

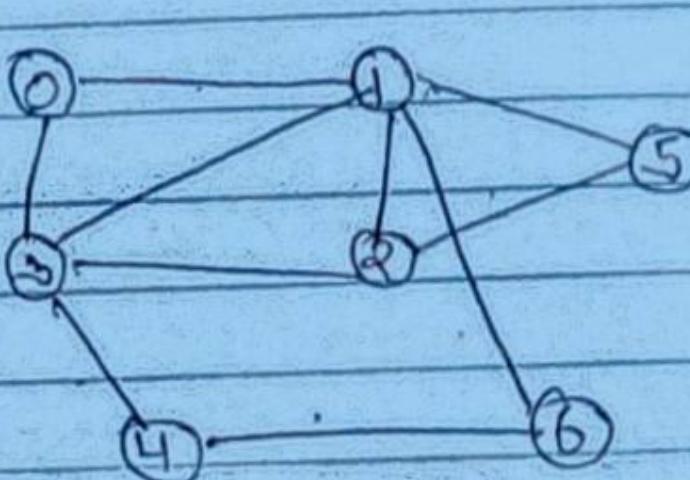
Graph

Date: / / Page no: _____

Representation of Graph

using matrix

0	1	2	3	4	5	6
0	0	1	0	0	0	0
1	0	1	0	1	0	0
2	1	0	1	0	1	0
3	1	1	1	0	1	0
4	0	0	0	1	0	0
5	0	1	1	0	0	0
6	0	1	0	0	1	0

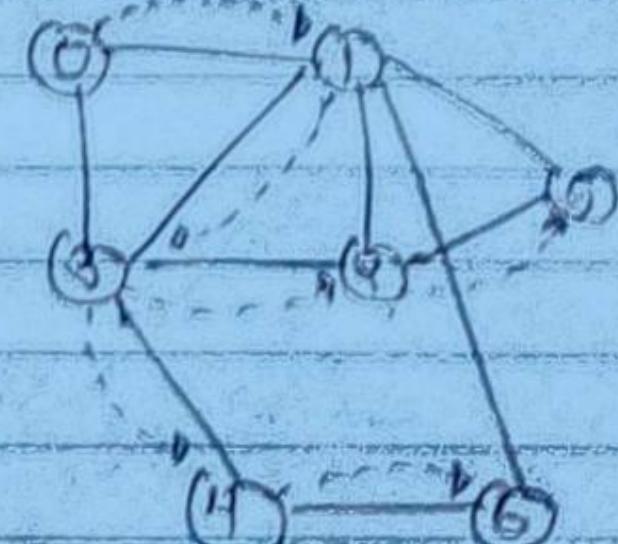


DFS

stack is used

(0)	↓
(5)	↓
(1)	↓
(2)	↓
(3)	↓
(4)	↓
(6)	↓
(7)	↓

DFS → 0 1 3 2 5 4 6



Types of edges in DFS :

- ① tree → members of DFS
- ② forward → $e(x,y)$ where y appears after x and there is a path from x to y
- ③ backward → $e(x,y)$ where y appears before x and there is a path from y to x
- ④ cross → $e(x,y)$ where there is no path from y to x

imp

Graph Traversal

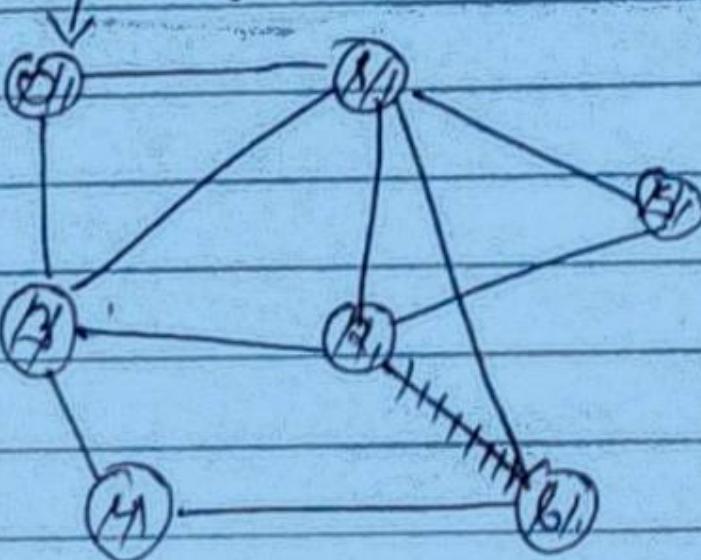
BFS

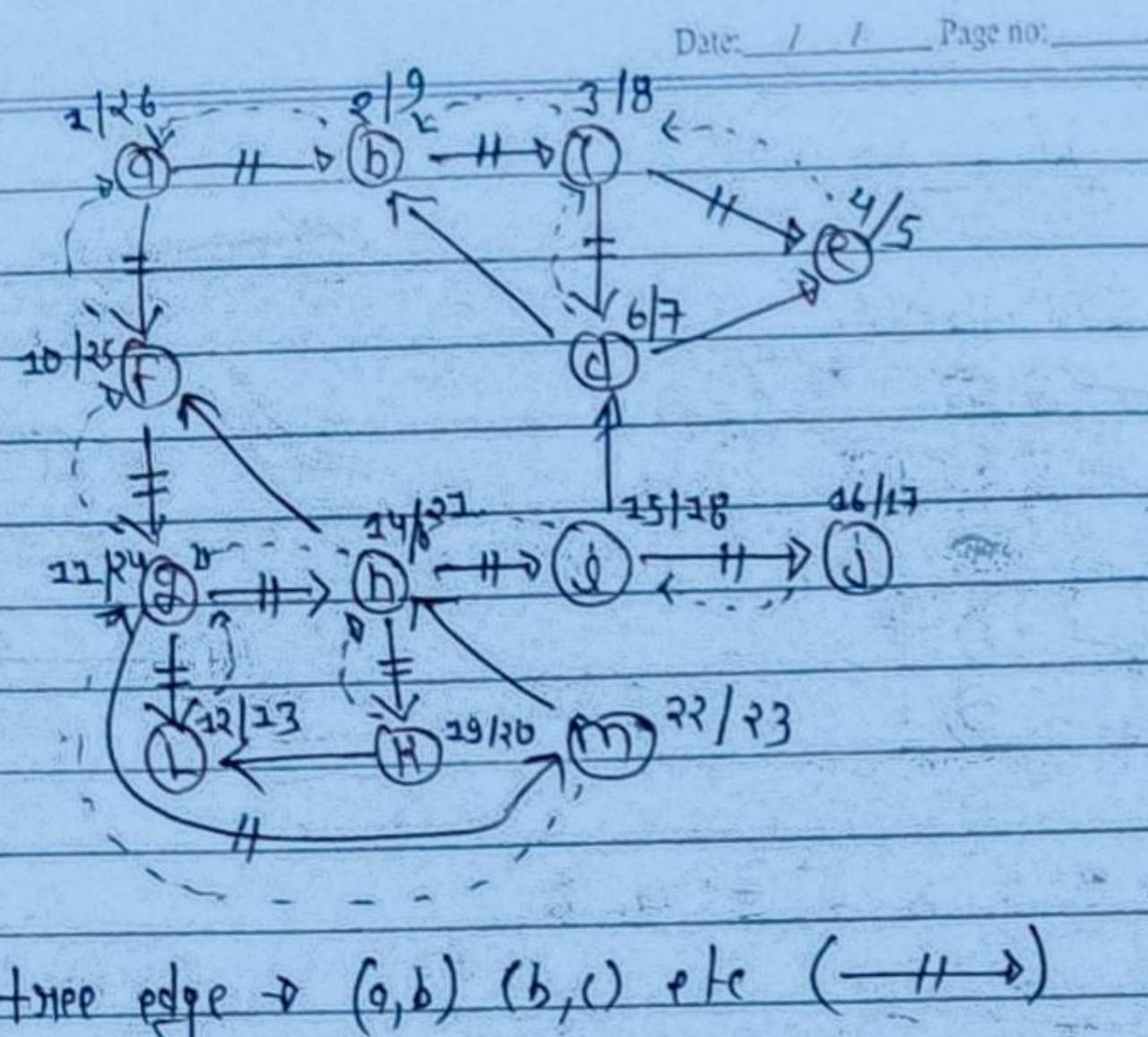
Queue is used

taking 0 as root node

0	1	3	2	6	5	4
0	1	3	2	6	5	4

BFS → 0 1 3 2 6 5 4





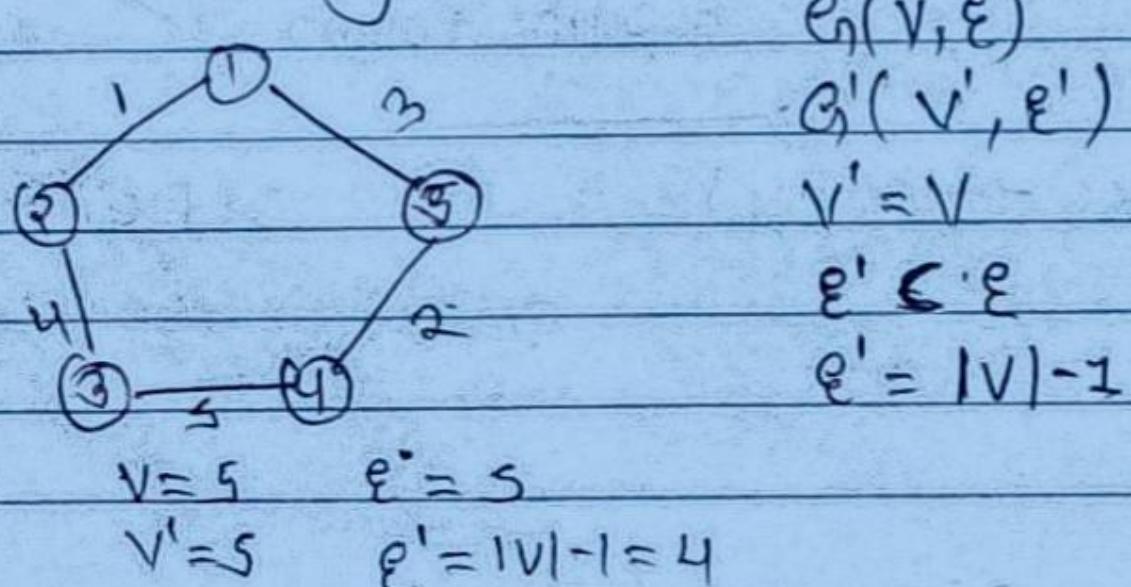
tree edge $\rightarrow (a,b) (b,c) \text{ etc } (- \parallel \rightarrow)$

forward edge $\rightarrow (g,m)$

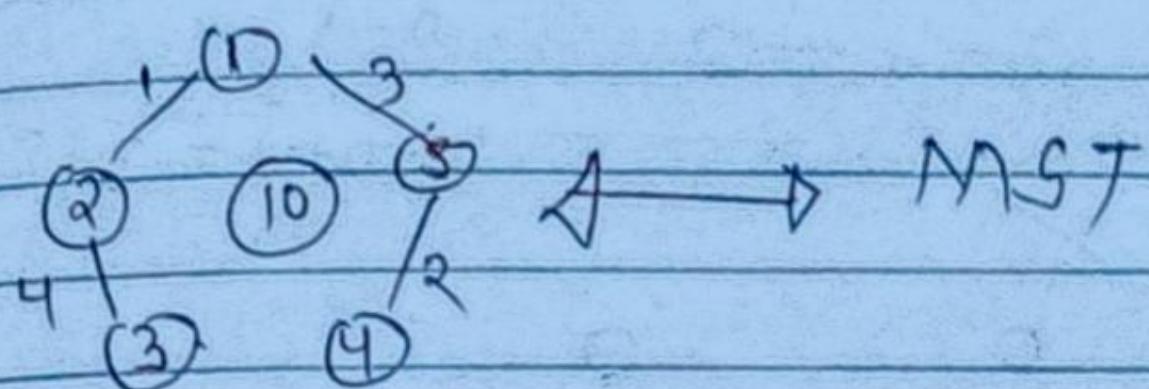
backward $\rightarrow (d,b)$

cross $\rightarrow (d,e)$

Min. spanning tree.



