Bayesian Statistics

Sunday, 13 September 2020

Model:
$$X_{n} = N(\theta, 0^{2})$$

$$\Rightarrow f(x_{n}|\theta) \propto Q - \frac{(x_{n}-\theta)^{2}}{20^{2}}$$

Probably: $\theta \sim N(\mu, \frac{\sigma^{2}}{n_{0}})$

$$\Rightarrow f(\theta) \propto Q - \frac{(\theta - \mu)^{2}}{2\frac{\sigma^{2}}{n_{0}}}$$

Posterby: $\rho(\theta|X_{1}, X_{n}) \propto \rho(X_{1}, X_{n}|\theta) \rho(\theta)$

$$\propto Q - \frac{\frac{2}{2}(x_{n}-\theta)^{2}}{2\sigma^{2}} Q - \frac{\frac{(\theta - \mu)^{2}}{n_{0}}}{\frac{2\sigma^{2}}{n_{0}}}$$

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$$\sim Q - \frac{1}{2\sigma^{2}} (n_{0}+n_{0})\theta^{2} - 2(n_{0}+n_{0})\theta)$$

$$\sim Q - \frac{1}{2\sigma^{2}} (n_{0}+n_{0})\theta^{2} - 2(n_{0}+n_{0})\theta)$$

$$\sim Q - \frac{(n_{0}+n_{0})}{2\sigma^{2}} (n_{0}+n_{0})\theta^{2} - 2(n_{0}+n_{0})\theta)$$

$$\sim Q - \frac{(n_{0}+n_{0})}{2\sigma^{2}} (n_{0}+n_{0})\theta^{2}$$

$$\sim Q - \frac{(n_{0}+n_{0})}{2\sigma^{2}} (n_{0}+n_{0})\theta$$

 $\sqrt{N+N^{\circ}}, \frac{\sqrt{N+N^{\circ}}}{\sqrt{N+N^{\circ}}}$