Ch.5 Formulas and operator

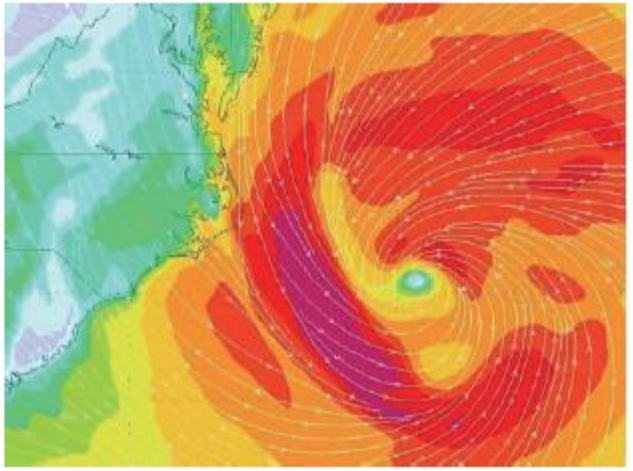
What you will learn in this chapter

* What are formulas and operators ?
* Assignment operation
* Arithmetic operations
* Logical operations
* Relational operations
* Priority and associativity rules

In this chapter, we will look at formulas and operators .

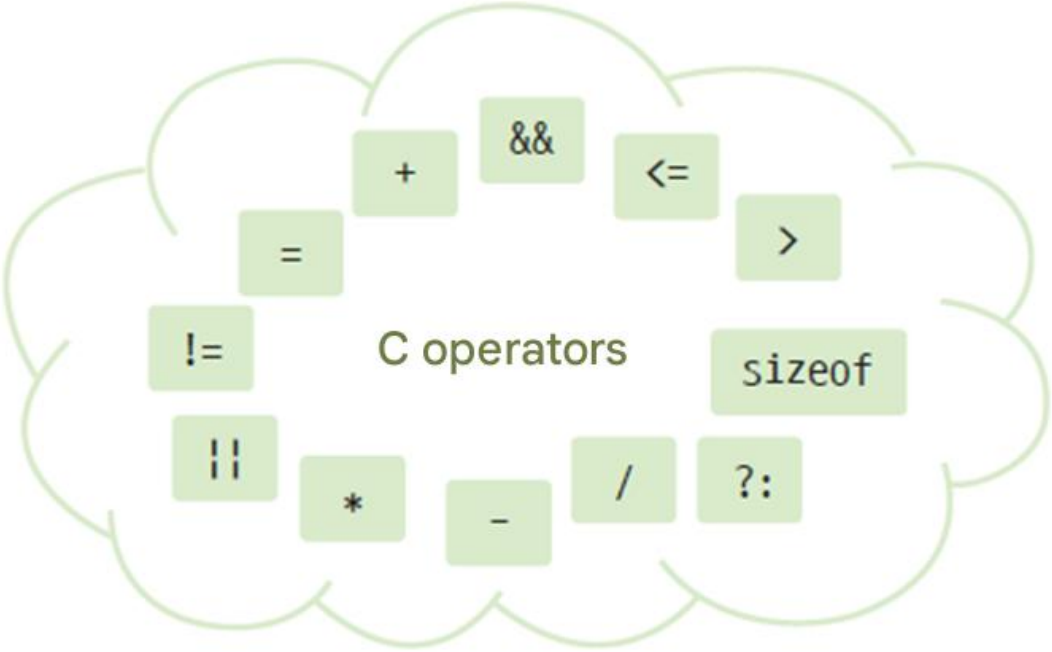
A computer is fundamentally a calculating machine.

The Korea Meteorological Administration uses supercomputers to calculate the weather .

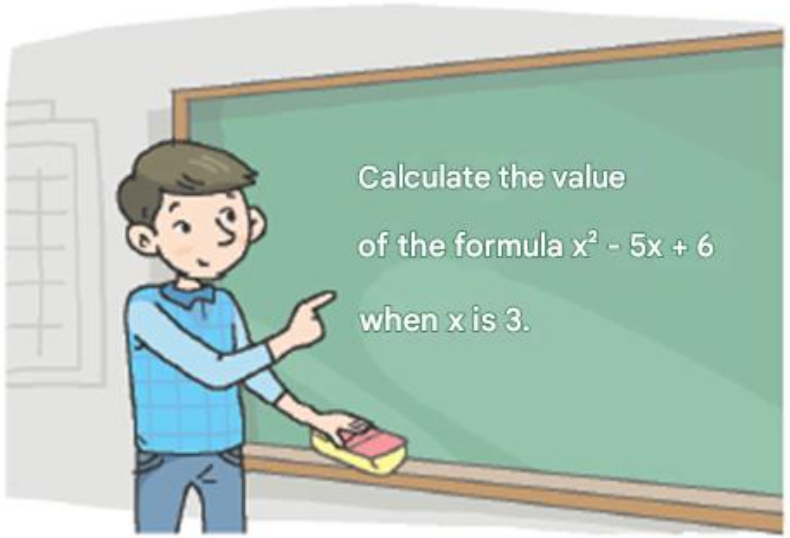


Operators in the C language

- The de facto industry standard
- Modern languages such as Java , C++, Python , and JavaScript use C language operators almost as they are.



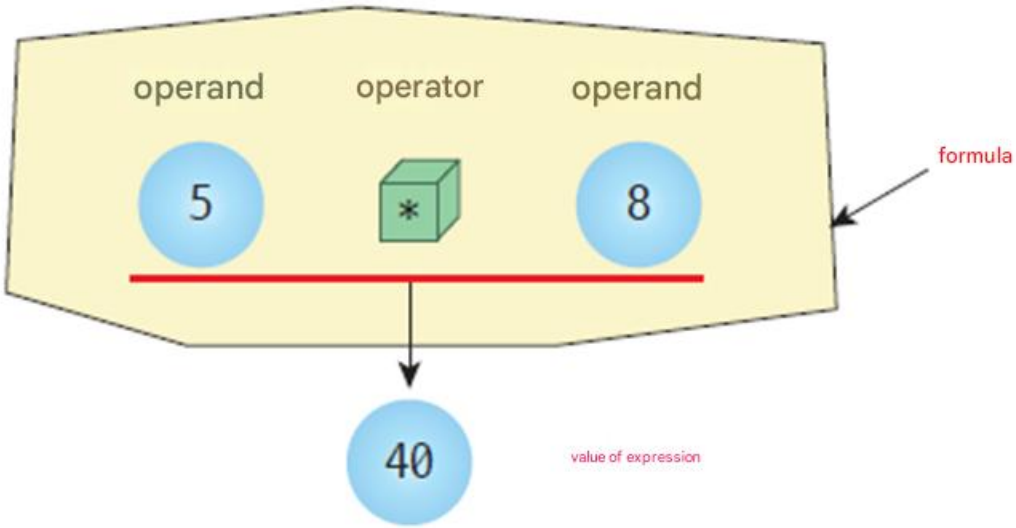
Example of a formula



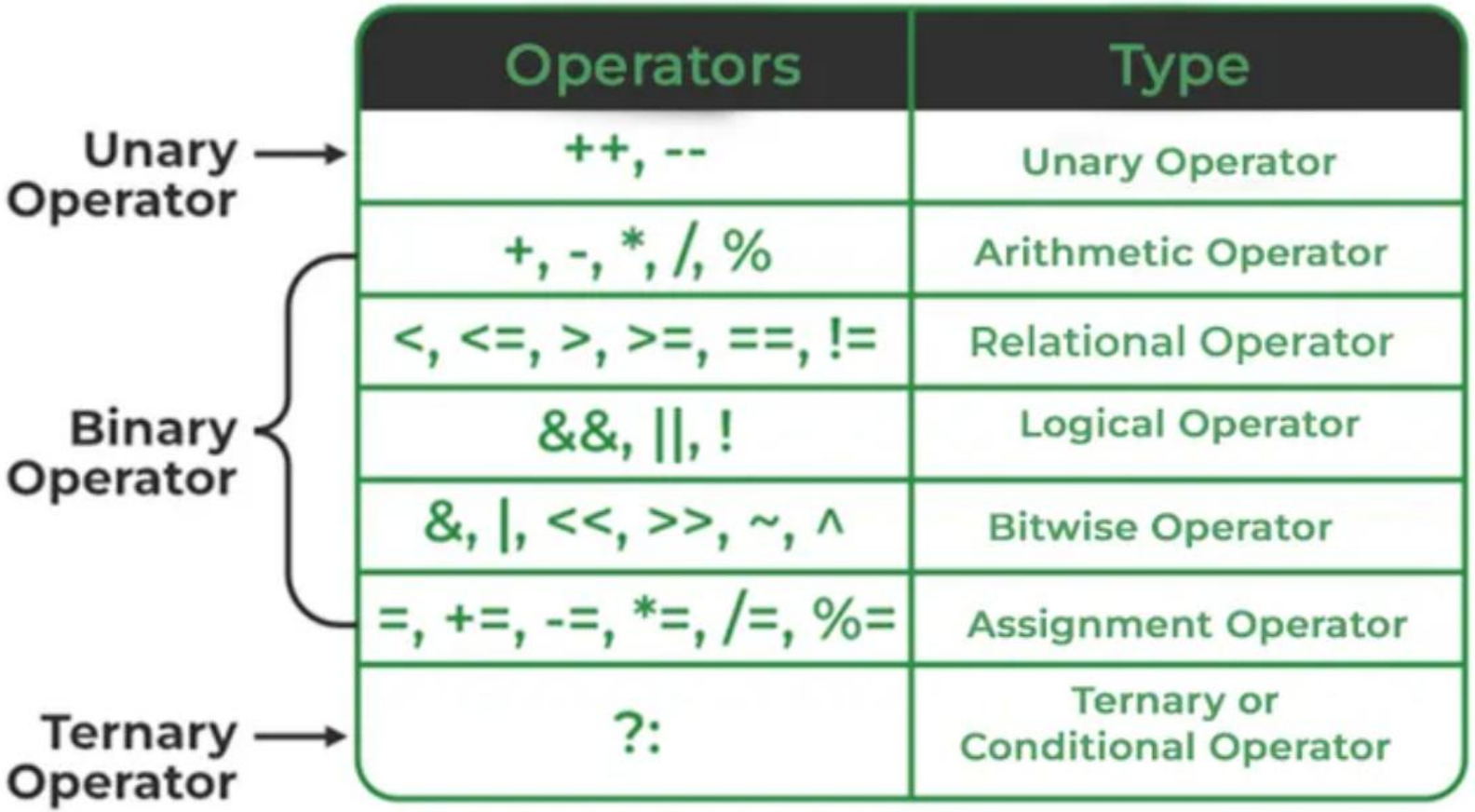

```
int x, y;

x = 3;
y = x*x - 5*x + 6;
printf("%d\n", y);
```

formula

- expression
  - constants , variables , and operators
  - It is divided into operators and operands .



Classification of operators by function



Arithmetic Operators

- Arithmetic Operations : The Most Basic Operations on a Com puter
- Operators that perform basic arithmetic operations such as a ddition , subtraction , multiplication , and division.

operator	sign	Example of use	result
addition	+	7 + 4	11
subtraction	–	7 – 4	3
multiplication	*	7 * 4	28
division	/	7 / 4	1
remain	%	7 % 4	3

Examples of arithmetic operators

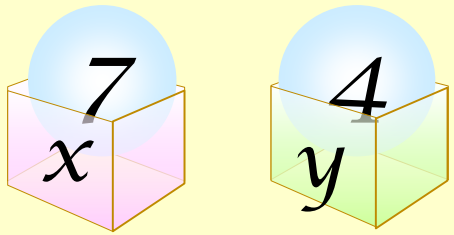
$y=mx+b$	`--> y = m*x + b;`
$y=ax^2+bx+c$	`--> y = a*x*x + b*x + c;`
$m=\frac{x+y+z}{3}$	`--> m = (x+y+z)/3;`

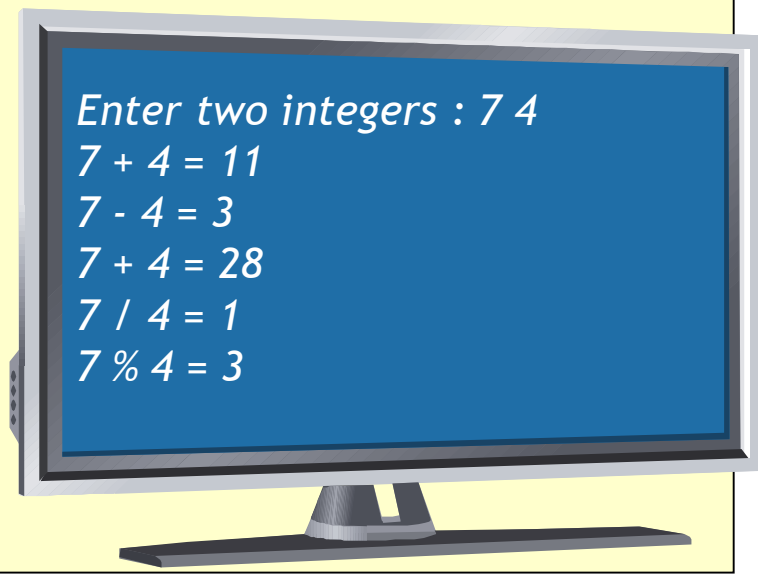
(Note) What is the exponentiation operator ?

C does not have an operator for exponentiation .
Simply multiply the variable twice, like x * x .

Integer arithmetic operations

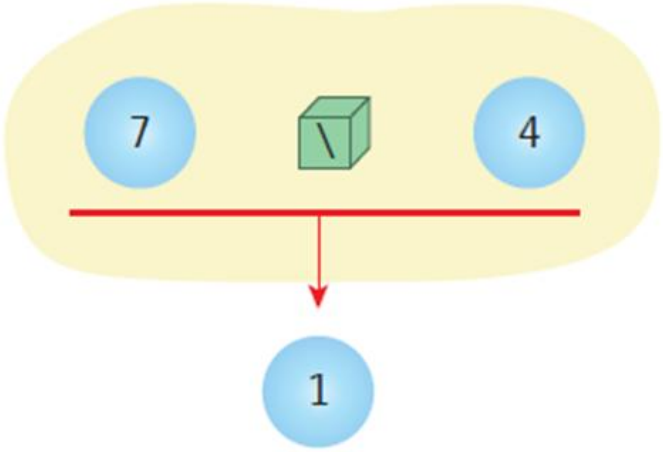
```
#include < stdio.h >

int main(void)
{
      int x, y, result;
      printf ( " Enter two integers : ");
      scanf( "%d %d" , &x, &y);

     result = x + y;
     printf( "%d + %d = %d" , x, y, result);

     result = x - y; // subtraction
     printf( "%d - %d = %d" , x, y, result);
     result = x * y; // multiplication
     printf( "%d + %d = %d" , x, y, result);
     result = x / y; // division
     printf( "%d / %d = %d" , x, y, result);
     result = x % y; // remainder
     printf( "%d %% %d = %d" , x, y, result);
      return 0;
}
```



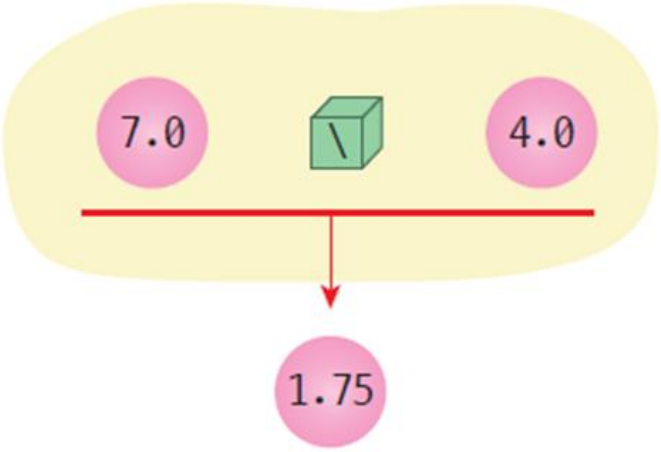


Division operator

- Division between integers produces an integer result, and division between floating-point numbers produces a floating-point value.
- In division between integers, the decimal places are discarded.