MST has min sum of weight of edges min.



① Removing one edge from the ST will make it disconnected

② Adding one edge to ST will create a loop

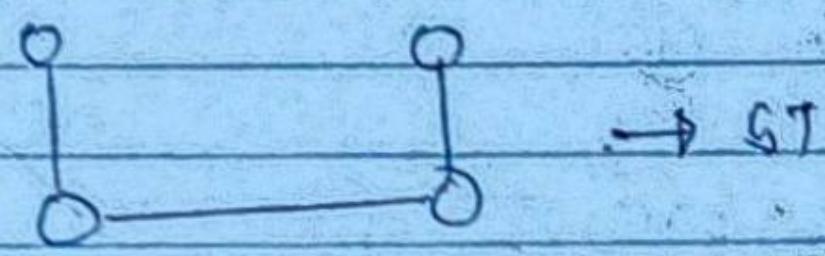
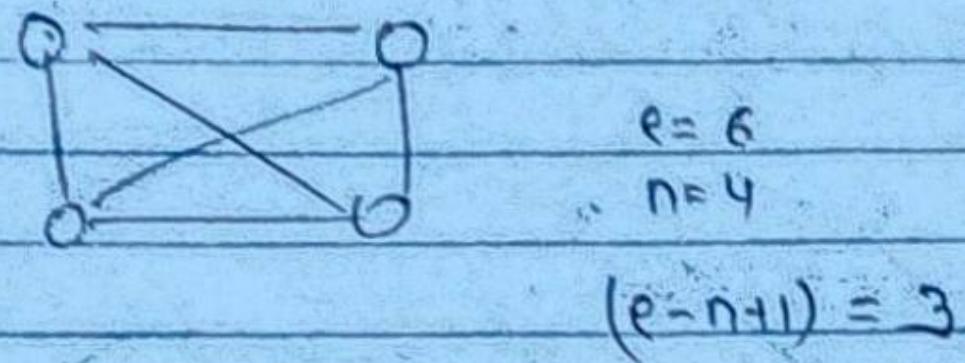
③ if each edge having distinct weight then there will be only one MST

④ complete undirected graph can have $n^{n-2} \cdot ST$
 $n \rightarrow \text{no. of vertices}$

⑤ every connected and undirected graph has at least one ST

⑥ disconnect graph does not have an ST

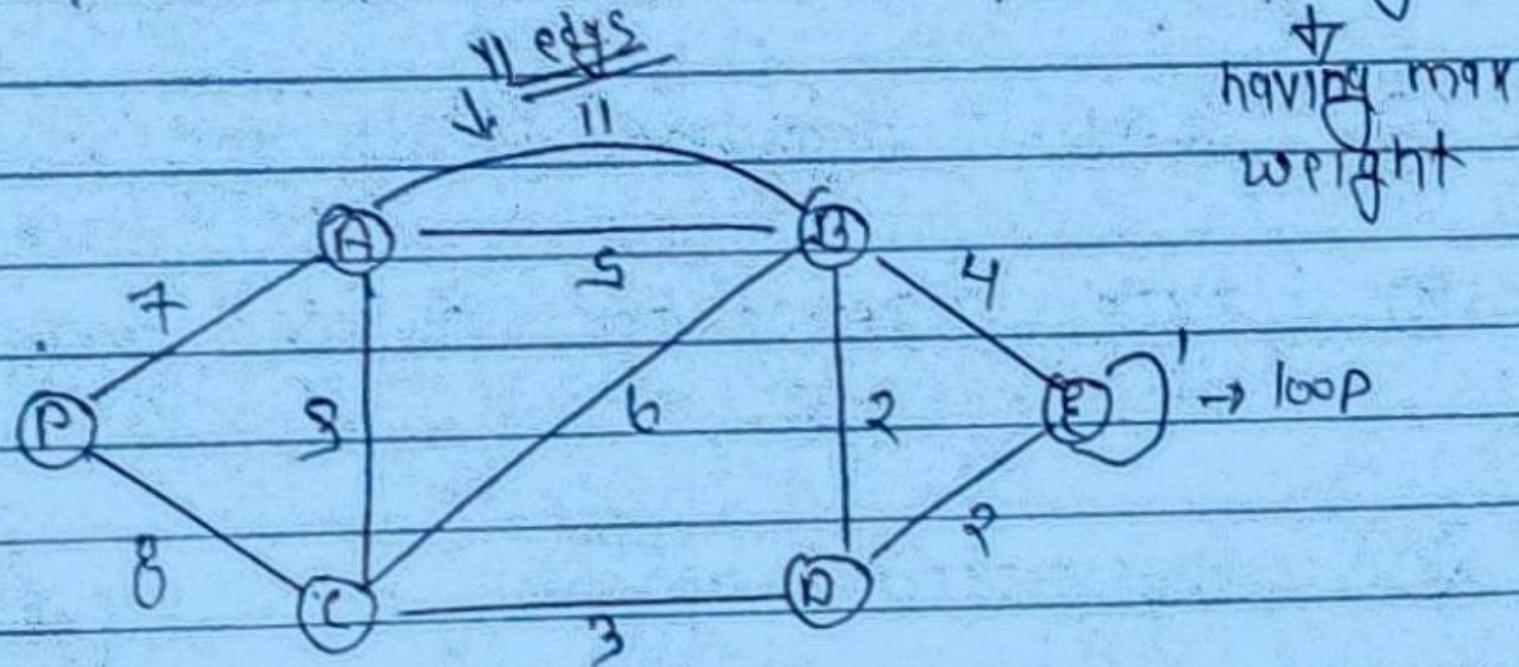
⑦ From complete graph by removing $(e-n+1)$ edges, we can construct 1 ST



$$\text{Total no. of ST} = n^{n-2} = 4^2 = 16$$

Kruskals Algo. of MST

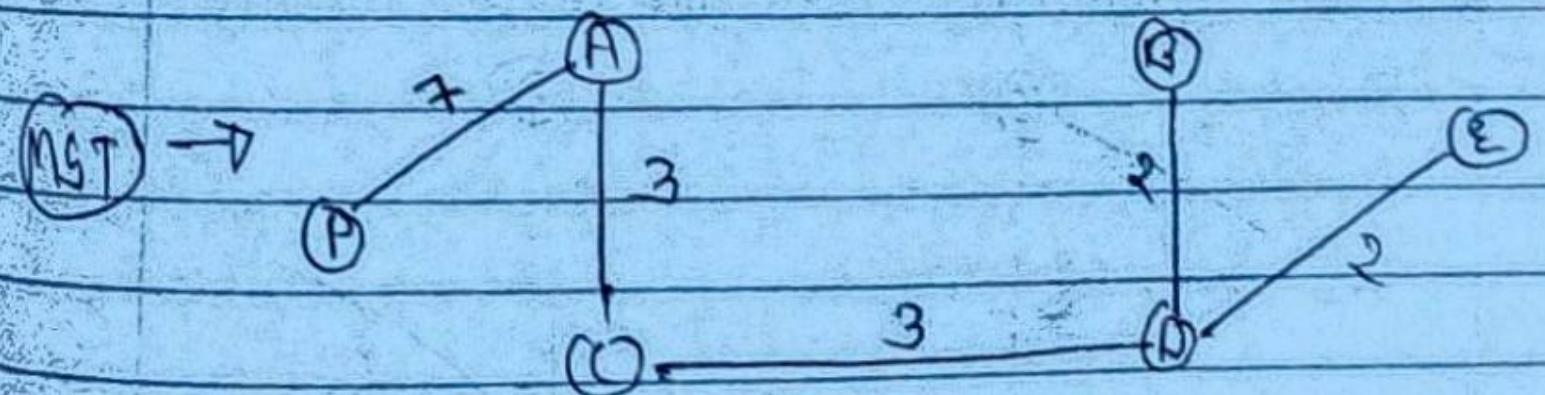
Step 1 → Remove all the loops and || edges



Step 2 → Arranging all the edges in increasing order of edge weight

- 2 → BP, DE
- 3 → CD, AC
- 4 → BE
- 5 → AB
- 6 → BC
- 7 → PA
- 8 → PC

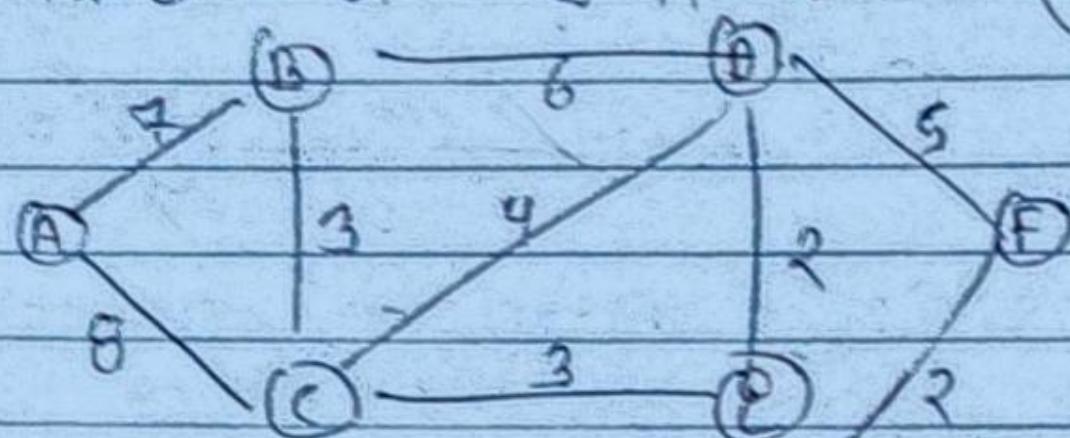
Step 3 → choose edge having min weight



Note ⇒ we can't connect edge which form circle.

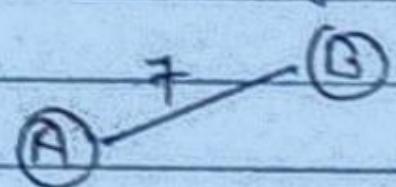
Prim's algo of MST

Step ① → Same as Kruskal's algo

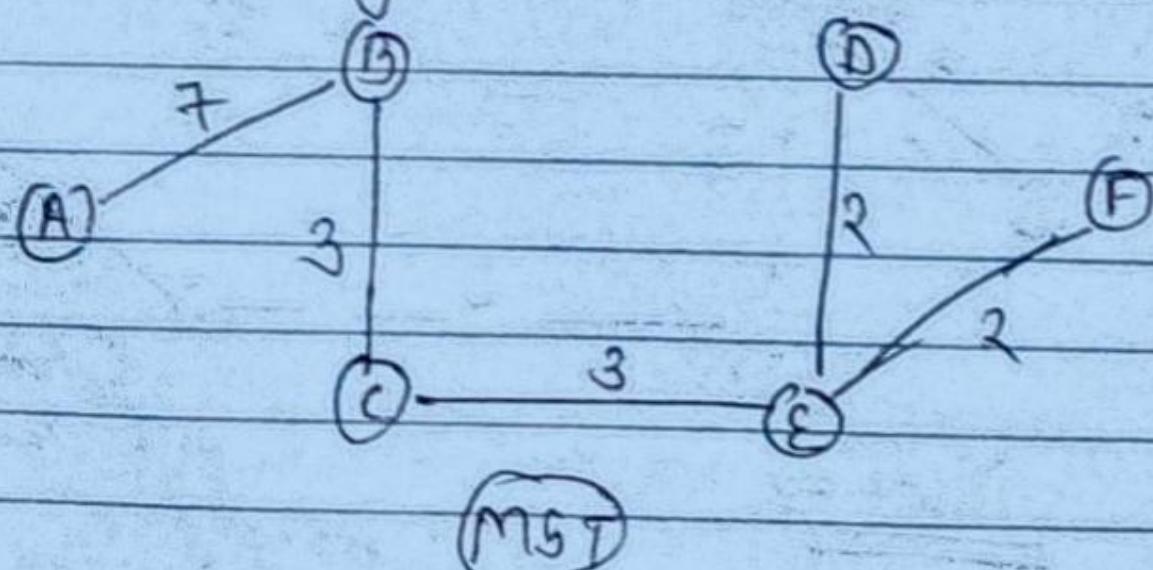


Step ② → choose any start node one as

Step ③ → check all edges connected to start and select which having min. weight



Step ④ → check all edges connected to A and B and select which having min weight and not form circuit

