry the sign of x and are floats.

pow(x, y, /)

Return  $x^y$  ( $x$  to the power of  $y$ ).

`radians(x, /)`

Convert angle  $x$  from degrees to radians.

`remainder(x, y, /)`

Difference between  $x$  and the closest integer multiple of  $y$ .

Return  $x - n*y$  where  $n*y$  is the closest integer multiple of  $y$ .

In the case where  $x$  is exactly halfway between two multiples of  $y$ , the nearest even value of  $n$  is used. The result is always exact.

`sin(x, /)`

Return the sine of  $x$  (measured in radians).

`sinh(x, /)`

Return the hyperbolic sine of  $x$ .

`sqrt(x, /)`

Return the square root of  $x$ .

`tan(x, /)`

Return the tangent of  $x$  (measured in radians).

`tanh(x, /)`

Return the hyperbolic tangent of  $x$ .

`trunc(x, /)`

Truncates the Real  $x$  to the nearest Integral toward 0.

Uses the `__trunc__` magic method.

DATA

`e = 2.718281828459045`

`inf = inf`

`nan = nan`

`pi = 3.141592653589793`

`tau = 6.283185307179586`

FILE

(built-in)

## Constants

[4]: `math.pi`

[4]: 3.141592653589793

[5]: `math.e`

[5]: 2.718281828459045

[6]: `math.inf`

[6]: `inf`

[7]: `math.nan`

[7]: `nan`

[8]: `math.tau`

[8]: 6.283185307179586

**Functions** `math.ceil`, `math.floor`, `math.trunc` and `int()`

[9]: `math.ceil(9.7), math.ceil(9.5), math.ceil(9.1), math.ceil(9.000000000000000000000001), math.ceil(9)`

[9]: (10, 10, 10, 9, 9)

[10]: `math.floor(9.7), math.floor(9.5), math.floor(9.1), math.floor(9.000000000000000000000001), math.floor(9)`

[10]: (9, 9, 9, 9, 9)

[11]: `math.trunc(9.7), math.trunc(9.5), math.trunc(9.1), math.trunc(9.000000000000000000000001), math.trunc(9)`

[11]: (9, 9, 9, 9, 9)

[12]: `int(9.7), int(9.5), int(9.1), int(9.000000000000000000000001), int(9)`

[12]: (9, 9, 9, 9, 9)

[13]: `round(9.7), round(9.5), round(9.4), round(9.1), round(9.000000000000000000000001)`  
*→ # works in python 3 only*

[13]: (10, 10, 9, 9, 9)

[14]: `for each_num in range(10):  
 print(each_num, '->', round(math.pi, each_num))`

```
0 -> 3.0
1 -> 3.1
2 -> 3.14
3 -> 3.142
4 -> 3.1416
5 -> 3.14159
6 -> 3.141593
7 -> 3.1415927
8 -> 3.14159265
9 -> 3.141592654
```

math.pow

```
[15]: math.pow(2, 4), pow(2, 4)
```

[15]: (16.0, 16)

```
[16]: math.pow(2.0, 4), pow(2.0, 4)
```

[16]: (16.0, 16.0)

```
[17]: pow(2, 4, 8) == (2 ** 4) % 8
```

```
[17]: True
```

```
[18]: pow(2, 4, 8)
```

[18]: 0

```
[19]: math.pow(2, 4, 8)
```

↳ `TypeError` `Traceback (most recent call last)`

```
<ipython-input-19-40227826ccd1> in <module>
----> 1 math.pow(2, 4, 8)
```

```
TypeError: pow() takes exactly 2 arguments (3 given)
```

## math.remainder vs %

```
[20]: math.remainder(10, 2), 10 % 2
```

[20]: (0.0, 0)

```
[21]: math.remainder(10, 3), 10 % 3
```

[21]: (1.0, 1)

## math.fmod vs %

```
[22]: math.fmod(10, 2), 10 % 2
```

[22]: (0.0, 0)

```
[23]: math.fmod(10, 3), 10 % 3
```

[23]: (1.0, 1)