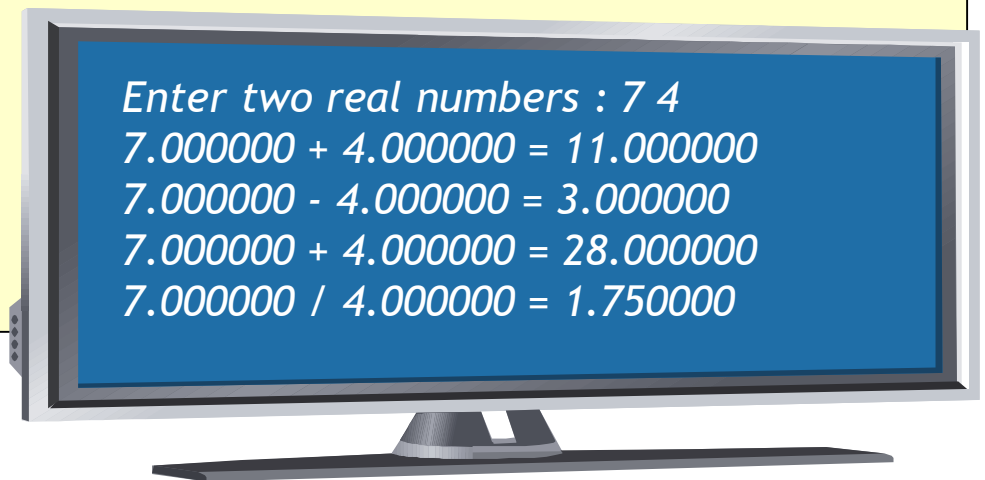
Division of integers



Division of real numbers and real numbers

Real number Arithmetic operations

```
#include < stdio.h >

int main()
{
      double x, y, result;

      printf ( " Enter two real numbers : ");
      scanf( "%lf %lf" , &x, &y);

      result = x + y; // Perform addition operation and assign the result to result
      printf( "%f / %f = %f" , x, y, result);


         ...
      result = x / y;
      printf( "%f / %f = %f" , x, y, result);

      return 0;
}
```



Remainder operator

- The modulus operator calculates the remainder when the first operand is divided by the second operand.
  - 10 % 2 is 0 .
  - 5 % 7 is 5 .
  - 30 % 9 is 3 .

- (Example) Distinguishing between even and odd numbers using the remainder operator
  - Even if x % 2 is 0

- (Example) Determining multiples of 3 using the remainder op erator
  - x % 3 is 0, then it is a multiple of 3.

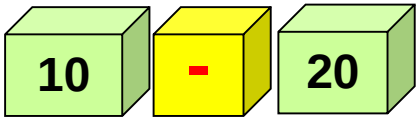
Remainder operator

```
// Remainder operator program
#include < stdio.h >
#define SEC_PER_MINUTE 60 // 1 minute is 60 seconds

int main( void )
{
      int input, minute, second;

      printf (  "  Please enter seconds : " );
      scanf ( "%d" , &input); // Read the time in seconds .

      minute = input / SEC_PER_MINUTE; // how many minutes
      second = input % SEC_PER_MINUTE; // how many seconds

      printf ( "%d seconds are %d minutes %d seconds . \n" , input, minute, second);
      return 0;
}
```

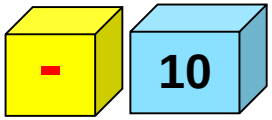
Sign operator

- Change the sign of a variable or constant

```
x = -10;
y = -x; // The value of variable y becomes 10 .
```



Binary operator

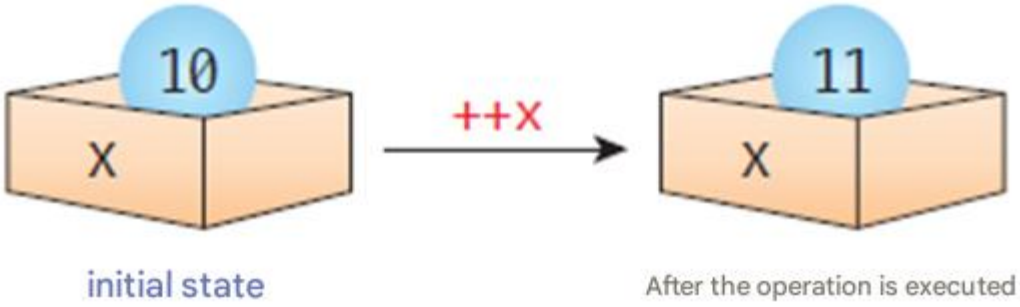


Unary operator

- is both a binary operator and a unary operator.

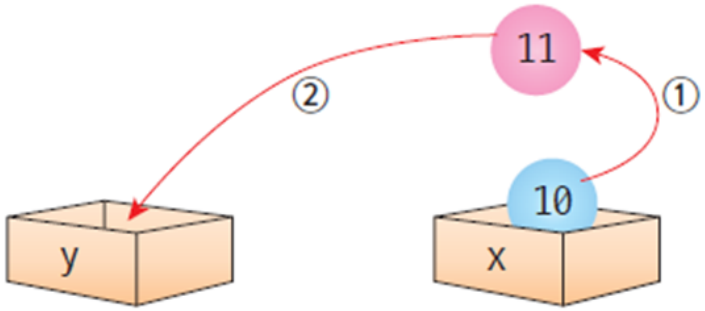
Increment/decrement operator

- Increment/decrement operators : ++, --
- Operator that increases or decreases the value of a variable by one.
- (Example) ++x, --x;



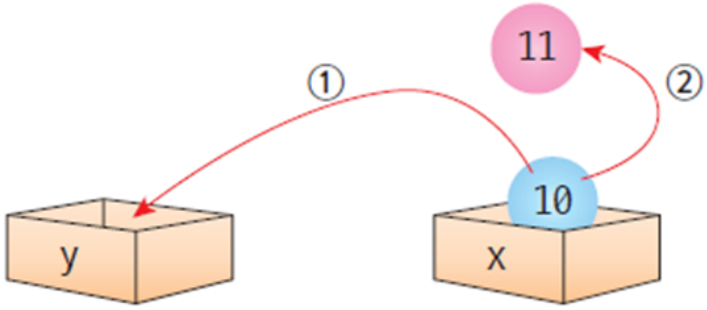
Difference between ++x and x++

```
y=++x;
```



The increased value of x is assigned to y.

```
y=x++;
```



Substitute first, then increase later.

Increment/decrement operator summary

increment operator	difference
++X	The value of the formula is the incremented value.
X++	The value of the formula is the original x value that has not been increased.
--X	The value of the formula is the reduced value.
X--	The value of the formula is the original, undecreased x-value.

Examples of increment and decrement operators

```
y = (1 + x++) + 10; // Even if there are parentheses, the increase in the value of x is executed last .
```

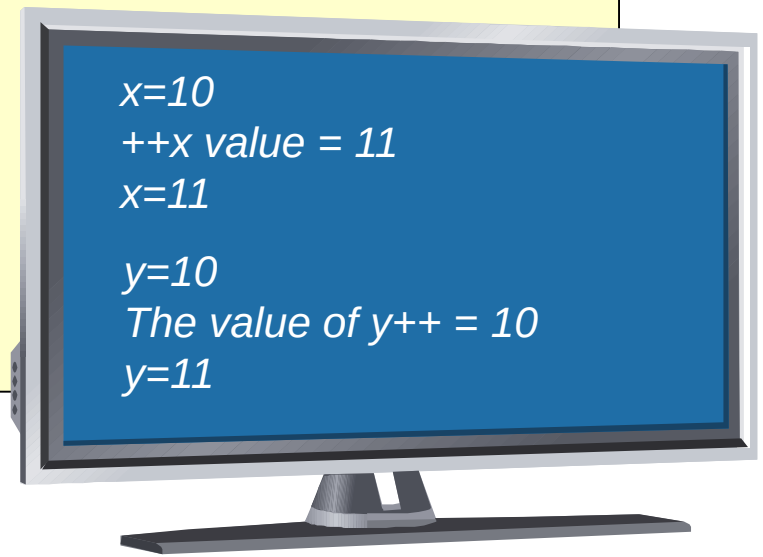
```
x = 10++; // Cannot be applied to constants .
y = (x+1)++; // Cannot be applied to formulas .
```

Example : Increment/decrement operator

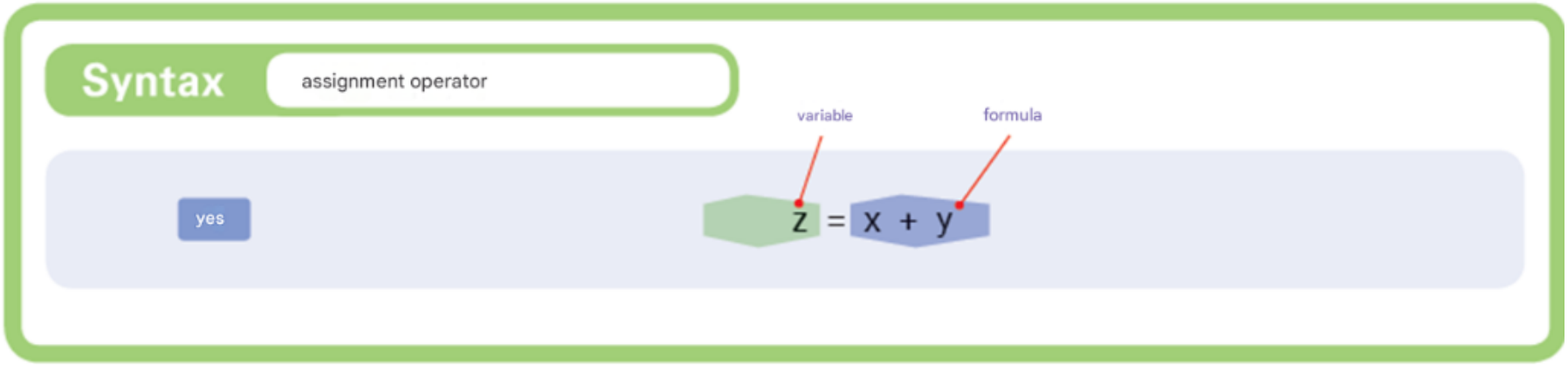
```
#include < stdio.h >
int main( void )
{
    int x=10, y=10;

    printf ( "x=%d\n" , x);
    printf ( "++x value =%d\n" , ++x);
    printf ( "x=%d\n\n" , x);

    printf ( "y=%d\n" , y);
    printf ( " value of y++ =%d\n" , y++);
    printf ( "y=%d\n" , y);

    return 0;
}
```

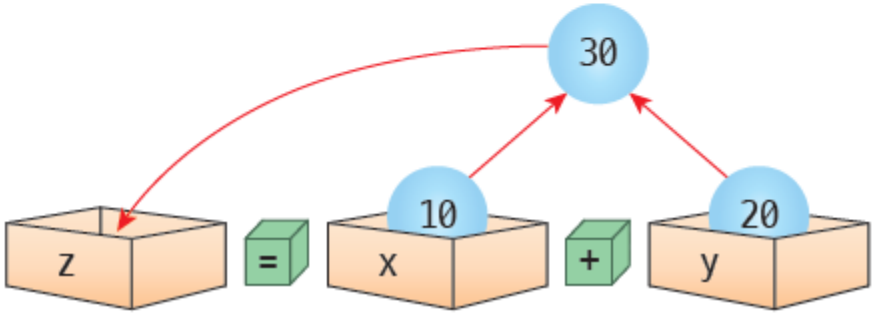
First, the value is increased and the increased value is used in the formula .

Use the current value in the formula first and increases later .



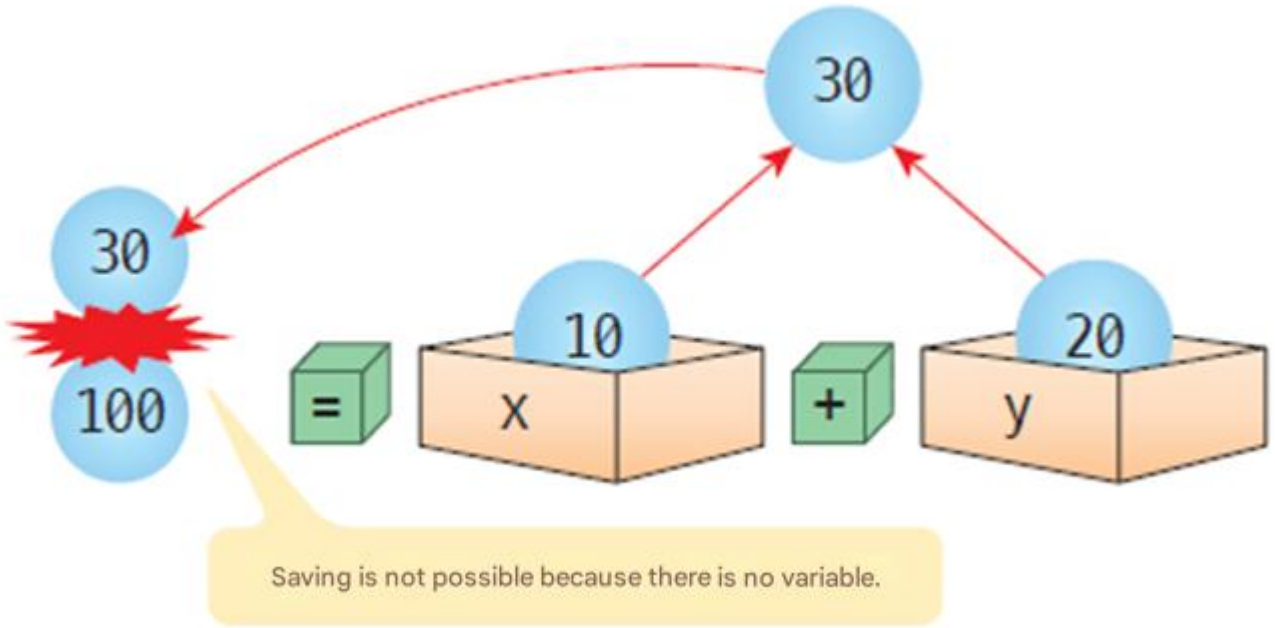
Assignment operator





Caution: assignment operators

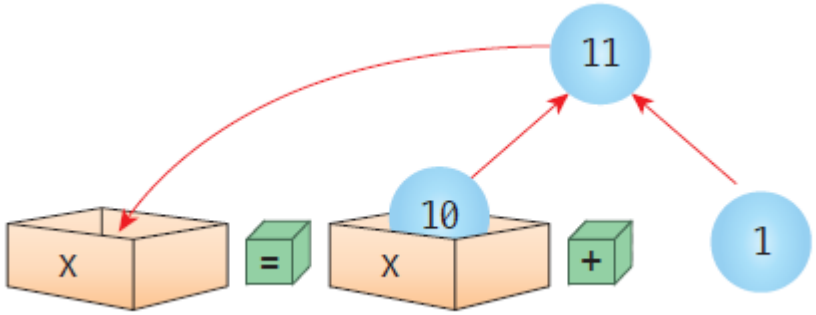
- 100 = x + y; // Compile error !



