

Combustion of Packed Pellets of Core-Shell Particle

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Chapter 1

combustion-packed-pellet-core-shell-particle

Chapter 2

Namespace Index

2.1 Namespace List

Here is a list of all documented namespaces with brief descriptions:

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Chapter 3

Class Index

3.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

GMatrix< real_t >	Class to implement a memory efficient Givens' Rotation Matrix that can vanish the element $a_{k+1,k}$ of a matrix A	11
QMatrix< real_t >	Class to implement a memory efficient model of $N \times N$ Q Matrix	15
QRSolver< real_t >	Class to implement QR factorization algorithm for solving matrix equations of the $A \cdot x = b$ where A is a $N \times N$ tridiagonal matrix and x and b are $N \times 1$ vectors	18
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Chapter 4

File Index

4.1 File List

Here is a list of all documented files with brief descriptions:

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This header serves the definition of an implementation of Givens' Rotation matrix. The rotation matrix is used to solve matrix equations through QR factorization method, particularly tridiagonal matrix equation	33
include/qrsolver/ Q_Matrix.hpp	
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include/qrsolver/ R_Matrix.hpp	
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Chapter 5

Namespace Documentation

5.1 QR_Factorization.py Namespace Reference

5.1.1 Detailed Description

Python program to quickly check out and understand QR Factorization method for solving matrix equations

The matrices are printed at each step of factorization to understand the transformation of the matrices

Chapter 6

Class Documentation

6.1 GMatrix< real_t > Class Template Reference

Class to implement a memory efficient Givens' Rotation Matrix that can vanish the element $a_{k+1,k}$ of a matrix A .

```
#include <G_Matrix.hpp>
```

Public Member Functions

- [GMatrix](#) ([RMatrix](#)< real_t > &matrix, unsigned int index)
Construct a new Givens Rotation Matrix to vanish the element at position $(k + 1, k)$ of R matrix.
- void [multiply](#) ([RMatrix](#)< real_t > &R)
Multiplies the Givens Rotation Matrix to the R Matrix and updates the R matrix in place.
- void [multiplyLastRow](#) ([RMatrix](#)< real_t > &R)
Multiplies the Givens rotation matrix to the R matrix where the rotation matrix is formed to vanish the sub diagonal element of the last row $(N, N - 1)$ of the $N \times N$ R matrix.
- void [multiply](#) ([QMatrix](#)< real_t > &Q)
Multiplies the Givens Rotation Matrix to the Q Matrix and updates the Q matrix in place.

Private Attributes

- real_t [g_k_k](#)
Element of Givens Rotation Matrix at position k, k .
- real_t [g_k_kp1](#)
Element of Givens Rotation Matrix at position $k, k + 1$.
- real_t [g_kp1_k](#)
Element of Givens Rotation Matrix at position $k + 1, k$.
- real_t [g_kp1_kp1](#)
Element of Givens Rotation Matrix at position $k + 1, k + 1$.
- unsigned int [k](#)
Index k , where we want to vanish the element at position $k + 1, k$.

6.1.1 Detailed Description

```
template<typename real_t>
class GMatrix< real_t >
```

Class to implement a memory efficient Givens' Rotation Matrix that can vanish the element $a_{k+1,k}$ of a matrix A .

A Givens rotation matrix is an orthogonal such that $G_{N \times N} = [g_{ij}]_{N \times N}$ where

$$g_{ij} = \begin{cases} 1 & i = j \neq k, k+1 \\ \cos \theta & i = j = k, k+1 \\ \sin \theta & i = k, j = k+1 \\ -\sin \theta & i = k+1, j = k \\ 0 & \text{otherwise} \end{cases} \quad (6.1)$$

When the Givens Rotation Matrix is multiplied to another matrix $B_{N \times N} = [b_{i,j}]_{N \times N}$

$$C_{N \times N} = G_{N \times N} \cdot B_{N \times N} \quad (6.2)$$

$$\Rightarrow c_{ij} = \sum_{l=1}^N g_{i,l} b_{l,j} \quad (6.3)$$

$$\Rightarrow c_{ij} = \begin{cases} g_{k,k} b_{k,j} + g_{k,k+1} b_{k+1,j} & i = k \\ g_{k+1,k} b_{k,j} + g_{k+1,k+1} b_{k+1,j} & i = k+1 \\ b_{i,j} & \text{otherwise} \end{cases} \quad (6.4)$$

Template Parameters

<i>real_t</i>	float, double or long double data types to represent real numbers
---------------	---

Definition at line 58 of file G_Matrix.hpp.

6.1.2 Constructor & Destructor Documentation

6.1.2.1 GMatrix()

```
template<typename real_t >
GMatrix< real_t >::GMatrix (
    RMatrix< real_t > & matrix,
    unsigned int index )
```

Construct a new Givens Rotation Matrix to vanish the element at position $(k+1, k)$ of R matrix.

Parameters

<i>R</i>	R matrix whose element at position $(k+1, k)$ needs to be vanished
<i>index</i>	k

Definition at line 18 of file G_Matrix.cpp.

