Ch.5 Formulas and operator

What you will learn in this chapter

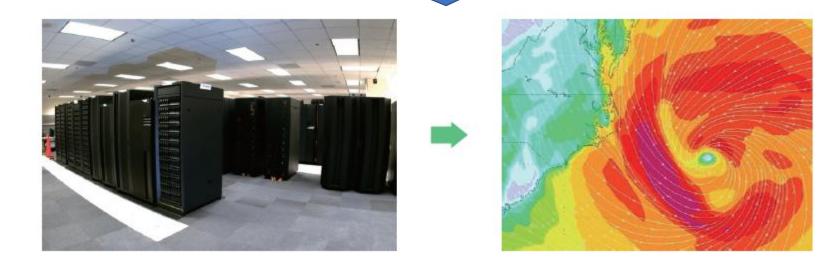
- * What are formulas and operators?
- * Assignment operation
- * Arithmetic operations
- * Logical operations
- * Relational operations
- * Priority and associativity rules

In this chapter, we will look at formulas and operators.



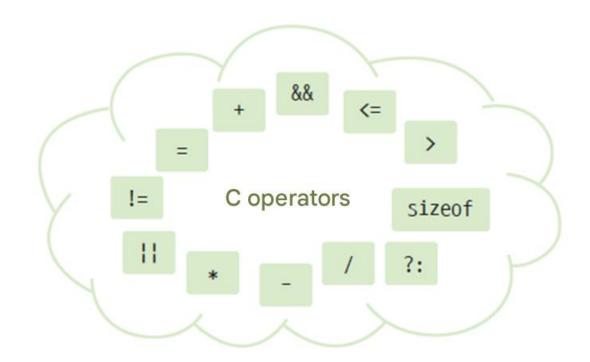
A computer is fundamentally a calculating machine.

The Korea Meteorological Administration uses supercomputers to calculate the weather .

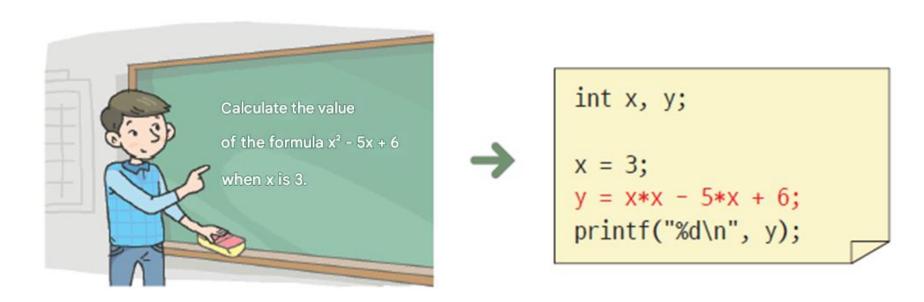


Operators in the C language

- The de facto industry standard
- Modern languages such as Java, C++, Python, and JavaScript use C language operators almost as they are.

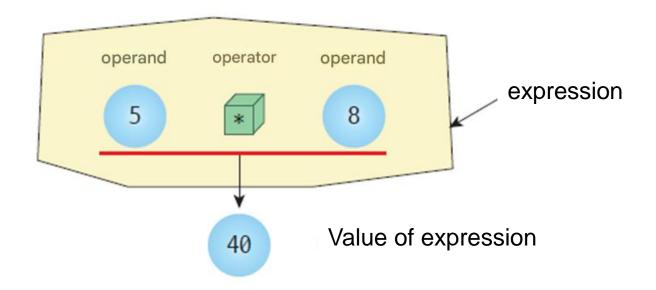


Example of expression

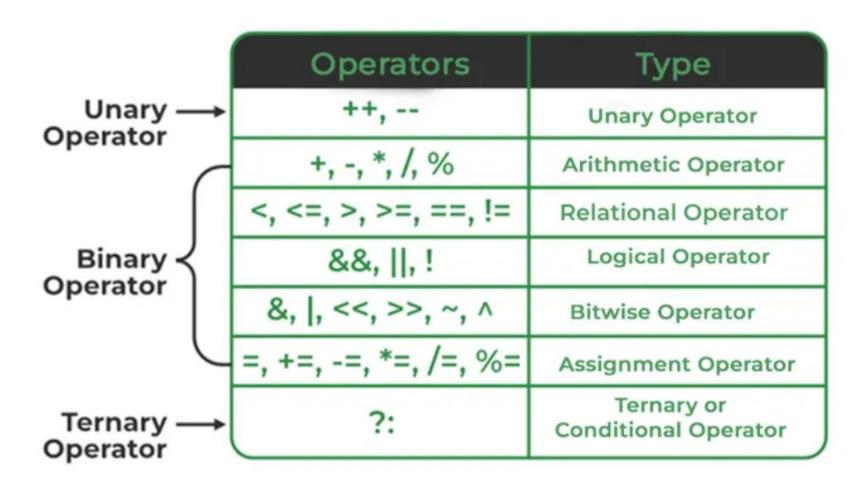


Expression

- expression
 - constants , variables , and operators
 - It is divided into operators and operands.



Classification of operators by function



Arithmetic Operators

- Arithmetic Operations : The Most Basic Operations on a Computer
- Operators that perform basic arithmetic operations such as addition, subtraction, multiplication, and division.

operator	sign	Example of use	result
addition	+	7 + 4	11
subtraction	_	7 – 4	3
multiplication	*	7*4	28
division	/	7 / 4	1
remain	%	7 % 4	3

Examples of arithmetic operators

$$y=mx+b \qquad -\rightarrow y = m*x + b;$$

$$y=ax^2+bx+c \qquad -\rightarrow y = a*x*x + b*x + c;$$

$$m=\frac{x+y+z}{3} \qquad -\rightarrow m = (x+y+z)/3;$$



(Note) What is the exponentiation operator?

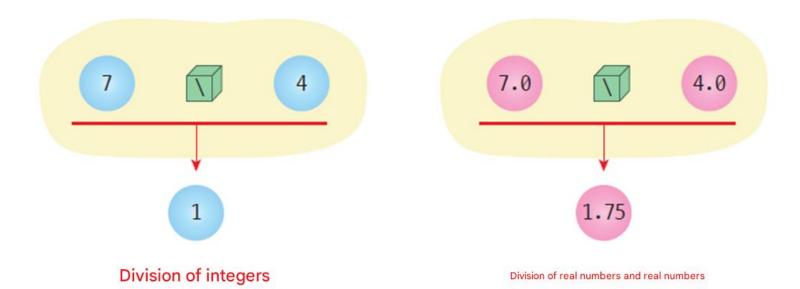
C does not have an operator for exponentiation . Simply multiply the variable twice, like x * x.