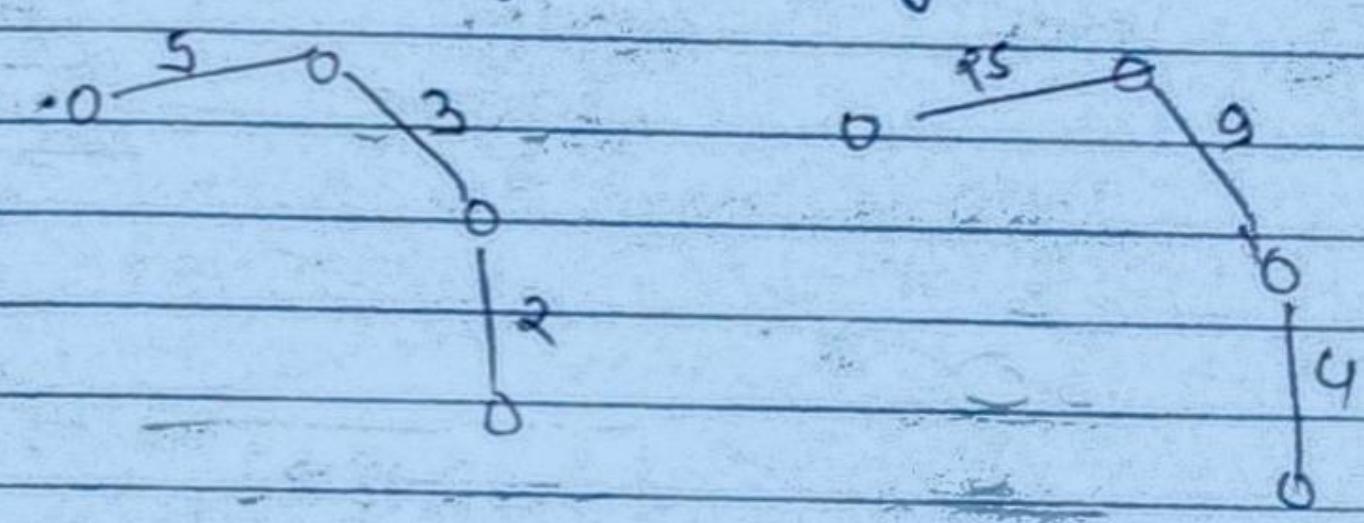


$\Rightarrow x$ is cost of MST $G(V, E)$ & y is cost of MST $G(V, E')$ where E' means \Rightarrow

If $w(u, v) \in E$ then $w^2(u, v) \in E'$

Find relationship b/w $x \& y$ ($w \in R$)

- i) $x > y$
- ii) $x \leq y$
- iii) $x = y$
- iv) None.



$x = 10$

$y = 38$

ii) ✓

$x = 1$

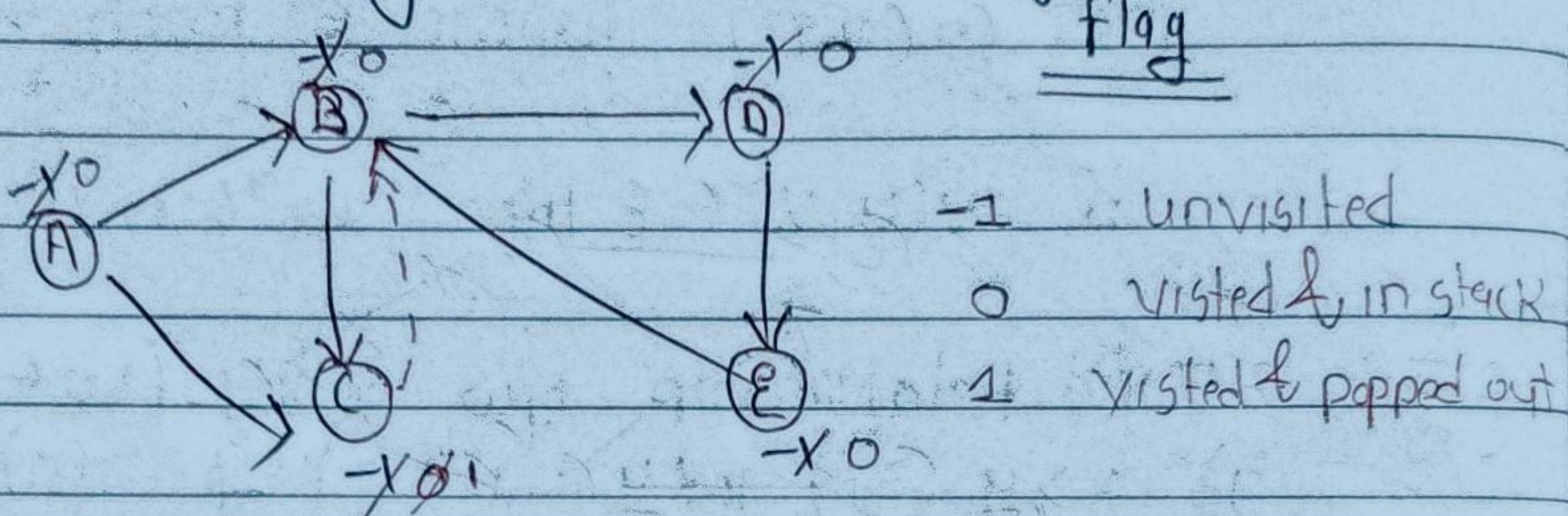
$y = 0.38$

i) ✓

iii) ✓

F all 1, 1, 1

Detect cycle in directed graph.