6.1.3 Member Function Documentation

6.1.3.1 multiply() [1/2]

```
template<typename real_t >
void GMatrix< real_t >::multiply (
    QMatrix< real_t > & Q )
```

Multiplies the Givens Rotation Matrix to the Q Matrix and updates the Q matrix in place.

Parameters

Q	Q Matrix passed as reference
---	------------------------------

Q matrix may be represented as $Q_{N \times N} = [q_{i,j}]_{N \times N}$ where

$$q_{i,j} = 0, \quad j > i$$

Thus, when a rotation matrix is multiplied to Q matrix

$$C_{N \times N} = G_{N \times N} \cdot Q_{N \times N} \quad (6.5)$$

$$\Rightarrow c_{ij} = \sum_{l=1}^N g_{i,l} q_{l,j} \quad (6.6)$$

$$\Rightarrow c_{ij} = \begin{cases} g_{k,k} l_{k,j} + g_{k,k+1} q_{k+1,j} & i = k \\ g_{k+1,k} l_{k,j} + g_{k+1,k+1} q_{k+1,j} & i = k + 1 \\ q_{i,j} & \text{otherwise} \end{cases} \quad (6.7)$$

Definition at line 49 of file G_Matrix.cpp.

6.1.3.2 multiply() [2/2]

```
template<typename real_t >
void GMatrix< real_t >::multiply (
    RMatrix< real_t > & R )
```

Multiplies the Givens Rotation Matrix to the R Matrix and updates the R matrix in place.

Parameters

R	R Matrix that will be converted into upper tridiagonal matrix after multiplication
---	--

R matrix can be represented as $R_{N \times N} = [r_{i,j}]_{N \times N}$ where

$$r_{i,j} = 0 \quad \text{if } j < i - 1 \quad \text{or } j > i + 1 \quad (6.8)$$

Thus, upon multiplying the R matrix with the rotation matrix, we get matrix $C_{N \times N}$

$$c_{ij} = \begin{cases} g_{k,k}r_{k,j} + g_{k,k+1}r_{k+1,j} & i = k \\ g_{k+1,k}r_{k,j} + g_{k+1,k+1}r_{k+1,j} & i = k + 1 \\ r_{i,j} & \text{otherwise} \end{cases} \quad (6.9)$$

$$\Rightarrow c_{ij} = \begin{cases} g_{k,k}r_{k,k-1} & i = k & j = k - 1 \\ g_{k,k}r_{k,k} + g_{k,k+1}r_{k+1,k} & i = k & j = k \\ g_{k,k}r_{k,k+1} + g_{k,k+1}r_{k+1,k+1} & i = k & j = k + 1 \\ g_{k,k+1}r_{k+1,k+2} & i = k & j = k + 2 \\ g_{k+1,k}r_{k,k-1} & i = k + 1 & j = k - 1 \\ g_{k+1,k}r_{k,k} + g_{k+1,k+1}r_{k+1,k} & i = k + 1 & j = k \\ g_{k+1,k}r_{k,k+1} + g_{k+1,k+1}r_{k+1,k+1} & i = k + 1 & j = k + 1 \\ g_{k+1,k+1}r_{k+1,k+2} & i = k + 1 & j = k + 2 \\ r_{i,j} & \text{otherwise} \end{cases} \quad (6.10)$$

But as we iterate over k and multiply the corresponding rotation matrix, the sub-diagonal ($r_{i,i-1}$) becomes zero and the super-super-diagonal ($r_{i,i+2}$) fills up with non-zero values.

$$\Rightarrow c_{ij} = \begin{cases} 0 & i = k & j = k - 1 \\ g_{k,k}r_{k,k} + g_{k,k+1}r_{k+1,k} & i = k & j = k \\ g_{k,k}r_{k,k+1} + g_{k,k+1}r_{k+1,k+1} & i = k & j = k + 1 \\ g_{k,k+1}r_{k+1,k+2} & i = k & j = k + 2 \\ 0 & i = k + 1 & j = k - 1 \\ 0 & i = k + 1 & j = k \\ g_{k+1,k}r_{k,k+1} + g_{k+1,k+1}r_{k+1,k+1} & i = k + 1 & j = k + 1 \\ g_{k+1,k+1}r_{k+1,k+2} & i = k + 1 & j = k + 2 \\ r_{i,j} & \text{otherwise} \end{cases} \quad (6.11)$$

Definition at line 80 of file G_Matrix.cpp.

6.1.3.3 multiplyLastRow()

```
template<typename real_t >
void GMatrix< real_t >::multiplyLastRow (
    RMatrix< real_t > & R )
```

Multiplies the Givens rotation matrix to the R matrix where the rotation matrix is formed to vanish the sub diagonal element of the last row ($N, N - 1$) of the $N \times N$ R matrix.

$$\Rightarrow c_{ij} = \begin{cases} 0 & i = k & j = k - 1 \\ g_{N-1,N-1}r_{N-1,N-1} + g_{N-1,N}r_{N,N-1} & i = k & j = k \\ g_{N-1,N-1}r_{N-1,N} + g_{N-1,N}r_{N,N} & i = k & j = k + 1 \\ 0 & i = k + 1 & j = k - 1 \\ 0 & i = k + 1 & j = k \\ g_{N,N-1}r_{N-1,N} + g_{N,N}r_{N,N} & i = k + 1 & j = k + 1 \\ r_{i,j} & \text{otherwise} \end{cases} \quad (6.12)$$

Parameters

<i>R</i>	R Matrix that will be converted into upper tridiagonal matrix after multiplication
----------	--

Definition at line 135 of file G_Matrix.cpp.