Caution: assignment operators

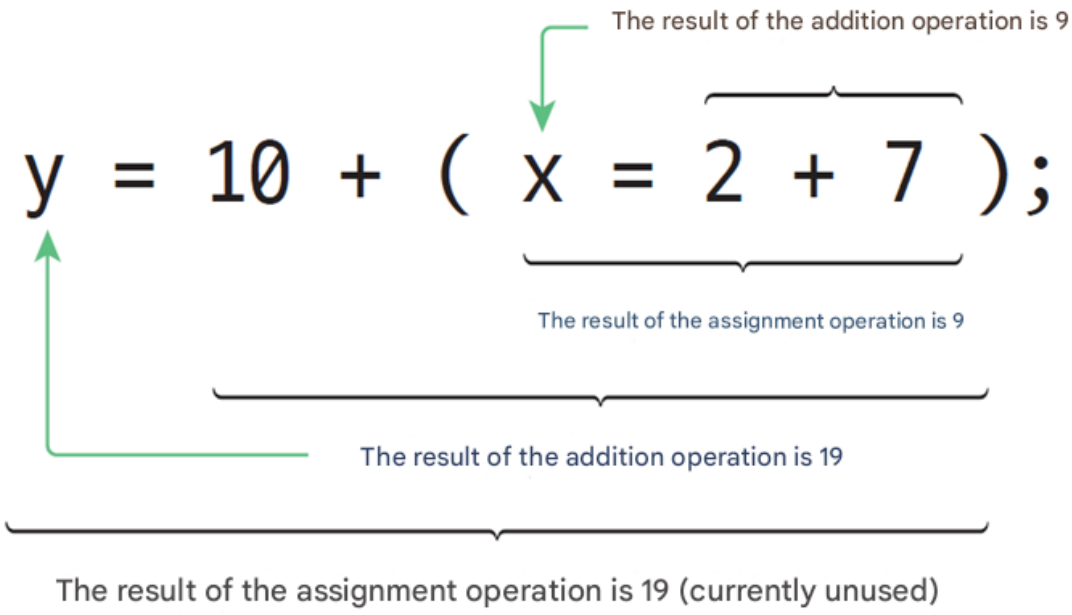
It is a correct statement in C , but mathematically incorrect.

```
x = x + 1;
```

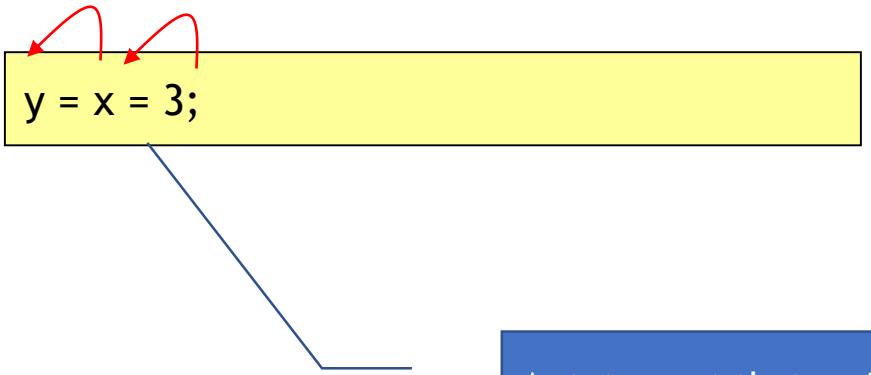


The result of the assignment operation

All operations involve
There is a result value
Substitution operation
There is a result value .



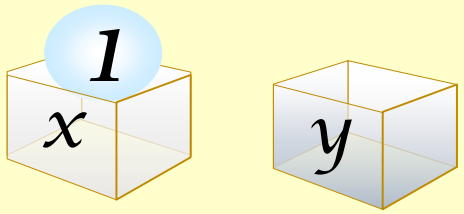
Next sentence is also possible .

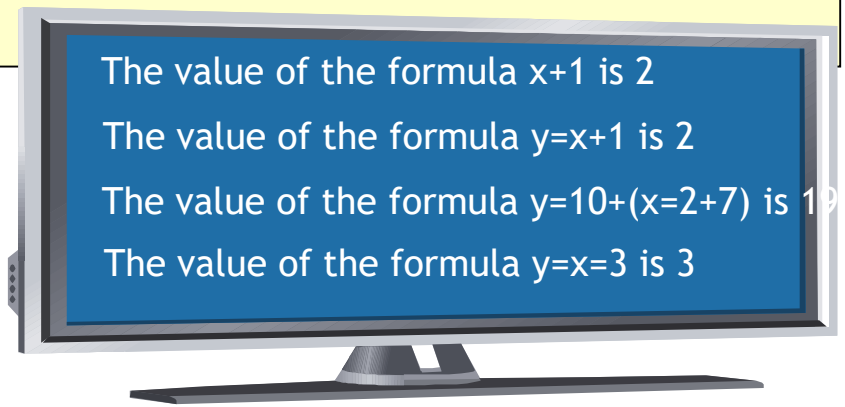


A statement that assigns the same value to multiple variables can be written as follows . Here, x = 3 is first performed, and then the resulting value, 3 , is assigned to

Example

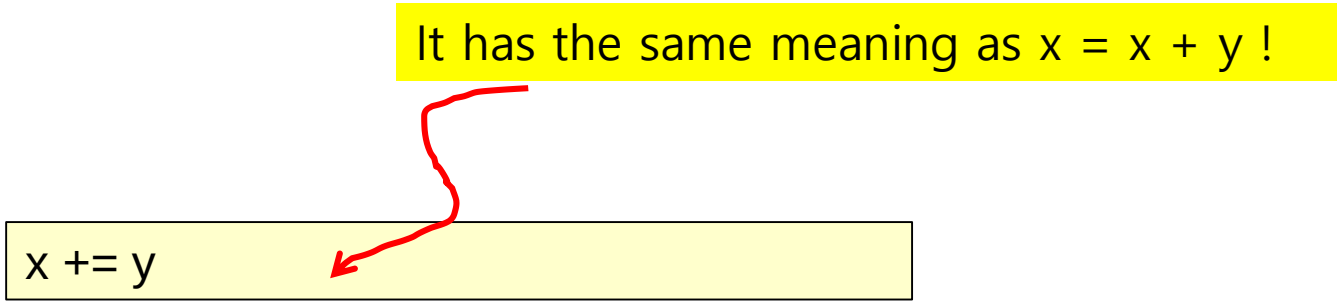
```
/* Assignment operator program * /
#include < stdio.h >

int main( void )
{
        int x, y;

        x = 1;
        printf ( " The value of formula x+1 is %d\n" , x+1);
        printf ( " The value of the formula y=x+1 is %d\n" , y=x+1);
        printf ( " The value of the formula y=10+(x=2+7) is %d\n" , y=10+(x=2+7));
        printf ( " The value of the formula y=x=3 is %d\n" , y=x=3);

        return 0;
}
```





Compound assignment operator

- A compound assignment operator is an operator that combines
- You can make the source simpler



Compound assignment operator

compound assignment operator	meaning	compound assignment operator	meaning
x += y	x = x + y	x &= y	x = x & y
x -= y	x = x - y	x ¦= y	x = x ¦ y
x *= y	x = x * y	x^=y	x = x ^ y
x /= y	x = x / y	x >>= y	x = x >> y
x%=y	x = x % y	x <<= y	x = x << y

Quiz

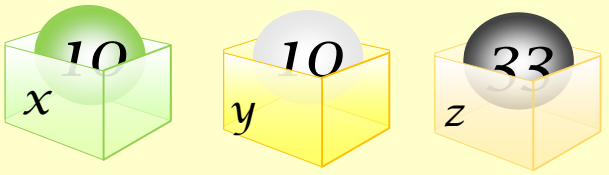
- If we solve the following equation and rewrite it, what would it be?

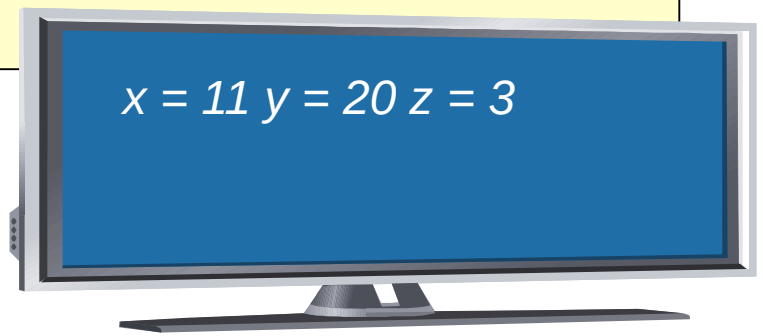
```
x *= y + 1
x %= x + y
```

```
x = x * (y + 1)
x = x % (x + y)
```

Compound assignment operator

```
// Compound assignment operator program
#include < stdio.h >

int main( void )
{
        int x = 10, y = 10, z = 33;

       x += 1;
       y *= 2;
       z %= 10 + 20;

        printf ( "x = %d y = %d z = %d \n" , x, y, z);
        return 0;
}
```





Error Alert

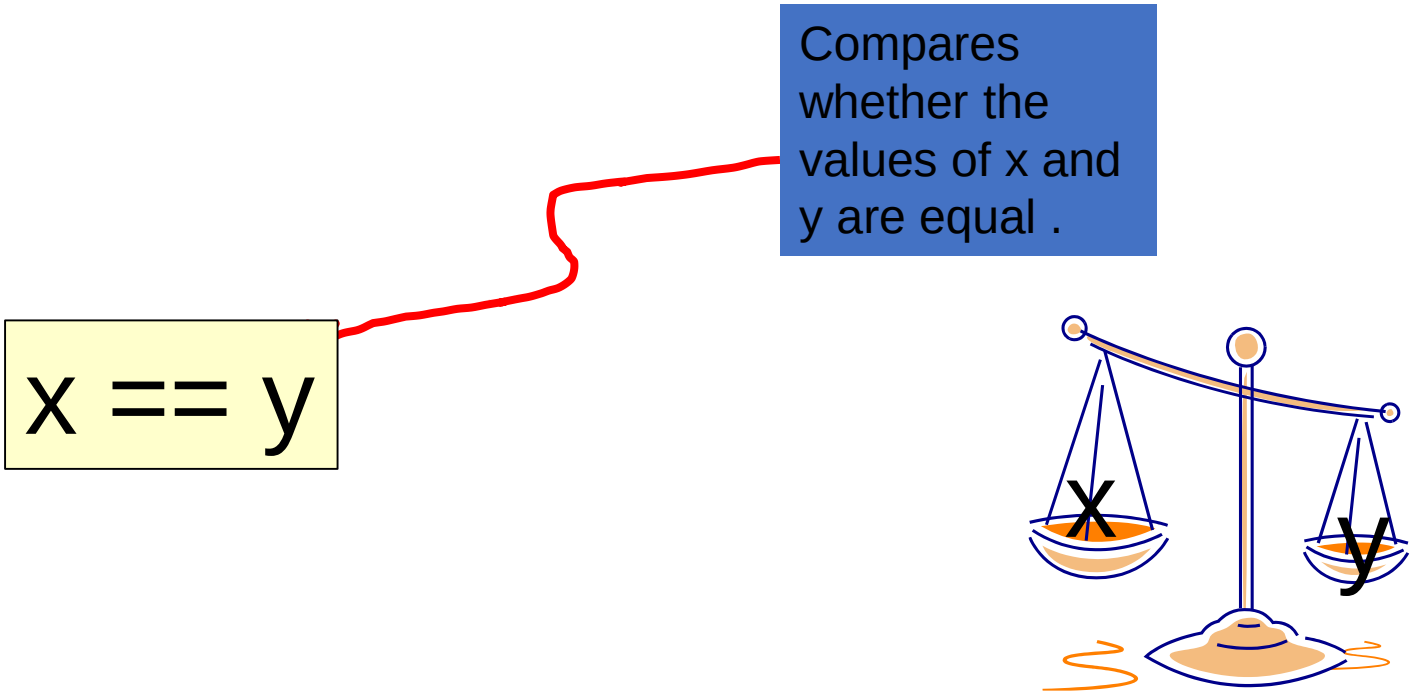
beware of errors

The following formula is incorrect. Why is that?

```
++x = 10;      // The left side of the equal sign must always be a variable.
x + 1 = 20;    // The left side of the equal sign must always be a variable.
x =*y;         // It's *=, not =*.
```

Relational Operators

- Operator that compares two operands
- The result is true (1) or false (0).



Relational Operators

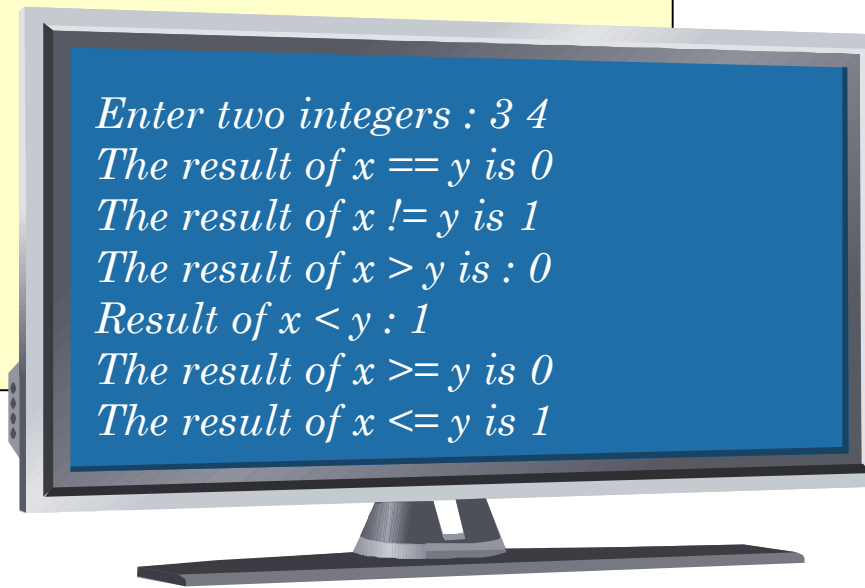
calculation	meaning	calculation	meaning
x == y	Are x and y equal?	x < y	Is x less than y?
x != y	Are x and y different?	x >= y	Is x greater than or equal to y?
x > y	Is x greater than y?	x <= y	Is x less than or equal to y?