DFS

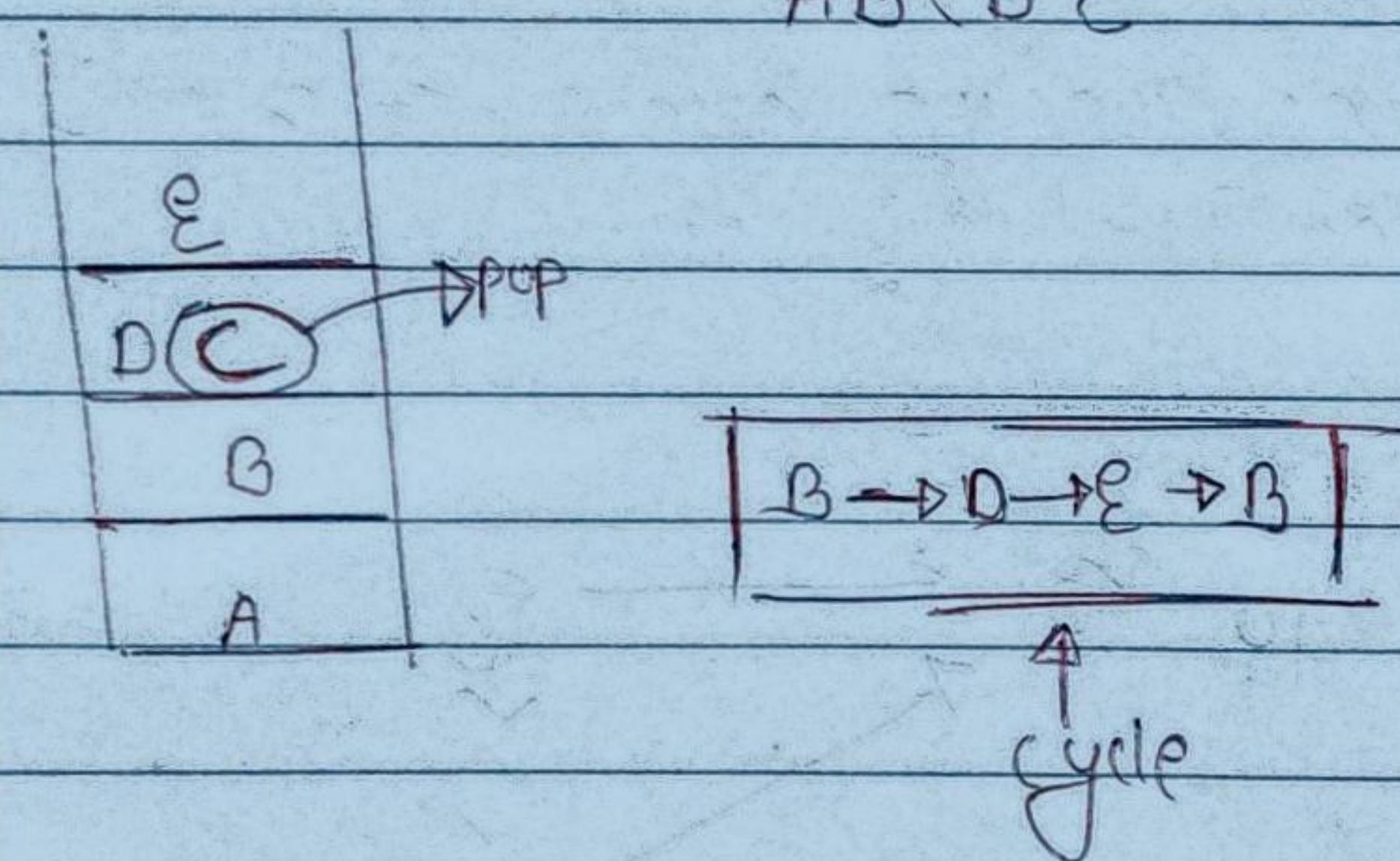
stack

visited set

A B C D E

parent map

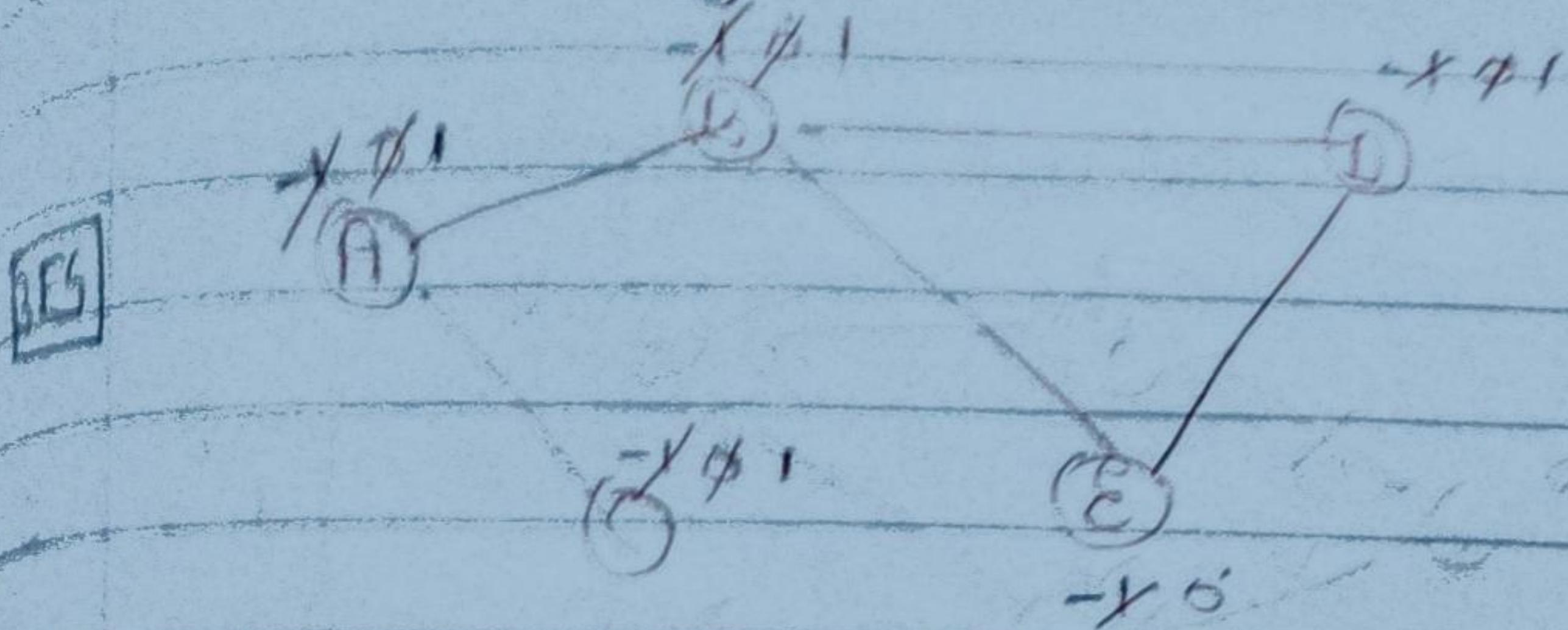
Node	parent
A	-
B	A
C	B
D	B
E	D



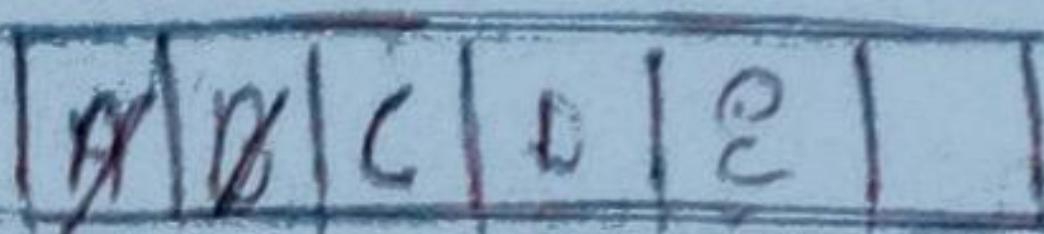
Note → when you get adjacent vertex of current vertex having flag 0 or 1 it means graph contain cycle.
eg → (E to B)

Time complexity $O(V+E)$

Detect cycle in Undirected graph



Queue



visited get

A B C D

IF ($F[V] == 0$)

return 1

IF ($F[V] == -1$)

return 0

insert

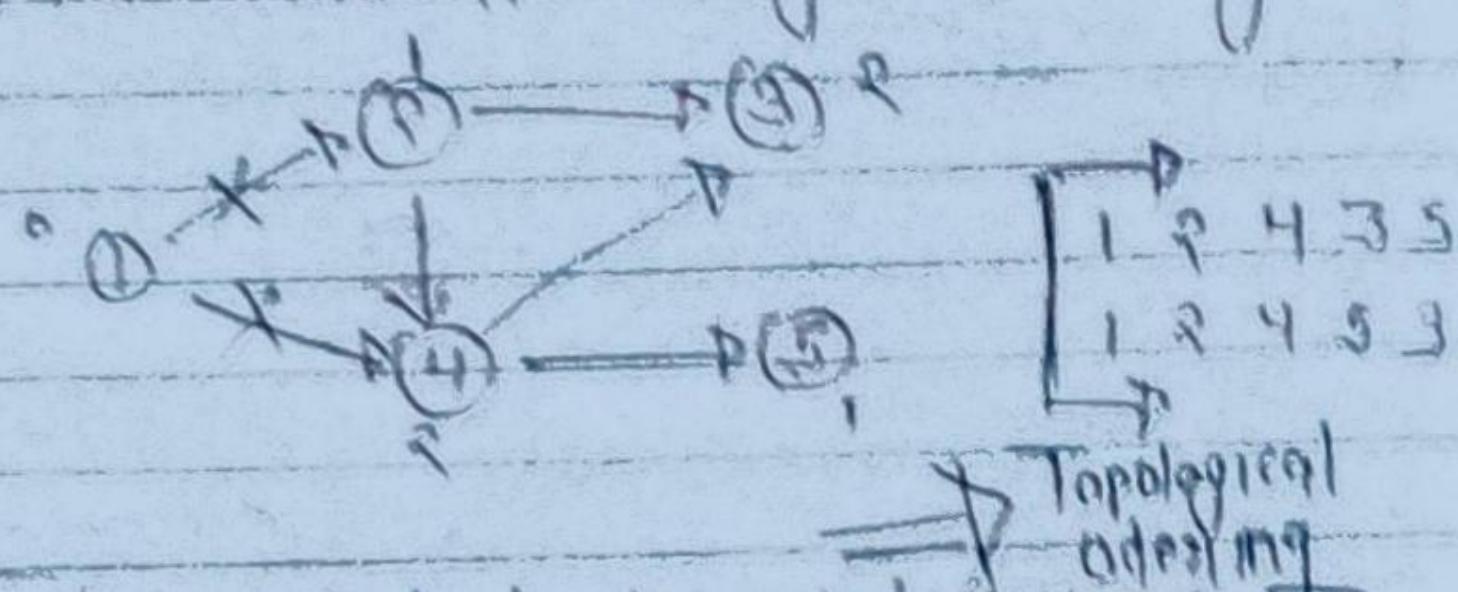
if any vertex find its adjacent vertex
with flag 0, that contain cycle

Topological sort

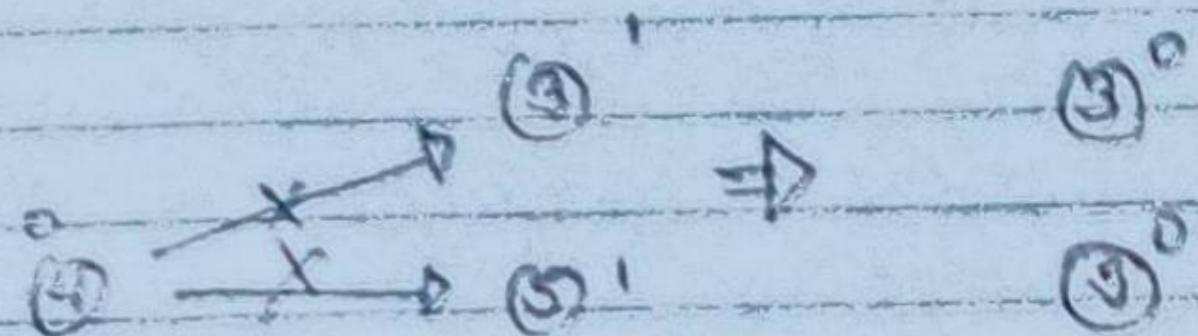
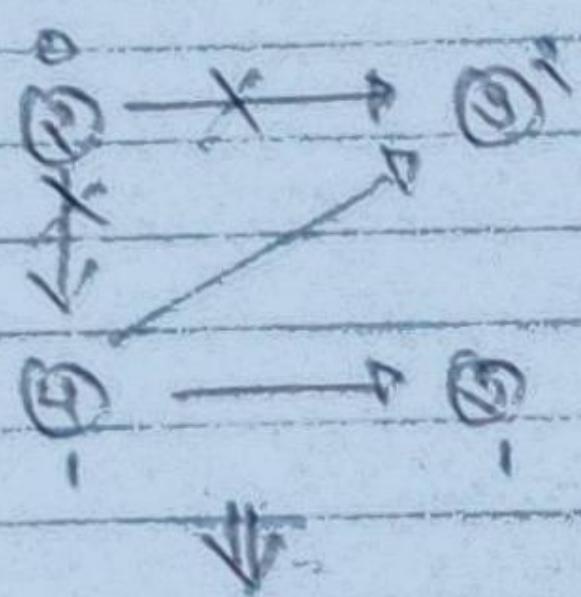
It is linear ordering of its vertices, such that for every directed edge uv for vertices $u \neq v$, u comes before vertex v in the ordering.
graph should be open (directed Acyclic graph).
Every open will have at least one topological ordering.

$u \rightarrow v$

Step 1 → Find out indegree of every vertex

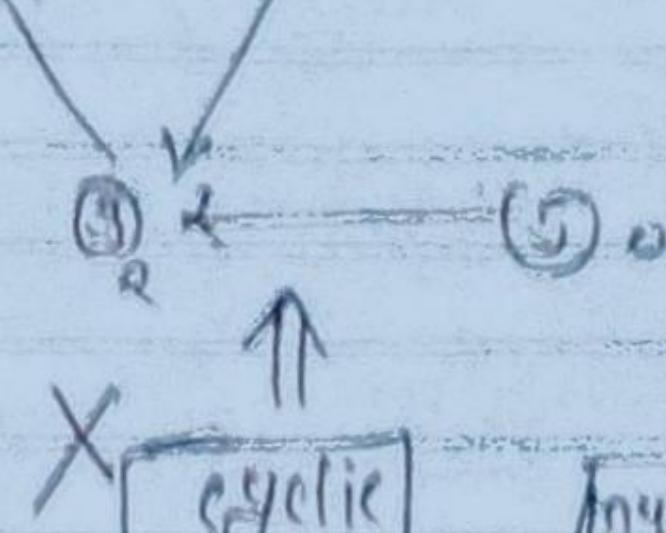


Step 2 → which having indegree = 0 starts from that



g. Find TO

, (1) → (2) < (3) < (4) < (5)

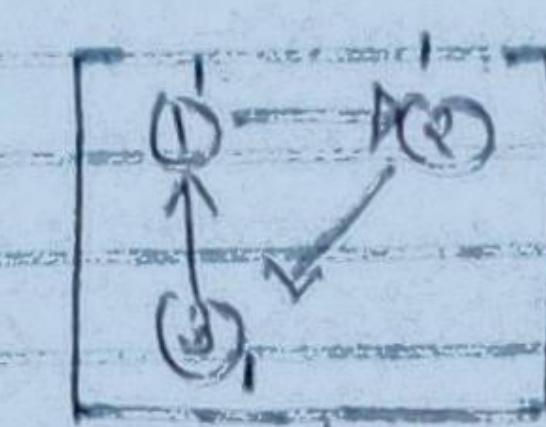
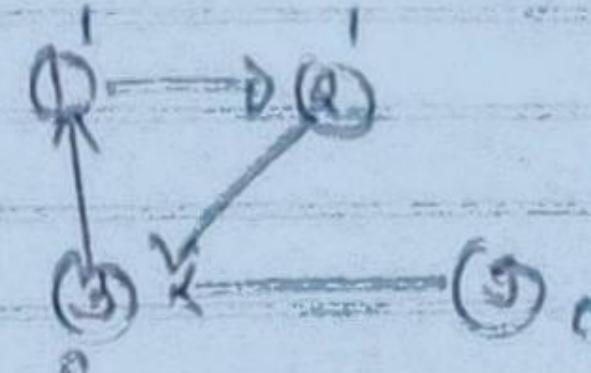