The documentation for this class was generated from the following files:

- include/qrsolver/G_Matrix.hpp
- src/qrsolver/G_Matrix.cpp

6.2 QMatrix< real_t > Class Template Reference

Class to implement a memory efficient model of $N \times N$ Q Matrix.

```
#include <Q_Matrix.hpp>
```

Public Member Functions

- [QMatrix](#) (unsigned int n)
Construct a new Q Matrix.
- [~QMatrix](#) ()
Destroy the Q Matrix object.
- [real_t getElement](#) (unsigned int row_index, unsigned int column_index)
Get the i,j th element of the Q Matrix.
- [void setElement](#) (unsigned int row_index, unsigned int column_index, real_t value)
Set the value of the i,j th element of the Q Matrix.
- [void printMatrix](#) ()
Prints the Q Matrix in form of a 2D array.
- [void identity](#) ()
Makes Q matrix an identity matrix.
- [void multiply](#) (real_t *b, real_t *x)
Multiplies the Q matrix with the column vector b and stores the result in the column vector x.

Private Member Functions

- unsigned int [getIndex](#) (unsigned int row_index, unsigned int column_index)
Get the index of i,j th element of Q matrix in the flattened array.
- bool [indexOfZeroElement](#) (unsigned int row_index, unsigned int column_index)
Checks if the row index i and the column index j belong to a zero element of the Q matrix.

Private Attributes

- [real_t * array](#)
One dimensional array to store only non zero elements of the lower triangular matrix.
- [const unsigned int N](#)
Number of rows in a $N \times N$ square matrix.

6.2.1 Detailed Description

```
template<typename real_t>
class QMatrix< real_t >
```

Class to implement a memory efficient model of $N \times N$ Q Matrix.

Template Parameters

<i>real_t</i>	float, double or long double data types to represent real numbers
---------------	---

Definition at line 25 of file Q_Matrix.hpp.

6.2.2 Constructor & Destructor Documentation

6.2.2.1 QMatrix()

```
template<typename real_t >
QMatrix< real_t >::QMatrix (
    unsigned int n )
```

Construct a new Q Matrix.

Parameters

<i>n</i>	Number of rows in the $N \times N$ square matrix
----------	--

Definition at line 21 of file Q_Matrix.cpp.

6.2.3 Member Function Documentation

6.2.3.1 getElement()

```
template<typename real_t >
real_t QMatrix< real_t >::getElement (
    unsigned int row_index,
    unsigned int column_index )
```

Get the i,j th element of the Q Matrix.

Parameters

<i>row_index</i>	Row index i
<i>column_index</i>	Column index j

Returns

Value of the i,j th element of the Q Matrix

Definition at line 62 of file Q_Matrix.cpp.

6.2.3.2 getIndex()

```
template<typename real_t >
unsigned int QMatrix< real_t >::getIndex (
    unsigned int row_index,
    unsigned int column_index ) [private]
```

Get the index of i,j th element of Q matrix in the flattened array.

Parameters

<i>row_index</i>	Row index i
<i>column_index</i>	Column index j

Returns

Index of the i,j th element in the flattened array

Definition at line 41 of file Q_Matrix.cpp.

6.2.3.3 indexOfZeroElement()

```
template<typename real_t >
bool QMatrix< real_t >::indexOfZeroElement (
    unsigned int row_index,
    unsigned int column_index ) [private]
```

Checks if the row index i and the column index j belong to a zero element of the Q matrix.

Parameters

<i>row_index</i>	Row index i
<i>column_index</i>	Column index j

Returns

true if i,j are indices of zero elements in a Q matrix
false if i,j are indices of non zero elements in a Q matrix

Definition at line 52 of file Q_Matrix.cpp.

6.2.3.4 multiply()

```
template<typename real_t >
void QMatrix< real_t >::multiply (
    real_t * b,
    real_t * x )
```

Multiplies the Q matrix with the column vector b and stores the result in the column vector x.

Parameters

<i>b</i>	
<i>x</i>	

Definition at line 132 of file Q_Matrix.cpp.

6.2.3.5 setElement()

```
template<typename real_t >
void QMatrix< real_t >::setElement (
    unsigned int row_index,
    unsigned int column_index,
    real_t value )
```

Set the value of the i,j th element of the Q Matrix.

Parameters

<i>row_index</i>	Row index i
<i>column_index</i>	Column index j
<i>value</i>	Value to be set at the i,j th position

Definition at line 80 of file Q_Matrix.cpp.