Examples of relational operators

```
1 == 1 // true (1)
1 != 2 // true (1)
2 > 1 // true (1)
x >= y // true if x is greater than or equal to y (1) , otherwise false (0)
```

Example

```
#include < stdio.h >
int main( void )
{
       int x, y;

      printf ( " Enter two integers : ");
      scanf ( "% d%d " , &x, &y);

      printf ( " The result of x == y : %d", x == y);
      printf ( " The result of x != y : %d", x != y);
      printf ( " Result of x > y : %d", x > y);
      printf ( " The result of x < y : %d", x < y);
      printf ( " The result of x >= y : %d", x >= y);
      printf ( " The result of x <= y : %d", x <= y);

      return 0;
}
```



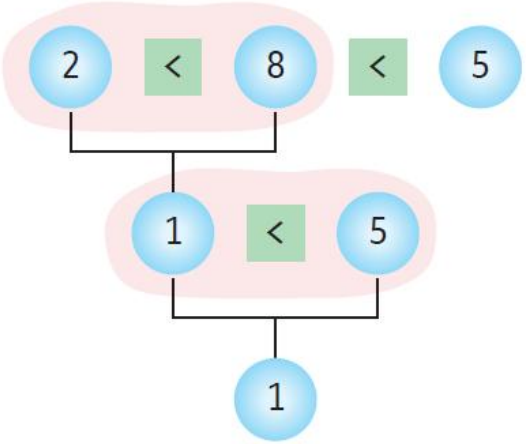
Caution!

- (x = y)
  - Substitute the value of y into x . The value of this formula is the valu e of x .

- (x == y)
  - x and y are equal, the value of the formula is 1, otherwise it is 0 .
  - (x == y) to (x = y) Be careful not to use it incorrectly !

Caution: when using relational operators

- As in mathematics, 2 < x < 5 and If you write them together, you will get wrong results .



- The right way : (2 < x) && (x < 5)

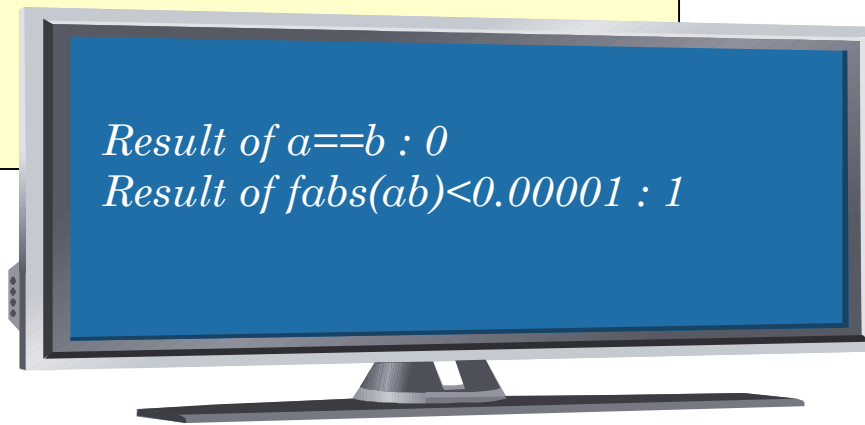
When comparing real numbers

- (1e32 + 0.01) > 1e32
  - -> False because the values on both sides are considered equal

- (fabs(xy)) < 0.0001
  - Correct formula

Example

```
#include < stdio.h >
#include < math.h >

int main( void )
{
 double a, b;
a = (0.3 * 3) + 0.1;
b = 1;
 printf ( " Result of a==b : %d \n" , a == b);


 printf ( " Result of fabs(ab)<0.00001 : %d \n" , fabs(a - b) < 0.0001);
 return 0;
}
```

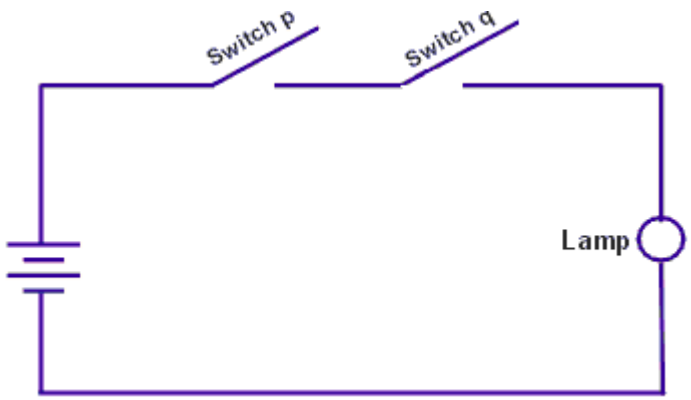


Logical Operators

- An operator that combines multiple conditions to determine true or false.
- The result is true (1) or false (0).

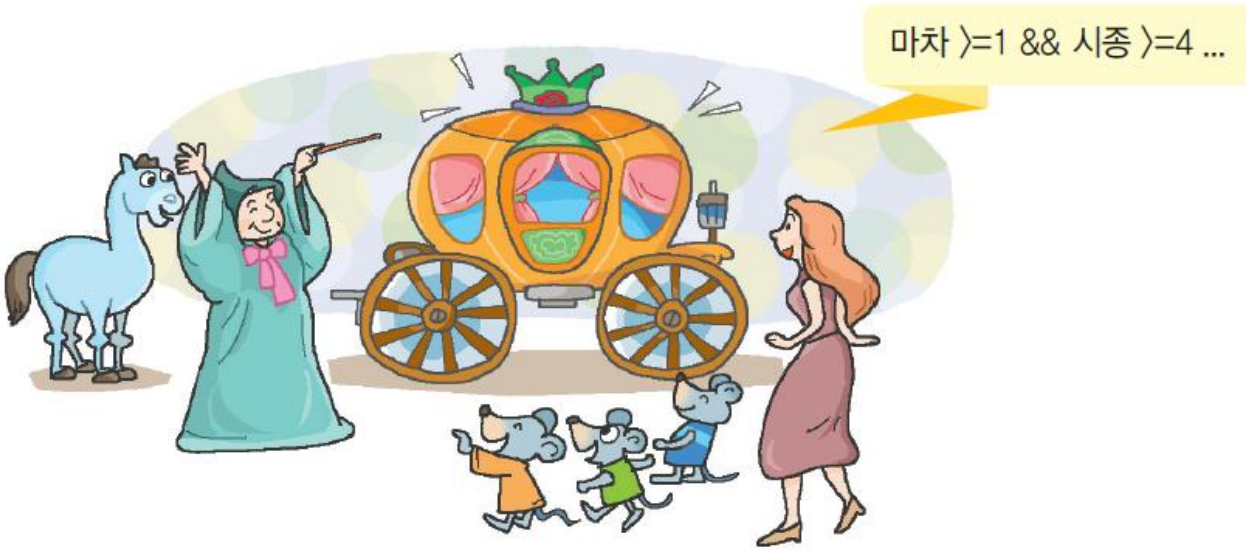
Both x and y are true
It is true only if .

x && y



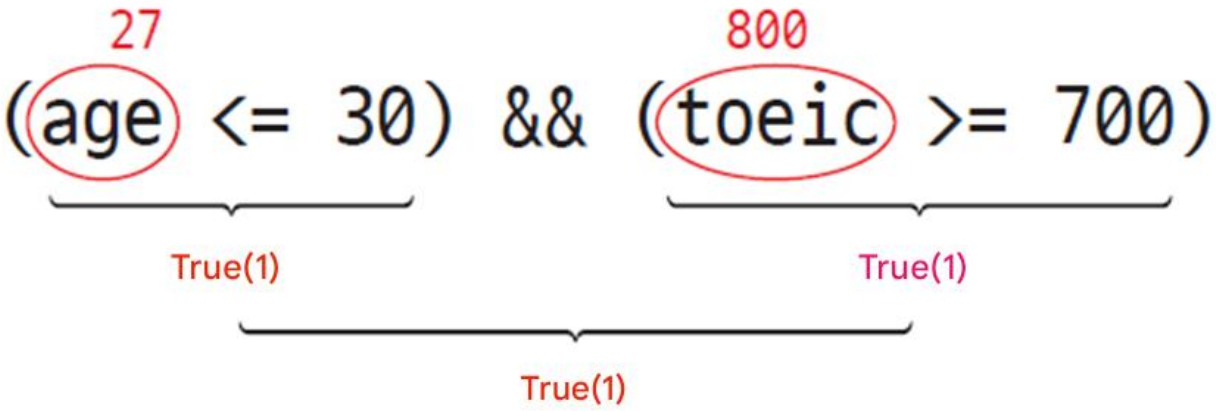
Logical Operators

calculation	meaning
x && y	AND operation, true if both x and y are true, otherwise false
x || y	OR operation, true if only one of x or y is true, false if both are false
!x	NOT operation, false if x is true, true if x is false



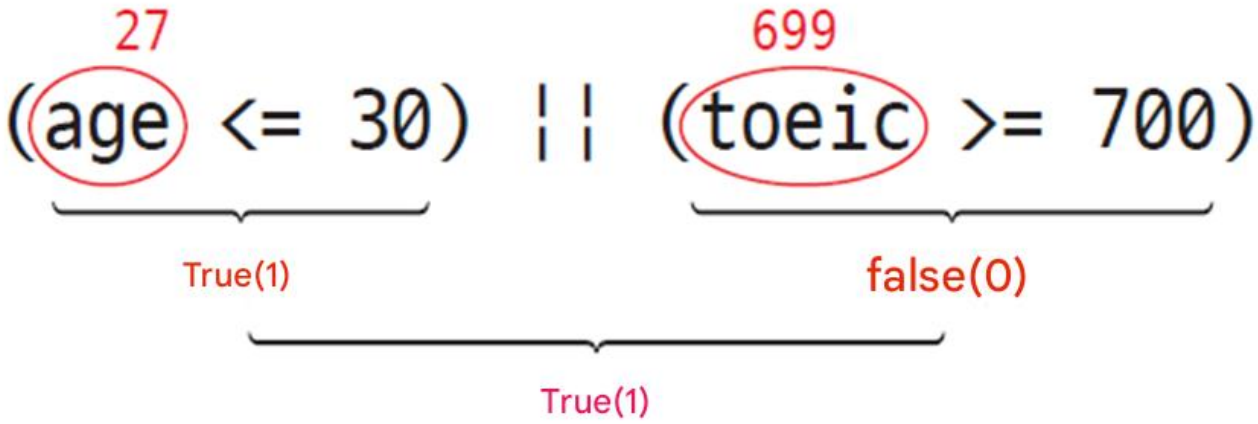
AND operator

- a company is hiring new employees and they set a requirement that the applicants be under 30 years old and have a TOEIC scor e of 700 or higher .



OR operator

- the conditions for hiring new employees have changed so that they must be under 30 years old or have a TOEIC score of 700 or higher .



Examples of logical operators

- " Is x one of 1, 2, or 3 ?"
  - (x == 1) || (x == 2) || (x == 3)

- " x is greater than or equal to 60 and less than 100 ."
  - (x >= 60) && (x < 100)

- " x is neither 0 nor 1 ."
  - (x != 0) && (x != 1) //

NOT operator

- If the value of the operand is true, the result of the operation is made false , and if the value of the operand is false, the res ult of the operation is made true .


```
result = !1; // 0 is assigned to result .
result = !(2==3); // 1 is assigned to result .
```

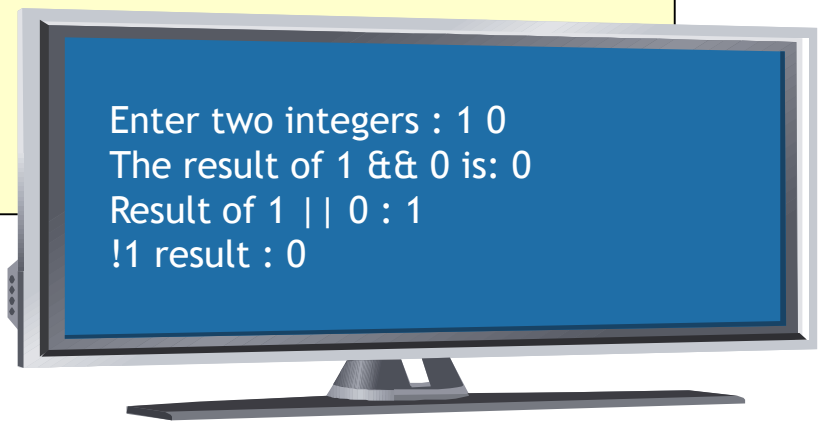
How to express truth and false

- If a relational formula or logical formula is true, 1 is generate, and if it is false, 0 is generated .
- the truth or falsity of an operand, it is considered true if it is not 0 , and false if it is 0 .
- Negative numbers are considered false .
- (Example) When applying the NOT operator

```
!0 // The value of the expression is 1
!3 // The value of the expression is 0
!-3          // The value of the expression is 0
```

Example

```
#include < stdio.h >

int main( void )
{
      int x, y;

      printf ( " Enter two integers : ");
      scanf ( "%d %d" , &x, &y) ;

      printf ( "%d && %d result : %d", x, y, x && y) ;
      printf ( "%d || %d result : %d", x, y, x || y) ;
      printf ( "!%d result : %d", x, !x );

      return 0;
}
```



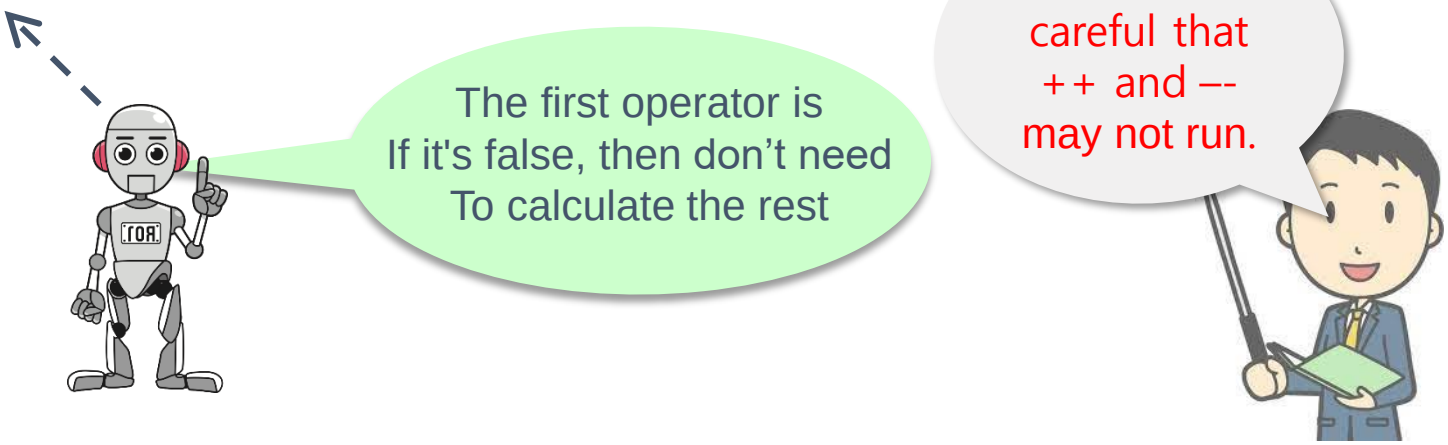
Shortcut calculation

- For the && operator , if the first operand is false, the other operands are not evaluated .

```
( 2 > 3 ) && ( ++x < 5 )
```

- For the || operator , if the first operand is true, the other operands are not evaluated .

```
( 3 > 2 ) || ( --x < 5 )
```

