

Presenting

The Rail Guardians

in requirement of the course project for ST699 – Special Topics in Games

Presented By

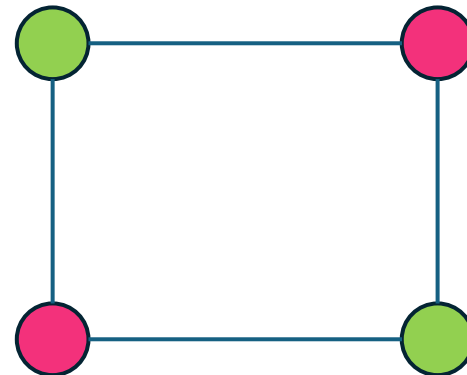
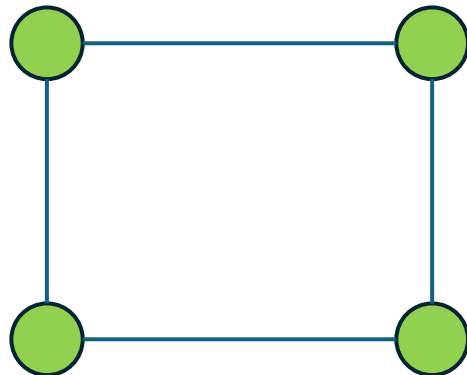
Soumyaratna Debnath, 22270004,
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Inspired from Eternal Vertex Cover problem, *The Rail Guardians* is a two-player game where the players alternate between defending and attacking positions in a dynamic, strategic showdown.

Minimum Vertex Cover

For a graph $G(V, E)$, a set $S \subseteq V(G)$ is said to be a vertex cover of G if for any $(u, v) \in E(G)$ either $u \in S$ or $v \in S$.

The size of the smallest vertex cover of graph G is called the minimum vertex cover of G , denoted by $\text{mvc}(G)$.



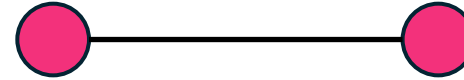
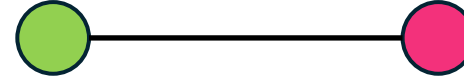
Eternal Vertex Cover

- Dynamic variant of the vertex cover problem.
- Guards are placed on some vertices of a graph.
- In every move, the attacker attacks an edge. In response, the defender moves the guards along the edges in such a manner that at least one guard moves along the attacked edge.
- If such a movement is not possible, **attacker wins**. If the defender can defend an *infinite sequence of attacks*, **defender wins**.
- The minimum number of guards with which defender has a winning strategy is called the Eternal Vertex Cover Number of the Graph G known as $evc(G)$.
- Klostermeyer and Mynhardt showed $mvc(G) \leq evc(G) \leq 2mvc(G)$