13

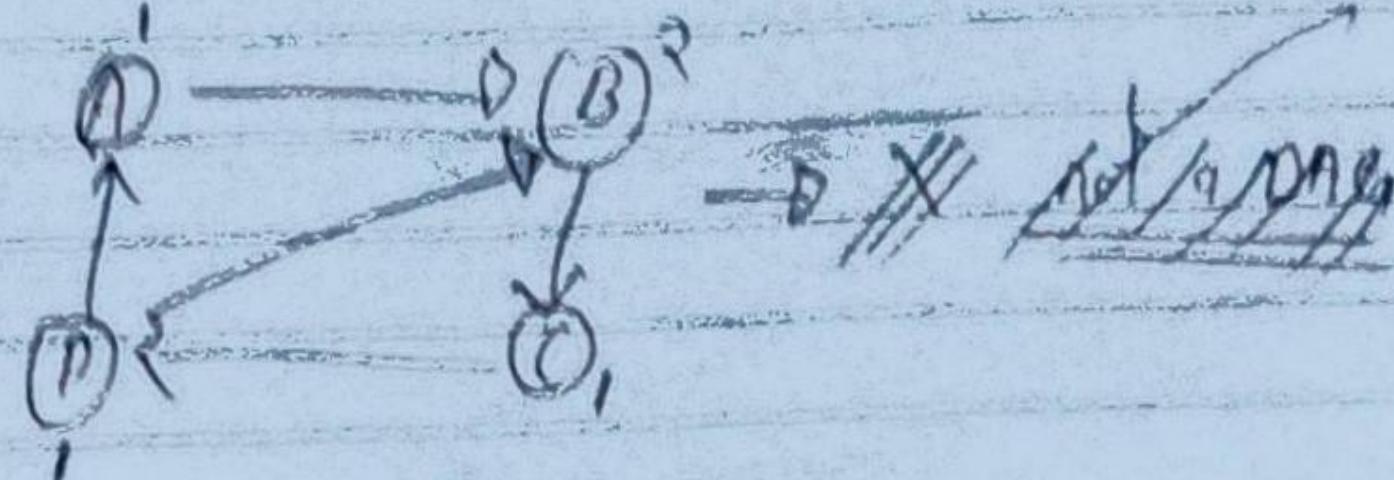
9

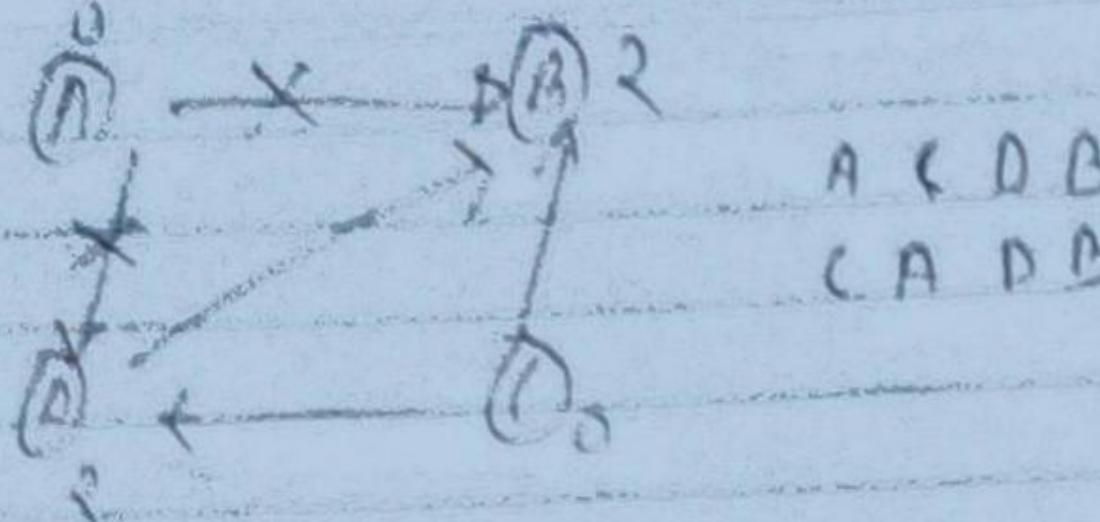
5

.

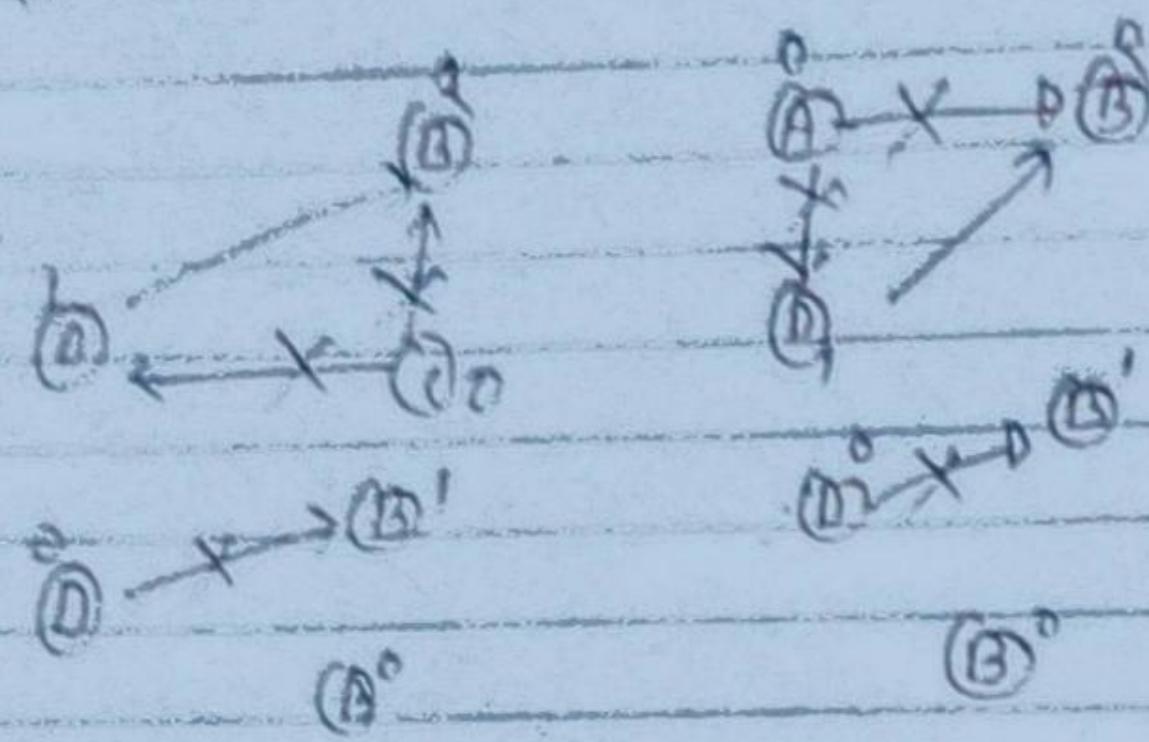


beoz must be DAG



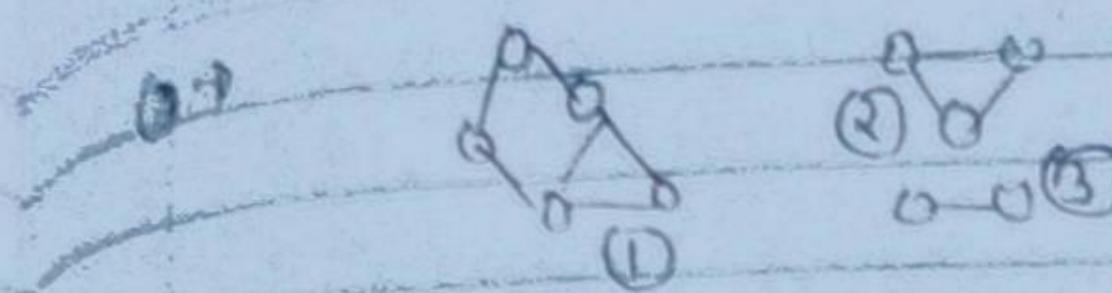
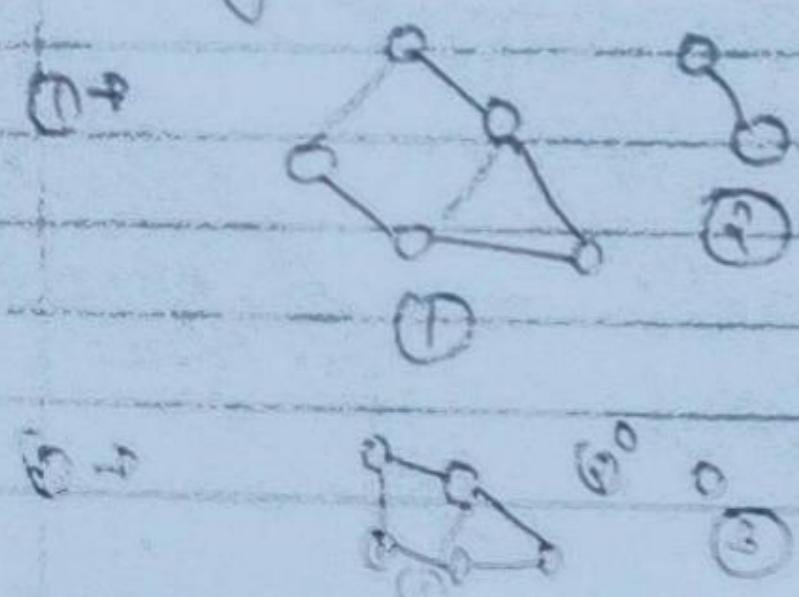


A < DB
CA DB



\Rightarrow Connected Components

* Subgraph in which every two vertices connected by path. And no vertex is connected with any other vertex in superset graph.



Connected components (C_i) {

for each vertex $v \in N$

Flag[v] = -1

count = 0

for (int v=0, v < N, v++)

{

if (Flag[v] == -1)

{

DFS(v, flag)

count++;

cout << count << endl;

}

cout << count << endl;

}

DFS (int v, int flag) { flag[v] = 1, cout < v;

for each adjacent node u of v

if (Flag[u] == -1)

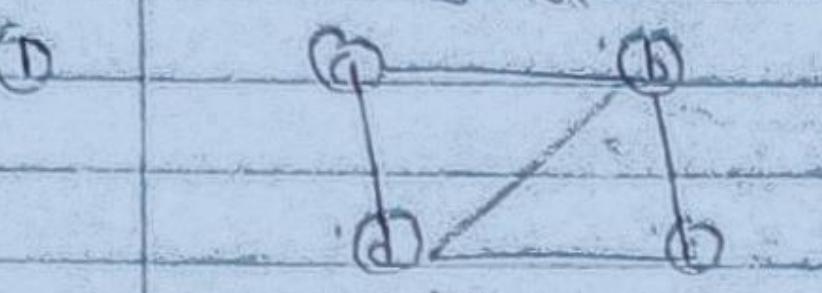
DFS(u, flag)

}

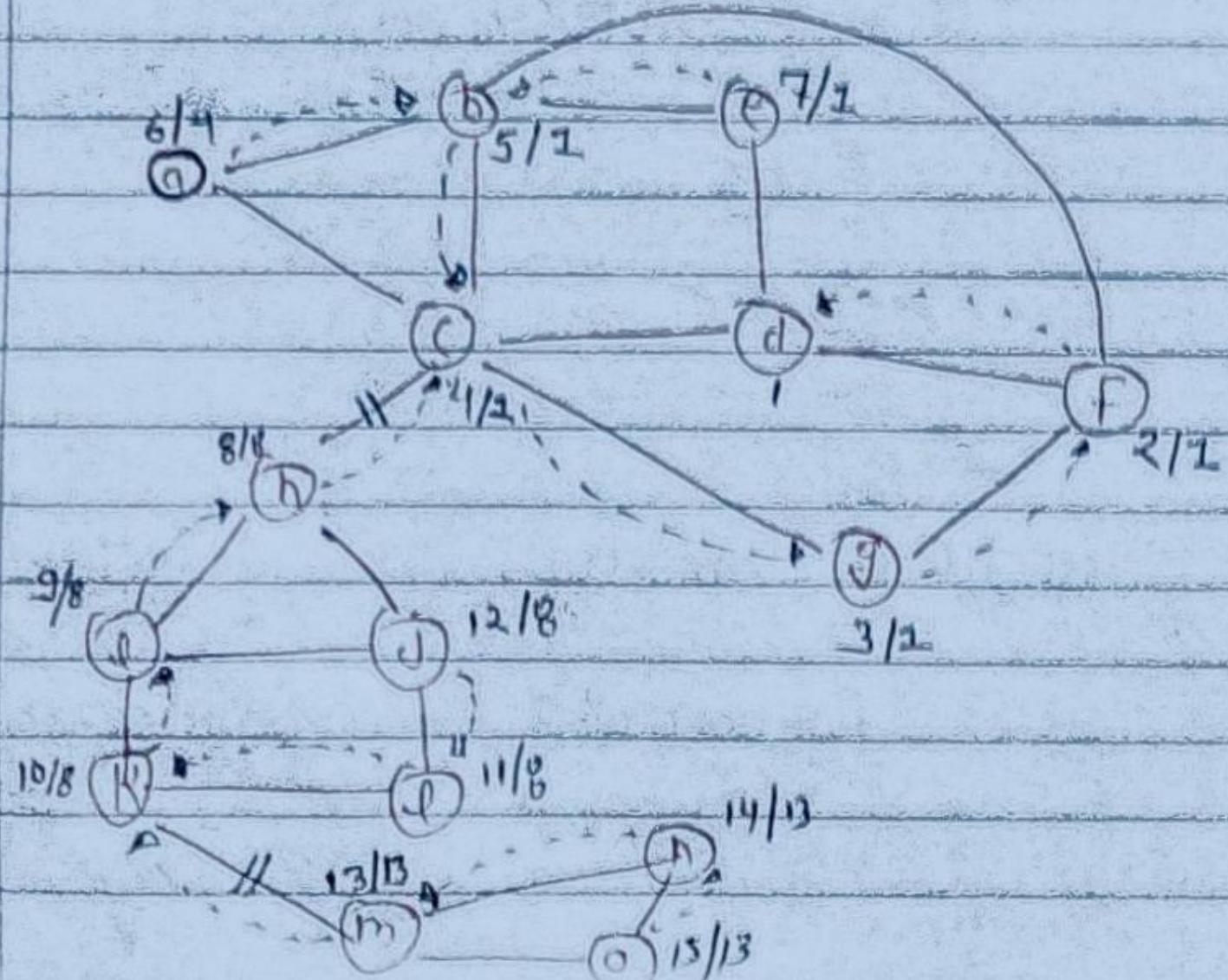
Date: / / Page No.:
Finding all the Bridges of a graph.

