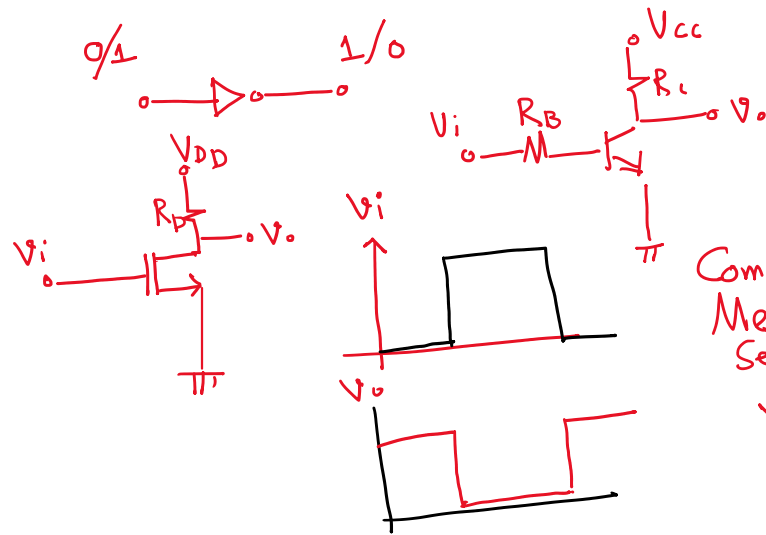
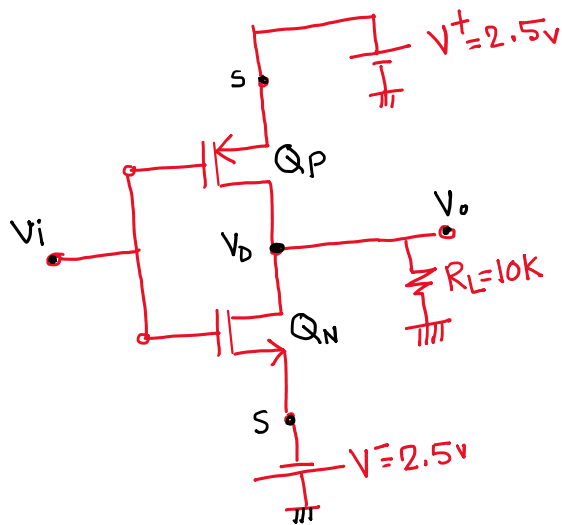
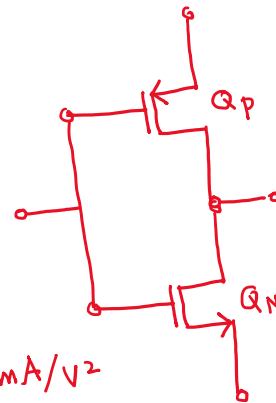


CMOS Inverter Lecture

Monday, December 29, 2025 12:36 PM



CMOS
Complementary
Metal Oxide
Semiconductor
VLSI. EEE
411



$$K_n = K_p = 1 \text{ mA/V}^2$$

$$V_{TN} = -V_{TP} = 1 \text{ V}$$

$$V_I = 0 \text{ V}, +2.5 \text{ V}, -2.5 \text{ V}$$

Case I. $V_I = 0 \text{ V}$

check if ch. is induced or not.

$$Q_p: V_{GS} = V_G - V_S = 0 - 2.5 < V_{TP} \text{ [ch. Ind]}$$

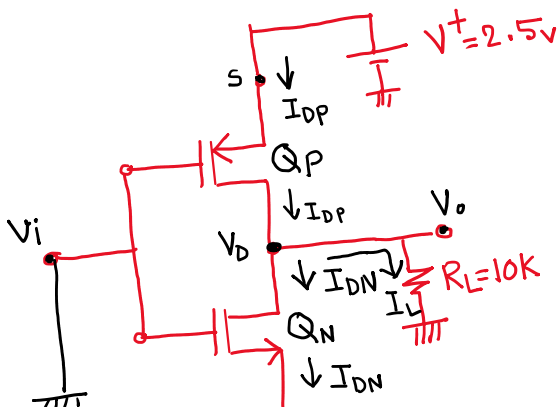
$$Q_n: V_{GS} = V_G - V_S = 0 - (-2.5) = 2.5 \text{ V} > V_{TN} \text{ [ch. Ind]}$$