Integer arithmetic operations

```
#include < stdio.h >
int main(void)
{
    int x, y, result;
    printf ( " Enter two integers : ");
    scanf( "%d %d" , &x, &y);
    result = x + y;
    printf( "d + d = d", x, y, result);
    result = x - y; // subtraction
    printf( "%d - %d = %d" , x, y, result);
                                                     Enter two integers: 74
    result = x * y; // multiplication
                                                     7 + 4 = 11
    printf( "d + d = d", x, y, result);
                                                     7 - 4 = 3
                                                     7 + 4 = 28
    result = x / y; // division
                                                     7/4 = 1
    printf( "%d / %d = %d" , x, y, result);
                                                     7 % 4 = 3
    result = x % y; // remainder
    printf( "%d %% %d = %d" , x, y, result);
    return 0;
```

Division operator

- Division between integers produces an integer result, and division between floating-point numbers produces a floating-point value.
- In division between integers, the decimal places are discarded.



Real number Arithmetic operations

```
#include < stdio.h >
int main()
    double x, y, result;
     printf ( " Enter two real numbers : ");
    scanf( "%lf %lf", &x, &y);
     result = x + y; // Perform addition operation and assign the result to result
     printf( "%f / %f = %f" , x, y, result);
     result = x / y;
     printf( "%f / %f = %f", x, y, result);
                                                Enter two real numbers: 74
    return 0;
                                                7.000000 + 4.000000 = 11.000000
                                                7.000000 - 4.000000 = 3.000000
                                                7.000000 + 4.000000 = 28.000000
```

7.000000 / 4.000000 = 1.750000

Remainder operator

- The modulus operator calculates the remainder when the first operand is divided by the second operand.
 - 10 % 2 is 0
 - 5 % 7 is 5
 - 30 % 9 is 3
- (Example) Distinguishing between even and odd numbers using the remainder operator
 - Even if x % 2 is 0
- (Example) Determining "multiples of 3" using the remainder operator
 - x % 3 is 0, then it is a multiple of 3

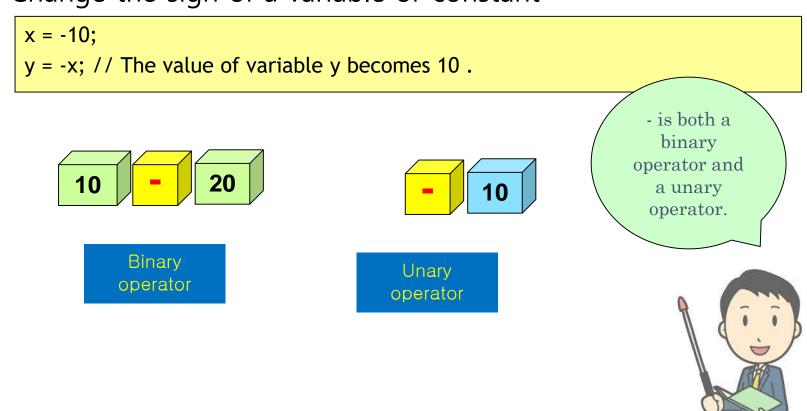


Remainder operator

```
// Remainder operator program
#include < stdio.h >
#define SEC_PER_MINUTE 60 // 1 minute is 60 seconds
int main( void )
                                                                    minute
                                                                               second
{
    int input, minute, second;
    printf ("Please enter seconds : " );
    scanf ("%d", &input); // Read the time in seconds.
    minute = input / SEC_PER_MINUTE; // how many minutes
    second = input % SEC_PER_MINUTE; // how many seconds
    printf ( "%d seconds are %d minutes %d seconds. \n", input, minute, second);
    return 0;
                                      Enter seconds: 1000
                                      1000 seconds is 16 minutes and 40 seconds.
```

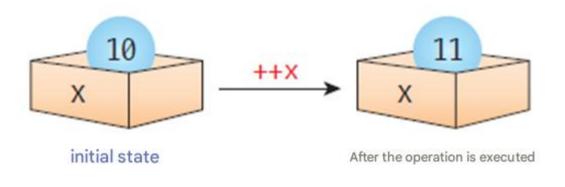
Sign operator

• Change the sign of a variable or constant



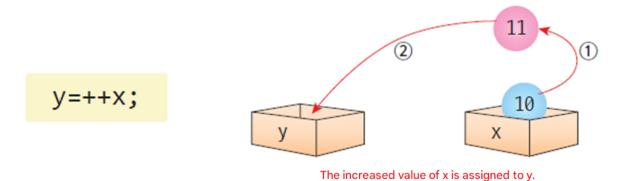
Increment/decrement operator

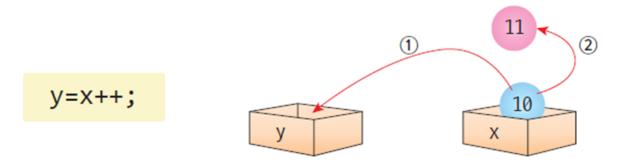
- Increment/decrement operators : ++, --
- Operator that increases or decreases the value of a variable by one.
- (Example) ++x, --x;





Difference between ++x and x++





Substitute first, then increase later.

Increment/decrement operator summary

increment operator	difference	
++χ	The value of the formula is the incremented value.	
χ++	The value of the formula is the original x value that has not been increased.	
χ	The value of the formula is the reduced value.	
χ	The value of the formula is the original, undecreased x-value.	



Example: Increment/decrement operator

```
#include < stdio.h >
int main( void )
                                                           First, the value is increased
{
                                                           and the increased value is
                                                              used in the formula.
  int x=10, y=10;
  printf("x=%d\n", x);
                                                          Use the current value in the
  printf("++x value =%d\n", ++x);
                                                                  formula first
                                                             and increases later.
  printf("x=%d\n\n", x);
  printf("y=%d\n", y);
                                                             x = 10
  printf("value of y++=\%d\n", y++);
                                                             ++x value = 11
  printf("y=%d\n", y);
                                                             x = 11
                                                             y = 10
return 0;
                                                             The value of y++=10
                                                             y = 11
```

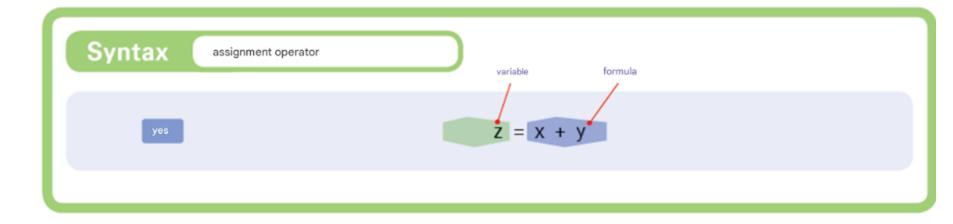
Examples of increment and decrement operators