It's an edges whose removal res.no. of connected components.

* DFS is use



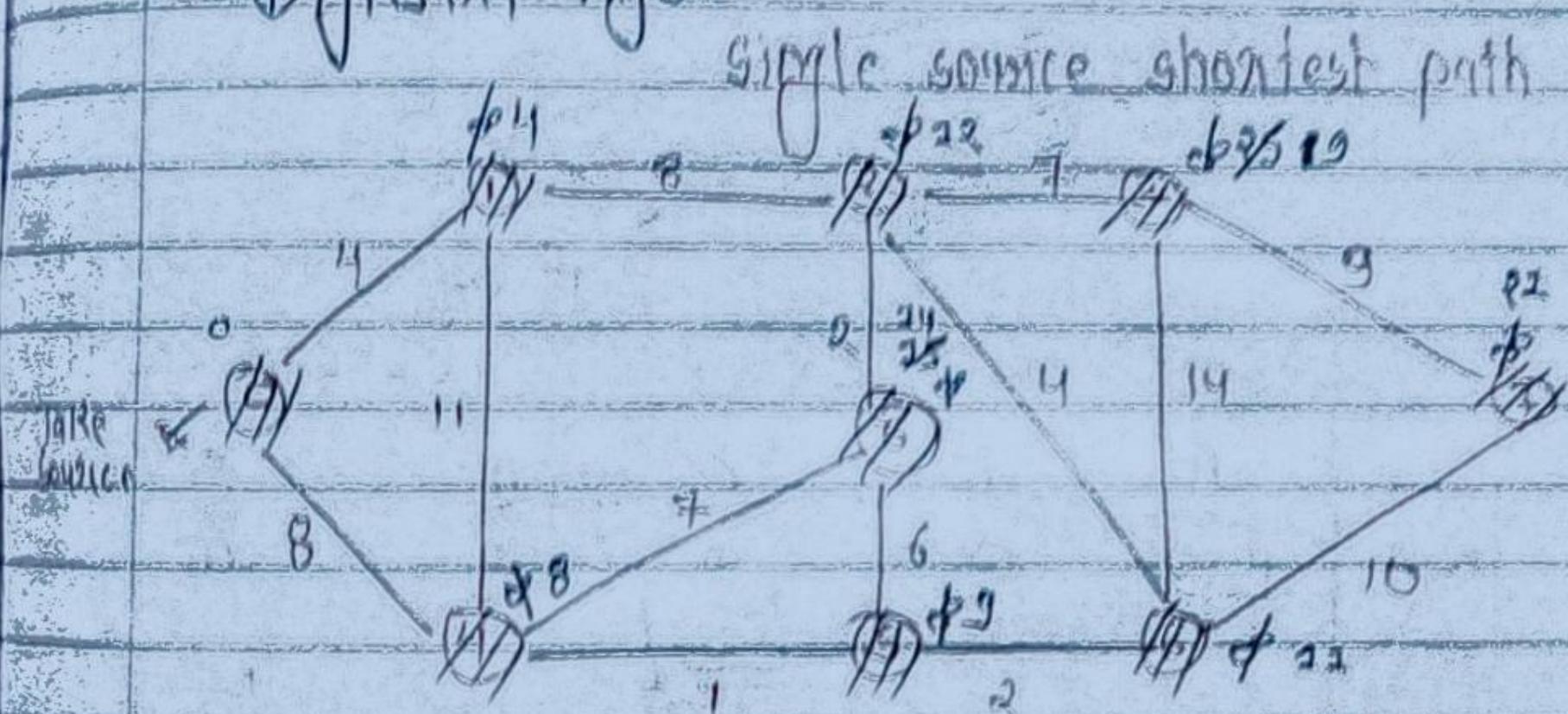
Bridge
Bridge



Time which a particular vertex can take from mid that min of all mid so that we can check if that time is greater than or equal to its parent's start time then bridge is exists.

Time complexity $O(V+E)$

Dijkstra's algo.



Step 1 → calculate distance of all vertex from source vertex that is 0 for source and infinity for all other.

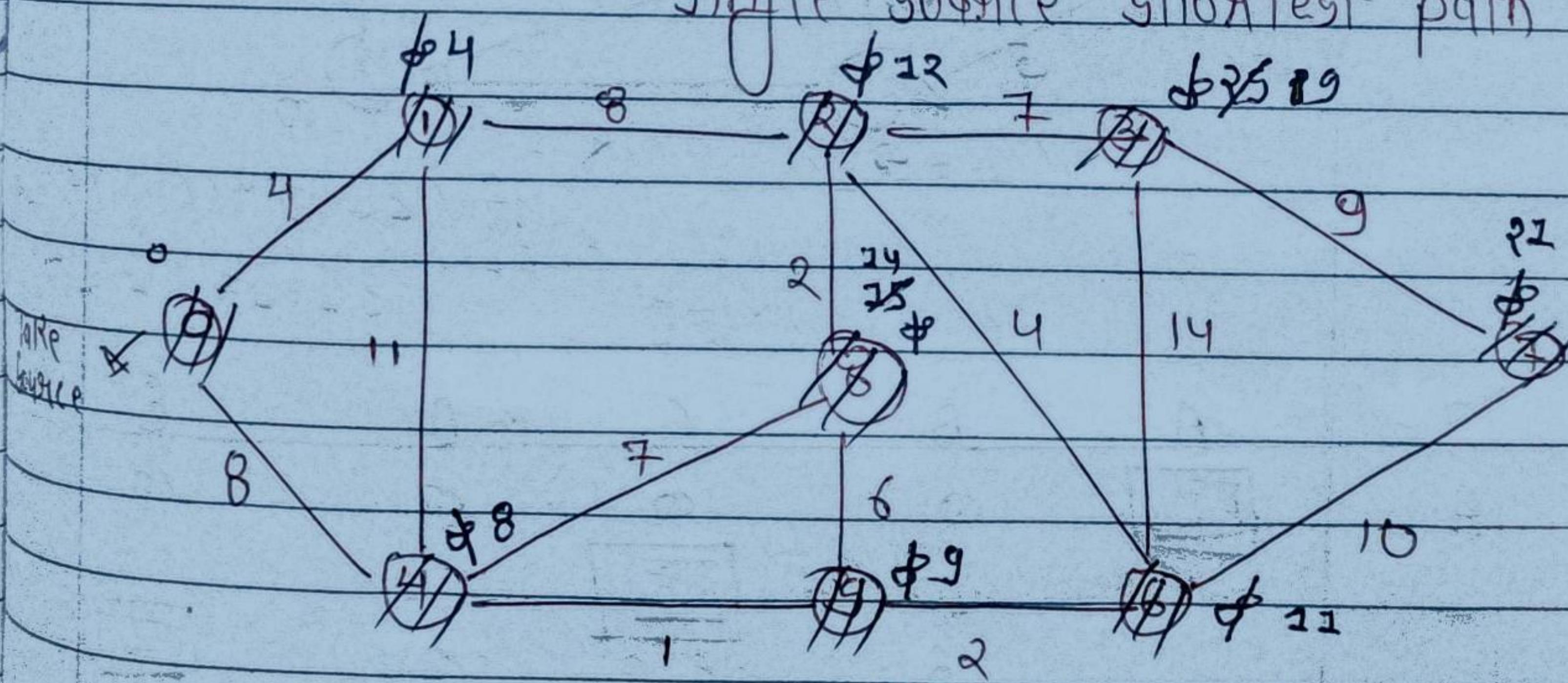
IF $d(u) + c(u,v) < d(v)$
update $d[v] = d(u) + c(u,v)$

⇒ Time which a particular vertex can take
 ↗ from nbd. that min of all nbd. so that
 we can check if that time is greater
 than or equal to its parents start
 time then bridge is exists.

Time complexity $\Theta(v+e)$

Dijkstra Algo.

single source shortest path



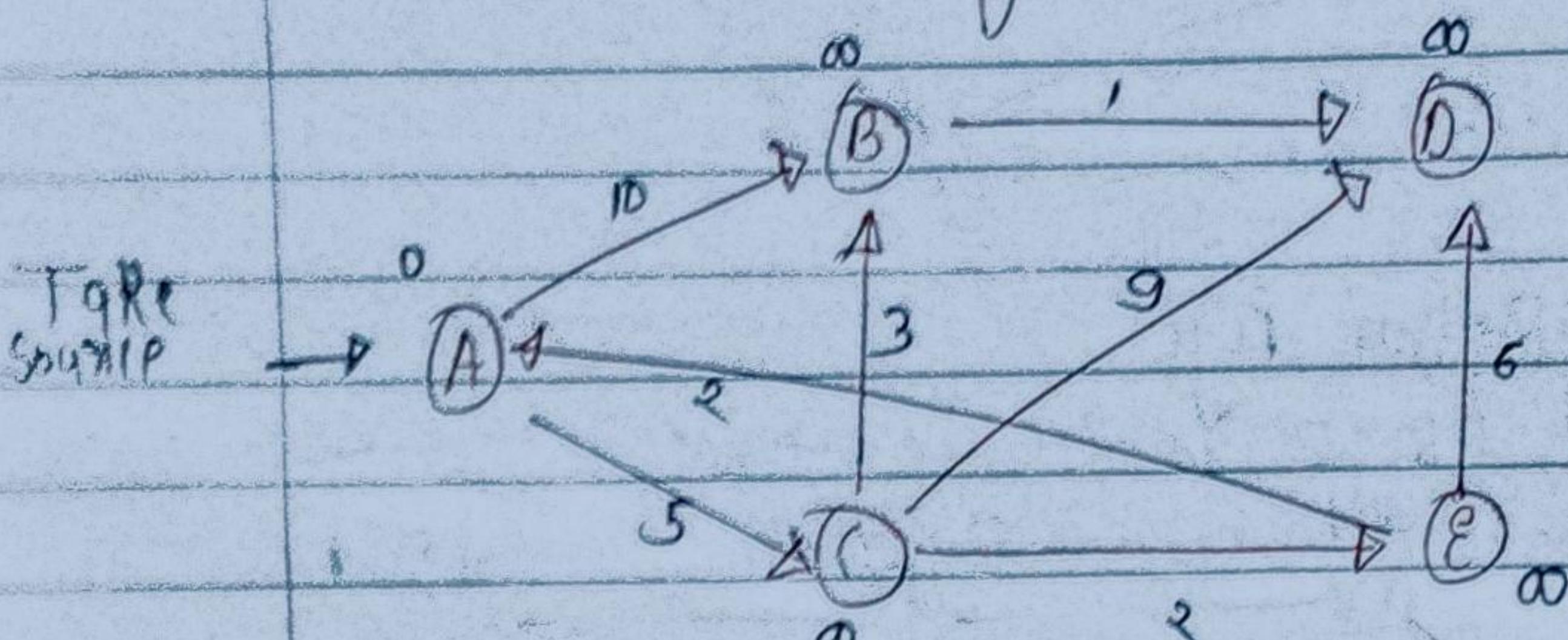
Step 1 → calculate distance of all vertex
 from source vertex that is 0 for
 source and infinity for all other

if $d(u) + c(u, v) < d(v)$

update $d[v] = d(u) + c(u, v)$

Step 2 → Select vertex having min distⁿ

Note → Dijkstra Algo work on both directed and undirected graph.