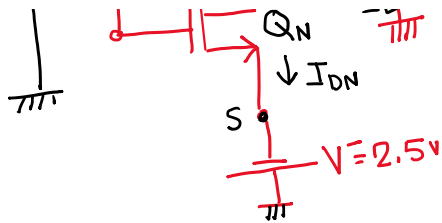
$$Do \ V_{GD} = V_G - V_D = 0 - V_D (?)$$

Assume saturation for both Mosfets

$$Q_n: I_{DN} = K_n (V_{GS} - V_{TN})^2 = 1 (2.5 - 1)^2 = 2.25 \text{ mA}$$

$$Q_p: I_{DP} = K_p (V_{GS} - V_{TP})^2 = 1 (-2.5 + 1)^2 = 2.25 \text{ mA}$$





$$Q_P: I_{DP} = K_P (V_{GS} - V_{TP})^2 = 1(-2.5 + 1)^2 = 2.25 \text{ mA}$$

$$I_{DN} = I_{DP} = 2.25 \text{ mA}$$

$$V_D = V_O = I_L R_L = 0 \text{ V} \rightarrow V_{GD} = 0 - 0 = 0 \text{ V}$$

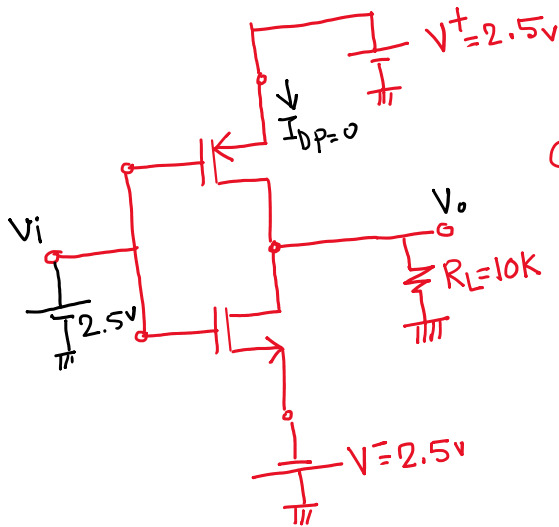
$$\text{KCL @ D: } I_{DP} = I_{DN} + I_L \Rightarrow I_L = 0$$

For Q_N : $V_{GD} = 0 < V_{TN}$ [No ch. exists at drain end]

For Q_P : $V_{GD} = 0 > V_{TP}$ [No ch. exists at drain end]

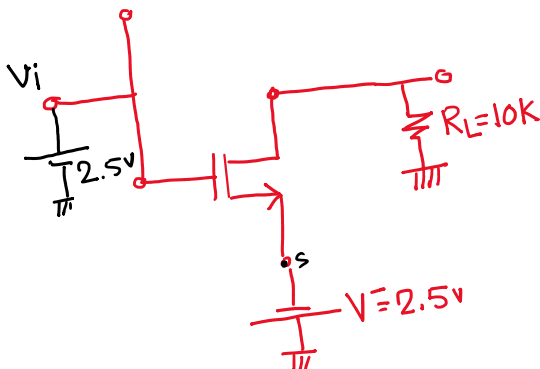
$$V_I = 0 \text{ V} \rightarrow V_O = 0 \text{ V}$$

Case II, $V_I = 2.5 \text{ V}$

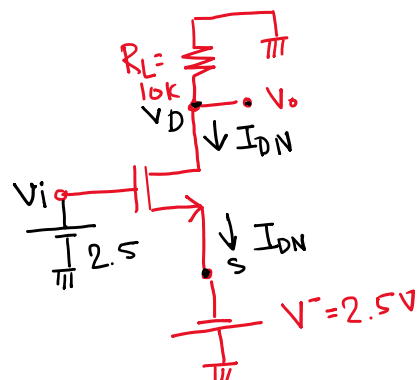


Q_P : $V_{GS} = V_G - V_S = 2.5 - 2.5 = 0 > V_{TP} (-1 \text{ V})$
No ch Ind. \rightarrow cut-off, $I_{DP} = 0$

Q_N : $V_{GS} = V_G - V_S = 2.5 - (-2.5) = 5 > V_{TN}$ [ch. Ind.]



