Week 1 Introduction and language model

Introduction to NLP

What is NLP?

- Computers using natural language as input (understanding) and/or output (generation)
- Key applications: machine translation, information extraction, text summarization, dialogue systems

Basic NLP problems

- Tagging (part-of-speech tagging, named entity recognition)
- Parsing

Why is NLP hard?

Ambiguity (acoustic level 声学、 semantic level语义、 syntactic level句法、 discourse level 语 境)

What will this course be about?

- NLP sub-problems: part-speech tagging, parsing, word-sense disambiguation, etc.
- Machine learning techniques: probabilistic context-free grammars, hidden markov models, estimation / smoothing techniques, the EM algorithm, log-liner models, etc.
- Applications: information extraction, machine translation, natural language interfaces.

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- Language modeling, smoothed estimation
- Tagging, hidden Markov models
- Statistical parsing
- Machine translations
- Log-linear model, discriminative methods
- Semi-supervised and unsupervised learning for NLP

Books

- Comprehensive notes for course: http://www.cs.columbia.edu/~mcollins
- Jurafsky and Martin: Speech and Language Processing (2nd edition)

二、The language modeling problem

The language modeling problem

• Traing set

 ${\cal V}$: finite set of vocabulary

 \mathcal{V}^{\dagger} : an infinite set of strings (quite large, may have hundreds of billions of words nowdays)

Task

to learn a probability distribution p that satisfies

$$\sum_{x \in \mathcal{V}^\dagger} p(x) = 1, p(x) \geq 0 \quad \textit{for all } x \in \mathcal{V}^\dagger$$

- Why do we need to do this:
 - Speech recognition was the original motivation. (Other applications: optical character recognition, handwriting recognition, machine translations)
 - The estimation techniques developed for this problem is VERY useful for other problems in NLP.

A naive method

We have N training sentences, for any sentence $x_1 cdots x_n$, $c(x_1 cdots x_n)$ is the count of the sentence in training data, then a naive estimate:

$$p(x_1 \ldots x_n) = rac{c(x_1 \ldots x_n)}{N}$$

Deficiencies:

probability of sentences that not seen in training data will be 0.

has no ability to generate the probability of new sentences.

Markov process

Definition

A sequence of random variables X_1, X_2, \ldots, X_n , each random variables can take any value in a finite set \mathcal{V} , then to model

$$P(X_1 = x_1, X_2 = x_2, \dots, X_n = x_n)$$

we can get $|\mathcal{V}|^n$ different sequences in this model.

• First-Order Markov process

$$egin{aligned} P(X_1 = x_1, X_2 = x_2, \dots, X_n = x_n) \ &= P(X_1 = x_1) \prod_{i=2}^n P(X_i = x_i | X_1 = x_1, \dots X_{i-1} = x_{i-1}) \end{aligned}$$

the first-order Markov assumption: for any $i \in \{2...n\}$, and for any $x_1 \ldots x_n$,

$$P(X_i = x_i | X_1 = x_1, \dots X_{i-1} = x_{i-1}) = P(X_i = x_i | X_{i-1} = x_{i-1})$$

then

$$egin{aligned} P(X_1 = x_1, X_2 = x_2, \dots, X_n = x_n) \ &= P(X_1 = x_1) \prod_{i=2}^n P(X_i = x_i | Xi - 1 = x_{i-1}) \end{aligned}$$

Second-Order Markov process

$$egin{aligned} &P(X_1=x_1,X_2=x_2,\ldots,X_n=x_n)\ &=P(X_1=x_1) imes P(X_2=x_2|X_1=x_1)\ & imes \prod_{i=3}^n P(X_i=x_i|X_{i-2}=x_{i-2},X_{i-1}=x_{i-1})\ &=\prod_{i=1}^n P(X_i=x_i|X_{i-2}=x_{i-2},X_{i-1}=x_{i-1}) \end{aligned}$$

Assume undefined , where * is a special "start" symbol. And define $X_n = \mathsf{STOP}$ where STOP is a special symbol.