The documentation for this class was generated from the following files:

- [include/qrsolver/Q_Matrix.hpp](#)
- [src/qrsolver/Q_Matrix.cpp](#)

6.3 QRSolver< real_t > Class Template Reference

Class to implement QR factorization algorithm for solving matrix equations of the $A \cdot x = b$ where A is a $N \times N$ tridiagonal matrix and x and b are $N \times 1$ vectors.

```
#include <QR_Solver.hpp>
```


Public Member Functions

- [QRSolver](#) (unsigned int **N**)
Construct a new [QRSolver](#) object.
- [~QRSolver](#) ()
Destroy the [QRSolver](#) object.
- void [setEquation](#) (unsigned int index, real_t e, real_t f, real_t g, real_t b)
Set up equation represented by i th row of the matrix equation $ex_{i-1} + fx_i + gx_{i+1} = b$.
- void [setEquationFirstRow](#) (real_t f, real_t g, real_t b)
Set up equation represented by the first row of the matrix equation $fx_i + gx_{i+1} = b$.
- void [setEquationLastRow](#) (real_t e, real_t f, real_t b)
Set up equation represented by the last row of the matrix equation $ex_{i-1} + fx_i = b$.
- void [printMatrixEquation](#) ()
Prints the matrix A and vector b .
- void [printQRMatrices](#) ()
Prints the factorized matrices $Q \cdot R$.
- void [getSolution](#) (real_t *x)
Finds the solution to matrix equation and saves it to array x .

Private Member Functions

- void [QRFactorize](#) ()
Factorizes the tridiagonal A matrix stored in R to $Q \cdot R$.

Private Attributes

- [QMatrix< real_t > Q](#)
 Q matrix for QR Factorization
- [RMatrix< real_t > R](#)
 R matrix for QR Factorization
- const unsigned int **N**
Number of rows N of the matrix A .
- real_t * **b**
One dimensional array to store $N \times N$ vector b .
- unsigned int **k**
Iterator.

6.3.1 Detailed Description

```
template<typename real_t>
class QRSolver< real_t >
```

Class to implement QR factorization algorithm for solving matrix equations of the $A \cdot x = b$ where A is a $N \times N$ tridiagonal matrix and x and b are $N \times 1$ vectors.

Template Parameters

<i>real</i>	
<i>_t</i>	

Definition at line 32 of file QR_Solver.hpp.

6.3.2 Constructor & Destructor Documentation

6.3.2.1 QRSolver()

```
template<typename real_t >
QRSolver< real_t >::QRSolver (
    unsigned int N )
```

Construct a new [QRSolver](#) object.

Parameters

N	Size of the matrix equations
-----	------------------------------

Definition at line 20 of file QR_Solver.cpp.

6.3.3 Member Function Documentation

6.3.3.1 getSolution()

```
template<typename real_t >
void QRSolver< real_t >::getSolution (
    real_t * x )
```

Finds the solution to matrix equation and saves it to array x .

Parameters

x	Array to store the solution of the matrix equation
-----	--

Definition at line 154 of file QR_Solver.cpp.

6.3.3.2 printMatrixEquation()

```
template<typename real_t >
void QRSolver< real_t >::printMatrixEquation
```

Prints the matrix A and vector b .

To be used before QR factorization is performed in `getSolution`

Definition at line 94 of file `QR_Solver.cpp`.

6.3.3.3 printQRMatrices()

```
template<typename real_t >
void QRSolver< real_t >::printQRMatrices
```

Prints the factorized matrices $Q \cdot R$.

To be used after QR factorization is performed in `getSolution`

Definition at line 140 of file `QR_Solver.cpp`.

6.3.3.4 setEquation()

```
template<typename real_t >
void QRSolver< real_t >::setEquation (
    unsigned int index,
    real_t e,
    real_t f,
    real_t g,
    real_t b )
```

Set up equation represented by i th row of the matrix equation $ex_{i-1} + fx_i + gx_{i+1} = b$.

Parameters

<i>index</i>	<i>i</i>
<i>e</i>	Coefficient to x_{i-1}
<i>f</i>	Coefficient to x_i
<i>g</i>	Coefficient to x_{i+1}
<i>b</i>	Constant

Definition at line 39 of file `QR_Solver.cpp`.

6.3.3.5 setEquationFirstRow()

```
template<typename real_t >
void QRSolver< real_t >::setEquationFirstRow (
    real_t f,
    real_t g,
    real_t b )
```

Set up equation represented by the first row of the matrix equation $fx_i + gx_{i+1} = b$.

Parameters

f	Coefficient to x_i
g	Coefficient to x_{i+1}
b	Constant

Definition at line 60 of file QR_Solver.cpp.

6.3.3.6 setEquationLastRow()

```
template<typename real_t >
void QRSolver< real_t >::setEquationLastRow (
    real_t e,
    real_t f,
    real_t b )
```

up equation represented by the last row of the matrix equation $ex_{i-1}fx_i = b$

Parameters

e	Coefficient to x_{i-1}
f	Coefficient to x_i
b	Constant

Definition at line 77 of file QR_Solver.cpp.