$$\text{if } d[v] + c(u, v) < d[v]$$

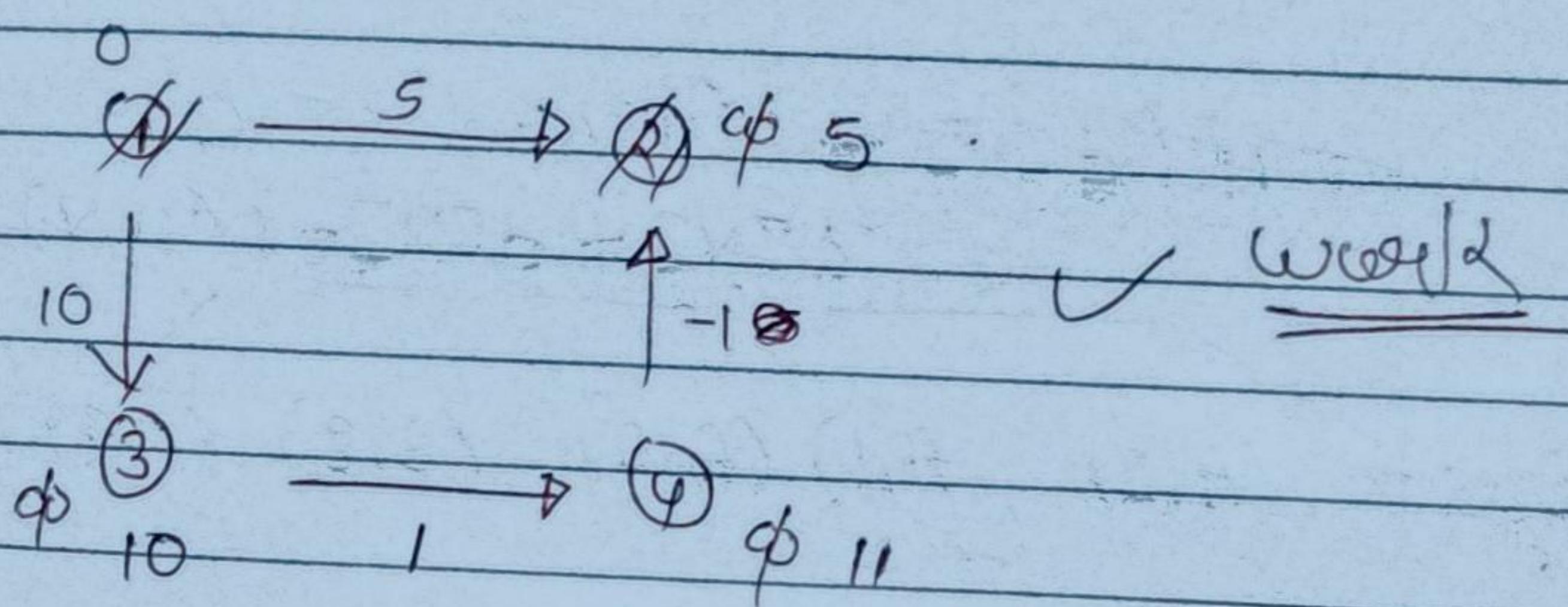
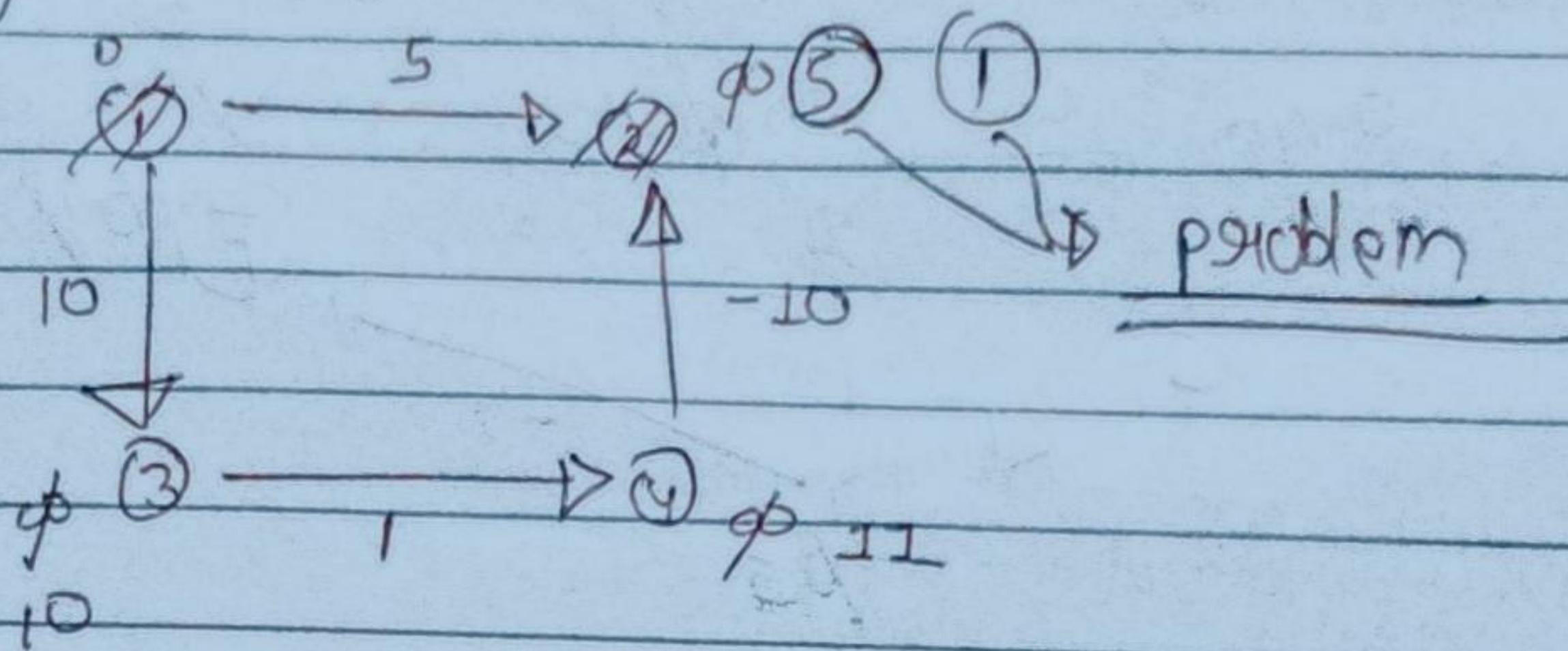
$$d[v] = d[u] + c(u, v)$$

	A	B	C	D	E
A	10	∞	∞	∞	∞
B		10	5	14	7
C			8		13
D				9	
E					

path
 $(A \rightarrow D) \Rightarrow ABCA$

$(A \rightarrow B) \Rightarrow BCA$

Note → Dijkstra's algo may or may not work when edge weight v is $-ve$.

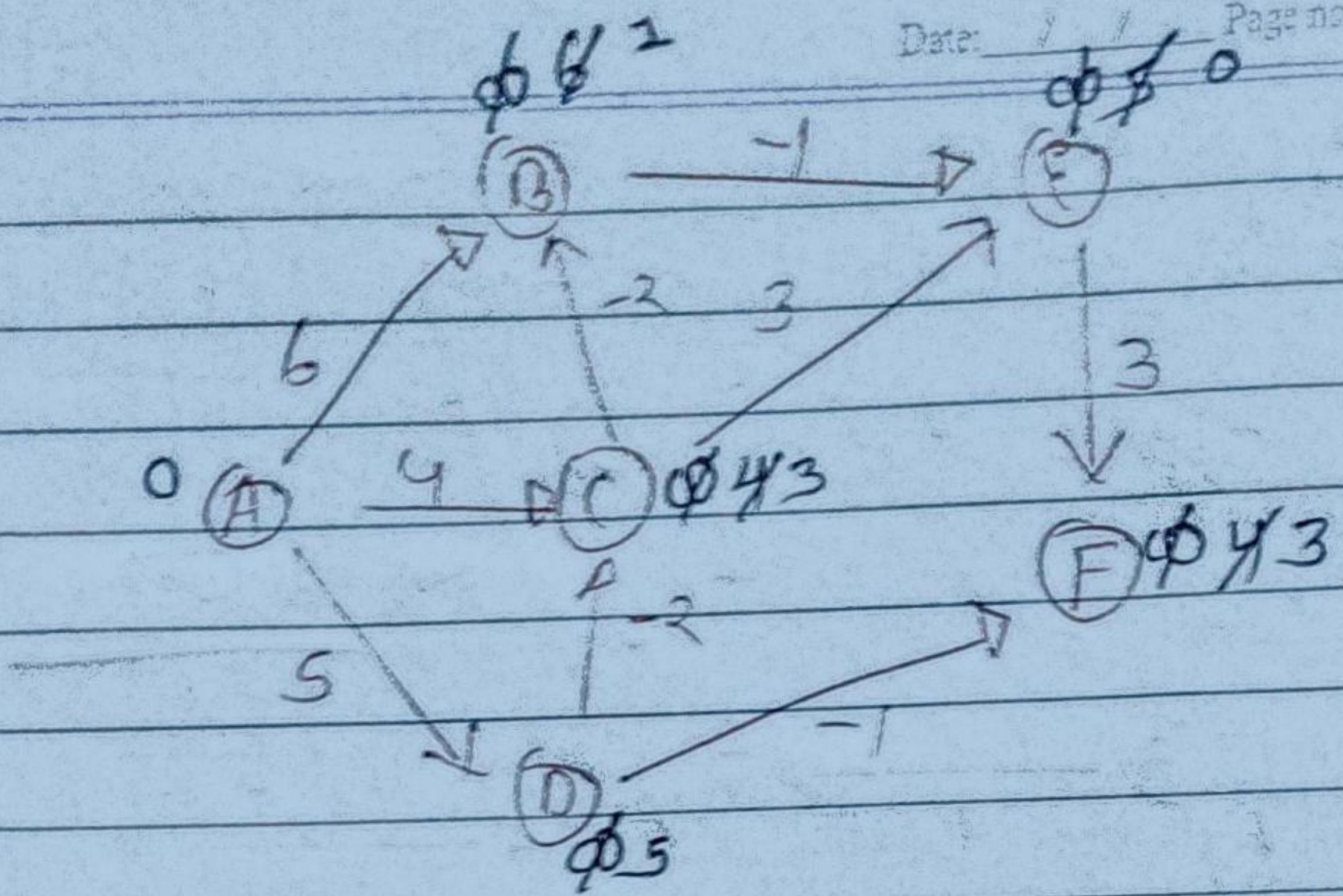


Bellman - Ford Algo.