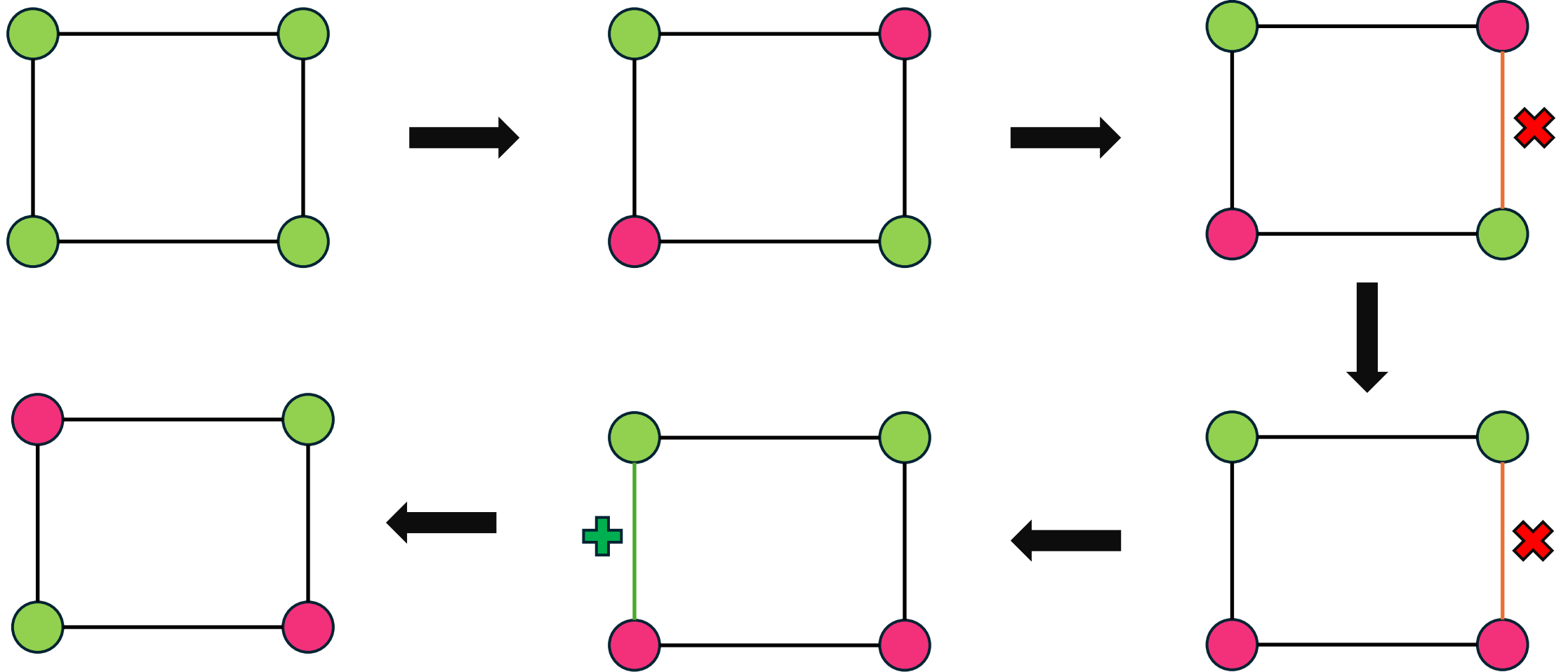
Eternal Vertex Cover – Some intuitions



Attacker Wins



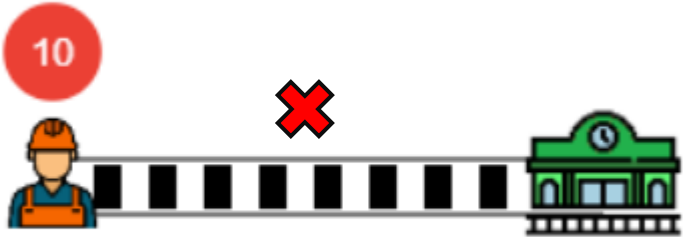
Eternal Vertex Cover – A walkthrough



Let's get to the GAME !

