

# Binary Fuse Filters: Fast and Tiny Immutable Filters

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# Probabilistic filters?

- Is  $x$  in the set  $S$ ?
- Maybe or *definitively not*

# Usage scenario?

- We have this expensive *database*. Querying it cost you.
- Most queries should not end up in the data.
- We want a small 'filter' that can prune out queries.

# Theoretical bound

- Given  $N$  elements in the set
- Spend  $k$  bits per element
- Get a false positive rate of  $1/2^k$

# Usual constraints

- Fixed initial capacity
- Difficult to update safely without access to the set
- To get a 1% false-positive rate:  $\approx 8$  bits?

# Hash function

- From any objet in the *universe* to a *word* (e.g., 64-bit word)
- Result looks random

```
uint64_t murmur64(uint64_t h) {  
    h ^= h >> 33;  
    h *= UINT64_C(0xff51afd7ed558ccd);  
    h ^= h >> 33;  
    h *= UINT64_C(0xc4ceb9fe1a85ec53);  
    h ^= h >> 33;  
    return h;  
}
```

# Conventional Bloom filter

- Start with a bitset  $B$ .
- Using  $k$  hash functions  $f_1, f_2, \dots$



# Adding an element

- Given an object  $x$  from the set, set up to  $k$  bits to 1
- $B[f_1(x)] \leftarrow 1, B[f_2(x)] \leftarrow 1, \dots$

# Checking an element

- Given an object  $x$  from the universe, set up to  $k$  bits to 1
- $(B[f_1(x)] = 1) \text{ AND } (B[f_2(x)] = 1) \text{ AND } \dots$

# Checking an element: implementation

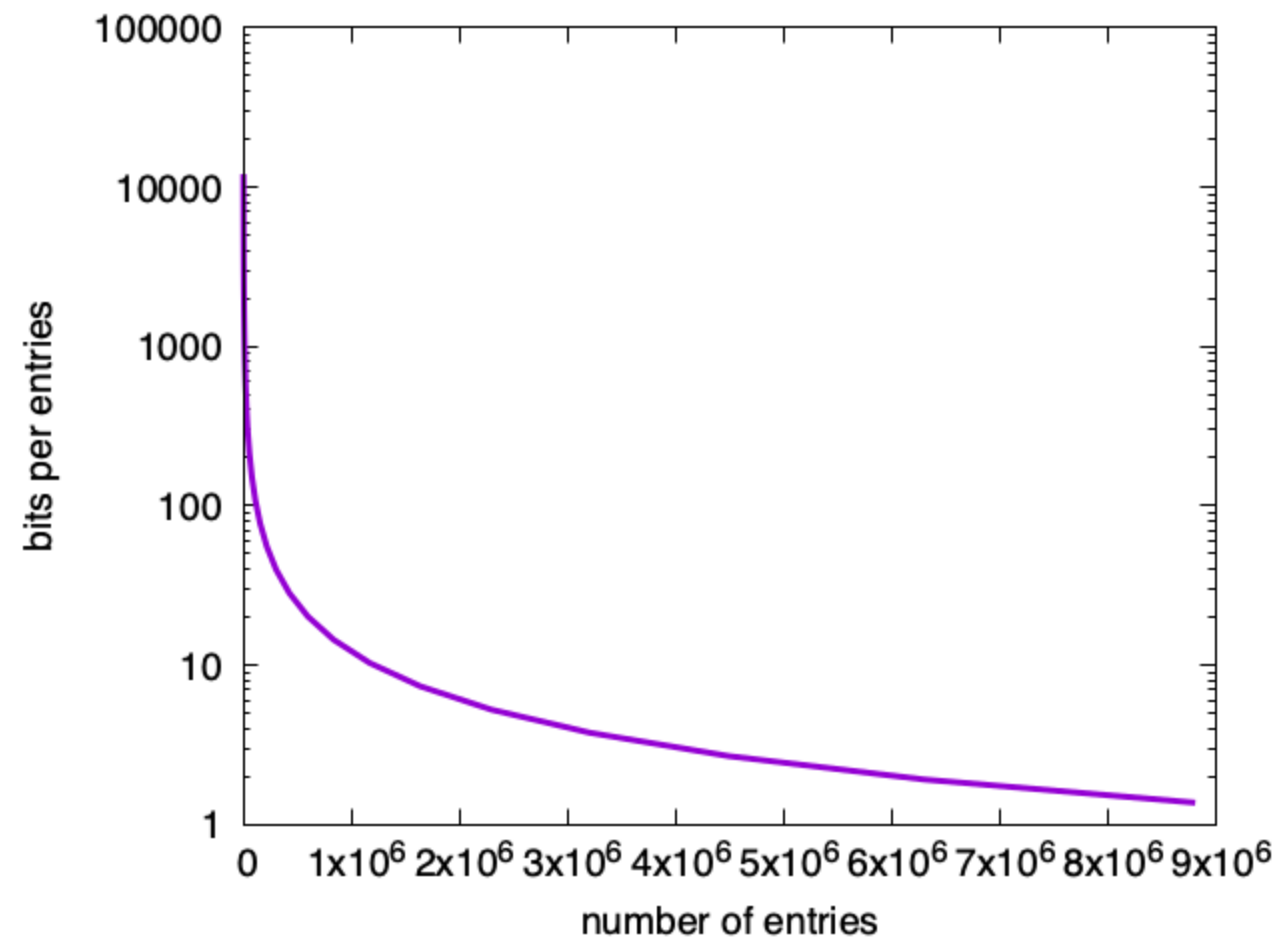
- Typical implementation is *branchy*
- If not  $(B[f_1(x)] = 1)$ , return false
- If not  $(B[f_2(x)] = 1)$ , return false
- ...
- return true