\rightarrow



Triode Region

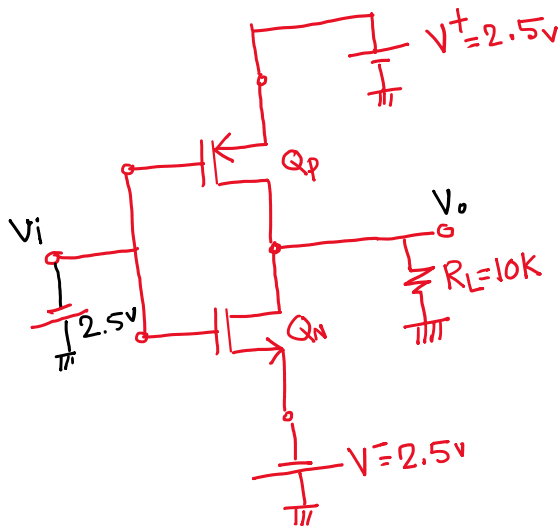
$$I_{DN} = K_n [2(V_{GS} - V_{TN})V_{DS} - V_{DS}^2] = \frac{0 - V_D}{R_L}$$

$$\Rightarrow 1 [2(5-1)(V_D - V_S) - (V_D - V_S)^2] = -\frac{V_D}{R_L}$$

$$\Rightarrow 8(V_D + 2.5) - (V_D + 2.5)^2 = -\frac{V_D}{10}$$

$$V_o = V_D = -2.44 \text{ V}$$

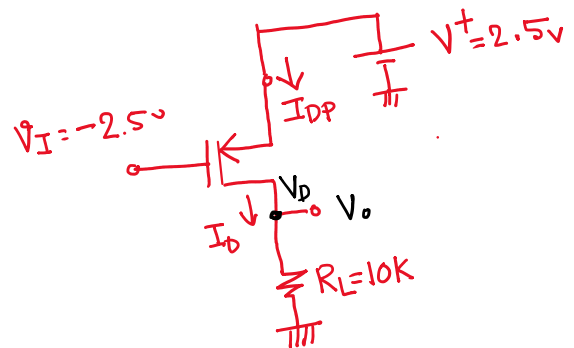
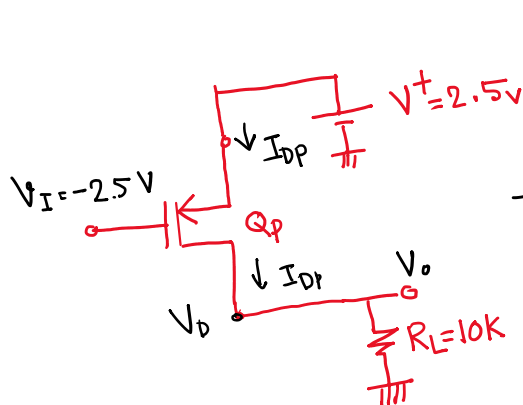
$$V_I = 2.5 \text{ V}, V_o = -2.44 \text{ V}$$



Case III, $V_I = -2.5 \text{ V}$

Q_p : ch. Ind

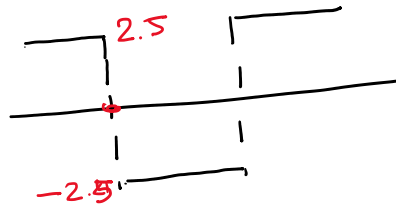
Q_n : Not Ind.



$$I_{DP} = K_p [2(V_{GS} - V_{TP})V_{DS} - V_{DS}^2] = \frac{V_D - 0}{R_L}$$

$$= 1 [2(-5+1)(V_D - V_S) - (V_D - V_S)^2] = \frac{V_D}{10}$$

$$V_D = 2.44 \text{ V}$$



V_I	V_O
$2.5V$	$-2.44V$
$0V$	$0V$
$-2.5V$	2.44