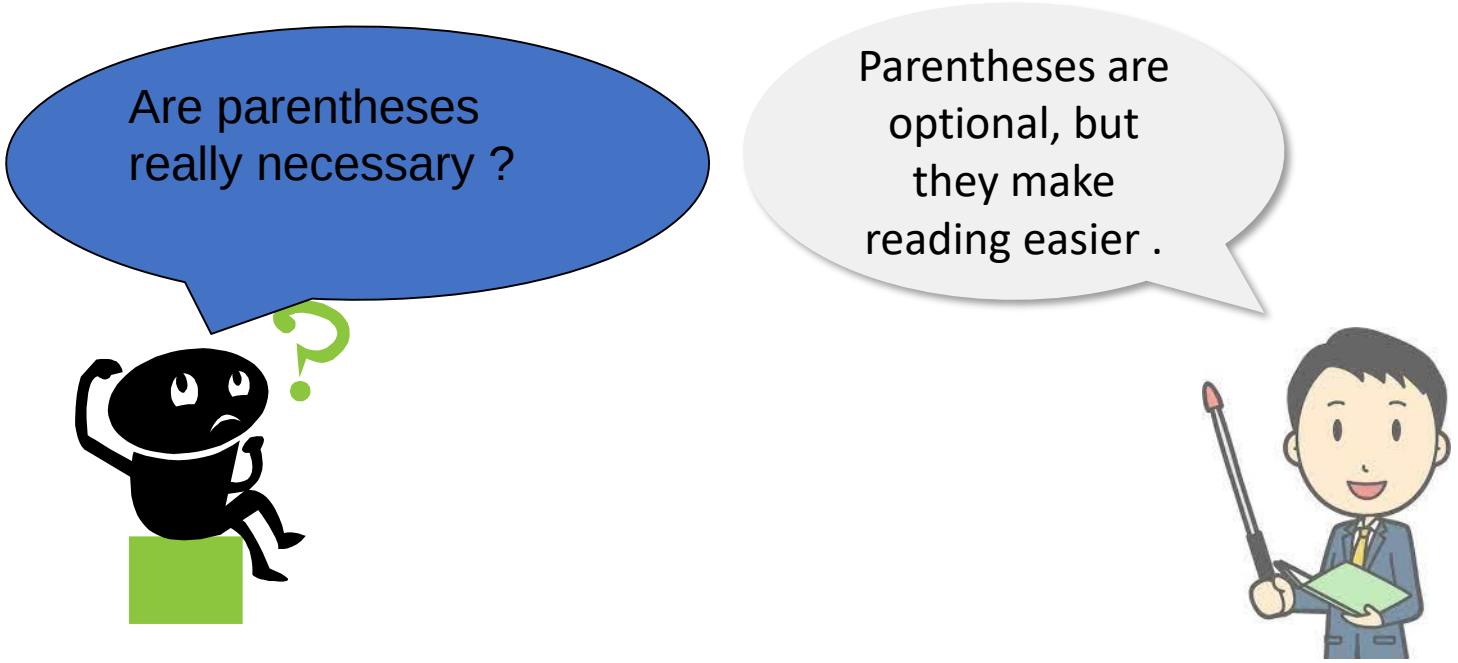


Lab: Leap year

- Conditions for a leap year
  - The year is divisible by 4 .
  - Years divisible by 100 are excluded .
  - A year that is divisible by 400 is a leap year .

Lab: Leap year

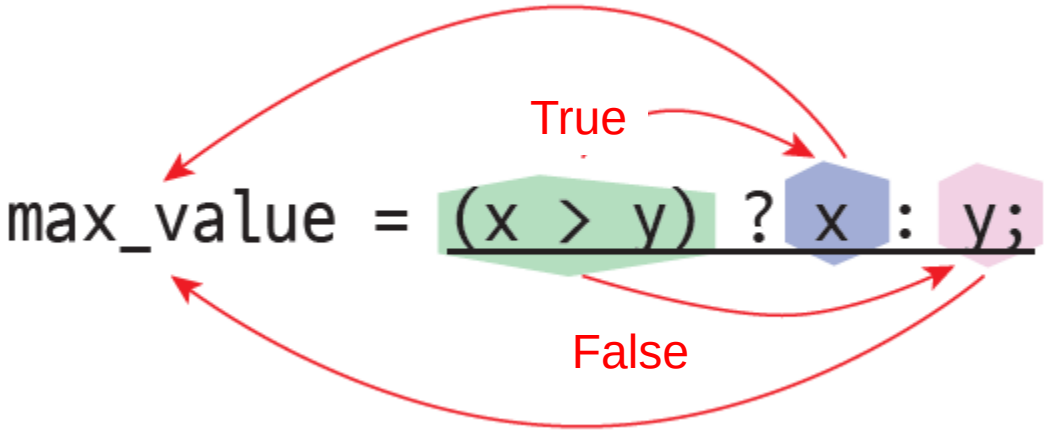
- Expressing the conditions for a leap year in a formula
  - ((year % 4 == 0) && (year % 100 != 0)) || (year % 400 == 0)



Lab: Leap year

```
#include < stdio.h >
int main( void )
{
    int year, result;

    printf ( " Enter the year : " );
    scanf ( "%d" , &year);

    result = ( (year % 4 == 0) && (year % 100 != 0)) || (year % 400 == 0);
    printf ( "result=%d \n" , result);

    return 0;
}
```

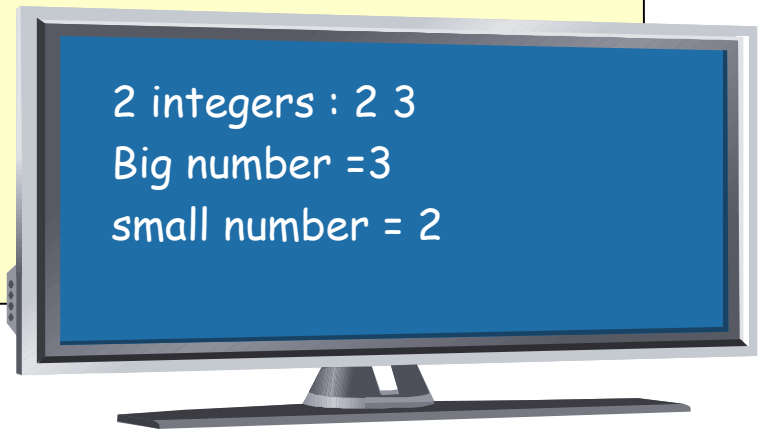
Conditional Operator



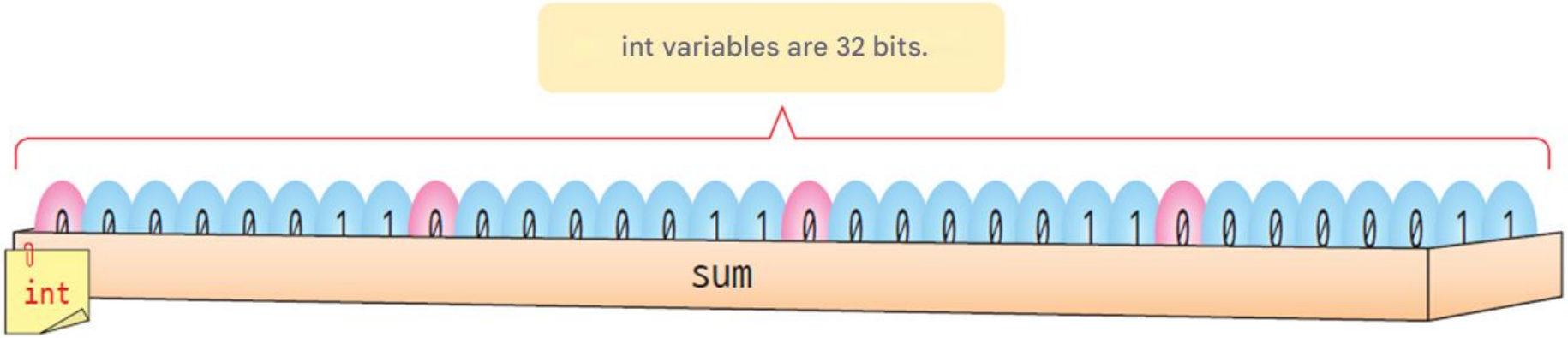

```
absolute_value = (x > 0) ? x : -x; // Calculate absolute value
max_value = (x > y) ? x : y; // Calculate maximum value
min_value = (x < y) ? x : y; // Calculate minimum value
(age > 20) ? printf ( " Adult \n" ): printf ( " Teenager \n" );
```

Example

```
// Conditional operator program
#include < stdio.h >

int main( void )
{
  int x,y ;

  printf ( " Two integers : " );
  scanf( "%d %d" , &x, &y);

  printf ( " large number =%d \n" , (x > y) ? x : y );
  printf ( " small number =%d \n" , (x < y) ? x : y );
}
```



All data is made up of bits .

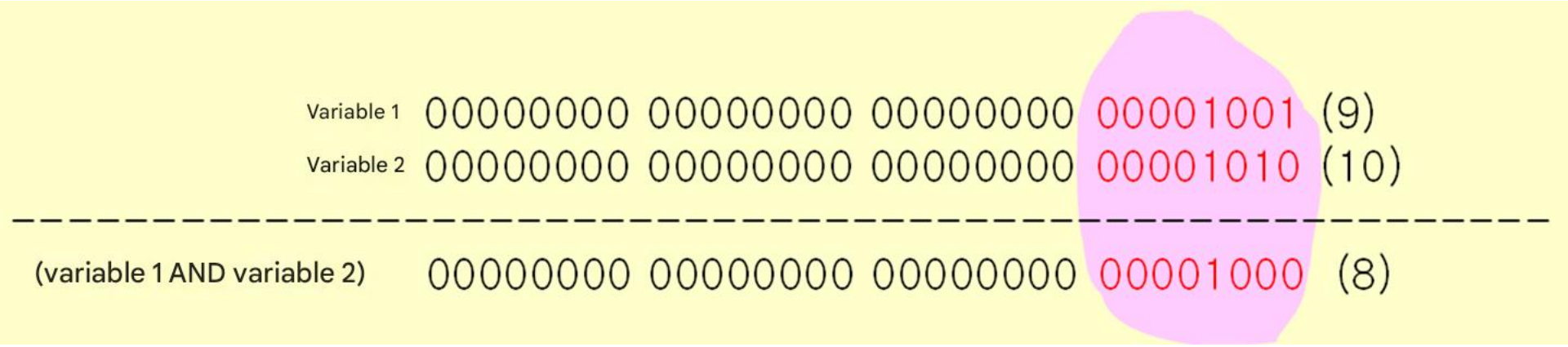


Bitwise Operator

operator	meaning of operator	yes
&	bitwise AND	1 if both corresponding bits of the two operands are 10, otherwise 0
¦	bit OR	1 if only one of the corresponding bits of the two operands is 10, otherwise 0
^	bitwise	If the corresponding bits of the two operands have the same value, 0; otherwise, 1.
<<	move left	Shifts all bits to the left by a specified number.
>>	move right	Shifts all bits to the right by the specified number.
~	bit NOT	0 becomes 1 and 1 becomes 0.

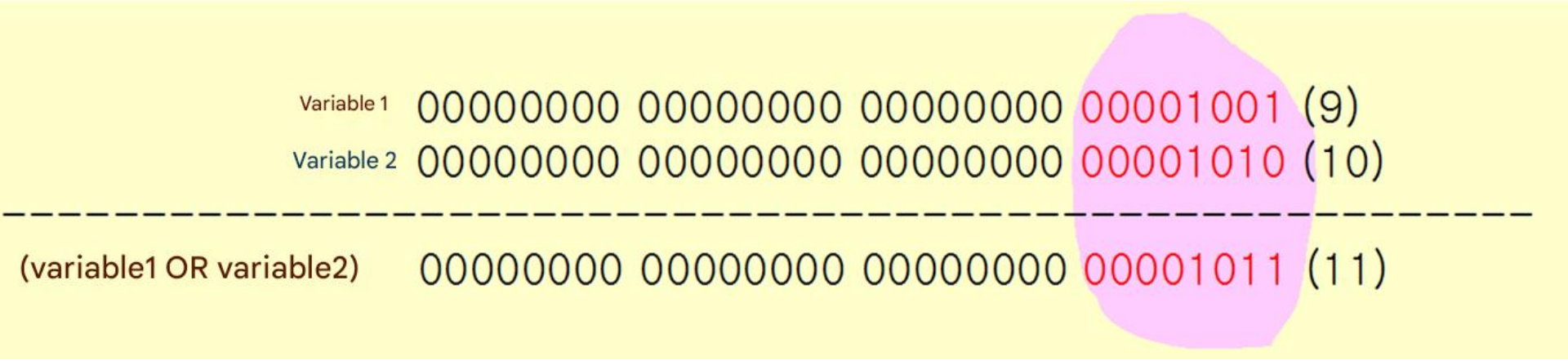
Bitwise AND operator

0 AND 0 = 0
1 AND 0 = 0
0 AND 1 = 0
1 AND 1 = 1



Bit OR operator

0 OR 0 = 0
1 OR 0 = 1
0 OR 1 = 1
1 OR 1 = 1



Bitwise XOR operator

0 XOR 0 = 0
1 XOR 0 = 1
0 XOR 1 = 1
1 XOR 1 = 0

Variable1 00000000 00000000 0000000000001001 (9)

Variable2 00000000 00000000 00000000 00001010 (10)

(variable1 XOR variable2) 00000000 00000000 0000000000000011 (3)

Bitwise NOT operator

NOT 0 = 1
NOT 1 = 0

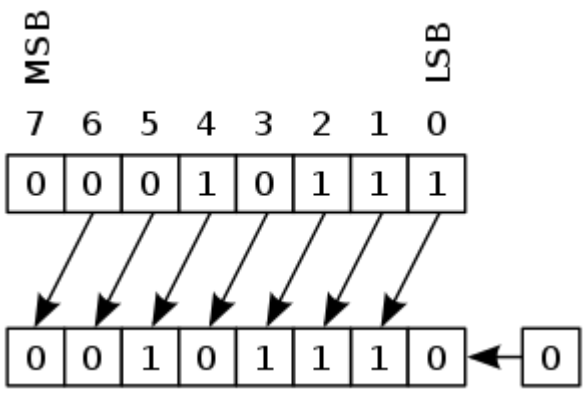
It becomes a negative number because the sign bit is inverted.