Analysis of Max Score for Energy Aware Eternal Vertex Cover on Linear Graphs

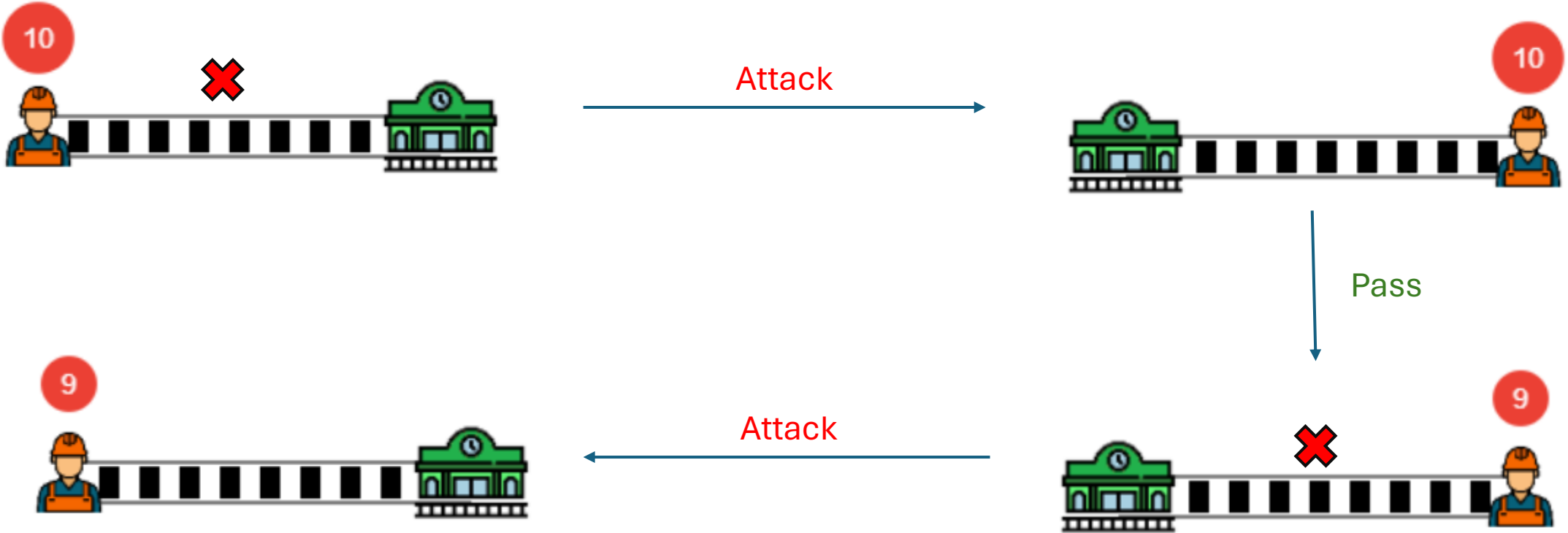
Stations	Builders	Energy	Max Score
2	1	K	?