6.3.4 Member Data Documentation**6.3.4.1 R**

```
template<typename real_t >
RMatrix<real_t> QRSolver< real_t >::R [private]
```

R matrix for QR Factorization

The R matrix also serves as the initial tridiagonal A matrix to save memory and more important reduce redundant memory copy operations

Definition at line 48 of file QR_Solver.hpp.

The documentation for this class was generated from the following files:

- include/qrsolver/QR_Solver.hpp
- src/qrsolver/QR_Solver.cpp

6.4 RMatrix< real_t > Class Template Reference

Class to implement a memory efficient $N \times N$ R matrix.

```
#include <R_Matrix.hpp>
```

Public Member Functions

- [RMatrix](#) (unsigned int n)
Construct a new R Matrix.
- [~RMatrix](#) ()
Destroy the R Matrix.
- [real_t getElement](#) (unsigned int row_index, unsigned int column_index)
Get the i,j th element of R Matrix.
- void [setElement](#) (unsigned int row_index, unsigned int column_index, real_t value)
Set the value of the i,j th element of R Matrix.
- void [printMatrix](#) ()
Prints the R Matrix in form of a 2D array.
- void [print](#) ()
Prints the R Matrix in form of a flattened array.

Private Member Functions

- unsigned int [getIndex](#) (unsigned int row_index, unsigned int column_index)
Get the index of the i,j th element of R Matrix in the flattened array.
- bool [indexOfZeroElement](#) (unsigned int row_index, unsigned int column_index)
Checks if the row index i and the column index j belong to a zero element of the R matrix.

Private Attributes

- [real_t * array](#)
*Flattened array of size $4 * N$ to represent R matrix of size $N \times N$.*
- const unsigned int [N](#)
Size of main diagonal of the $N \times N$ R Matrix.

6.4.1 Detailed Description

```
template<typename real_t>
class RMatrix< real_t >
```

Class to implement a memory efficient $N \times N$ R matrix.

The class is specifically built for implementation in a QR factorization algorithm for solving matrix equations of the form $A \cdot x = b$. The QR algo converts a normal tridiagonal matrix (a matrix with non zero entries only at indices $(i, i - 1)$, (i, i) and $(i, i + 1)$) to an upper tridiagonal matrix (a matrix with non zero entries only at indices (i, i) , $(i, i + 1)$ and $(i, i + 2)$). Thus only indices $(i, i - 1)$, (i, i) , $(i, i + 1)$ and $(i, i + 2)$ are stored in memory for this matrix

Definition at line 30 of file R_Matrix.hpp.

6.4.2 Constructor & Destructor Documentation

6.4.2.1 RMatrix()

```
template<typename real_t >
RMatrix< real_t >::RMatrix (
    unsigned int n )
```

Construct a new R Matrix.

Parameters

<i>n</i>	Size of main diagonal of the $N \times N$ R Matrix
----------	--

Definition at line 18 of file R_Matrix.cpp.

6.4.2.2 ~RMatrix()

```
template<typename real_t >
RMatrix< real_t >::~~RMatrix
```

Destroy the R Matrix.

Definition at line 29 of file R_Matrix.cpp.

6.4.3 Member Function Documentation

6.4.3.1 getElement()

```
template<typename real_t >
real_t RMatrix< real_t >::getElement (
    unsigned int row_index,
    unsigned int column_index )
```

Get the i, j th element of R Matrix.

Parameters

<i>row_index</i>	Row index i
<i>column_index</i>	Column index j

Returns

Value of the i,j th element of a R Matrix

Definition at line 36 of file R_Matrix.cpp.

6.4.3.2 getIndex()

```
template<typename real_t >
unsigned int RMatrix< real_t >::getIndex (
    unsigned int row_index,
    unsigned int column_index ) [private]
```

Get the index of the i,j th element of R Matrix in the flattened array.

Parameters

<i>row_index</i>	Row index i
<i>column_index</i>	Column index j

Returns

Returns the index in the the flattened array

Definition at line 109 of file R_Matrix.cpp.

6.4.3.3 indexOfZeroElement()

```
template<typename real_t >
bool RMatrix< real_t >::indexOfZeroElement (
    unsigned int row_index,
    unsigned int column_index ) [private]
```

Checks if the row index i and the column index j belong to a zero element of the R matrix.

Parameters

<i>row_index</i>	
<i>column_index</i>	

Returns

true if i,j are indices of zero elements in a R matrix
false if i,j are indices of non-zero elements in a R matrix

Definition at line 125 of file R_Matrix.cpp.

6.4.3.4 print()

```
template<typename real_t >
void RMatrix< real_t >::print
```

Prints the R Matrix in form of a flattened array.

Definition at line 94 of file R_Matrix.cpp.

6.4.3.5 printMatrix()

```
template<typename real_t >
void RMatrix< real_t >::printMatrix
```

Prints the R Matrix in form of a 2D array.

Definition at line 75 of file R_Matrix.cpp.

6.4.3.6 setElement()

```
template<typename real_t >
void RMatrix< real_t >::setElement (
    unsigned int row_index,
    unsigned int column_index,
    real_t value )
```

Set the value of the i,j th element of R Matrix.

Parameters

<i>row_index</i>	Row index i
<i>column_index</i>	Column index j
<i>value</i>	Value to be set at the i,j th element

Definition at line 54 of file R_Matrix.cpp.