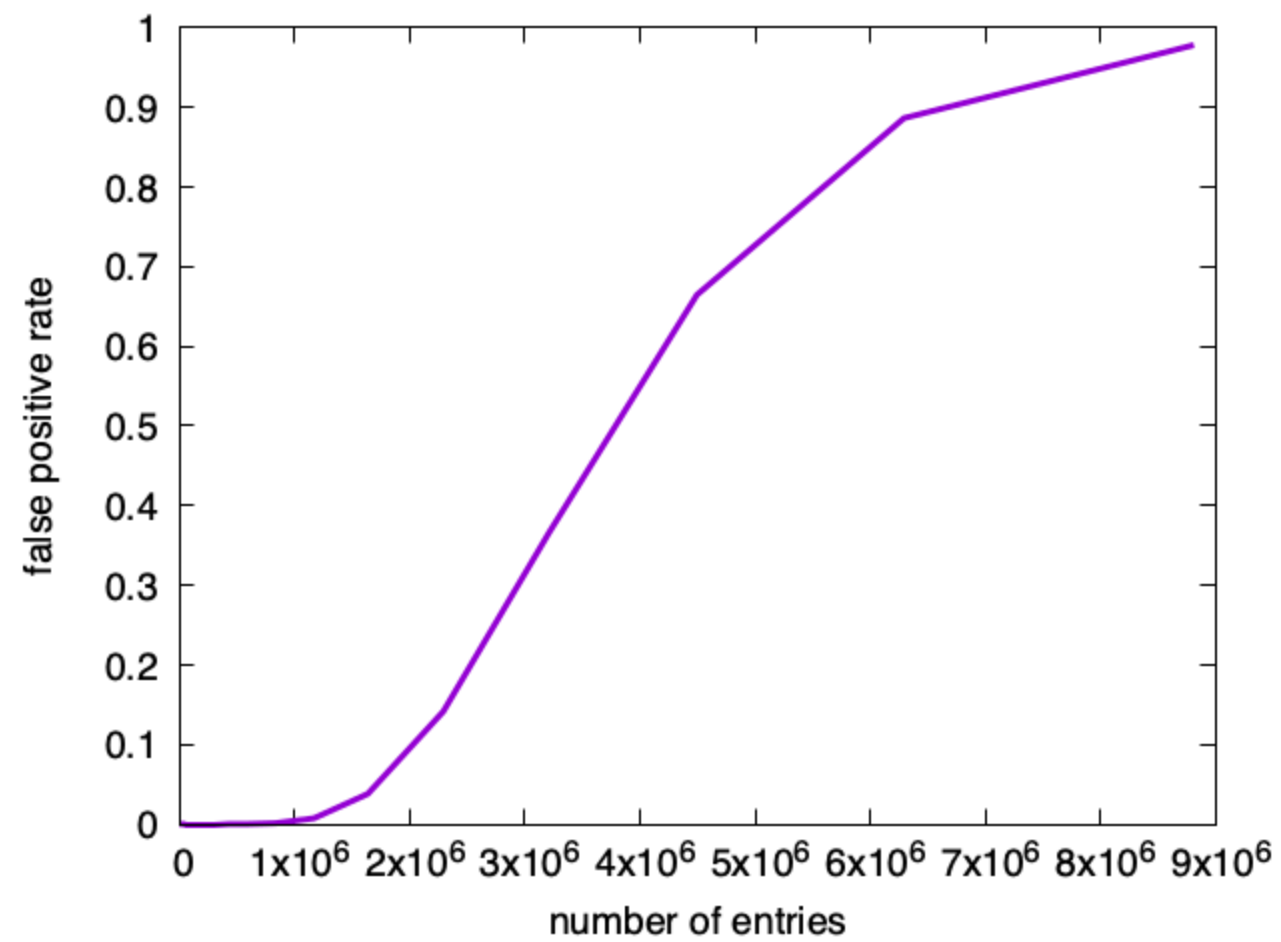
# False positive rate

bits per element	hash functions	fpp
9	6	1.3%
10	7	0.8%
12	8	0.3%
13	9	0.2%
15	10	0.07%
16	11	0.04%

## Bloom filters: upsides

- Fast construction
- Flexible: excess capacity translates into lower false positive rate
- Degrades smoothly to a useless but 'correct' filter