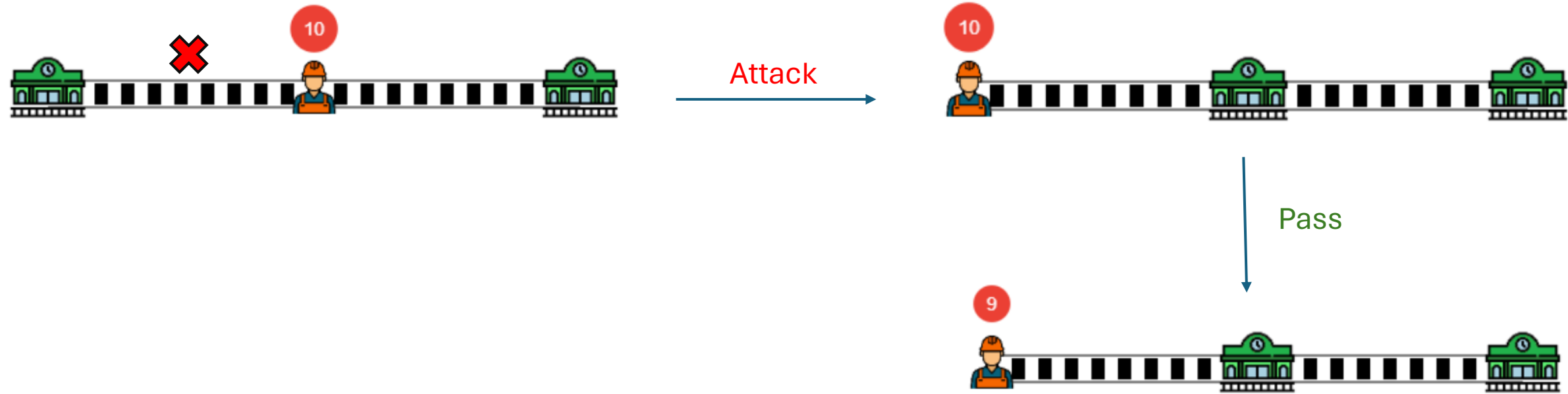
Attack



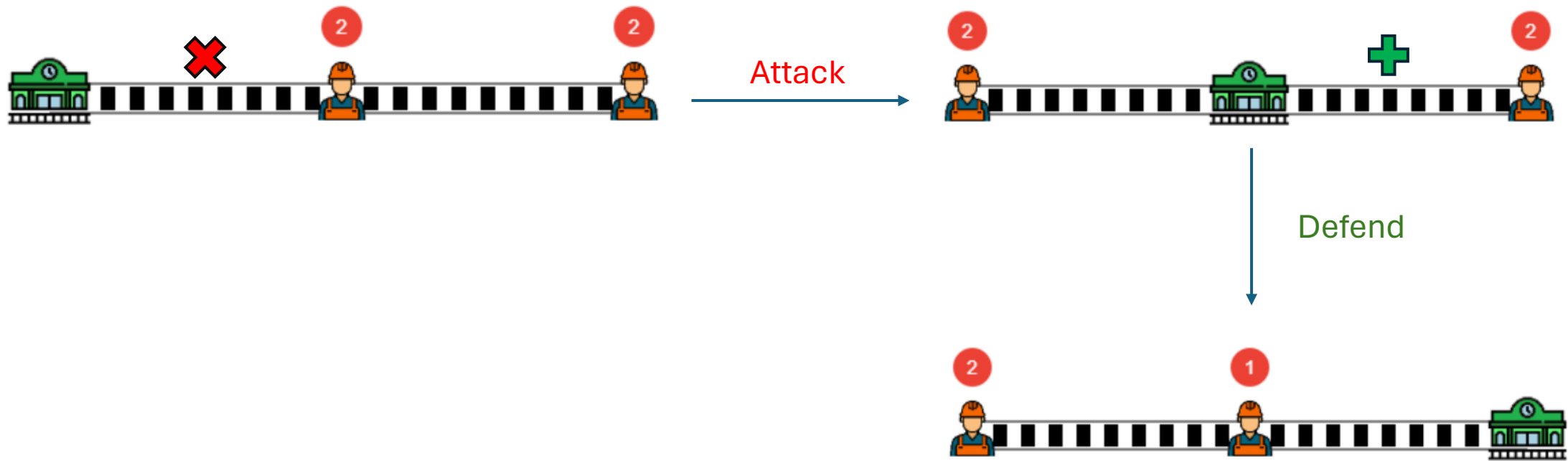
Stations	Builders	Energy	Max Score
2	1	K	K