Trigram models

- A trigram language model consists of:
 - \circ A finite set $\mathcal V$
 - A parameter q(w|u,v) for each trigram u,v,w such that $w\in\mathcal{V}\cup\{\mathsf{STOP}\}$, and $u,v\in\mathcal{V}\cup\{*\}$
- For any sentence $x_1\cdots x_n$ where $x_i\in \mathcal{V}$ for $i=1\cdots (n-1)$, and $x_n=\mathsf{STOP}$, the probability of the sentence under the trigram language model is

$$p(x_1\cdots x_n) = \prod_{i=1}^n q(x_i|x_{i-2},x_{i-1})$$

where $x_0 = x_{-1} = *$.

Evaluating language models: perplexity

ullet For test data s_1, s_2, \cdots, s_m , define perplexity as

$$\mathsf{Perplexity} = 2^{-l} \quad \mathsf{where} \quad l = \frac{1}{M} \sum_{i=1}^m \log p(s_i)$$

where M is the total number of words in the test data, and the log base is 2.

The lower quantity of perplexity is, the better the model is.

Intuition about perplexity

Vocabulary is ${\mathcal V}$, and $N=|{\mathcal V}|+1$, and model predicts

$$q(w|u,v)=rac{1}{N}$$

for all $w \in \mathcal{V} \cup \{\mathsf{STOP}\}$, and all $u, v \in \mathcal{V} \cup \{*\}$, we can get perplexity equals to N.

Estimation techniques:

Maximum likelihood estimate

$$q(w_i|w_{i-2},w_{i-1}) = rac{\mathsf{Count}(w_{i-2},w_{i-1},w_i)}{\mathsf{Count}(w_{i-2},w_{i-1})}$$

Deficiencies:

- \circ Huge number of parameters: vocabulary size $|\mathcal{V}|=N$,then there are N^3 parameters in the model.
- Numerator and denominator may be 0, which will lead to estimates being unrealistically low or ill defined.
- Liner interpolation
 - o Trigram maximum-likelihood estimate

$$q_{\mathsf{ML}}(w_i|w_{i-2},w_{i-1}) = rac{\mathsf{Count}(w_{i-2},w_{i-1},w_i)}{\mathsf{Count}(w_{i-2},w_{i-1})}$$

Bigram maximum-likelihood estimate

$$q_{\mathsf{ML}}(w_i|w_{i-1}) = rac{\mathsf{Count}(w_{i-1},w_i)}{\mathsf{Count}(w_{i-1})}$$

Unigram maximun-likelihood estimate

$$q_{\mathsf{ML}}(w_i) = rac{\mathsf{Count}(w_i)}{\mathsf{Count}()}$$

o Then,

$$egin{aligned} q(w_i|w_{i-2},w_{i-1}) &= & \lambda_1 imes q_{\mathsf{ML}}(w_i|w_{i-2},w_{i-1}) \ &+ \lambda_2 imes q_{\mathsf{ML}}(w_i|w_{i-1}) \ &+ \lambda_3 imes q_{\mathsf{ML}}(w_i) \end{aligned}$$

where $\lambda_1 + \lambda_2 + \lambda_3 = 1$, and $\lambda_i > 0$ for all i .

- Estimate the value of λ
 - Hold out part of training data set as validation data
 - Define $c'(w_1, w_2, w_3)$ to be the number of times the trigram (w_1, w_2, w_3) is seen in validation set
 - Choose to maximize:

$$L(\lambda_1,\lambda_2,\lambda_3) = \sum_{w_1,w_2,w_3} c'(w_1,w_2,w_3) \log q(w_3|w_1,w_2)$$

such that $\lambda_1 + \lambda_2 + \lambda_3 = 1$, and $\lambda_i \geq 0$ for all i .