⇒ here is no problem when edge weight is $-ve$.
It is slower than Dijkstra.

go on relaxing all the edges
($n-1$) times

$n = \text{no. of vertices}$



~~if $d[u] + ((u, v) \in E)$~~
 $d[v] = d[u] + ((u, v))$

edges $\rightarrow (A, B), (A, C), (A, D), (B, C), (B, D), (C, E), (D, E), (D, F), (E, F)$

Ist $\rightarrow \checkmark$

Ind $\rightarrow \checkmark$

IIIrd $\rightarrow \checkmark \rightarrow$ There is no change then over

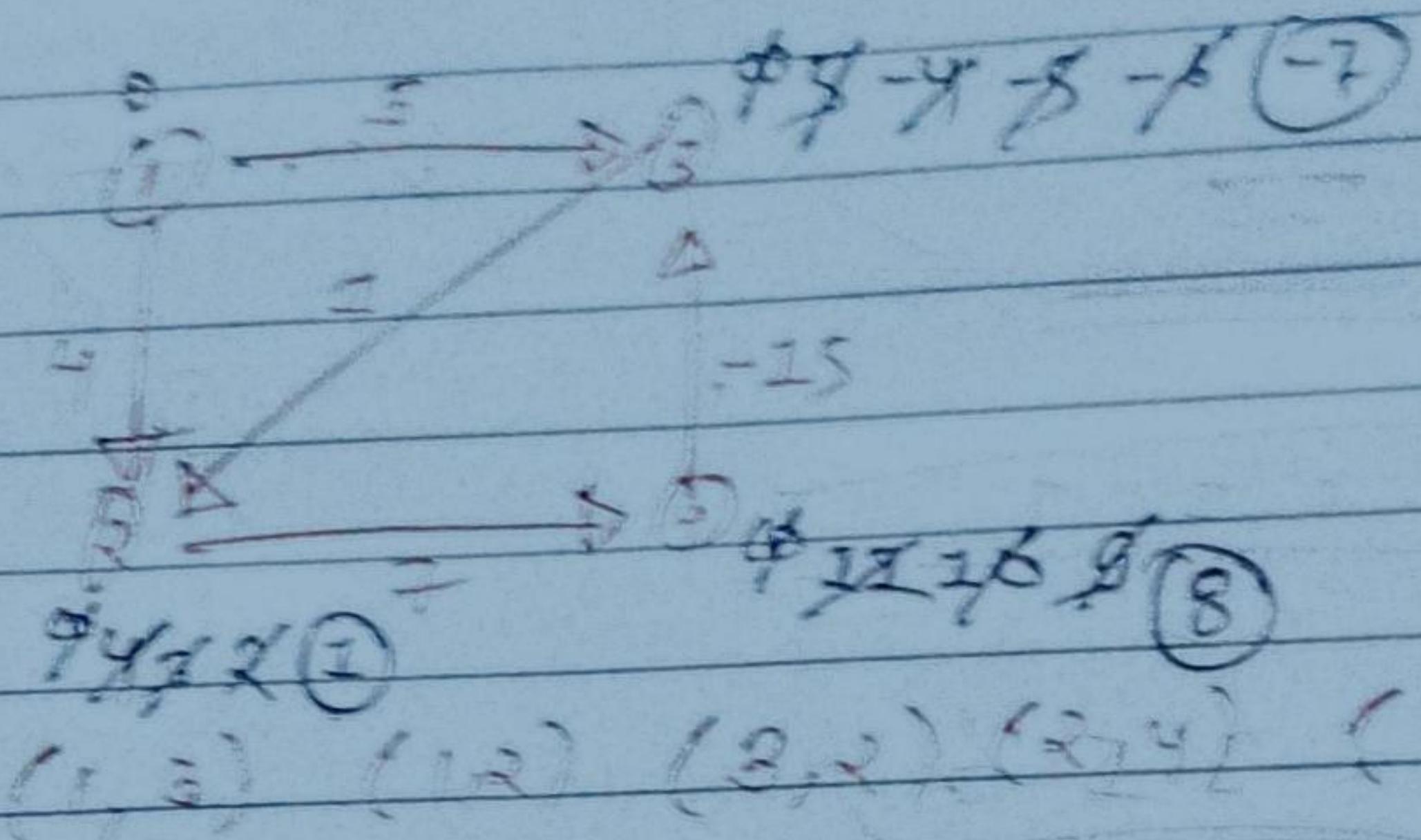
IVth \rightarrow

\downarrow $n-1$ times

Time complexity $\Theta(\epsilon(n-1))$

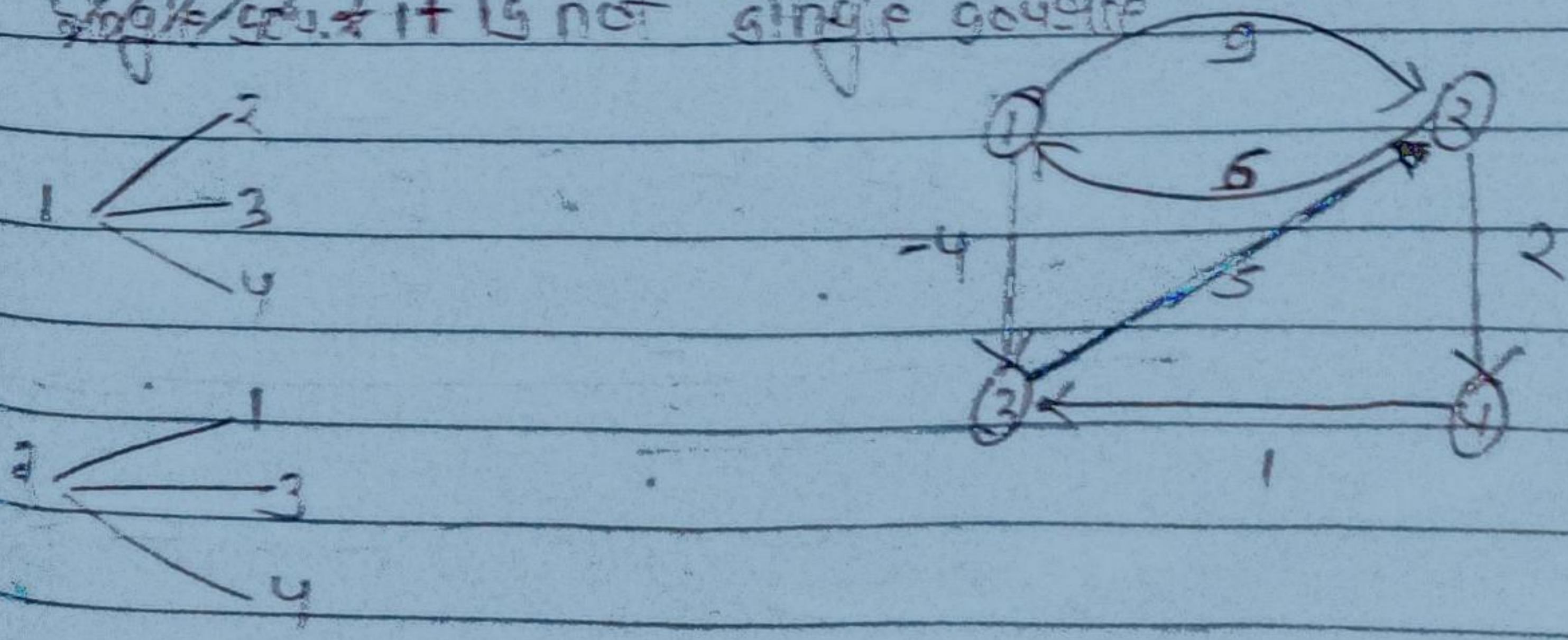
If complete graph $\Theta\left(\frac{n(n-1)^2}{2}\right) \cong n^3$

if each pair's ratio and whose total sum
is less than 1 then Belman-Ford will work



in 4th iteration distribution shows so not working
because contain -ve cycle.

All pair shortest path (Floyd Warshall Algo)
Single/Double it is not single source



SORTING

1) \Rightarrow Bubble sort \rightarrow each pairs of adjacent elements are compared and swapped if they are not in order.

\Rightarrow working \Rightarrow

14	33	27	35	10
----	----	----	----	----

\rightarrow start with first two elements and compare those

14	33	27	35	10
\downarrow	\downarrow			

\rightarrow No swapping ($14 < 33$)

14	33	27	35	10
\downarrow	\downarrow			

\rightarrow swapping ($33 > 27$)

14	27	33	35	10
\downarrow	\downarrow			

\rightarrow No swapping ($35 > 33$)

14	27	35	33	10
\downarrow	\downarrow			

\rightarrow swapping ($10 < 35$)

14	27	33	10	35
\downarrow	\downarrow			

\rightarrow Array after 1st iteration

repeat iteration for $(size - 1)$ time.

Note \Rightarrow if in any iteration there is no swapping then break. the whole process because array become sorted.

HTML → Responsive

CSS ←

JS → Left

PYTHON → ✓

DJANGO → ✓

*

C++ → ✓

OPPS in C++ → Left

DS / ALGO → Left

CP → Left

*

JS

elements events

- 1) onclick
- 2) on hover
- 3) on mouseover
- 4) onmousedown
- 5) onmouseup
- 6) onsubmit

Date() var dt = new Date()

dt.getDay()

-1 - full year()

-1 - Hours()

minutes

months

seconds
milliseconds

[ev] (doc. exam. calc. value)

getTime

1 Jan 1970

Dialogs → 1) prompt

box → 2) alert

3) confirm

1) random

Maths → 2) floor

3) ceil

4) round

5) log

6) sqrt

get, date

get, time

`<script> src="js/dom.js" </script>`

DOM

Date _____

1st

Page no. _____

Date _____

Page no. _____

→ How to target DOM objects?

- 1) id → doc.getElementById("-")
- 2) class name → - - - - (ClassName("))
- 3) Tag name → - - - - TagName()

DOM Set Methods

- 1) innerText
- 2) innerHTML
- 3) getAttribute.
- 4) Attribute.
- 5) removeAttribute

- 1) doc.
- 2) doc.all
- 3) doc.documentElement
- 4) doc.head
- 5) doc.title
- 6) doc.body
- 7) doc.images
- 8) docanchors
- 9) doc.links
- 10) doc.forms
- 11) doc doctype
- 12) doc.URL
- 13) doc.baseUrl
- 14) doc.domain
- 15) doc.getElementsByTagName("ClassName")
- 16) doc.getElementsByTagName("TagName")
- 17) doc.getElementById("ID")

what we can get with DOM?

- 1) HTML
- 2) Text
- 3) Attribute

→ innerText
innerHTML
getAttribute
getAttributeNode
Attributes

.value
.name

⇒ `doc.querySelector` → select 1st one
`doc.querySelectorAll` → select all elements

DOM CSS styling methods:

- 1) style
- 2) className
- 3) classList → return list (Array)

click (onClick)

Doubleclick (ondblclick)

Right click (oncontextmenu)

Mouseover

MouseOut

MouseDown

Mouse Up

Key Press

Key Up

Load

Unload

Resize

Scroll

classlist

- 1) add (class1, class2, ...)
- 2) remove (class1, class2, ...)
- 3) toggle (class)
- 4) contains (class)
- 5) item (index)
- 6) length .

addEventListener () .

```
doc.getElementById('id').addEventListener("click", myf)  
| | | | | | ("click", myf)  
start ?);
```

access children of body
doc.body.children ;

add a new child in body

```
var pchild = doc.createElement('p');  
var TextNode = doc.createTextNode(" - ");  
pchild.appendChild (TextNode);  
doc.body.appendChild(pchild);
```

var list = doc.querySelectorAll ("ul")

```
console.log (list.firstChild);  
(list.lastChild);
```

id.nextElementSibling, nextElementSibling

css styling using DOM

```
doc.getElementById('').style.color = "Red";  
doc.getElementById('').setAttribute ("style", "color:red;  
font:italic;");
```

window.location;

window.location.hostname

window.location.href

window.location = "https://www.youtube.com"

window.location.assign ("https://www - (-)");

Print the Page

For whole function my() { window.print(); }

For div fun my(id) {

Var bakiyp = doc.body.innerHTML;
Var divcont = doc.getElementById(id).innerHTML;

doc.body.innerHTML = divcont;
window.print();
doc.body.innerHTML = bakiyp;

Date and Time

Var d = new Date();
Var n = d.getTime();

Var hours = d.getHours;
min;
Second;
dtolocalTimeString();

Var clock = setInterval (clockTiming,
1000)

fun clockTiming() {

Var d = new Date();
Var x = d.toLocaleTimeString();
doc.write(x);
doc.getElementById(id).innerHTML = x;

.clearInterval(clock);