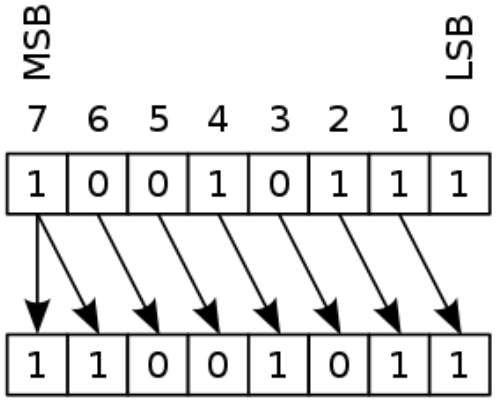
Variable1 00000000 00000000 00000000 00001001 (9)

(NOT variable 1) 11111111 11111111 11111111 11110110 (−10)

Bit shift operator

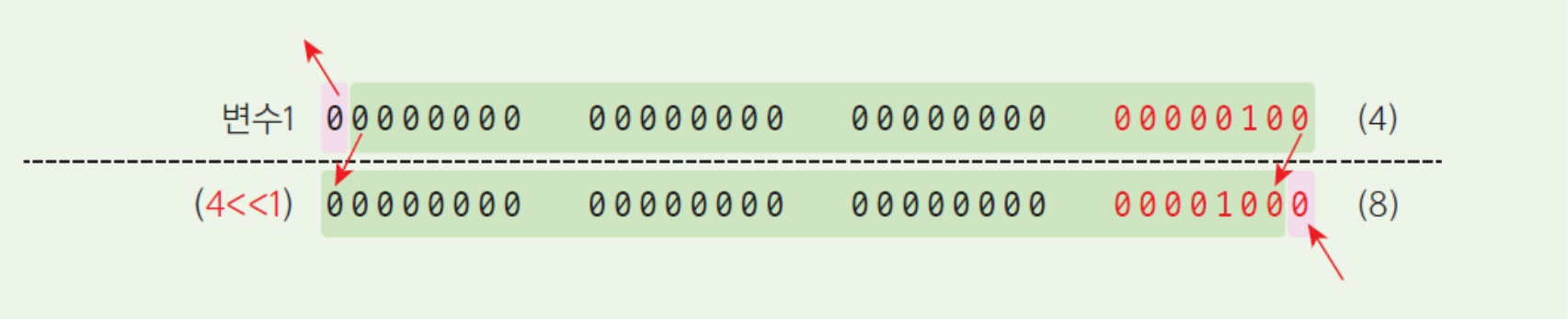
operator	sign	explanation
shift left bit	<<	x <<y shift the bits of x y spaces to the left
shift right bit	>>	x 〉〉 y Shift the bits of x y places to_the right





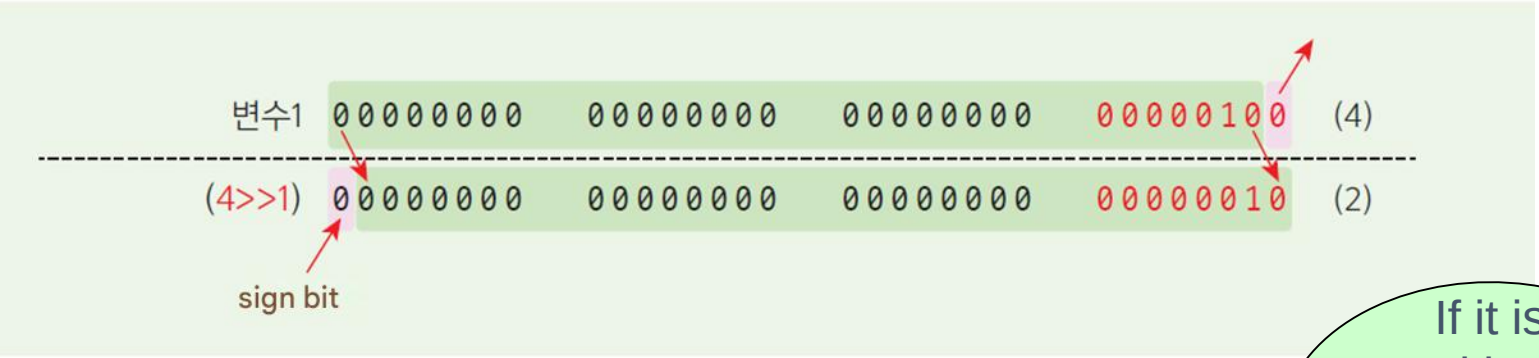
<< operator

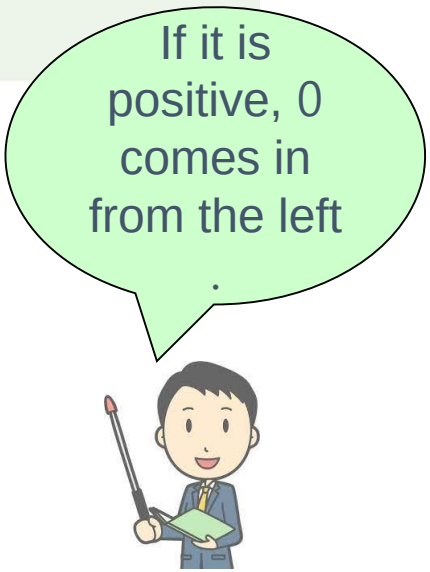
- bit left
- The value is doubled .



>> operator

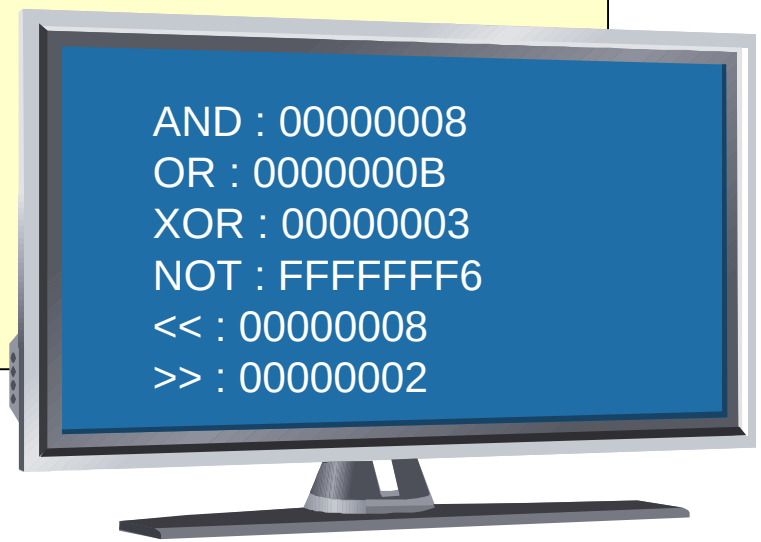
- move
- The value is multiplied by 1/2 .





Example : Bitwise Operators

```c
#include < stdio.h >

int main( void )
{
        printf ( "AND : %08X\n" , 0x9 & 0xA);
        printf( "OR : %08X\n" , 0x9 | 0xA);
        printf( "XOR : %08X\n" , 0x9 ^ 0xA);
        printf ( "NOT : %08X\n" , ~0x9);
        printf( "<< : %08X\n" , 0x4 << 1);
        printf( ">> : %08X\n" , 0x4 >> 1);

        return 0;
}
```

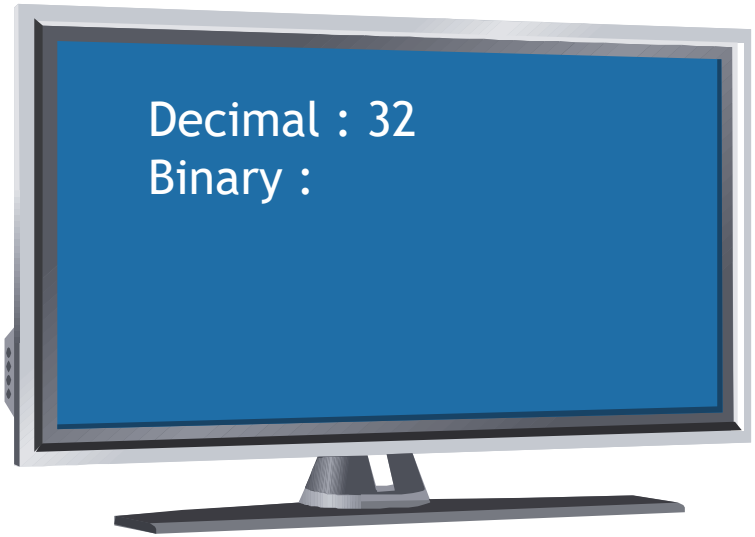


Example : Creating 2 's Complement with Bitwise Operators

```
#include < stdio.h >

int main( void )
{
    int a = 32;
    a = ~a; // Make it 1 's complement using NOT operator .
    a = a + 0x01; // add 1 .
    printf( "a= %d \n" , a);

    return 0;
}
```

Lab: Outputting decimal to binary

- use bitwise operators to display decimal numbers less than 128 in binary format on the screen .



Lab: Outputting decimal to binary

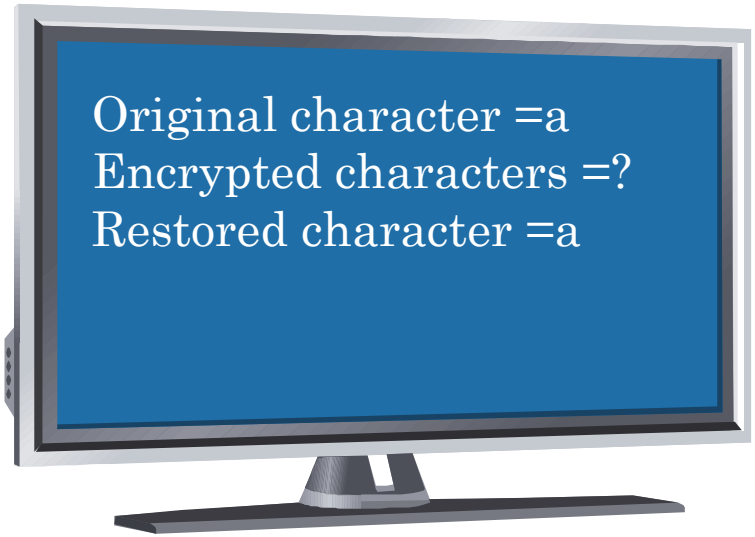
```
#define _CRT_SECURE_NO_WARNINGS
#include <stdio.h>

int main( void )
{
	unsigned int num;
	printf ( " Decimal : " );
	scanf ( "%u" , &num);

	unsigned int mask = 1 << 7; // mask = 10000000
	printf ( " Binary : " );

	((num & mask) == 0) ? printf( "0" ) : printf( "1" );
	mask = mask >> 1; // Shift 1 bit to the right .
	((num & mask) == 0) ? printf( "0" ) : printf( "1" );
	mask = mask >> 1; // Shift 1 bit to the right .
	((num & mask) == 0) ? printf( "0" ) : printf( "1" );
```

Lab: Outputting decimal to binary

```
        mask = mask >> 1; // Shift 1 bit to the right .
        ((num & mask) == 0) ? printf( "0" ) : printf( "1" );
         mask = mask >> 1;
         ((num & mask) == 0) ? printf( "0" ) : printf( "1" );
         mask = mask >> 1;
         ((num & mask) == 0) ? printf( "0" ) : printf( "1" );
         mask = mask >> 1;
         ((num & mask) == 0) ? printf( "0" ) : printf( "1" );
         mask = mask >> 1;
         ((num & mask) == 0) ? printf( "0" ) : printf( "1" );
         printf ( "\n" );

         return 0;
}
```

Lab: Encryption using XOR

- To encrypt a single character, just do x= x^key ; . Decryption is also possible . x= x^key ; That's it .

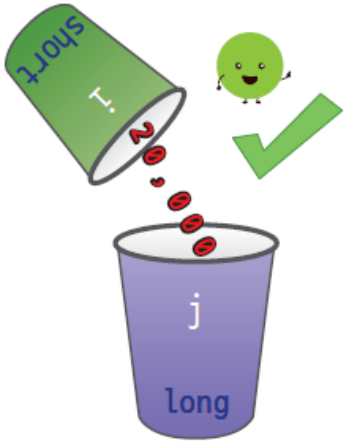


Lab: Encryption using XOR

```
#include < stdio.h >
int main(void)
{
 char data = 'a' ;
 char key = 0xff;
 char encrpted_data , orig_data ;

 printf ( " Original character =%c\n" , data );

 encrpted_data = data ^ key;
 printf ( " Encrypted character =%c \n" , encrpted_data );

 orig_data = encrpted_data ^ key;
 printf ( " Restored character =%c\n" , orig_data );

 return 0;
}
```

Type conversion

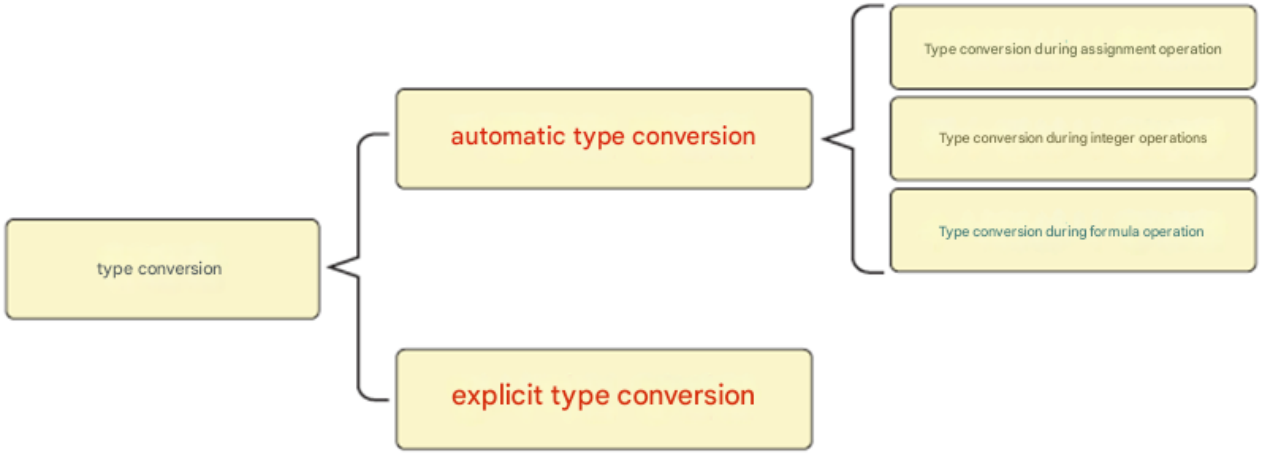
- Type conversion is changing the type of data during execution.



Be careful because if you do the conversion incorrectly, some of the data may be lost.
Do it .

Type conversion

- The type of data is converted during operation.

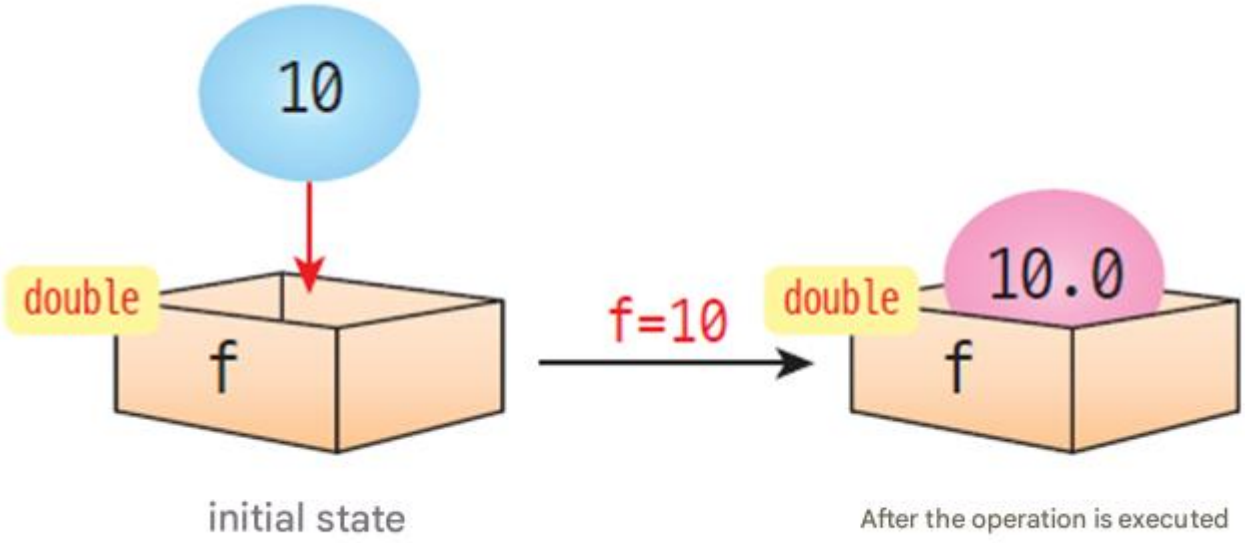


The type of the variable does not change, but the type of data stored in the variable changes .