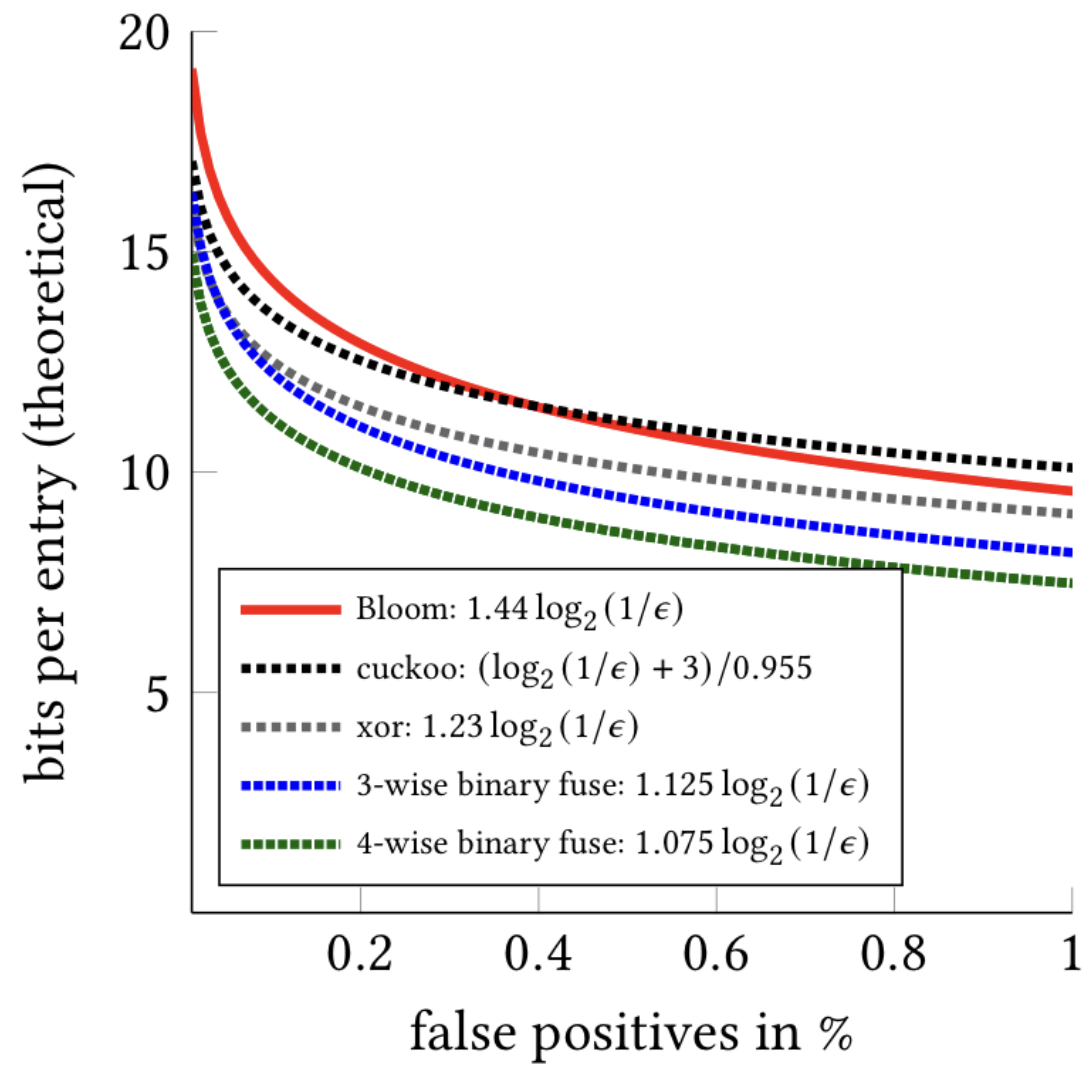




## Bloom filters: downsides

- 44% above the theoretical minimum in storage
- Slower than alternatives (lots of memory accesses)





# Memory accesses

number of hash functions	cache misses (miss)	cache misses (hit)
8	3.5	7.5
11	3.8	10.5

(Intel Ice Lake processor, out-of-cache filter)

# Mispredicted branches

number of hash functions	all out	all in
8	0.95	0.0
11	0.95	0.0

(Intel Ice Lake processor, out-of-cache filter)

# Performance

number of hash functions	always out (cycles/entry)	always in (cycles/entry)
8	135	170
11	140	230

(Intel Ice Lake processor, out-of-cache filter)

## Blocked Bloom filters

- Same as a Bloom filters, but for a given object, put all bits in one cache line
- Optional: Use SIMD instructions to reduce instruction count

## Blocked Bloom filters: pros/cons

- Stupidly fast in both construction and queries
- ~56% above the theoretical minimum in storage

# Binary fuse filters

- Based on theoretical work by Dietzfelbinger and Walzer
- Immutable datastructure: build it once
- Fill it to capacity
- Fast construction
- Fast and simple queries

## Arity : 3-wise, 4-wise

- 3-wise version has three hits, 12% overhead
- 4-wise version has four hits, 8% overhead



