

## What happens when two bodies collide in a dynamics point of view?

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I'm a high school student learning about energy and momentum. What confuses me is the things with elastic and inelastic collisions.

I completely (in my opinion) understand those concepts in energy and momentum point of views. The problem is I can't reconcile these concepts with what I learned about forces.

Suppose we have two masses  $m_1$  and  $m_2$  traveling with velocities  $v_1$  and  $v_2$  and collides each other. To simplify let it be in 1-dimensional case. Here is my picture of what is going on. After the collision there is a change in velocity, so there is an acceleration. Since there is an acceleration there is also force. But how do we calculate that force? The velocity function is a constant function which has a discontinuity at the time of collision. So it is not differentiable at that time, which means the concept of force and acceleration is meaningless at that time!? I have always thought that energy is just a convenient computational tool and we can do everything with classical mechanics based solely on the concepts of forces and Newton's law.

If my suspect is right, we should go to molecular level to understand what is going on? Because in my understanding collision is the result of some repulsive forces between the atoms and without them there would be no collision as the bodies just go through each other. So if possible, can someone elaborate on this and also explain what causes the two different types of collisions (elastic and inelastic) ?

forces

kinematics

energy-conservation

momentum

collision

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asked Dec 1, 2015 at 23:48



Tung Nguyen

175 ● 1 ● 6

There isn't such a thing as a purely elastic collision. All collisions are inelastic to some degree on another. – [John Alexiou](#) Dec 1, 2015 at 23:55

There isn't such a thing as a PEC but we still use it for modeling. – [Jay](#) Dec 2, 2015 at 0:10

What the above poster said is right. Check out [physics.stackexchange.com/questions/184388/...](http://physics.stackexchange.com/questions/184388/...) – [boson](#) Dec 2, 2015 at 4:48

1 watch this first: [youtube.com/watch?v=AkB81u5IM3I](https://youtube.com/watch?v=AkB81u5IM3I) – [John Alexiou](#) Dec 2, 2015 at 19:26

2 Answers

Sorted by:

Highest score (default)

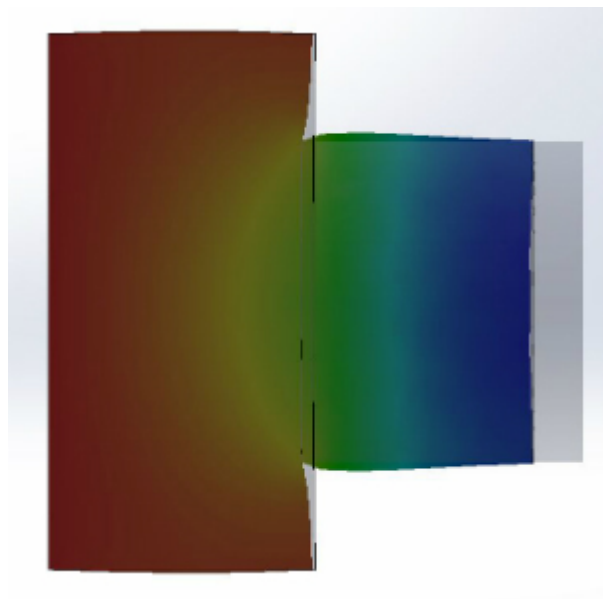


▲ You are correct that this is a difficult problem. **Energy methods are required to determine the contact force because kinetic energy is stored in strain ('spring')**

2 **energy during the collision, when both bodies deform.**

✓ If the bodies are assumed rigid, the contact force is undefined. As you correctly conclude from  $a = \frac{dv}{dt}$ , bodies cannot decelerate instantly (ie.  $t = 0$ ). In reality, the bodies decelerate during the time (and distance) of deformation. Without deformation,  $d = 0 = \frac{v' - v}{2}t$ , and  $F = \frac{dP}{dt}$ , require  $t = 0$  and  $F \rightarrow \infty$ . Therefore, to determine the contact force between colliding bodies, deformation must be solved.

🕒 Impact Mechanics have been studied extensively for engineering applications. Complex collision problems are solved numerically via Continuum Mechanics and Finite Element Methods, as shown below.



In practice, analytical approximations are possible with simple geometry (and conservative assumptions)- this is discussed in the following.

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### Think of the problem in three time steps:

#### 1) Before contact:

Both bodies have mass ( $m_1, m_2$ ) and velocity ( $v_{1,i}, v_{2,i}$ ).