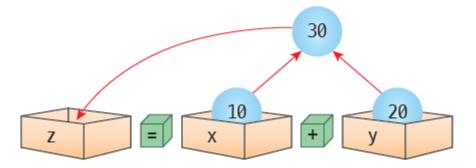
Practice

y = (1 + x++) + 10; // Even if there are parentheses, the increase in the value of x is executed last .

```
x = 10++; // Cannot be applied to constants . 
 y = (x+1)++; // Cannot be applied to formulas .
```

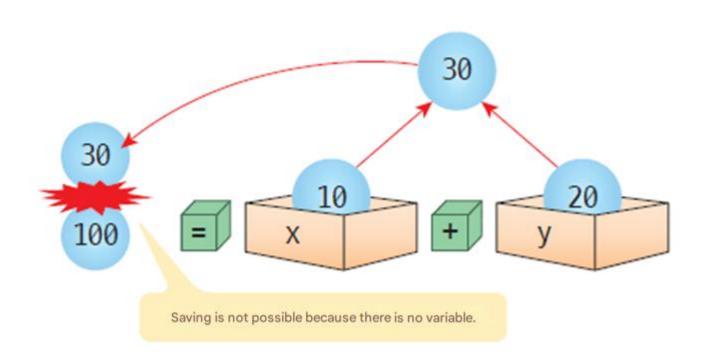
Assignment operator



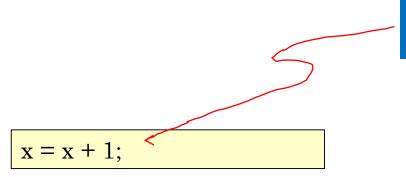


Caution: assignment operators

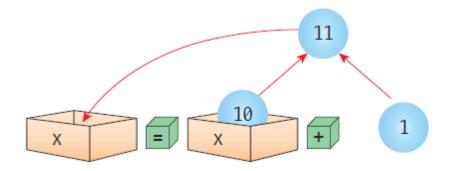
• 100 = x + y; // Compile error!



Caution: assignment operators

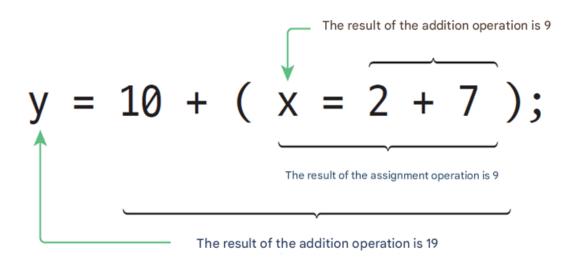


It is a correct statement in C, but mathematically incorrect.



The result of the assignment operation

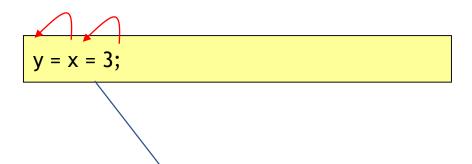
Every operation has a result, and assignment operations also have a result.





The result of the assignment operation is 19 (currently unused)

Next sentence is also possible.



A statement that assigns the same value to multiple variables can be written as follows. Here x = 3 is first performed, and then the resulting value 3 is assigned to y



Example

```
/* Assignment operator program * /
#include < stdio.h >
int main( void )
                                                     X
     int x, y;
     x = 1;
     printf ( "The value of formula x+1 is %d\n", x+1);
     printf ( "The value of the formula y=x+1 is %d\n", y=x+1);
     printf ("The value of the formula y=10+(x=2+7) is %d\n", y=10+(x=2+7));
     printf ( "The value of the formula y=x=3 is %d\n", y=x=3);
     return 0;
                                           The value of the formula x+1 is 2
```

The value of the formula y=x+1 is 2

The value of the formula y=x+1 is 2

The value of the formula y=x+1 is 19

The value of the formula y=x+3 is 3

Compound assignment operator

- A compound assignment operator is an operator that combines an assignment operator = and an arithmetic operator, such as +=.
- You can make the source simpler

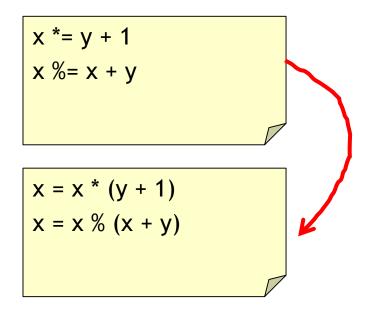
It has the same meaning as x = x + y! x += y

Compound assignment operator

compound assignment operator	meaning	compound assignment operator	meaning
x += y	x = x + y	x &= y	x = x & y
x -= y	x = x - y	x	x = x ¦ y
x *= y	x = x * y	x^=y	x = x ^ y
x /= y	x = x / y	x >>= y	x = x >> y
x%=y	x = x % y	x <<= y	x = x << y

Quiz

• If we solve the following equation and rewrite it, what would it be?





Compound assignment operator

```
// Compound assignment operator program
#include < stdio.h >
int main( void )
{
     int x = 10, y = 10, z = 33;
    x += 1;
    y *= 2;
     z %= 10 + 20;
     printf ( "x = \%d y = \%d z = \%d \n" , x, y, z);
     return 0;
}
                                                          x = 11 \ y = 20 \ z = 3
```

Error

beware of errors

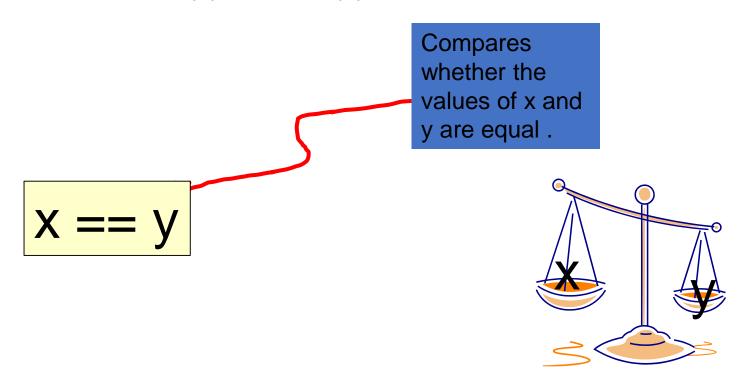
The following formula is incorrect. Why is that?

```
++x = 10; // The left side of the equal sign must always be a variable.
```

$$x + 1 = 20$$
; // The left side of the equal sign must always be a variable.

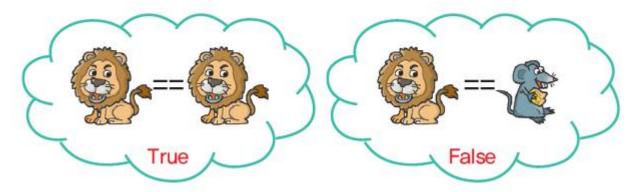
Relational Operators

- Operator that compares two operands
- The result is true (1) or false (0).



