

DESIGN AND ANALYSIS OF ALGORITHMS

CS402

TIME ALLOTTED: 3 HOURS

FULL MARKS: 70

*The figures in the margin indicate full marks.
Candidates are required to give their answers in their own words as far as practicable*

GROUP – A
(Multiple Choice Type Questions)

1. Answer any **ten** from the following, choosing the correct alternative of each question: **10×1=10**

SL. NO.	Question	CO No.	Marks
(i)	Linked lists are not suitable for (A) Insertion sort (B) Binary search (C) Radix sort (D) Polynomial manipulation	1	1
(ii)	Average successful search time for sequential search on 'n' items is (A) $n/2$ (B) $(n-1)/2$ (C) $(n+1)/2$ (D) n^2	4	1
(iii)	In Randomized Quick sort, the expected running time of any input is (A) $O(n)$ (B) $O(n^2)$ (C) $O(n \log n)$ (D) $O(n^3)$	4	1
(iv)	kruskal's algorithm uses----- and prim's algorithm uses----- in determining the MST (A) edges, vertex (B) vertex, edges (C) edges, edges (D) vertex, vertex	3	1
(v)	$T(n) = 2T(n/2) + (n \log n)$ then $T(n) =$ (A) $\Theta(n \log n)$ (B) $\Theta(n \log(n \log n))$ (C) $\Theta(n^2 \log(n \log n))$ (D) $\Theta(n^2 \log n)$	4	1
(vi)	"In which of the following cases n-queen problem does not exist" (A) $n=2$ and $n=4$ (B) $n=4$ and $n=6$ (C) $n=2$ and $n=3$ (D) $n=4$ and $n=8$	1	1
(vii)	If each node in a tree has value greater than every value in its left sub tree and value less than every value in its right sub tree, the tree is known as	3	1

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	(A) complete tree (B) full binary tree (C) binary search tree (D) threaded tree		
(viii)	The depth of a complete binary tree with 'n' nodes is (A) $\log(n+1)-1$ (B) $\log n$ (C) $\log(n-1)+1$ (D) $\log n +1$	4	1
(ix)	The running time of Dijkstra's algorithm is- (A) $O(V^2)$ (B) $O(V+E)$ (C) $O(n \log n)$ (D) all of the above"	2	1
(x)	Given 2 sorted lists of size 'm' and 'n' respectively. Number of comparisons needed in the worst case by the merge sort algorithm will be (A) mn (B) $\max(m,n)$ (C) $\min(m,n)$ (D) $m+n-1$	2	1
(xi)	Which of the following best described sorting? (A) Accessing and processing each record exactly once (B) Finding the location of the record with a given key (C) Arranging the data in some given order (D) Adding a new record to the data structure	3	1
(xii)	Find an optimal parenthesization of a matrix chain product whose sequence of dimension s is $\langle 5,4,3 \rangle$ (for three matrices) (A) 125 (B) 130 (C) 135 (D) 140	1	1

GROUP – B*
(Short Answer Type Questions)

Answer any *three* from the following: $3 \times 5 = 15$

SL. NO.			CO No.	Marks
2.	(a)	Describe the role of space complexity and time complexity of a Program?	1	3
	(b)	Explain quick sort algorithm and simulate it for the following data 20, 5, 10, 16, 54, 21	1	2
3.		Illustrate quick sort algorithm and discuss its best case and average case time complexity	1	5
4.		Construct a max-heap using the above algorithm with the following data. $\langle 14, 16, 11, 10, 3, 7, 2, 9, 4, 8, 1 \rangle$	2	5
5.	(a)	What is order of growth?, Explain.	2	3
	(b)	What is meant by 'divide and conquer'.	3	2
6.	(a)	Define Class P and NP problem.	2	2

- (b) Show that C-SAT problem is NP Complete problem 4 3

GROUP – C*
(Long Answer Type Questions)

Answer any *three* from the following: **3×15=45**

SL. NO.		CO No.	Marks
7.	(a) Define Ω -notation.	2	2
	(b) Prove that the running time of an algorithm is $\Theta(g(n))$ if and only if its worst case running time is $O(g(n))$ and its best case running time is $\Omega(g(n))$.	4	5
	(c) Explain how do you solve the Job sequencing with deadline by greedy approach.	2	8
8.	(a) Discuss activity selection problem for job sequencing	1	4
	(b) Solve the recurrence $T(n)=3T(n/2)+n$ by substitution method	2	5
	(c) Differentiate the main features of greedy method and dynamic programming.	2	6
9.	(a) Write a Matrix Chain Multiplication Algorithm to find the optimal parenthesis for given n numbers of matrices. What is the time complexity?	3	8
	(b) Find an optimal solution of parenthesization of a matrix-chain Multiplication whose sequence of dimension {4, 10, 3, 12, 20, and 7}.	2	7
10.	(a) What do you mean by recursion tree?	1	3
	(b) Write non deterministic algorithm for sorting and searching	1	7
	(c) Using KRUSKAL's algorithm find the Minimal Spanning Tree of the following graph.	2	5
11.	(a) Explain the Strassen's Matrix Multiplication algorithm using Divide and Conquer approach	3	7
	(b) Consider the following instance of the Knapsack Problem: $n=4$ Weight Vector $= (20, 18, 10, 15)$ and Profit Vector $= (36, 40, 60, 50)$ Knapsack Capacity is 25. Find the optimal solution of the problem using above algorithm.	2	8