1

ASSIGNMENT 8

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Download all python codes from

https://github.com/Sowmyabandi99/Assignment9/blob/main/assignment9.py

Latex-tikz codes from

https://github.com/Sowmyabandi99/Assignment9/blob/main/main.tex

1 Question No 2.50

Balance the following chemical equation.

$$NaOH + H_2SO_4 \rightarrow Na_2SO_4 + H_2O$$
 (1.0.1)

2 SOLUTION

Let the balanced version of (1.0.1) be

$$x_1 NaOH + x_2 H_2 S O_4 \rightarrow x_3 Na_2 S O_4 + x_4 H_2 O$$
 (2.0.1)

which results in the following equations:

$$(x_1 - 2x_3)Na = 0 (2.0.2)$$

$$(x_1 + 4x_2 - 4x_3 - x_4)O = 0 (2.0.3)$$

$$(x_1 + 2x_2 - 2x_4)H = 0 (2.0.4)$$

$$(x_2 - x_3)S = 0 (2.0.5)$$

which can be expressed as

$$x_1 + 0.x_2 - 2x_3 + 0.x_4 = 0 (2.0.6)$$

$$x_1 + 4x_2 - 4x_3 - x_4 = 0 (2.0.7)$$

$$x_1 + 2x_2 + 0.x_3 - 2x_4 = 0 (2.0.8)$$

$$0.x_1 + x_2 - x_3 + 0.x_4 = 0 (2.0.9)$$

resulting in the matrix equation

$$\begin{pmatrix} 1 & 0 & -2 & 0 \\ 1 & 4 & -4 & -1 \\ 1 & 2 & 0 & -2 \\ 0 & 1 & -1 & 0 \end{pmatrix} \mathbf{x} = \mathbf{0}$$
 (2.0.10)

where,

$$\mathbf{x} = \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{pmatrix} \tag{2.0.11}$$

(2.0.10) can be reduced as follows:

$$\begin{pmatrix}
1 & 0 & -2 & 0 \\
1 & 4 & -4 & -1 \\
1 & 2 & 0 & -2 \\
0 & 1 & -1 & 0
\end{pmatrix}
\xrightarrow{R_2 \leftarrow R_2 - R_1}
\begin{pmatrix}
1 & 0 & -2 & 0 \\
0 & 4 & -2 & -1 \\
0 & 2 & 2 & -2 \\
0 & 1 & -1 & 0
\end{pmatrix}$$
(2.0.12)

$$\stackrel{R_2 \leftarrow \frac{R_2}{4}}{\longleftrightarrow} \begin{pmatrix}
1 & 0 & -2 & 0 \\
0 & 1 & -\frac{1}{2} & -\frac{1}{4} \\
0 & 2 & 2 & -2 \\
0 & 1 & -1 & 0
\end{pmatrix}$$
(2.0.13)

$$\begin{array}{c}
R_3 \leftarrow R_3 - 2R_2 \\
R_4 \leftarrow R_4 - R_2
\end{array}
\begin{pmatrix}
1 & 0 & -2 & 0 \\
0 & 1 & -\frac{1}{2} & -\frac{1}{4} \\
0 & 0 & 3 & -\frac{3}{2} \\
0 & 0 & -\frac{1}{2} & \frac{1}{4}
\end{pmatrix}$$
(2.0.14)

$$\stackrel{R_3 \leftarrow \frac{R_3}{3}}{\longleftrightarrow} \begin{pmatrix}
1 & 0 & -2 & 0 \\
0 & 1 & -\frac{1}{2} & -\frac{1}{4} \\
0 & 0 & 1 & -\frac{1}{2} \\
0 & 0 & -\frac{1}{2} & \frac{1}{4}
\end{pmatrix}$$
(2.0.15)

$$\begin{array}{c}
\stackrel{R_2 \leftarrow R_2 + \frac{R_3}{2}}{\longleftrightarrow} \begin{pmatrix}
1 & 0 & -2 & 0 \\
0 & 1 & 0 & -\frac{1}{2} \\
0 & 0 & 1 & -\frac{1}{2} \\
0 & 0 & 0 & 0
\end{pmatrix}$$
(2.0.16)

$$\stackrel{R_1 \leftarrow R_1 + 2R_3}{\longleftrightarrow} \begin{pmatrix}
1 & 0 & 0 & -1 \\
0 & 1 & 0 & -\frac{1}{2} \\
0 & 0 & 1 & -\frac{1}{2} \\
0 & 0 & 0 & 0
\end{pmatrix}$$
(2.0.17)

Thus,

$$x_1 = x_4, x_2 = \frac{1}{2}x_4, x_3 = \frac{1}{2}x_4$$
 (2.0.18)

$$x_1 = x_4, x_2 = \frac{1}{2}x_4, x_3 = \frac{1}{2}x_4$$
 (2.0.18)

$$\implies \mathbf{x} = x_4 \begin{pmatrix} 1 \\ \frac{1}{2} \\ \frac{1}{2} \\ 1 \end{pmatrix}$$
 (2.0.19)

by substituting $x_4 = 2$

$$\mathbf{x} = \begin{pmatrix} 2\\1\\1\\2 \end{pmatrix} \tag{2.0.20}$$

Hence, (2.0.1) finally becomes

$$2NaOH + H_2SO_4 \rightarrow Na_2SO_4 + 2H_2O$$
 (2.0.21)