Relational Operators

calculation	meaning	calculation	meaning
x == y	Are x and y equal?	x < y	Is x less than y?
x != y	Are x and y different?	x >= y	Is x greater than or equal to y?
x > y	Is x greater than y?	x <= y	Is x less than or equal to y?



Examples of relational operators

```
1 == 1 // true (1)

1!= 2 // true (1)

2 > 1 // true (1)

x >= y // true if x is greater than or equal to y (1), otherwise false (0)
```

Example



```
#include < stdio.h >
int main( void )
{
     int x, y;
     printf ( " Enter two integers : ");
     scanf ( "% d%d " , &x, &y);
     printf ( "The result of x == y : %d\n'', x == y);
     printf ( "The result of x != y : %d\n", x != y);
     printf ( "Result of x > y : %d\n'', x > y);
     printf ( "The result of x < y : %d n ", x < y);
     printf ( "The result of x \ge y : %d n ", x \ge y)
     printf ( "The result of x \leq y : %d\n ", x \leq y)
     return 0;
```

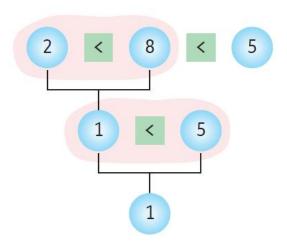
Enter two integers: $3\ 4$ The result of x == y is The result of x != y is The result of x > y is: Result of x < y: The result of x >= y is The result of x <= y is

Caution!

- $\bullet (x = y)$
 - Substitute the value of y into x. The value of this formula is the value of x.
- (x == y)
 - x and y are equal, the value of the formula is 1, otherwise it is 0.
 - Be careful not to use (x == y) and (x = y) incorrectly!

Caution: when using relational operators

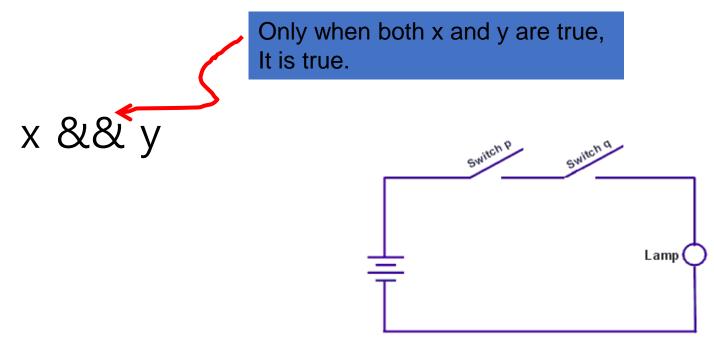
• As in mathematics, 2 < x < 5 and If you write them together, you will get wrong results .



• The right way : (2 < x) && (x < 5)

Logical Operators

- An operator that combines multiple conditions to determine true or false.
- The result is true (1) or false (0).



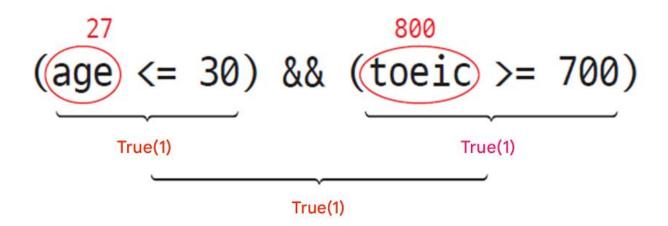
Logical Operators

calculation	meaning	
x && y	AND operation, true if both x and y are true, otherwise false	
x y	OR operation, true if only one of x or y is true, false if both are false	
!x	NOT operation, false if x is true, true if x is false	



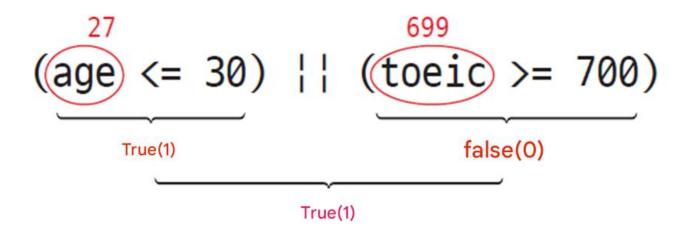
AND operator

 A company is hiring new employees and they set a requirement that the applicants be under 30 years old and have a TOEIC score of 700 or higher.



OR operator

• The conditions for hiring new employees have changed so that they may be under 30 years old or have a TOEIC score of 700 or higher .

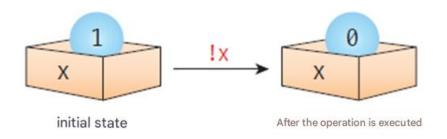


Examples of logical operators

- " Is x one of 1, 2, or 3?"
 - (x == 1) || (x == 2) || (x == 3)
- " x is greater than or equal to 60 and less than 100 ."
 - (x > = 60) && (x < 100)
- " x is neither 0 nor 1 ."
 - $(x != 0) \&\& (x != 1) // x \neq 0 \text{ and } x \neq 1$

NOT operator

• If the value of the operand is true, the result of the operation is made false, and if the value of the operand is false, the result of the operation is made true.



```
result = !1; // 0 is assigned to result .
result = !(2==3); // 1 is assigned to result .
```

How to express truth and false

- If a relational formula or logical formula is true, 1 is generated, and if it is false, 0 is generated.
- It is considered true if it is not 0, and false if it is 0.
- Negative numbers are considered false. (X)
 (Example) When applying the NOT operator (True -> False)

```
!0  // The value of the expression is 1
!3  // The value of the expression is 0
!-3  // The value of the expression is 0
```

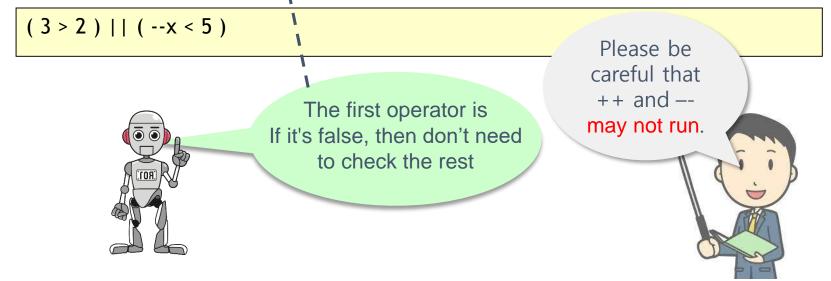
Example

```
#include < stdio.h >
int main( void )
{
     int x, y;
     printf ( " Enter two integers : ");
     scanf ( "%d %d" , &x, &y) ;
     printf ( "%d && %d result : %d", x, y, x && y);
     printf ( "%d || %d result : %d", x, y, x \mid | y);
     printf ( "!%d result : %d", x, !x );
                                                             Enter two integers: 10
     return 0;
                                                             The result of 1 && 0 is: 0
                                                             Result of 1 | | 0:1
                                                             !1 result : 0
```

Shortcut calculation

• For the && operator, if the first operand is false, the other operands are not evaluated.