• Allowing the λ 's to vary, define a function Π that partitions histories

$$\Pi(w_{i-2},w_{i-1}) = egin{cases} 1, & ext{if } ext{Count}(w_{i-1},w_{i-2}) = 0 \ 2, & ext{if } 1 \leq ext{Count}(w_{i-1},w_{i-2}) \leq 2 \ 3, & ext{if } 3 \leq ext{Count}(w_{i-1},w_{i-2}) \leq 5 \ 4, & ext{Otherwise} \end{cases}$$

Introducing a dependence of the λ 's on the partition:

$$egin{aligned} q(w_i|w_{i-2},w_{i-1}) &= & \lambda_1^{\Pi(w_{i-2},w_{i-1})} imes q_{\mathsf{ML}}(w_i|w_{i-2},w_{i-1}) \ &+ \lambda_2^{\Pi(w_{i-2},w_{i-1})} imes q_{\mathsf{ML}}(w_i|w_{i-1}) \ &+ \lambda_3^{\Pi(w_{i-2},w_{i-1})} imes q_{\mathsf{ML}}(w_i) \end{aligned}$$

where
$$\lambda_1^{\Pi(w_{i-2},w_{i-1})} + \lambda_2^{\Pi(w_{i-2},w_{i-1})} + \lambda_3^{\Pi(w_{i-2},w_{i-1})} = 1$$
 , and $\lambda_i^{\Pi(w_{i-2},w_{i-1})} \geq 0$ for all i .

- Discounting methods
 - discount counts: $Count^*(x) = Count(x) 0.5$
 - o miss probability mass:

$$lpha(w_{i-1}) = 1 - \sum_{w} rac{\mathsf{Count}^*(w_{i-1}, w_i)}{\mathsf{Count}(w_{i-1})}$$

- o Katz Back-Off models:
 - A bigram model

Define two sets

$$\mathcal{A}(w_{i-1}) = \{w : \mathsf{Count}(w_{i-1}, w) > 0\}$$

 $\mathcal{B}(w_{i-1}) = \{w : \mathsf{Count}(w_{i-1}, w) = 0\}$

The model

$$q_{BO}(w_i|w_{i-1}) = egin{cases} rac{\mathsf{Count}^*(w_{i-1},w_i)}{\mathsf{Count}(w_{i-1})} & ext{if } w_i \in \mathcal{A}(w_{i-1}) \ & \\ lpha(w_{i-1}) rac{q_{\mathsf{ML}(w_i)}}{\sum_{w \in \mathcal{B}(w_{i-1})} q_{\mathsf{ML}}(w)} & ext{if } w_i \in \mathcal{B}(w_{i-1}) \end{cases}$$

where

$$lpha(w_{i-1}) = 1 - \sum_{w \in \mathcal{A}(w_{i-1})} rac{\mathsf{Count}^*(w_{i-1}, w_i)}{\mathsf{Count}(w_{i-1})}$$

A trigram model

Define two sets:

$$\mathcal{A}(w_{i-2},w_{i-1})=\{w: \mathsf{Count}(w_{i-2},w_{i-1},w)>0\}$$
 $\mathcal{B}(w_{i-2},w_{i-1})=\{w: \mathsf{Count}(w_{i-2},w_{i-1},w)=0\}$

A trigram model is defined in terms of the bigram model:

$$q_{BO}(w_i|w_{i-2},w_{i-1}) = \begin{cases} \frac{\mathsf{Count}^*(w_{i-2},w_{i-1},w_i)}{\mathsf{Count}(w_{i-2},w_{i-1})} & \text{if } w_i \in \mathcal{A}(w_{i-2},w_{i-1}) \\ \\ \alpha(w_{i-2},w_{i-1}) \frac{q_{\mathsf{BO}(w_i|w_{i-1})}}{\sum_{w \in \mathcal{B}(w_{i-2},w_{i-1})} q_{\mathsf{BO}}(w|w_{i-1})} & \text{if } w_i \in \mathcal{B}(w_{i-2},w_{i-1}) \end{cases}$$

where

$$\alpha(w_{i-2},w_{i-1}) = 1 - \sum_{w \in \mathcal{A}(w_{i-2},w_{i-1})} \frac{\mathsf{Count}^*(w_{i-2},w_{i-1},w_i)}{\mathsf{Count}(w_{i-2},w_{i-1})}$$

Summary

- Three steps in deriving the language model probabilities:
 - Expand $p(w_1, w_2 \dots w_n)$ using Chain rule.
 - Make Markov Independence Assumptions.
 - Smooth the estimates using low order counts.

- Other methods to improve language models:
 - "Topic" or "long-range" features.
 - Syntactic models.

Further reading:

C. Shannon. Prediction and entropy of printed English. Bell Systems Technical Journal, 30:50–64, 1951.