Automatic type conversion during as signment operations

- Upward conversion

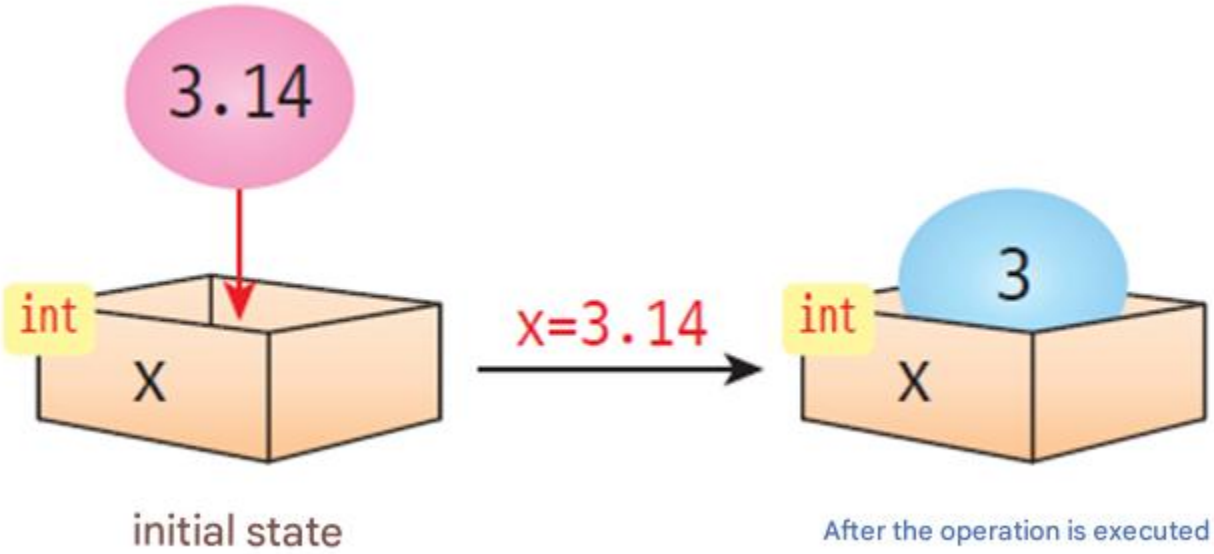
```
double f;
f = 10 ; // 10.0 is stored in f .
```



Automatic type conversion during as signment operations

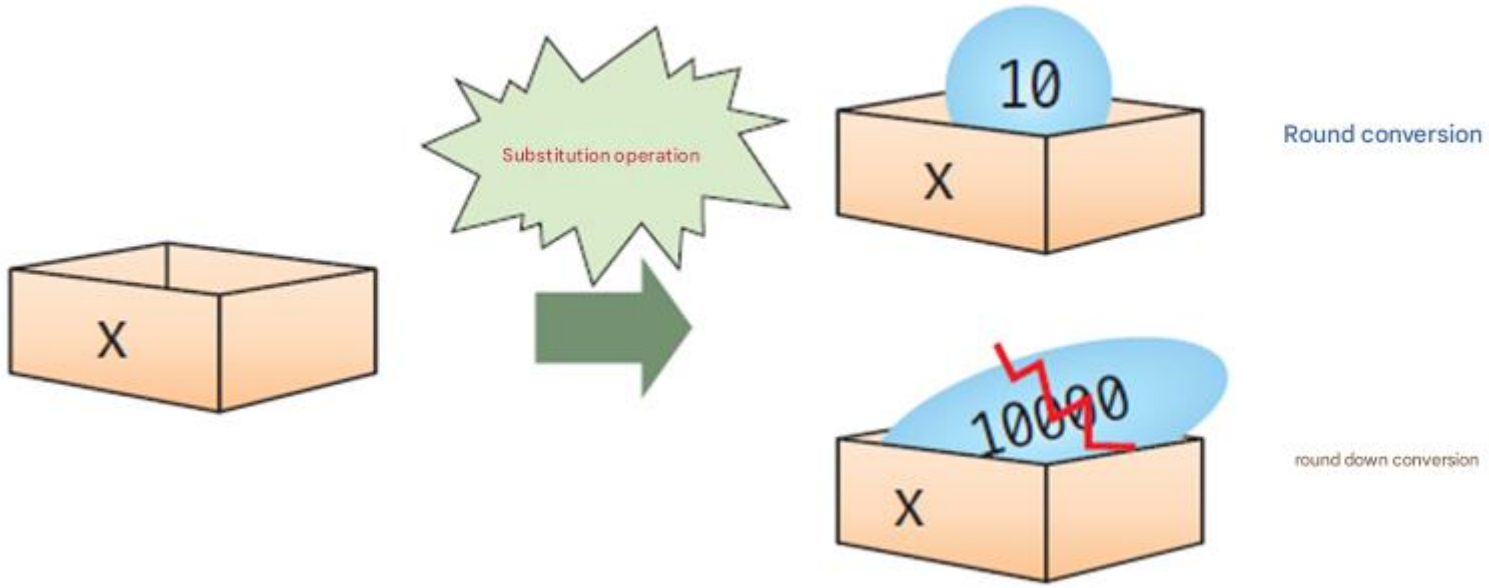
- Downward conversion

```
int i;
i = 3.141592; // 3 is stored in i .
```



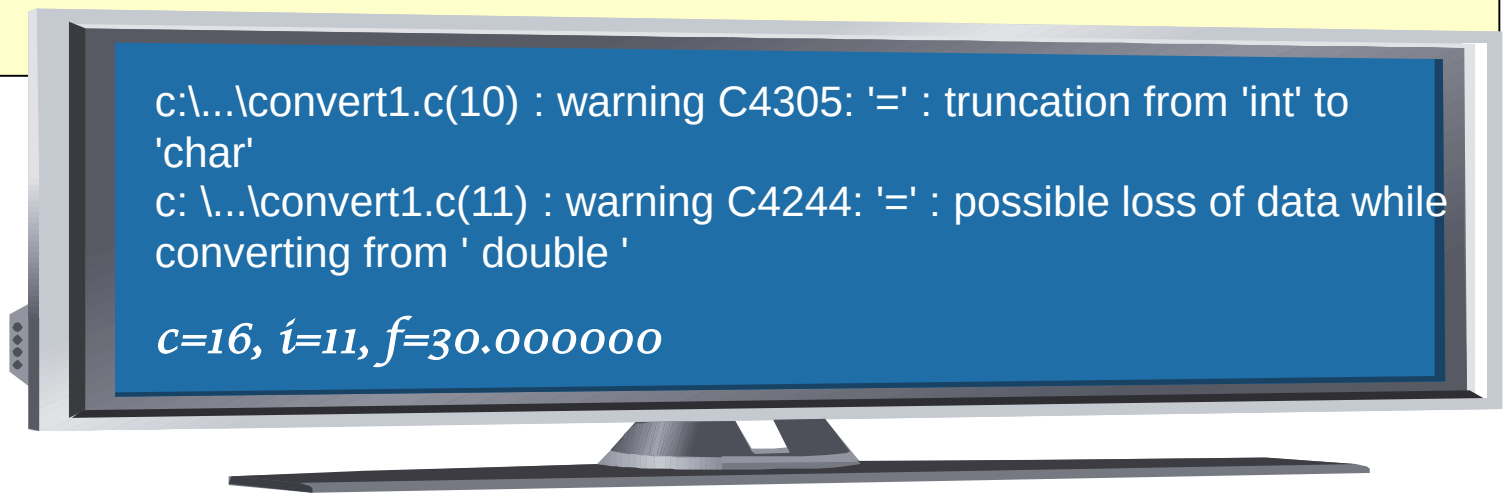
Integer type conversion

```
char x;

x = 10; // OK
x = 10000; // upper The bytes are gone .
```



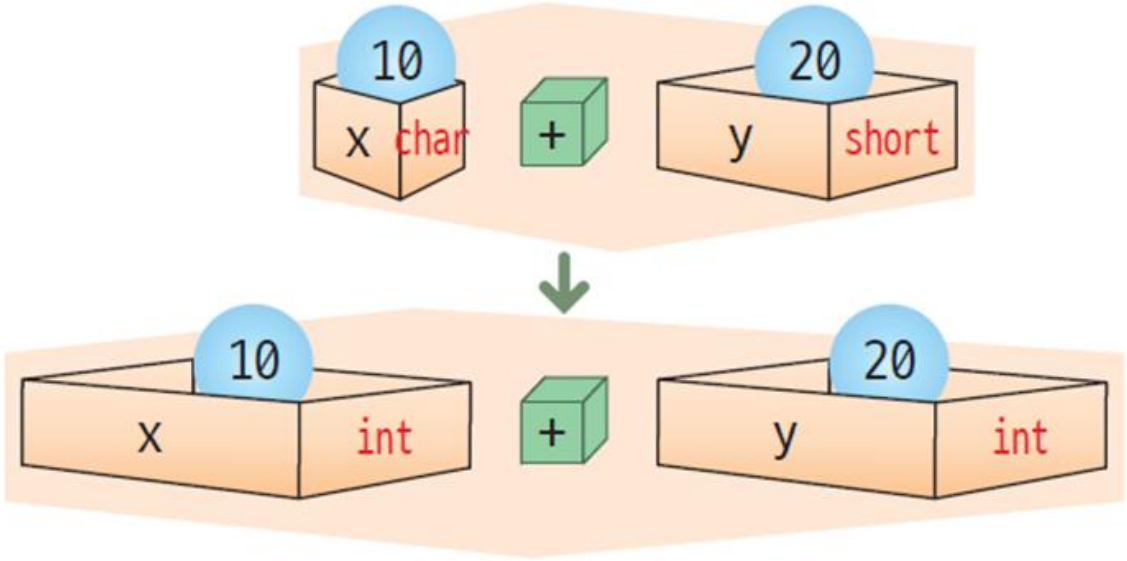
Up and down conversions

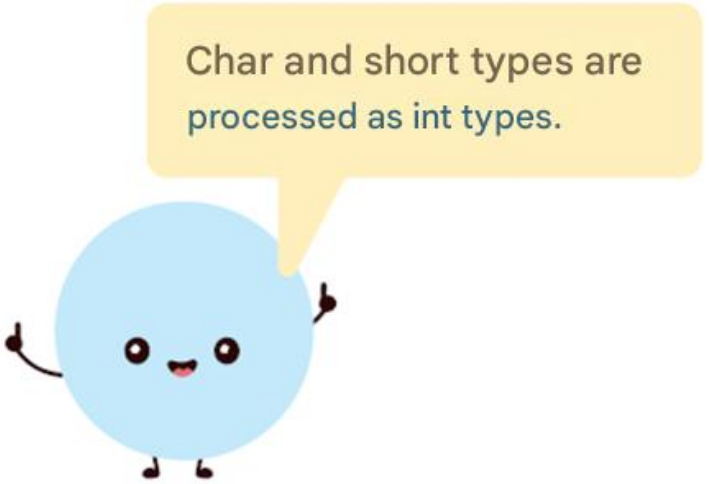
```c
#include <stdio.h>
int main( void )
{
        char c;
        int i;
        float f;

        c = 10000; // Round down
        i = 1.23456 + 10; // Round down
        f = 10 + 20; // round up
        printf( "c = %d, i = %d, f = %f \n" , c, i, f);
       return 0;
}
```



Automatic type conversion when performing integer operations

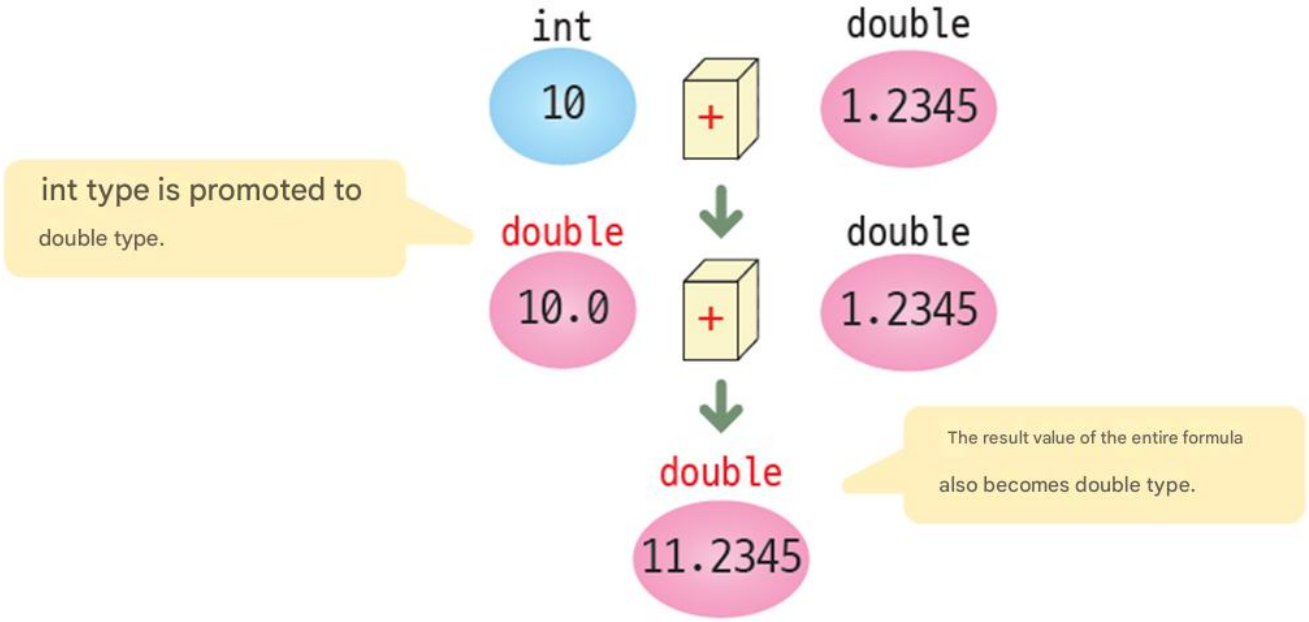
- When performing integer operations , if the type is char or short , it is automatically converted to int type and then calculated.





Automatic type conversion in formulas

- When different data types are used together, they are unified into a larger data type .