• For the || operator, if the first operand is true, the other operands are not evaluated.



Lab: Leap year

- Conditions for a leap year
 - The year is divisible by 4.
 - Years divisible by 100 are excluded.
 - A year that is divisible by 400 is a leap year.





Lab: Leap year (2000, 2004, 2008, 2012, 2016, 2020, 2024)

• Expressing the conditions for a leap year in a formula

• ((year % 4 == 0) && (year % 100 != 0)) || (year % 400 == 0)

Are parentheses really necessary?



Parentheses are optional, but they make reading easier.



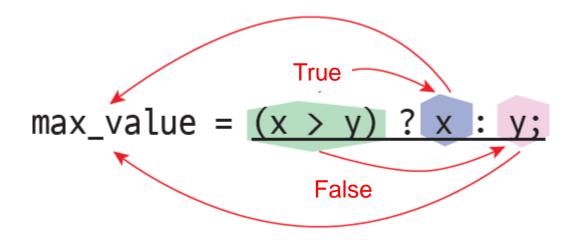


Lab: Leap year

// A leap year is a year in which an extra 29 days are added to February every four years, making it a year of 366 days. #include < stdio.h > int main(void) int year, result; printf (" Enter the year : "); scanf ("%d", &year); <u>result</u> = ((year % 4 == 0) && (year % 100 != 0)) || (year % 400 == 0); printf ("result=%d \n" , result); return 0;

Enter the year : 2012 result=1

Conditional Operator



```
absolute_value = (x > 0) ? x : -x; // Calculate absolute value max_value = (x > y) ? x : y; // Calculate maximum value min_value = (x < y) ? x : y; // Calculate minimum value (age > 20) ? printf ( " Adult \n" ): printf ( " Teenager \n" );
```

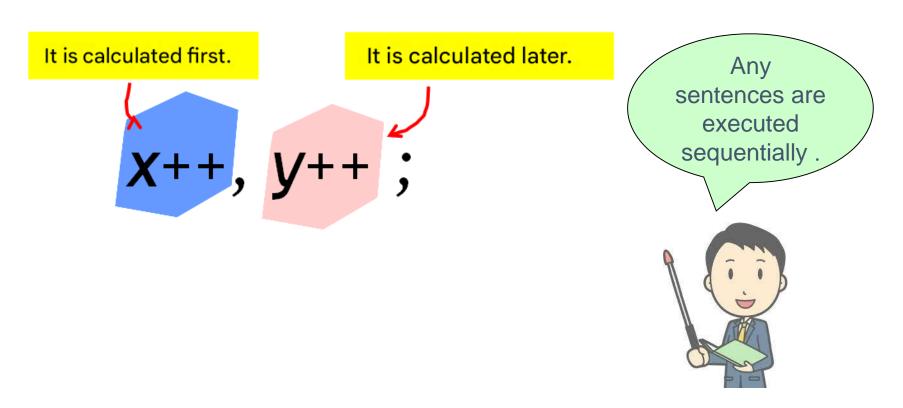
Example

```
Big number = 3
                                                       small number = 2
// Conditional operator program
#include < stdio.h >
int main( void )
{
     int x,y;
     printf("Two integers : " );
     scanf("%d %d", &x, &y);
     printf("large number = %d\n", (x > y) ? x : y);
     printf("small number = %d\n", (x < y) ? x : y);
     return 0;
```

2 integers: 23

comma operator

• Formulas connected by commas are calculated sequentially .



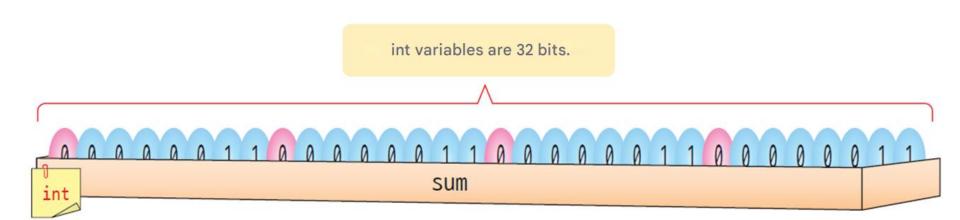
Examples of comma operators

```
x = 2+3, 5-3; // x=2+3 \text{ is executed first .}

printf ("Thank"), printf ("you!\n");

x = 2, y = 3, z = 4;
```

All data is made up of bits.



Bitwise Operator

operator	meaning of operator	yes	
&	bitwise AND	1 if both corresponding bits of the two operands are 10, otherwise 0	
1	bit OR	1 if only one of the corresponding bits of the two operands is 10, otherwise 0	
^	bitwise If the corresponding bits of the two operands have the same value, 0; otherwise, 1.		
<<	move left Shifts all bits to the left by a specified number.		
>>	move_right	move right Shifts all bits to the right by the specified number.	
~	bit NOT	0 becomes 1 and 1 becomes 0.	

Bitwise AND operator

0 AND 0 = 0
1 AND 0 = 0
0 AND 1 = 0
1 AND 1 = 1

```
Variable 1 00000000 00000000 00000000 00001001 (9)
Variable 2 0000000 0000000 0000000 00001010 (10)
```

(variable 1 AND variable 2) 0000000 0000000 0000000 00001000 (8)

Bit OR operator

0 OR 0 = 0
1 OR 0 = 1
0 OR 1 = 1
1 OR 1 = 1

```
Variable 1 00000000 00000000 00000000 00001001 (9)
Variable 2 00000000 00000000 0000000 00001010 (10)
```

(variable1 OR variable2) 00000000 00000000 00000000 00001011 (11)

Bitwise XOR operator

0 XOR 0 = 0
1 XOR 0 = 1
0 XOR 1 = 1
1 XOR 1 = 0

Variable1 00000000 00000000 00000000000001001 (9)
Variable2 0000000 00000000 0000000 00001010 (10)

Bitwise NOT operator

NOT
$$0 = 1$$

NOT 1 = 0

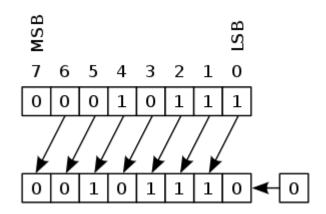
It becomes a negative number because the sign bit is inverted.