6.4.4 Member Data Documentation

6.4.4.1 array

```
template<typename real_t >
real_t* RMatrix< real_t >::array [private]
```


Flattened array of size $4 * N$ to represent R matrix of size $N \times N$.

Definition at line 93 of file R_Matrix.hpp.

6.4.4.2 N

```
template<typename real_t >
const unsigned int RMatrix< real_t >::N [private]
```

Size of main diagonal of the $N \times N$ R Matrix.

Definition at line 100 of file R_Matrix.hpp.

The documentation for this class was generated from the following files:

- [include/qrsolver/R_Matrix.hpp](#)
- [src/qrsolver/R_Matrix.cpp](#)

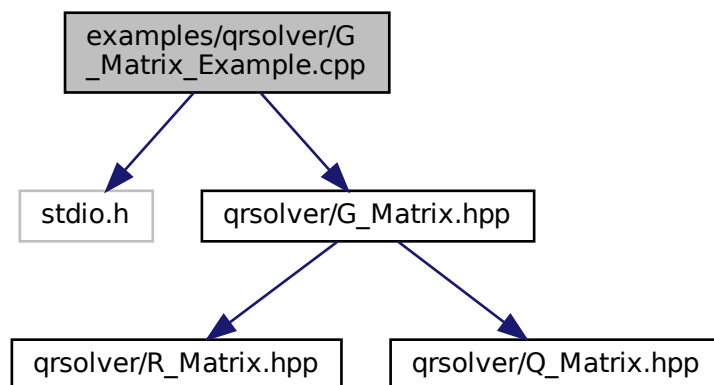
Chapter 7

File Documentation

7.1 examples/qrsolver/G_Matrix_Example.cpp File Reference

Example to test out [GMatrix](#) class.

```
#include <stdio.h>
#include "qrsolver/G_Matrix.hpp"
Include dependency graph for G_Matrix_Example.cpp:
```



Functions

- `int main (int argc, char const *argv[])`

7.1.1 Detailed Description

Example to test out [GMatrix](#) class.

Author

Souritra Garai (souritra.garai@iitgn.ac.in)

Version

0.1

Date

2021-07-01

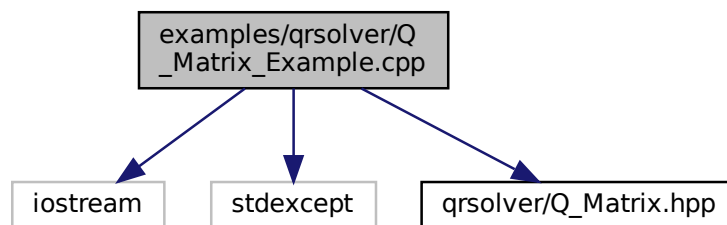
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7.2 examples/qrsolver/Q_Matrix_Example.cpp File Reference

Example to test [QMatrix](#) class.

```
#include <iostream>
#include <stdexcept>
#include "qrsolver/Q_Matrix.hpp"
Include dependency graph for Q_Matrix_Example.cpp:
```



Functions

- `int main (int argc, char const *argv[])`

7.2.1 Detailed Description

Example to test [QMatrix](#) class.

Author

Souritra Garai (souritra.garai@iitgn.ac.in)

Version

0.1

Date

2021-06-27

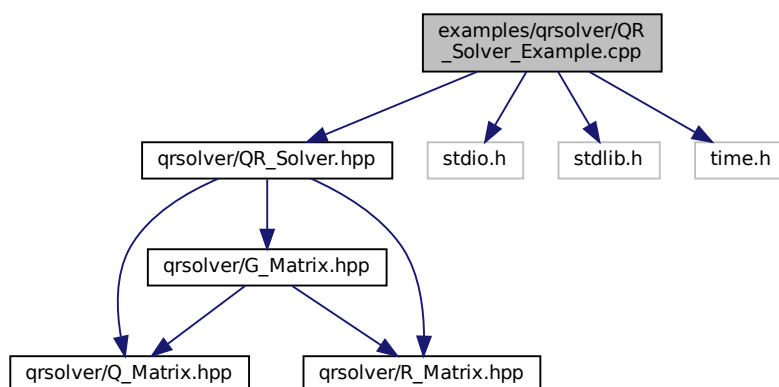
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7.3 examples/qrsolver/QR_Solver_Example.cpp File Reference

Example cpp file to test out [QRSolver](#) class.

```
#include "qrsolver/QR_Solver.hpp"
#include <stdio.h>
#include <stdlib.h>
#include <time.h>
Include dependency graph for QR_Solver_Example.cpp:
```



Functions

- `int main (int argc, char const *argv[])`

7.3.1 Detailed Description

Example cpp file to test out [QRSolver](#) class.

