

① $3! = 3 \times 2 \times 1 = \underline{\underline{6 \text{ ways}}}$

② 1 out of 5 = 5 ways

③ All 3 are unique \rightarrow permutation.

$3! = 3 \times 2 \times 1 = 6 \text{ ways}$

④
$${}^4C_2 = \frac{4!}{2!(4-2)!}$$

$$= \frac{4 \times 3}{2 \times 1} = \underline{\underline{6 \text{ ways}}}$$

⑤ Total outcomes = 2 (Head, Tail)

$P(\text{Head}) = \underline{\underline{\frac{1}{2}}}$

⑥ Total outcomes = 6 (1 to 6)
 Favourable = 1 (only 1)

$P(1) = \underline{\underline{\frac{1}{6}}}$

⑦ 1st digit: 3 options (1, 2, 3)
 2nd digit: 2 remaining options

$3 \times 2 = 6 \text{ numbers,}$

⑧ Total fruits = 3 + 4 = 7
 Apples = 3

$P(\text{Apple}) = \underline{\underline{\frac{3}{7}}}$

(9) $4! = 4 \times 3 \times 2 \times 1 = \underline{\underline{24 \text{ ways}}}$

(10) Total balls = 5
Green = 2

$$P = \frac{2}{5}$$

(11) 1st digit: 4 options
2nd - 1 - 3 - 1 -
3rd - 1 - 2 - 1 -

$$4 \times 3 \times 2 = \underline{\underline{24 \text{ numbers}}}$$

(12)

$${}^7C_3 = \frac{7!}{3!(7-3)!} = \frac{7 \times 6 \times 5}{3 \times 2 \times 1} = \underline{\underline{35 \text{ ways}}}$$

(13)

Total Cards = 52
Kings in deck = 4 (one/suit)
Favourable outcomes = 4
Total outcomes = 52

$$P = \frac{4}{52} = \underline{\underline{\frac{1}{13}}}$$

(14)

$$5! = 5 \times 4 \times 3 \times 2 \times 1 = \underline{\underline{120 \text{ ways}}}$$

(15)

Total Balls = 6 + 4 = 10
Black Balls = 4

$$P = \frac{4}{10} = \underline{\underline{\frac{2}{5}}}$$

(16)

$${}_4P_3 = \frac{4!}{(4-3)!} = 4 \times 3 \times 2 = \underline{\underline{24 \text{ permutations}}}$$

- (17) Even number in die = 2, 4, 6 \rightarrow Total = 3
Total outcomes = 6

$$P = \frac{3}{6} = \frac{1}{2}$$

- (18) Total letter = 4 (M, A, T, H)
ways to choose = 5

$${}^4C_2 = \frac{4 \times 3}{2 \times 1} = \underline{\underline{6 \text{ ways}}}$$

- (19) Total cards = 52
Hearts = 13

$$P = \frac{13}{52} = \frac{1}{4}$$

- (20) Circular permutation of n people = $(n-1)!$

$$(4-1)! = 3! = 3 \times 2 \times 1 = \underline{\underline{6 \text{ ways}}}$$

- (21) Digits : 1, 2, 3, 4, 5.

Even digits : 2 & 4 \rightarrow only these can be the last digit

• Case 1 : 2 \rightarrow 3 digits from remaining {1, 3, 4, 5}
 ${}_4P_3 = 4 \times 3 \times 2 = 24$

• Case 2 : 4 \rightarrow 3 digits from remaining {1, 2, 3, 5}
 ${}_4P_3 = 24$

$$\text{Total} = 24 + 24 = \underline{\underline{48}}$$

(22)

$$\text{Total Balls} = 3 + 4 + 5 = 12$$

ways to choose 2 balls from 12:

$${}^{12}C_2 = \frac{12 \times 11}{2} = 66$$

2 green balls from 5:

$${}^5C_2 = \frac{5 \times 4}{2} = 10$$

$$\text{probability} = P = \frac{10}{66} = \frac{5}{33}$$

(23)

Total arrangements of 5 students.

$$5! = 120$$

ways to arrange 4 students: $4! = 24$.

The 2 students can switch $2! = 2$

$$\text{Together} = 4! \times 2$$

$$= 24 \times 2$$

$$= 48$$

So, number of ways they are not together
 $120 - 48 = 72$ ways

(24)

Case 1: 2w, 2m

$${}^8C_2 \times {}^{10}C_2 = 28 \times 45 = 1260$$

Case 2: 3w, 1m

$${}^8C_3 \times {}^{10}C_1 = 56 \times 10 = 560$$

case 3:

$$8_{C_4} = 70$$

$$1260 + 560 + 70 = \underline{\underline{1890 \text{ ways}}}$$

(15)

Total outcomes = $6 \times 6 = 36$
Pairs that sum to 7

$(1,6), (2,5), (3,4), (4,3), (5,2), (6,1)$

$$P(\text{sum} = 7) = \frac{6}{36} = \underline{\underline{\frac{1}{6}}}$$