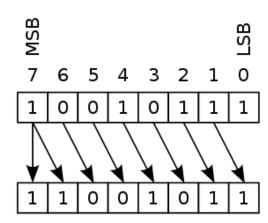
Variable 1 00000000 00000000 00000000 00001001 (9)

(NOT variable 1) 11111111 11111111 1111111 11110110 (-10)

Bit shift operator

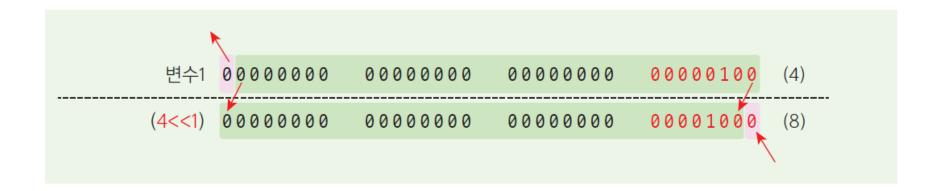
operator	sign	explanation
shift left bit	<<	x < <y bits="" left<="" of="" shift="" spaces="" td="" the="" to="" x="" y=""></y>
shift right bit	>>	x > > y Shift the bits of x y places to_the right





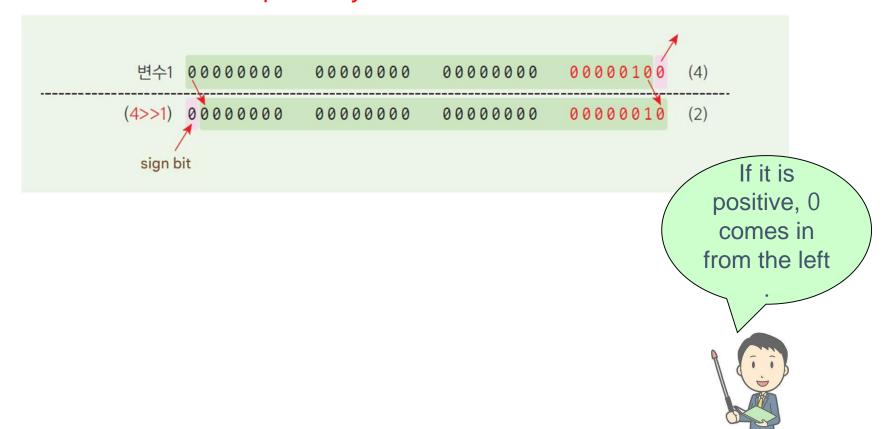
<< operator

- bit left
- The value is doubled



>> operator

- move
- The value is multiplied by 1/2



Example : Bitwise Operators

```
#include < stdio.h >
int main( void )
     printf ("AND: %08X\n", 0x9 & 0xA);
     printf( "OR: \%08X\n", 0x9 \mid 0xA);
     printf( "XOR : %08X\n" , 0x9 ^ 0xA);
     printf ("NOT: %08X\n", ~0x9);
     printf( "<<: %08X\n", 0x4 << 1);
                                                         AND: 00000008
     printf(">>: \%08X\n", 0x4 >> 1);
                                                         OR: 0000000B
                                                         XOR: 00000003
     return 0;
                                                         NOT: FFFFFF6
                                                         <<: 00000008
                                                         >>: 00000002
```

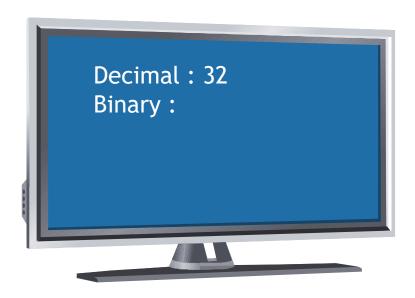
Example : Creating 2 's Complement with Bitwise Operators

```
#include < stdio.h >
int main(void)
  int a = 32;
  a = \sim a; // Make it 1 's complement using NOT operator .
  a = a + 0x01; // add 1.
  printf( "a = \%d \n", a);
  return 0;
```

a = -32

Lab: Outputting decimal to binary

• use bitwise operators to display decimal numbers less than 128 in binary format on the screen.



Lab: Outputting decimal to binary

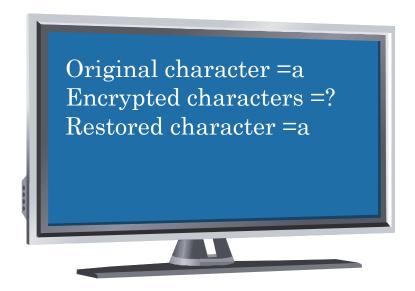
```
#include <stdio.h>
int main( void )
     unsigned int num;
     printf ( " Decimal : " );
     scanf ("%u", &num);
     unsigned int mask = 1 << 7; // mask = 10000000
     printf ( " Binary : " );
     ((num & mask) == 0) ? printf( "0" ) : printf( "1" );
     mask = mask >> 1; // Shift 1 bit to the right.
     ((num & mask) == 0) ? printf( "0" ) : printf( "1" );
     mask = mask >> 1; // Shift 1 bit to the right.
     ((num & mask) == 0) ? printf( "0" ) : printf( "1" );
```

Lab: Outputting decimal to binary

```
mask = mask >> 1; // Shift 1 bit to the right.
((num & mask) == 0) ? printf( "0" ) : printf( "1" );
mask = mask >> 1;
((num & mask) == 0) ? printf( "0" ) : printf( "1" );
mask = mask >> 1;
((num & mask) == 0) ? printf( "0" ) : printf( "1" );
mask = mask >> 1;
((num & mask) == 0) ? printf( "0" ) : printf( "1" );
mask = mask >> 1;
((num & mask) == 0) ? printf( "0" ) : printf( "1" );
printf ( "\n" );
return 0;
```

Lab: Encryption using XOR

• To encrypt a single character, just do $x=x^key$; . Decryption is also possible . $x=x^key$; That's it .

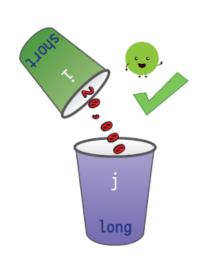


Lab: Encryption using XOR

```
#include < stdio.h >
int main(void)
    char data = 'a';
    char key = 0xff;
    char encrpted_data , orig_data ;
    printf ( " Original character =%c\n", data );
    encrpted_data = data ^ key;
    printf ("Encrypted character =%c \n", encrypted_data);
    orig_data = encrpted_data ^ key;
    printf ( " Restored character =%c\n" , orig_data );
    return 0;
```

Type conversion

• Type conversion is changing the type of data during execution.