## Queries are silly

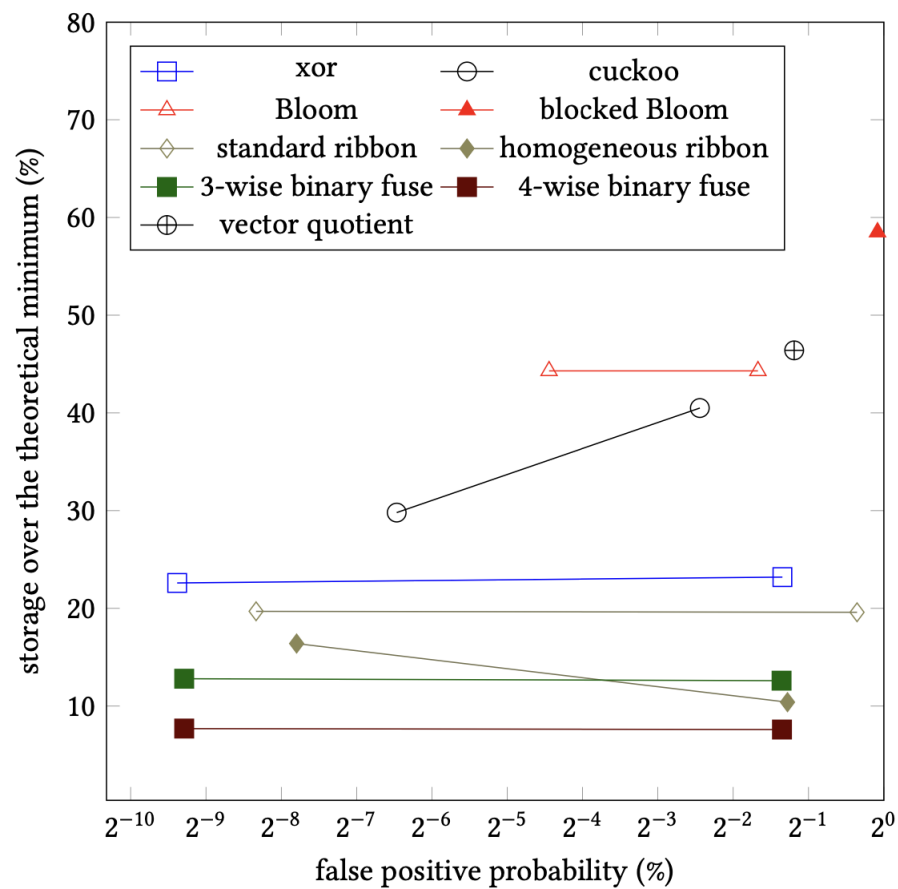
- Have an array of *fingerprints* (e.g., 8-bit words)
- Compute 3 (or 4) hash functions:  $f_1(x)$ ,  $f_2(x)$ ,  $f_3(x)$
- Compute fingerprint function ( $f(x) \rightarrow$  8-bit word)
- Compute XOR and compare with fingerprint:  
$$(B[f_1(x)] = 1) \text{ XOR } (B[f_2(x)] = 1) \text{ XOR } (B[f_3(x)] = 1) = f(x)$$

	<b>cache misses</b>	<b>mispredictions</b>
3-wise binary fuse	2.8	0.0
3-wise binary fuse	3.7	0.0