Author

Souritra Garai (souritra.garai@iitgn.ac.in)

Version

0.1

Date

2021-06-24

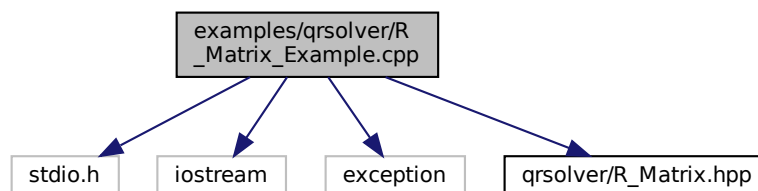
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7.4 examples/qrsolver/R_Matrix_Example.cpp File Reference

An example cpp program to test the [RMatrix](#) class.

```
#include <stdio.h>
#include <iostream>
#include <exception>
#include "qrsolver/R_Matrix.hpp"
Include dependency graph for R_Matrix_Example.cpp:
```



Functions

- `int main (int argc, char const *argv[])`

7.4.1 Detailed Description

An example cpp program to test the [RMatrix](#) class.

Author

Souritra Garai (you@domain.com)

Version

0.1

Date

2021-06-24

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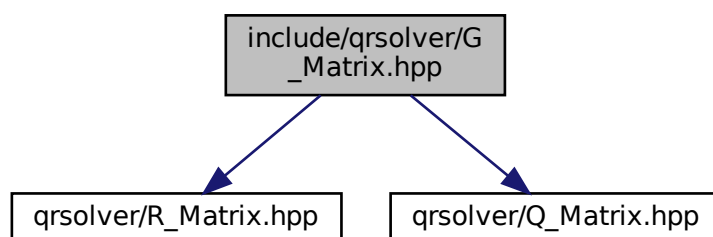
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7.5 include/qrsolver/G_Matrix.hpp File Reference

This header serves the definition of an implementation of Givens' Rotation matrix. The rotation matrix is used to solve matrix equations through QR factorization method, particularly tridiagonal matrix equation.

```
#include "qrsolver/R_Matrix.hpp"
#include "qrsolver/Q_Matrix.hpp"
```

Include dependency graph for G_Matrix.hpp:



Classes

- class [GMatrix< real_t >](#)

Class to implement a memory efficient Givens' Rotation Matrix that can vanish the element $a_{k+1,k}$ of a matrix A .

7.5.1 Detailed Description

This header serves the definition of an implementation of Givens' Rotation matrix. The rotation matrix is used to solve matrix equations through QR factorization method, particularly tridiagonal matrix equation.

Author

Souritra Garai (souritra.garai@iitgn.ac.in)

Version

0.1

Date

2021-06-28

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7.6 include/qrsolver/Q_Matrix.hpp File Reference

This header file defines a class for memory efficient implementation of Q matrix used for QR factorisation of tridiagonal matrix using Givens rotation matrix.

Classes

- class [QMatrix< real_t >](#)

Class to implement a memory efficient model of $N \times N$ Q Matrix.

7.6.1 Detailed Description

This header file defines a class for memory efficient implementation of Q matrix used for QR factorisation of tridiagonal matrix using Givens rotation matrix.

Author

Souritra Garai (souritra.garai@iitgn.ac.in)

Version

0.1

Date

2021-06-25

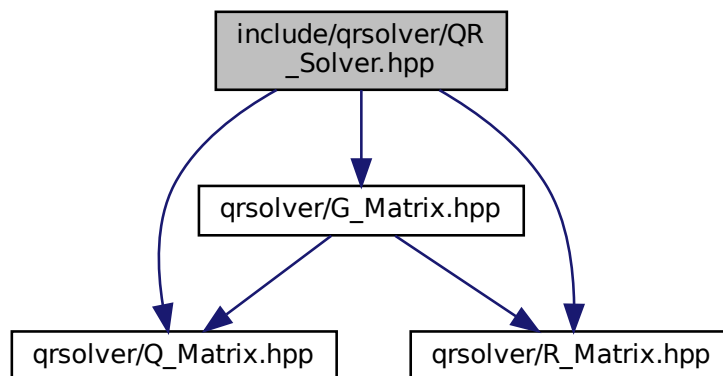
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7.7 include/qrsolver/QR_Solver.hpp File Reference

This header file defines a class for solving 2D matrix equations of the form $A \cdot x = b$ (where A is an $N \times N$ matrix and x and b are $N \times 1$ vectors) using QR factorization technique.

```
#include "qrsolver/Q_Matrix.hpp"
#include "qrsolver/R_Matrix.hpp"
#include "qrsolver/G_Matrix.hpp"
Include dependency graph for QR_Solver.hpp:
```



Classes

- class `QRSolver< real_t >`

Class to implement QR factorization algorithm for solving matrix equations of the $A \cdot x = b$ where A is a $N \times N$ tridiagonal matrix and x and b are $N \times 1$ vectors.

7.7.1 Detailed Description

This header file defines a class for solving 2D matrix equations of the form $A \cdot x = b$ (where A is an $N \times N$ matrix and x and b are $N \times 1$ vectors) using QR factorization technique.

Author

Souritra Garai (souritra.garai@iitgn.ac.in)

Version

0.1

Date

2021-06-23

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7.8 include/qrsolver/R_Matrix.hpp File Reference

This header file defines a class for memory efficient implementation of R matrix used for QR factorisation of tridiagonal matrix.

