

**Renewable Energy Technology**  
**Mid Term Assignment**  
**Spring 20-21**

**Last date of submission: 13.03.21**

1. When installing a fixed flat-panel collector on a roof in Sylhet city ( $24.8949^{\circ}$  N,  $91.8687^{\circ}$  E), what orientation (azimuth and tilt) should be chosen to maximize the total energy harnessed over the year?
2. Calculate the maximum and minimum solar elevation angles for Dhaka ( $23.8103^{\circ}$  N,  $90.4125^{\circ}$  E).
3. What is the angle of incident of solar radiation on a horizontal surface at solar noon in Khulna city ( $22.8456^{\circ}$  N,  $89.5403^{\circ}$  E) on the **A**th of July?

**A should be the first 2 digits of your ID. (eg. if your ID is 18-78253-2 then A = 18)**

4. What is the local solar time when it is 10h00 on the clock in Liverpool ( $53^{\circ}$ N,  $3^{\circ}$ W)?  
Liverpool uses Greenwich Mean Time with the standard time zone meridian at  $0^{\circ}$ W.  
Daylight saving time is not in effect in winter.

**Here, **Gregorian Calendar Day (n)** should be the last 2 digits of your ID. (eg. if your ID is 18-78253-2 then n = 32)**

5. Calculate the position (azimuth, elevation) of the Sun at 15h30 on the clock in Istanbul ( $41^{\circ}$ N,  $28^{\circ}$ E). Istanbul uses Eastern European Time, with the standard time zone meridian at  $30^{\circ}$ E. Daylight saving time is in effect (summer time is one hour ahead of winter time).

**Here, **Gregorian Calendar Day (n)** should be the last 2 digits of your ID. (eg. if your ID is 18-78253-2 then n = 32)**

6. If the dark saturation current of a solar cell is  $1.7 \times 10^{-8} \text{ A/m}^2$ , the cell temperature is  $27^{\circ}\text{C}$ , the short-circuit current density is  $250 \text{ A/m}^2$ , and the voltage at maximum power is  $0.47 \text{ V}$ , calculate the open circuit voltage,  $V_{oc}$ ; current density at maximum power,  $I_{max}$ ; maximum power,  $P_{max}$ ; and maximum efficiency,  $\eta_{max}$ . What cell area is required to get an output of  $20 \text{ W}$  when the available solar radiation is  $820 \text{ W/m}^2$ ?

Ans to the Q. NO-1:

For absorbing the maximum energy it should be non tracking all over the year. As it's located in north hemisphere, it should be faced to south hemisphere, so azimuthal angle is zero. Here, it is a flat plate collector, so optimum tilt angle is equal to latitude of the location.

$$\beta_c = \phi = 24.8949^\circ$$

Ans to the Q. NO-2:

For maximum solar elevation angle ( $\theta_s$ ):

We know that,

Long day at dhaka = 21 June

$$\therefore n = 21 \text{ June}$$

$$= 31 + 28 + 31 + 30 + 31 + 21 \quad \left| \begin{array}{l} \text{Here} \\ \phi = 23.8103 \end{array} \right.$$

$$= 172$$

$$\omega = \frac{\pi}{12} (t_s - 12)$$

$$= \frac{\pi}{12} (12 - 12)$$

$$\delta = \sin^{-1} \left[ 0.39795 \cos \left( 2\pi \frac{172 - 173}{365} \right) \right]$$

$$= 23.44^\circ$$

$$\theta_2 = \cos^{-1} (\cos \phi \cos \delta \cos \omega + \sin \phi \sin \delta)$$

$$= \cos^{-1} [\cos(23.8103) \cos(23.44) \cos 0 + \sin(23.8103) \sin(23.44)]$$

$$= 0.3703^\circ$$

Now,

$$\theta_g = 90 - 07$$

$$= 89.629^\circ$$

For minimum solar elevation ( $\theta_g$ ):

21<sup>st</sup> december is short day

So,  $n = 21^{\text{th}}$  december

$$= 365 - 10$$

$$= 355$$

$$\omega = \frac{\pi}{12} (t_s - 12)$$

$$= 0$$

$$[\because t_s = 012]$$

$$\delta = \sin^{-1} [0.39795 \cos(2\pi \frac{355 - 173}{365})]$$

$$= -23.44^\circ$$

$$\theta_T = \cos^{-1} [\cos(23.8103) \cos(-23.44) \cos 0 - \sin(23.8103) \sin(-23.44)]$$

$$= 47.25^\circ$$

$$\theta_s = \gamma_2 - \theta_z$$

$$= 42.74^\circ$$

Ans to the Q. no - 3:

$$\text{ID: 18-37400-1}$$

Hence,  $A = 18$

Hour angle,

$$\omega = \frac{\pi}{12} (t_s - 12)$$

$$= \frac{\pi}{12} (12 - 12)$$

$$= 0$$

Horizontal Surface,  $\beta_c = 0$

Now, Angle of incident of solar radiation-

$$\theta = \cos^{-1} [\cos \beta_c \cos \theta_z + \sin \beta_c \sin \theta_z \cos(\pi_s - \pi)]$$



$$\Rightarrow \theta = \cos^{-1} [\cos \theta_1 + \sin \theta_1 \sin \theta_2 \cos (\pi_s - \pi_e)]$$