Stations	Builders	Energy	Max Score
3	1	K	1



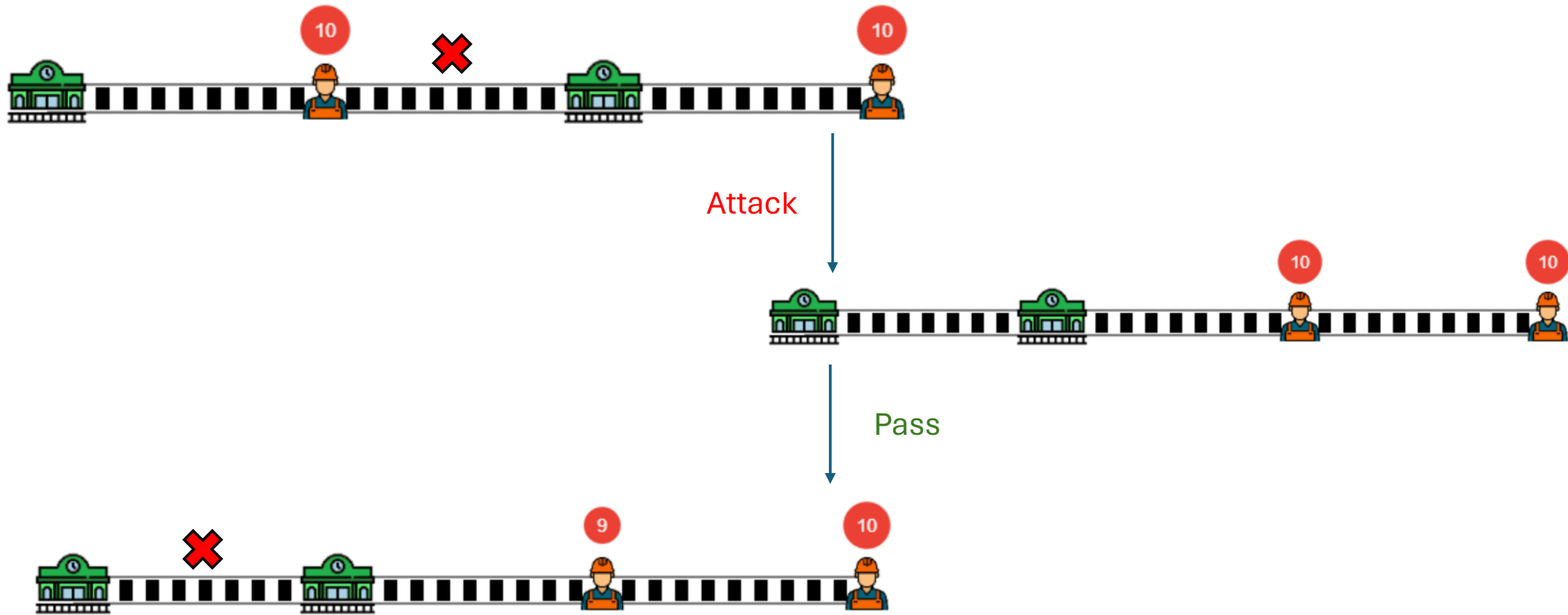
Stations	Builders	Energy	Max Score
3	2	K	2K - 1



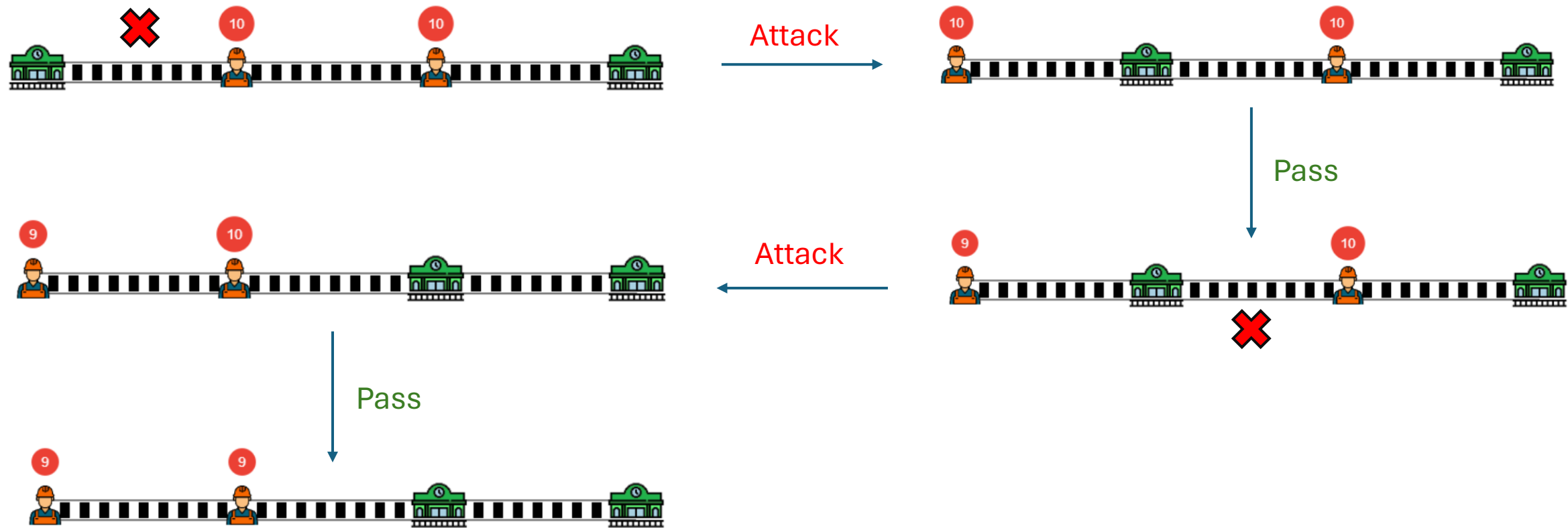
Stations	Builders	Energy	Max Score
4	1	K	0