## math.fabs vs abs()

```
[24]: math.fabs(-9), abs(-9)
```

[24]: (9.0, 9)

```
[25]: math.fabs(-9.6), abs(-9)
```

```
[25]: (9.6, 9)
```

math.factorial

```
[26]: math.factorial(5) , 5 * 4 * 3 * 2 * 1
```

```
[26]: (120, 120)
```

math.fsum() vs sum()

```
[27]: math.fsum((1, 2, 3, 5)), sum((1, 2, 3, 5))
```

```
[27]: (11.0, 11)
```

```
[28]: math.fsum((1.2, 2.5, 3.5, 5.5)), sum((1.2, 2.5, 3.5, 5.5))
```

```
[28]: (12.7, 12.7)
```

math.gcd

```
[29]: math.gcd(12, 4) # Takes two numbers and gives GCD
```

```
[29]: 4
```

math.sqrt

```
[30]: math.sqrt(81)
```

```
[30]: 9.0
```

```
[31]: math.sqrt(84)
```

```
[31]: 9.16515138991168
```

math.modf

```
[32]: math.modf(1.5) # returns fractical, integer parts of a number
```

```
[32]: (0.5, 1.0)
```

```
[33]: math.modf(32)
```

```
[33]: (0.0, 32.0)
```

math.exp

```
[34]: math.exp(10), math.e ** 10
```

```
[34]: (22026.465794806718, 22026.465794806703)
```

```
[35]: math.expm1(10), math.e ** 10 - 1 # helps in retaining the precision of digits
```

```
[35]: (22025.465794806718, 22025.465794806703)
```

logarithm

```
[36]: math.log(100)
```

```
[36]: 4.605170185988092
```

```
[37]: math.log10(100)
```

```
[37]: 2.0
```



```
[38]: math.log1p(100)
```

```
[38]: 4.61512051684126
```

```
[39]: math.log2(100)
```

```
[39]: 6.643856189774724
```

```
[40]: degrees = 45  
math.radians(degrees), (degrees/360.0) * 2 * math.pi
```

```
[40]: (0.7853981633974483, 0.7853981633974483)
```

```
[41]: radians = 90  
math.degrees(radians), 180 * radians/math.pi
```

```
[41]: (5156.620156177409, 5156.620156177409)
```

```
[42]: math.sin(90)
```

```
[42]: 0.8939966636005579
```

```
[43]: math.sin(math.radians(90))
```

```
[43]: 1.0
```

```
[44]: math.cos(math.radians(90))
```

```
[44]: 6.123233995736766e-17
```

```
[45]: math.tan(math.radians(90))
```

```
[45]: 1.633123935319537e+16
```

```
[46]: math.asin(1)
```

```
[46]: 1.5707963267948966
```

```
[47]: math.acos(1)
```

```
[47]: 0.0
```

```
[48]: math.atan(1)
```

```
[48]: 0.7853981633974483
```

```
[49]: print(math.sinh(1))  
print(math.cosh(1))  
print(math.tanh(1))
```

```
1.1752011936438014
```

```
1.5430806348152437
```

```
0.7615941559557649
```

```
[50]: print(math.asinh(1))  
print(math.acosh(1))  
print(math.atanh(0))
```

```
0.8813735870195429
0.0
0.0
```

math.hypot - returns Euclidean distance

```
[51]: math.hypot(2, 3), math.sqrt(2 * 2 + 3 * 3)
```

```
[51]: (3.605551275463989, 3.605551275463989)
```

math.copysign(x, y) - return x value, with sign of y

```
[52]: math.copysign(-9, 2)
```

```
[52]: 9.0
```

```
[53]: math.copysign(-9, -2)
```

```
[53]: -9.0
```

```
[54]: math.copysign(9, -2)
```

```
[54]: -9.0
```

```
[55]: math.copysign(9, 2)
```

```
[55]: 9.0
```

isfinite, isinf, isnan

```
[56]: math.isnan(math.nan)
```

```
[56]: True
```

```
[57]: math.isfinite(78)
```

```
[57]: True
```

```
[58]: math.isfinite(math.inf)
```

```
[58]: False
```

```
[59]: math.isinf(math.inf)
```

```
[59]: True
```

math.gamma - returns gamma function of a value

```
[60]: math.gamma(1)
```

```
[60]: 1.0
```

```
[61]: math.gamma(32)
```

```
[61]: 8.222838654177925e+33
```

```
[62]: math.lgamma(32)
```

```
[62]: 78.0922235533153
```

```
[63]: math.lgamma(1)
```

```
[63]: 0.0
```

`'erf', 'erfc', 'isclose', 'ldexp', 'frexp'`