Classes

- class [RMatrix< real_t >](#)
Class to implement a memory efficient $N \times N$ R matrix.

7.8.1 Detailed Description

This header file defines a class for memory efficient implementation of R matrix used for QR factorisation of tridiagonal matrix.

Author

Souritra Gari (souritra.garai@iitgn.ac.in)

Version

0.1

Date

2021-06-24

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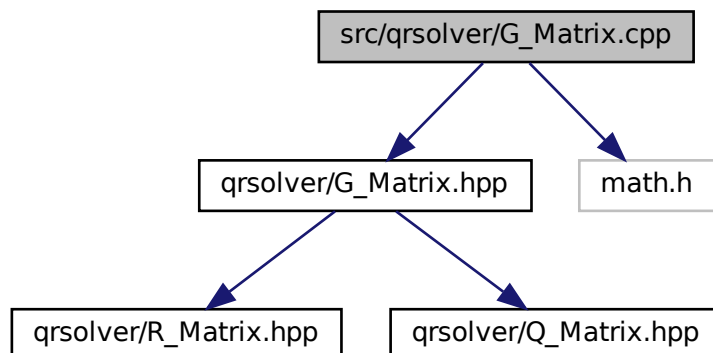
7.9 src/qrsolver/G_Matrix.cpp File Reference

Member function definitions for [GMatrix](#) class.

```
#include "qrsolver/G_Matrix.hpp"
```

```
#include <math.h>
```

Include dependency graph for G_Matrix.cpp:



7.9.1 Detailed Description

Member function definitions for [GMatrix](#) class.

Author

Souritra Garai (souritra.garai@iitgn.ac.in)

Version

0.1

Date

2021-07-01

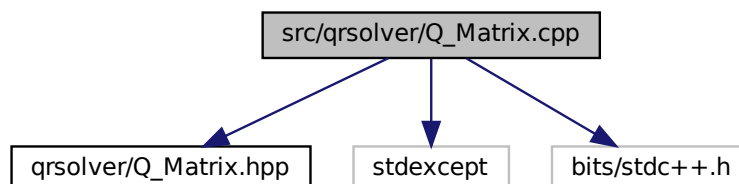
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7.10 src/qrsolver/Q_Matrix.cpp File Reference

Member function definitions for [QMatrix](#) class.

```
#include "qrsolver/Q_Matrix.hpp"
#include <stdexcept>
#include <bits/stdc++.h>
Include dependency graph for Q_Matrix.cpp:
```



7.10.1 Detailed Description

Member function definitions for [QMatrix](#) class.

Author

Souritra Garai (souritra.garai@iitgn.ac.in)

Version

0.1

Date

2021-06-25

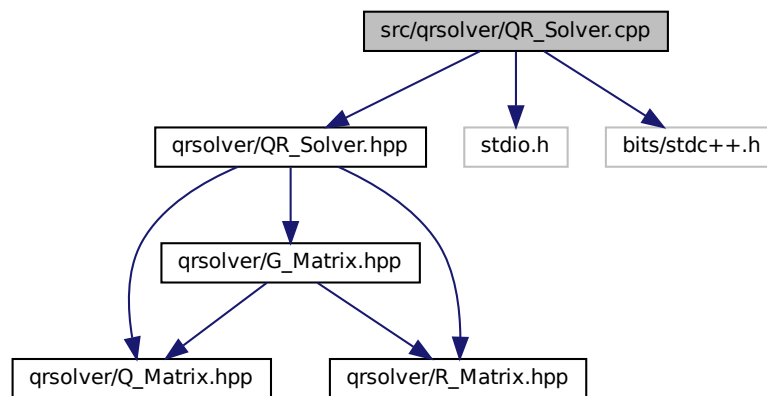
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7.11 src/qrsolver/QR_Solver.cpp File Reference

Member function definitions for [QRSolver](#) class.

```
#include "qrsolver/QR_Solver.hpp"  
#include <stdio.h>  
#include <bits/stdc++.h>  
Include dependency graph for QR_Solver.cpp:
```



7.11.1 Detailed Description

Member function definitions for [QRSolver](#) class.

Author

Souritra Garai (souritra.garai@iitgn.ac.in)

Version

0.1

Date

2021-07-01

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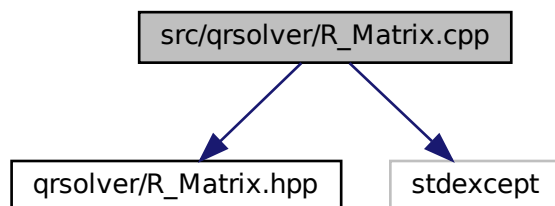
7.12 src/qrsolver/R_Matrix.cpp File Reference

Member function definitions for [RMatrix](#) class.

```
#include "qrsolver/R_Matrix.hpp"
```

```
#include <stdexcept>
```

Include dependency graph for R_Matrix.cpp:



7.12.1 Detailed Description

Member function definitions for [RMatrix](#) class.

Author

Souritra Gari (souritra.garai@iitgn.ac.in)

Version

0.1

Date

2021-06-24

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