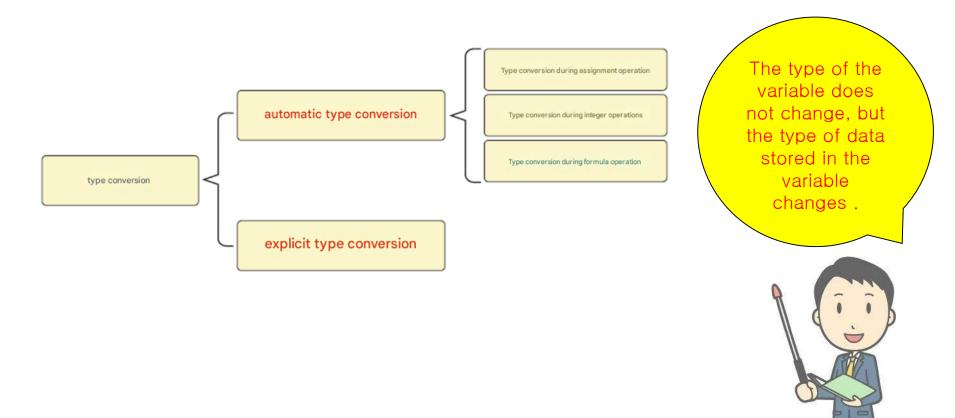


Be careful
because if you do
the conversion
incorrectly, some
of the data may be
lost.
Do it.



Type conversion

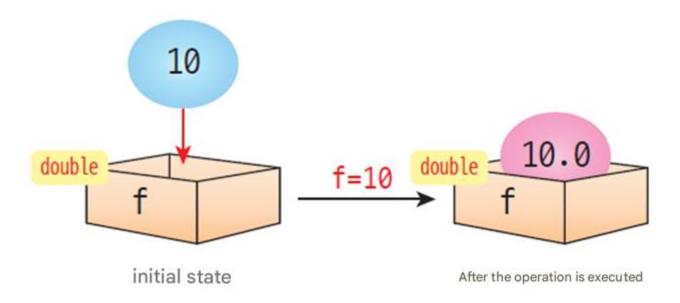
• The type of data is converted during operation.



Automatic type conversion during as signment operations

Upward conversion

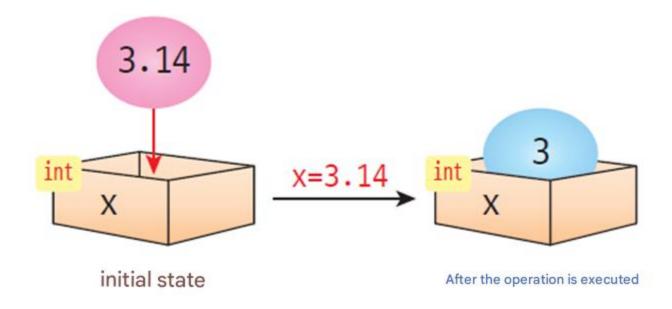
```
double f;
f = 10; // 10.0 is stored in f.
```



Automatic type conversion during as signment operations

Downward conversion

```
int i;
i = 3.141592; // 3 is stored in i .
```

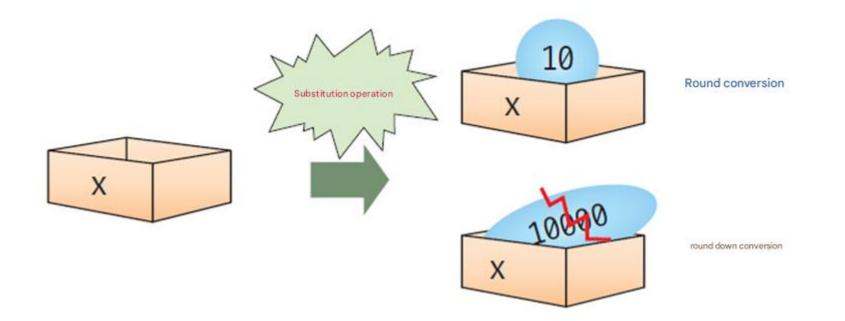


Integer type conversion

```
char x;

x = 10;  // OK

x = 10000;  // upper bytes are gone .
```



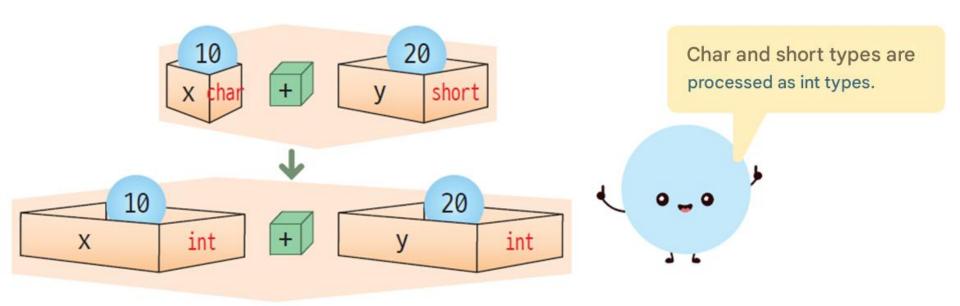
Up and down conversions

```
#include <stdio.h>
int main( void )
    char c;
    int i;
    float f;
    c = 10000;
                // Round down
    i = 1.23456 + 10; // Round down
    f = 10 + 20; // round up
     printf( "c = %d, i = %d, f = %f \n", c, i, f);
    r eturn 0;
```

```
c:\...\convert1.c(10): warning C4305: '=': truncation from 'int' to 'char' c: \...\convert1.c(11): warning C4244: '=': possible loss of data while converting from 'double 'c=16, i=11, f=30.000000
```

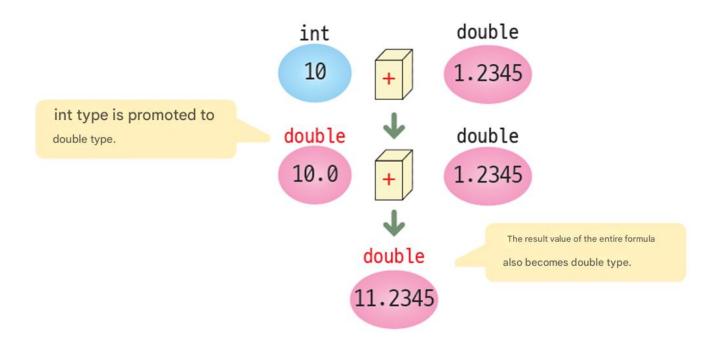
Automatic type conversion when performing integer operations

• When performing integer operations, if the type is char or short, it is automatically converted to int type and then calculated .

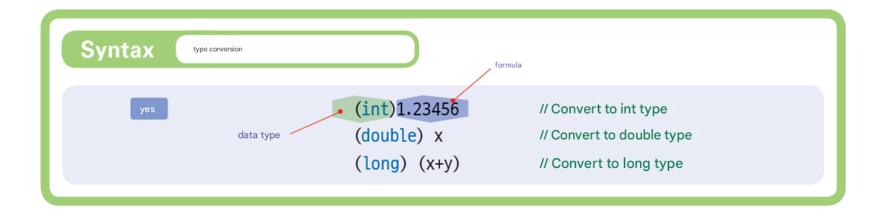


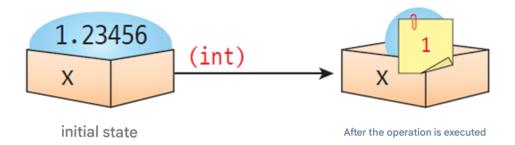
Automatic type conversion in formulas

 When different data types are used together, they are unified into a larger data type.