$$\Rightarrow \theta = \cos^{-1} (\cos \theta_2 + 0)$$

$$\Rightarrow \theta = \theta_2$$

For Khulna latitude,  $\phi = 22.8456^\circ$

$n = 1^{\text{th}}$  July

$= 18^{\text{th}}$  July

$$= 31 + 28 + 31 + 30 + 31 + 30 + 18$$

$$= 199$$

$$\delta = \sin^{-1} \left( 0.39795 \cos \left( 2\pi \frac{n-173}{365} \right) \right)$$

$$= 21.02^\circ$$

$$\theta_z = \cos^{-1} [\cos(22.8456) \cos(21.02) \cos 0 + \sin(22.8456) \sin(21.02)]$$

$$= 1.825^\circ$$

The angle of incident of solar radiation is

$$\theta = \theta_z = \theta_7 = 1.825^\circ$$

Ans to the question No. - 9

ID: 18-37900-1

$n: 01 = 1$

$t_{clk} = 10 \text{ hours}$

$\psi_{std} = 0$

$\psi_{loc} = 3^\circ$

$\Delta t_{DST} = 0$

$$A = 0.258$$

$$B = -7.416$$

$$C = -3.648$$

$$D = -9.228$$

Now,

$$\Delta t_{EOT} = A \cos\left(2\pi \frac{n-1}{365}\right) + B \sin\left(2\pi \frac{n-1}{365}\right) + C \cos\left(4\pi \frac{n-1}{365}\right) + D \sin\left(4\pi \frac{n-1}{365}\right)$$
$$= -3.39$$

$$t_s = t_{clk} + \frac{\psi_{std} - \psi_{loc}}{15^\circ} + \frac{\Delta t_{EOT}}{60} + \Delta t_{DST}$$
$$= 10 + \frac{0 - 3}{15} + \frac{-3.39}{60} + 0$$
$$= 9.74 \text{ hours}$$

Solar time  $t_s = 9.74 \text{ hours}$





Ans to the question No. 5

ID: 18-37400-1

$n = 1$

$t_{clk} = 15.5$  hour

$\phi = 41^\circ$

$\psi_{loc} = 28^\circ$   $\psi_{sid} = 30^\circ$

$\Delta t_{dst} = 1$

$$\Delta t_{EOT} = A \cos\left(2\pi \frac{n-1}{365}\right) + B \sin\left(2\pi \frac{n-1}{365}\right) + C \cos\left(4\pi \frac{n-1}{365}\right) + D \sin\left(4\pi \frac{n-1}{365}\right)$$
$$= -3.39$$

$$t_s = 15.5 + \frac{30-28}{15} + \frac{-3.39}{60} + 1 = 16.57 \text{ hour}$$

$$\omega = \frac{\pi}{12} (t_s - 12)$$

$$= \frac{\pi}{12} (16.57 - 12) = 68.55^\circ$$

$$\delta = \sin^{-1} \left( 0.39795 \cos\left(2\pi \frac{1-173}{365}\right) \right) = -23.04^\circ$$

$$\theta_z = \cos^{-1} \left[ \cos(41) \cos(-23.04) \cos(68.55) + \sin(41) \sin(-23.04) \right]$$

$$= 90.15^\circ$$

$$\theta_s = \frac{\pi}{2} - \theta_2 = -0.159$$

$$\gamma_s = \operatorname{sgn}(\omega) \cos^{-1} \left[ \frac{\cos \theta_2 \sin \phi - \sin \delta}{\sin \theta_2 \cos \phi} \right]$$

$$\operatorname{sgn}(68.95) = +1$$

$$= 58.91^\circ$$

$$\text{Azimuth angle} = 58.91^\circ$$

$$\text{Elevation angle} = -0.159^\circ$$

Ans to the Q. No - 6.

Here,

$$I_s / = 1.7 \times 10^{-8} \text{ A/m}^2$$

$$I_{sc} = 250 \text{ Am}^{-1}$$

$$T_e = 27^\circ \text{C}$$

$$V_m = 0.47 \text{ V}$$

$$= 300 \text{ K}$$

We know that,

$$\frac{e}{k T_e} = \frac{1.602 \times 10^{-19}}{1.381 \times 10^{-23} \times 300}$$
$$= 38.67$$

$$I_{max} = \frac{e V_m}{k T_e + e V_m} (I_{sc} + I_0)$$

$$= \frac{(1.602 \times 10^{-19} \times 0.47) (250 + 1.7 \times 10^{-8})}{(1.381 \times 10^{-23} \times 300) + (1.602 \times 10^{-19} \times 0.47)}$$
$$= 236.97 \text{ Am}^{-2}$$

$$V_{Ac} = \frac{k T_e}{e} \ln \left( \frac{I_{sc}}{I_0} + 1 \right)$$

$$= \frac{1.38 \times 10^{-23} \times 300}{1.602 \times 10^{-19}} \times \ln \left( \frac{250}{1.7 \times 10^{-8}} + 1 \right)$$
$$= 0.605 \text{ V}$$

$$P_{max} = V_m I_m$$
$$= 0.47 \times 236.96$$
$$= 111.37 \text{ W}$$

$$T_{max} = \frac{111.37}{820} \times 100$$

$$T_{max} = \frac{111.37}{820} \times 100$$
$$= 13.587$$

$$A = \frac{20}{111.37} = 0.179$$