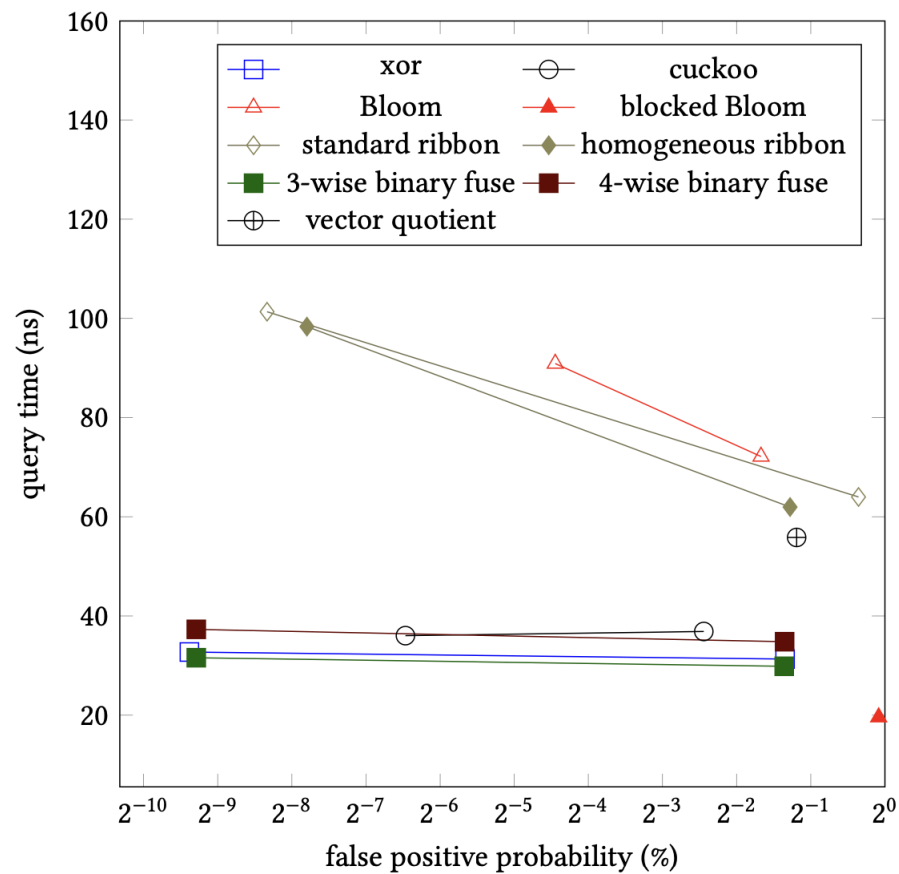
(Intel Ice Lake processor, out-of-cache filter)

	<b>always out (cycles/entry)</b>	<b>always in (cycles/entry)</b>	<b>bits per entry</b>
Bloom $k = 8$	135	170	12
3-wise bin. fuse	85	85	9.0
4-wise bin. fuse	100	100	8.6

(Intel Ice Lake processor, out-of-cache filter)



(a) Relative space usage



(b) Query time

# Construction 1

- Start with array for fingerprints containing slightly more fingerprints than you have elements in the set
- Divide the array into segments (e.g., 300 disjoint)
- Number of fingerprints in segment: power of two (hence *binary*)

## Construction 2

- Map each object  $x$  in set, to locations  $B[f_1(x)], B[f_2(x)], B[f_3(x)]$
- The locations should be in three consecutive segments (so relatively nearby in memory).

## Construction 3

- At the end, each location  $B[i]$  is associated with some number of objects from the set

## Construction 4

- Find a location mapped from a single set element  $x$ , e.g.,  $B[f_1(x)]$
- Record this location which is owned by  $x$
- Remove the mapping of  $x$  to locations  $B[f_1(x)], B[f_2(x)], B[f_3(x)]$
- Repeat