Explicit type conversion





Example

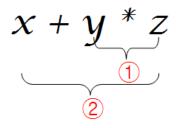
```
#include < stdio.h >
                                                          5/4 becomes 1,
int main( void )
                                                        which becomes 1.0
{
     int i;
     double f;
     f = 5 / 4;
                                                     5 becomes 5.0, so the
     printf ( "%f\n" , f);
                                                       overall result is 1.25
     f = ( double )5 / 4;
     printf ( "%f\n" , f);
     f = 5.0 / 4;
     printf ( "%f\n" , f);
```

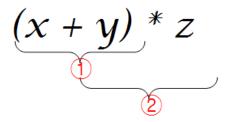
Example

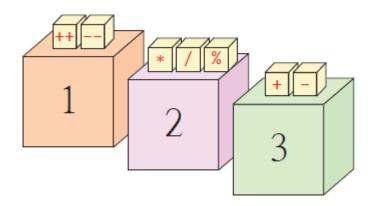
```
f = ( double )5 / ( double )4;
printf ( "%f\n" , f);
                                              1.3 becomes 1 and
i = 1.3 + 1.8;
                                              1.8 also becomes 1,
printf ( "%d\n" , i );
                                             so the final result is 2
i = (int)1.3 + (int)1.8;
printf ( "%d\n" , i );
return 0;
                                             1.000000
                                             1.250000
                                             1.250000
                                             1.250000
```

Priority

• Rules for which operator to evaluate first







Priority

priority	operator	explaration	Combinability
1	++	postfix increment/decrement operator	→(from left to right)
	()	function call	
	[]	array index operator	
	•	Accessing structure members	
	->	Structure pointer access	
	(type){list}	Compound literals (C99 standard)	
2	++	Potential increment/decrement operator	← (right to left)
	+ -	positive and negative signs	
	! ~	Logical negation, bitwise NOT	
	(type)	type conversion	
	*	indirect reference operator	
	&	address extraction operator	
	sizeof	size calculation operator	
	_Alignof	Alignment Requirement Operator (C11 Specification)	

3	* / %	Multiplication, Division, Remainder	
4	+ -	Addition, subtraction	
5	« »	bit shift operator	→(from left to right)
6	< <=	relational operators	
	> >=	relational operators	
7	== !=	relational operators	
8	&	bitwise AND	
9	^	bitwise	
10	I	bit OR	
11	&&	Logical AND operator	
12	H	Logical OR operator	
13	?:	Ternary Conditional Operator	← (right to left)
14	=	assignment operator	
	+= -=	compound assignment operator	
	*= /= %=	compound assignment operator	
	<<= >>=	compound assignment operator	
	&= ^= =	compound assignment operator	
15	,	comma operator	→(from left to right)

General guidelines for priorities

- Comma < Assignment < Logic < Relation < Arithmetic < Unary
- Parentheses operators have the highest precedence.
- All unary operators have higher precedence than binary operators.
- Assignment operators have the lowest precedence, except for the comma operator.
- If you can't remember the precedence of operators, use parentheses.
 - (x <= 10) && (y >= 20)
- Relational and logical operators have lower precedence than arithmetic operators.
 - x + 2 == y + 3
- Relational operators have higher precedence than logical operators. Therefore, you can use sentences like the following with confidence.
 - x > y && z > y // Same as (x > y) && (z > y)

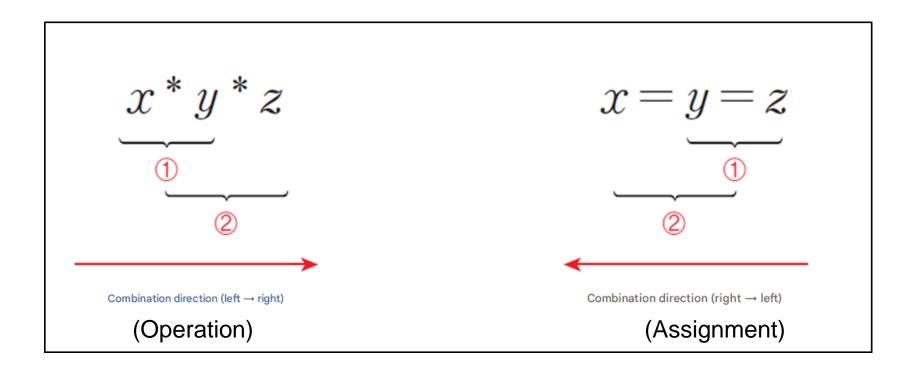
General guidelines for priorities

among logical operators, the && operator has higher precedence than the || operator.

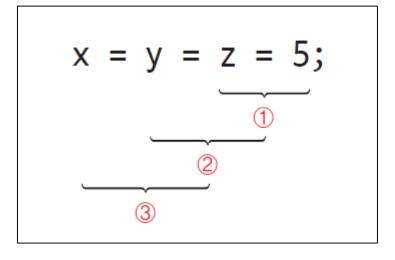
• Sometimes the order of evaluation of operators can be quite confusing. In x * y + w * y It is unclear which of x * y and w * y will be computed first.

Combination Rules

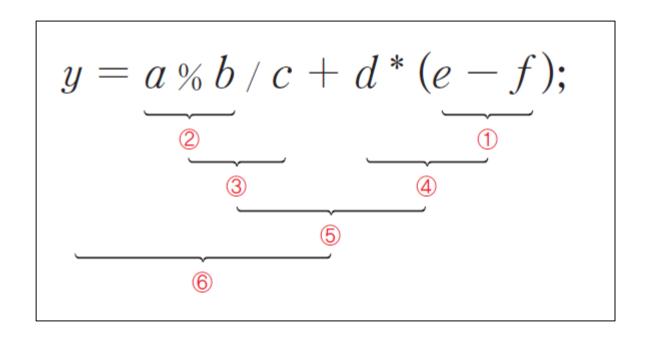
• If there are multiple operators with the same priority, the rule for which one should be performed first



Example of a combination rule



Example of a combination rule



Example

```
#include < stdio.h >
int main( void )
{
     int x=0, y=0;
     int result;
     result = 2 > 3 | | 6 > 7;
     printf ( "%d" , result);
     result = 2 | | 3 \&\& 3 > 2;
     printf ( "%d" , result);
     result = x = y = 1;
     printf ( "%d" , result);
     result = \frac{- ++x + y--}{}
     printf ( "%d" , result);
     return 0;
```

Q & A