Stations	Builders	Energy	Max Score
4	2	K	1?



Stations	Builders	Energy	Max Score
4	2	K	2



Stations	Builders	Energy	Max Score
4	3	K	3k - 2



Attack



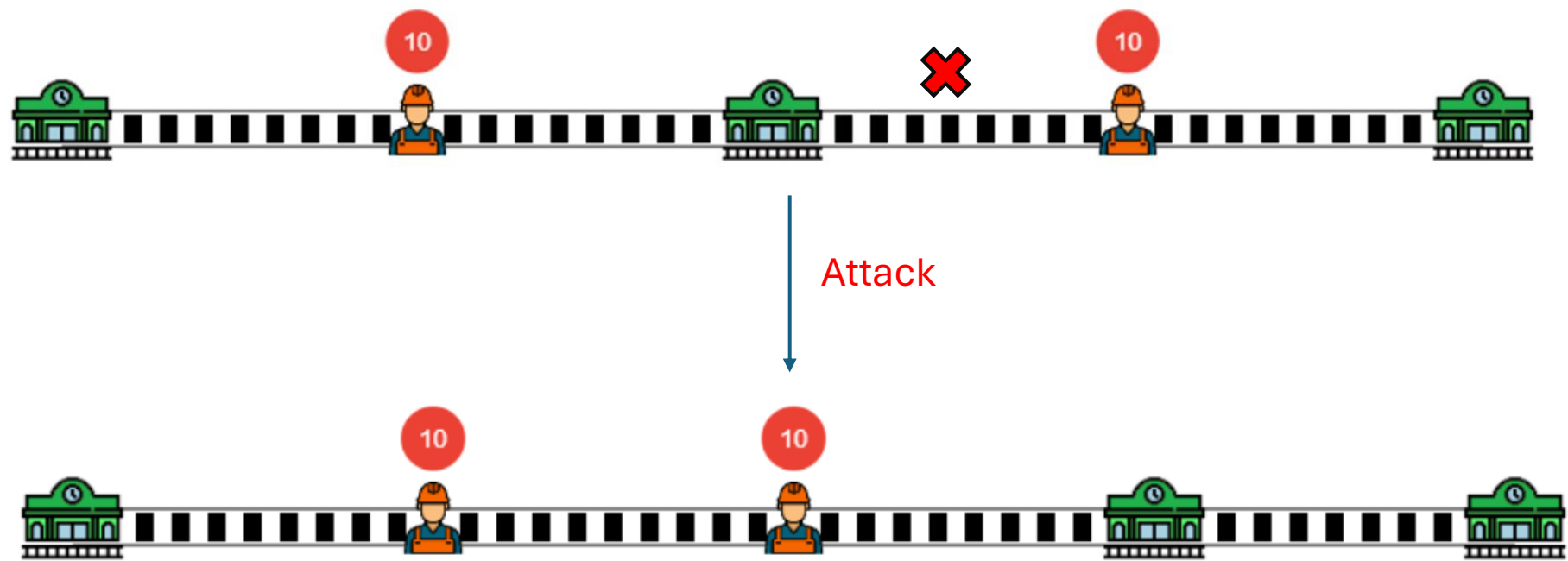
Pass



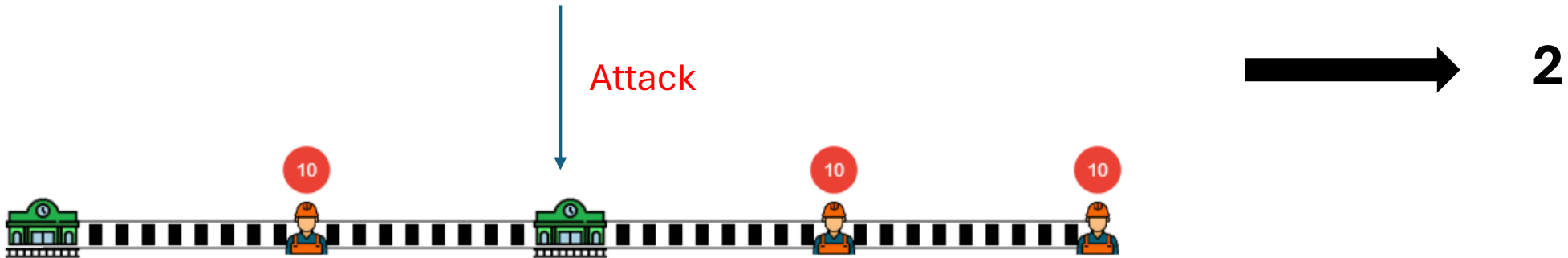
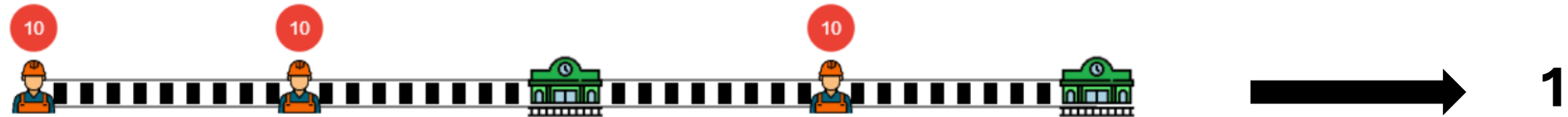
Stations	Builders	Energy	Max Score
5	1	K	0



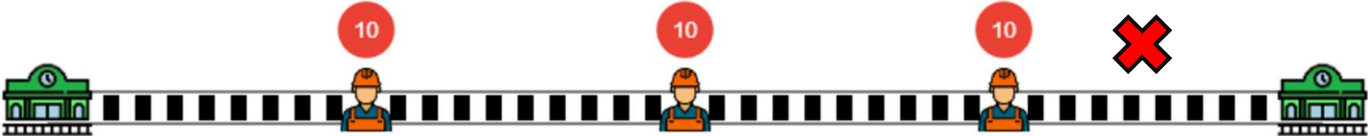
Stations	Builders	Energy	Max Score
5	2	K	1



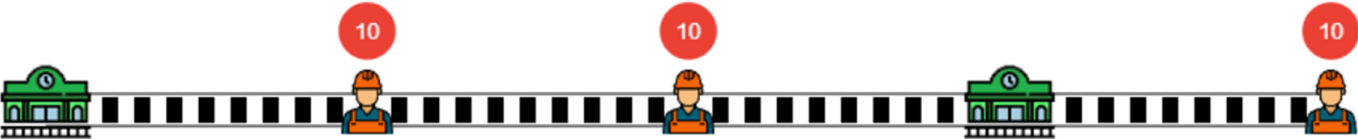
Stations	Builders	Energy	Max Score
5	3	K	?



Stations	Builders	Energy	Max Score
5	3	K	3



Attack



3



2, 3

Stations	Builders	Energy	Max Score
5	4	K	4K - 3



Observation Summary

Stations	Builders	Energy	Max Score
2	1	K	K
3	1	K	1
3	2	K	2K – 1
4	1	K	0
4	2	K	2
4	3	K	3K – 2
5	1	K	0
5	2	K	1
5	3	K	3
5	4	K	4K – 1

Thank You

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