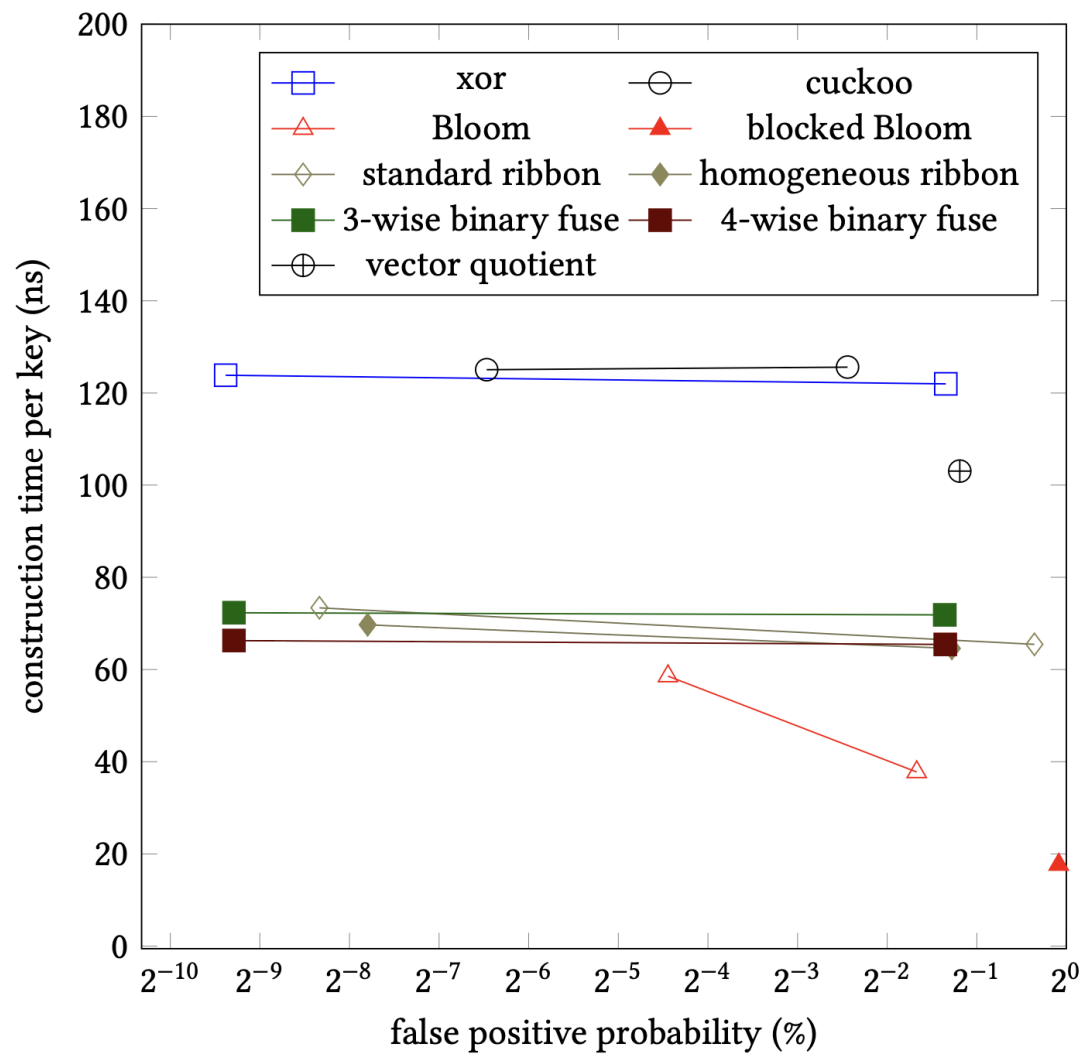
## Construction 5

- Almost always, the construction terminates after one trial
- Go through the matched keys, in reverse order, and set (e.g.)

$$B[f_1(x)] = f(x) \text{ XOR } B[f_2(x)] \text{ XOR } B[f_3(x)]$$

# Construction: Performance

- Implemented naively: terrible performance (random access!!!)
- Before the construction begins, sort the elements of the sets according to the segments they are mapped to.
- This greatly accelerates the construction



# Compressibility

	bits per entry (raw)	bits per entry (zstd)
Bloom $k = 8$	12.0	12.0
3-wise bin. fuse	9.0	8.59
4-wise bin. fuse	8.60	8.39
theory	8.0	8.0

## Some links

- Bloom filters in Go: <https://github.com/bits-and-blooms/bloom>
- Binary fuse filters in Go: <https://github.com/FastFilter/xorfilter>
- Binary fuse filters in C: [https://github.com/FastFilter/xor\\_singleheader](https://github.com/FastFilter/xor_singleheader)
- Binary fuse filters in Java: [https://github.com/FastFilter/fastfilter\\_java](https://github.com/FastFilter/fastfilter_java)
- Giant benchmarking platform: [https://github.com/FastFilter/fastfilter\\_cpp](https://github.com/FastFilter/fastfilter_cpp)

## Other Links

- Blog <https://lemire.me/blog/>
- Twitter: @lemire
- GitHub: <https://github.com/lemire>