Explicit type conversion

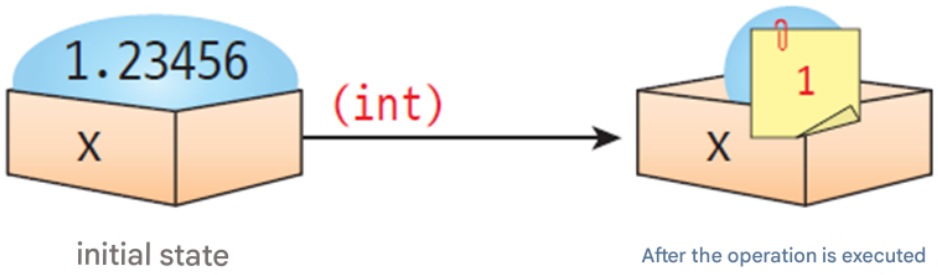
Syntax type conversion

yes

formula

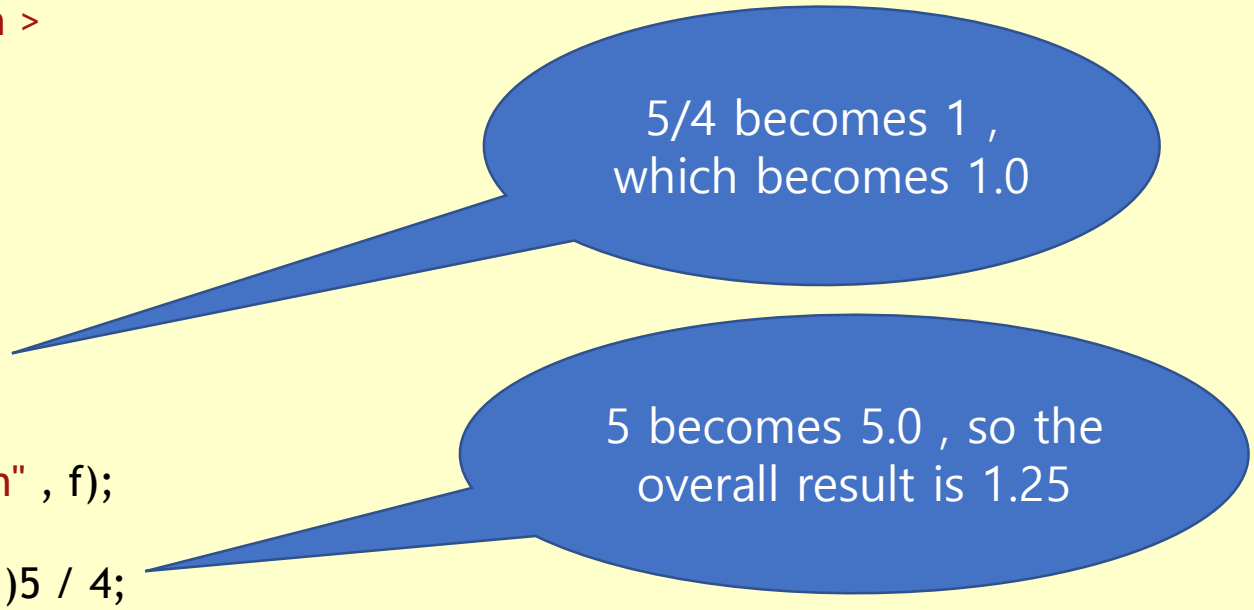
data type

```
(int)1.23456    // Convert to int type
(double) x      // Convert to double type
(long) (x+y)    // Convert to long type
```



Example

```
#define _CRT_SECURE_NO_WARNINGS
#include < stdio.h >

int main( void )
{
        int i ;
        double f;

        f = 5 / 4;

        printf ( "%f\n" , f);

        f = ( double )5 / 4;
        printf ( "%f\n" , f);

        f = 5.0 / 4;
        printf ( "%f\n" , f);
```



Example

```
        f = ( double )5 / ( double )4;
        printf ( "%f\n" , f);

        i = 1.3 + 1.8;
        printf ( "%d\n" , i );

        i = ( int )1.3 + ( int )1.8;

        printf ( "%d\n" , i );
        return 0;
}
```

1.3 becomes 1 and
1.8 also becomes 1 ,
so the final result is 2

Priority

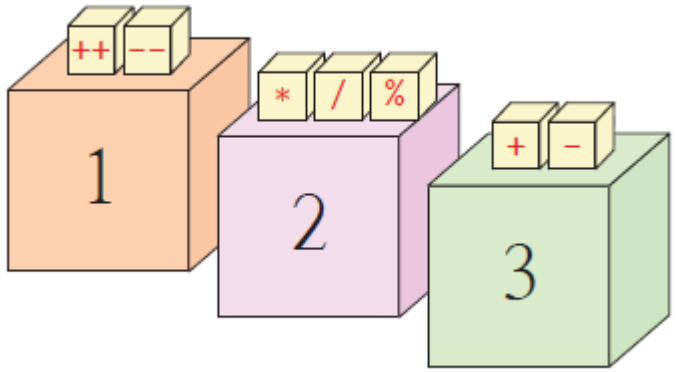
- Rules for which operator to evaluate first

$x + y * z$

① ②

$(x + y) * z$

① ②



Priority

priority	operator	explanation	Combinability
1	++ --	postfix increment/decrement operator	→(from left to right)
	()	function call	
	[]	array index operator	
	.	Accessing structure members	
	->	Structure pointer access	
	(type){list}	Compound literals (C99 standard)	
2	++ --	Potential increment/decrement operator	← (right to left)
	+ -	positive and negative signs	
	! ~	Logical negation, bitwise NOT	
	(type)	type conversion	
	*	indirect reference operator	
	&	address extraction operator	
	sizeof	size calculation operator	
	_Alignof	Alignment Requirement Operator (C11 Specification)	

3	* / %	Multiplication, Division, Remainder	
4	+ -	Addition, subtraction	
5	<< >>	bit shift operator	
6	< <=	relational operators	
	> >=	relational operators	
7	== !=	relational operators	→(from left to right)
8	&	bitwise AND	
9	^	bitwise	
10	¦	bit OR	
11	&&	Logical AND operator	
12	¦¦	Logical OR operator	
13	?:	Ternary Conditional Operator	
14	=	assignment operator	← (right to left)
	+= -=	compound assignment operator	
	*= /= %=	compound assignment operator	
	<<= >>=	compound assignment operator	
	&= ^= ¦=	compound assignment operator	
15	,	comma operator	→(from left to right)

General guidelines for priorities

- Comma < Assignment < Logic < Relation < Arithmetic < Unary
- Parentheses operators have the highest precedence.
- All unary operators have higher precedence than binary operators .
- Assignment operators have the lowest precedence, except for the comm a operator .
- If you can't remember the precedence of operators, use parentheses.
  - (x <= 10) && (y >= 20)
- Relational and logical operators have lower precedence than arithmetic operators .
  - x + 2 == y + 3
- Relational operators have higher precedence than logical operators . The refore, you can use sentences like the following with confidence .
  - x > y && z > y // Same as (x > y) && (z > y) .

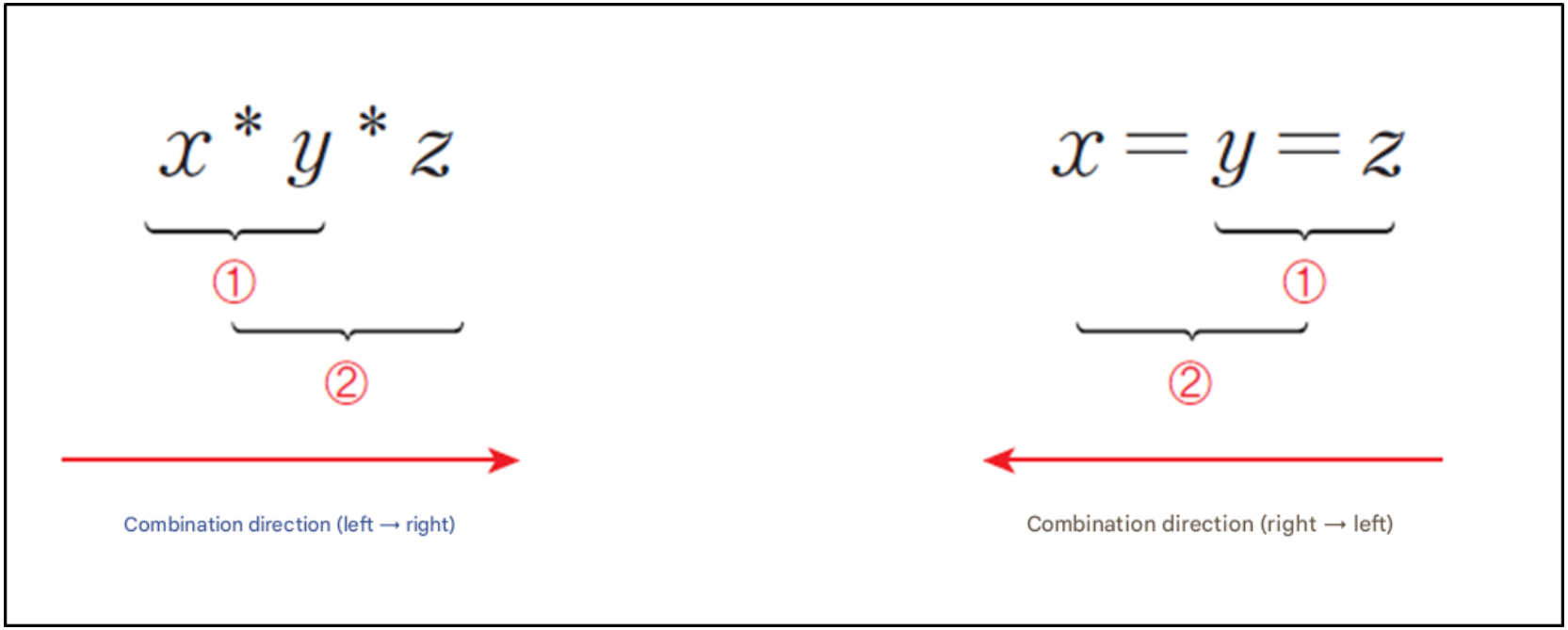
General guidelines for priorities

- among logical operators, the && operator has higher precedence than the || operator .
  - x < 5 || x > 10 && x > 0 // Same as x < 5 || (x > 10 && x > 0)

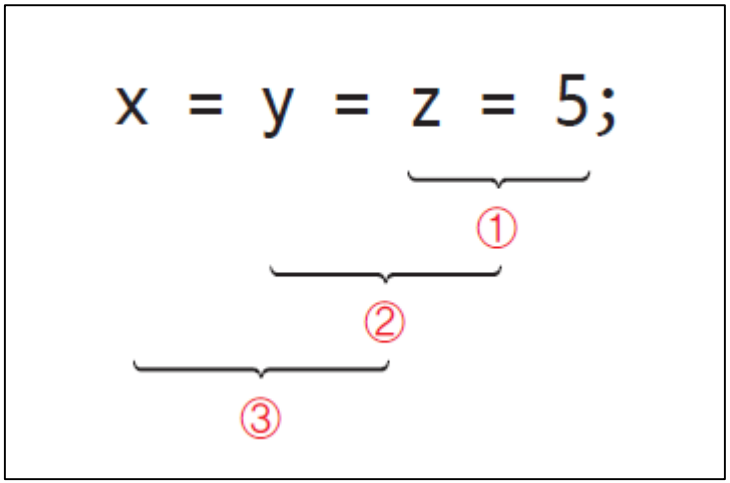
- Sometimes the order of evaluation of operators can be quite confusing . In x * y + w * y It is unclear which of x * y and w * y will be computed first .

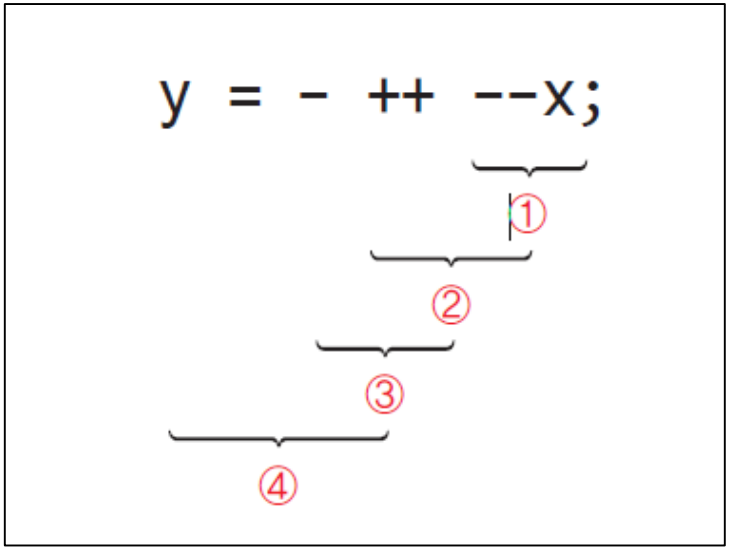
Combination Rules

- If there are multiple operators with the same priority, the rule for which one should be performed first

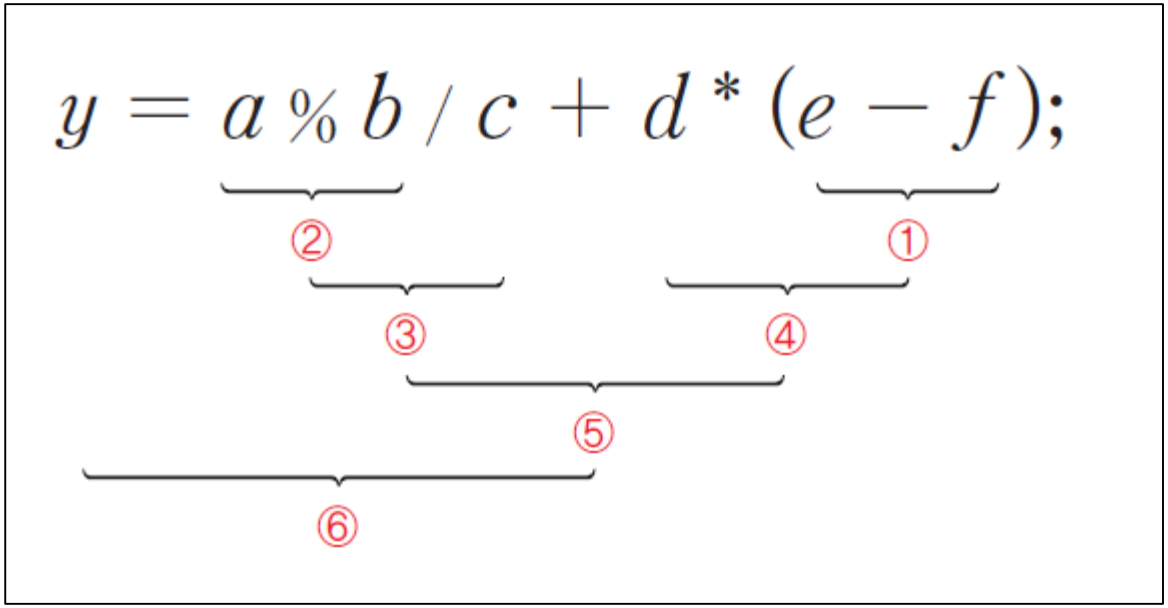


Example of a combination rule





Example of a combination rule



Example

```
#include < stdio.h >
int main( void )
{
	int x=0, y=0;
	int result;

	result = 2 > 3 || 6 > 7 ;
	printf ( "%d" , result);

	result = 2 || 3 && 3 > 2 ;
	printf ( "%d" , result);

	result = x = y = 1;
	printf ( "%d" , result);

	result = - ++x + y--;
	printf ( "%d" , result);

	return 0;
}
```

Q & A