#### 2) During contact:

The time interval begins at contact between bodies and ends at the instant  $v_f = v_{1,f} = v_{2,f}$ . The final velocity is solved by Conservation of Momentum:

$$m_1(v_f - v_{1,i}) = m_2(v_f - v_{2,i}) \Rightarrow \therefore v_f = \frac{m_1 v_{1,i} - m_2 v_{2,i}}{m_1 - m_2}$$

Next, apply Conservation of Energy and assume all energy is stored in strain energy (where no energy is lost to heat, sound, etc.). Strain energy is analogous to energy stored in a spring, where the effective spring constants,  $k = \frac{EA}{L}$ , depend on the geometry and material of the bodies

$$\Delta E_{Kinetic} = E_{Strain}$$

$$\left[\frac{1}{2}m_1v_{1,i}^2 + \frac{1}{2}m_2v_{2,i}^2\right]_i - \left[\frac{1}{2}(m_1 + m_2)v_f^2\right]_f = \frac{1}{2}k_1\delta_1^2 + \frac{1}{2}k_2\delta_2^2$$

While it is not possible to analytically solve for the displacement of both bodies ( $\delta = \delta_1 + \delta_2$ ), engineers simplify the problem and solve for the  $\delta$  they care about<sup>1</sup>; this is a conservative assumption because it predicts a higher contact force than if both bodies deformed.

$$\left[\frac{1}{2}m_1v_{1,i}^2 + \frac{1}{2}m_2v_{2,i}^2\right]_i - \left[\frac{1}{2}(m_1 + m_2)v_f^2\right]_f = \frac{1}{2}k\delta^2$$

$$\therefore \delta = \sqrt{\frac{\left[\frac{1}{2}m_1v_{1,i}^2 + \frac{1}{2}m_2v_{2,i}^2\right]_i - \left[\frac{1}{2}(m_1 + m_2)v_f^2\right]_f}{\frac{1}{2}k}}$$

Finally, the average contact force is determined from:

$$\therefore F_{contact} = k\delta$$

Similarly, the same result is obtained from the kinematic equations:

$$t = \frac{2\delta}{v_f - v_i} \Rightarrow a = \frac{v_f - v_i}{t} \Rightarrow \therefore F_{contact} = ma$$

### 3) After contact.

Elastic collisions are idealized so that all kinetic energy is conserved. Inelastic collisions describe real collisions- some kinetic energy is permanently lost to heat, sound, plastic deformation, etc. and the resulting final kinetic energies are lower (than predicted by the idealized elastic model). A [coefficient of restitution](#) ( $CoR$ ) is applied to the Conservation of Momentum to reflect the bodies' final velocities. Note that for elastic collisions, the  $CoR = 1$ . While inelastic collisions are more accurate, the  $CoR$  is often unknown; therefore, collisions are assumed elastic to provide a reasonable estimate.

<sup>1</sup> "Machine Design: An Integrated Approach (2nd Ed.)"- Robert L. Norton

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edited Jun 11, 2020 at 9:33



Community Bot

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answered Dec 2, 2015 at 7:44



OnStrike

684 ● 1 ● 6 ● 16

The acceleration is due to an impulse, which is the change in momentum. Assuming you know velocity before and after, you can find the impulse, which is just the change in momentum, or the integral over the force with respect to time.

$$\int_{t_1}^{t_2} \mathbf{F} dt = \Delta \mathbf{p} = m\mathbf{v}_2 - m\mathbf{v}_1$$

or more simply

$$\mathbf{F}\Delta t = \Delta \mathbf{p} = m\mathbf{v}_2 - m\mathbf{v}_1$$

Where  $\Delta t$  is the time the force is exerted. Note that this would give you an average acceleration, not instantaneous.

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answered Dec 2, 2015 at 0:09



Day

184 ● 1 ● 10

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The bodies travel at a constant speed after collision. So I guess there is only instantaneous acceleration and instantaneous force ? If so, what is the physical implications of the average force and acceleration from your formula ? – Tung Nguyen Dec 2, 2015 at 0:43 ✎

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When I say the  $\Delta t$  the force is exerted I'm talking about the collision time. Besides this way of looking at it, remember that you can also get the acceleration by  $a = \frac{F}{m}$  – Day Dec 2, 2015 at 1:36 ✎

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The general idea of your answer is correct, but  $\Delta t$  is unknown. – OnStrike Dec 2, 2015 at 8:15 ✎

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