

ESCOM - IPN

FUNDAMENTOS DE DISEÑO DIGITAL - 2CM2

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# Minimización Algebraíca

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## Reporte 2

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# 1. Comparador de Magnitud

## 1.1. Parte Teórica

ABCD	a	b	c	d	e	f	g
0000	1	1	1	1	1	1	0
0001	0	1	1	0	0	0	0
0010	1	1	0	1	1	0	1
0011	1	1	1	0	0	1	1
0100	0	1	1	0	0	1	1
0101	1	0	1	1	0	1	1
0110	1	0	1	0	0	1	1
0111	1	1	1	0	0	1	1
1000	1	1	1	1	1	1	1
1001	1	1	1	0	1	1	1
1010	x	x	x	x	x	x	x
1011	x	x	x	x	x	x	x
1100	x	x	x	x	x	x	x
1101	x	x	x	x	x	x	x
1110	x	x	x	x	x	x	x
1111	x	x	x	x	x	x	x

$$a = \sum (0, 2, 3, 5, 7, 8, 9) + \bar{F} (10-15)$$

$$b = \sum (0, 1, 2, 3, 4, 7, 8, 9) + \bar{F} (10-15)$$

$$c = \sum (0, 1, 3, 4, 5, 6, 7, 8, 9) + \bar{F} (10-15)$$

$$d = \sum (0, 2, 3, 5, 6, 8) + \bar{F} (10-15)$$
  

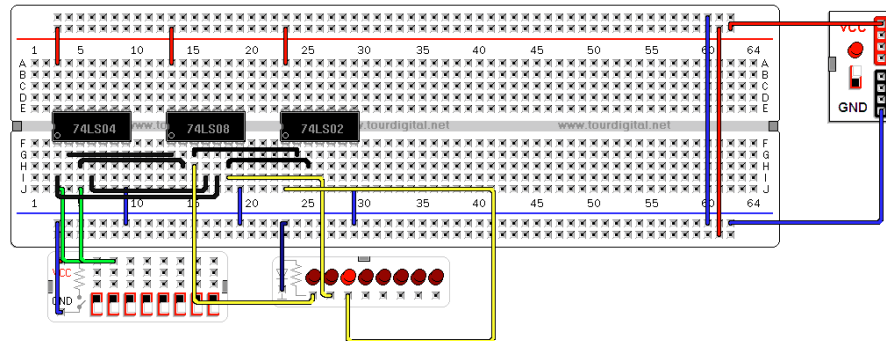
$$a = \bar{B}\bar{D} + A + C + BD$$

$$b = A + \bar{B} + \bar{C}\bar{D}$$

$$c = A + B + D + \bar{C}$$

$$d = A + \bar{B}\bar{D} + B\bar{C}D + \bar{B}C + C\bar{D}$$

## 1.2. Parte Practica



## 2. De Código Binario a Código Grey

### 2.1. Parte Teórica

Binario  $\rightarrow$  C. Grey

BIN $A_3 A_2 A_1 A_0$ $B_3 B_2 B_1 B_0$	GREY $G_3 G_2 G_1 G_0$
0 0 0 0	0 0 0 0
0 0 0 1	0 0 0 1
0 0 1 0	0 0 1 1
0 0 1 1	0 0 1 0
0 1 0 0	0 1 1 0
0 1 0 1	0 1 1 1
0 1 1 0	0 1 0 1
0 1 1 1	0 1 0 0
1 0 0 0	1 1 0 0
1 0 0 1	1 1 0 1
1 0 1 0	1 1 1 1
1 0 1 1	1 1 1 0
1 1 0 0	1 0 1 0
1 1 0 1	1 0 1 1
1 1 1 0	1 0 0 1
1 1 1 1	1 0 0 0

$$G_3 = A\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}D + A\bar{B}C\bar{D} + A\bar{B}CD + A\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}D + A\bar{B}C\bar{D} + A\bar{B}CD$$

$$= A(\bar{B}\bar{C}\bar{D} + \bar{B}\bar{C}D + \bar{B}C\bar{D} + \bar{B}CD + B\bar{C}\bar{D} + B\bar{C}D + BC\bar{D} + BCD)$$

$$= A(\bar{B}\bar{C}(\bar{D}+D) + \bar{B}C(\bar{D}+D) + B\bar{C}(\bar{D}+D) + BC(\bar{D}+D))$$

$$= A(\bar{B}\bar{C} + \bar{B}C + B\bar{C} + BC)$$

$$= A(\bar{B}(\bar{C}+C) + B(\bar{C}+C))$$

$$= A(\bar{B} + B) = A$$

$$G_2 = \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}CD + A\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}D + A\bar{B}C\bar{D} + A\bar{B}CD$$

$$= \bar{A}\bar{B}(\bar{C}\bar{D} + \bar{C}D + C\bar{D} + CD) + A\bar{B}(\bar{C}\bar{D} + \bar{C}D + C\bar{D} + CD)$$

$$= \bar{A}\bar{B}(\bar{C}(\bar{D}+D) + C(\bar{D}+D)) + A\bar{B}(\bar{C}(\bar{D}+D) + C(\bar{D}+D))$$

$$= \bar{A}\bar{B} + A\bar{B}$$

$$G_1 = \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}CD + A\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}D + A\bar{B}C\bar{D} + A\bar{B}CD$$

$$= \bar{A}(\bar{B}\bar{C}\bar{D} + \bar{B}\bar{C}D + \bar{B}C\bar{D} + \bar{B}CD) + A(\bar{B}\bar{C}\bar{D} + \bar{B}\bar{C}D + \bar{B}C\bar{D} + \bar{B}CD)$$

$$= \bar{A}(\bar{B}\bar{C}(\bar{D}+D) + \bar{B}C(\bar{D}+D)) + A(\bar{B}\bar{C}(\bar{D}+D) + \bar{B}C(\bar{D}+D))$$

$$= \bar{A}(\bar{B}\bar{C} + \bar{B}C) + A(\bar{B}\bar{C} + \bar{B}C)$$

$$= \bar{B}\bar{C} + \bar{B}C$$

$$G_0 = \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}CD + A\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}D + A\bar{B}C\bar{D} + A\bar{B}CD$$

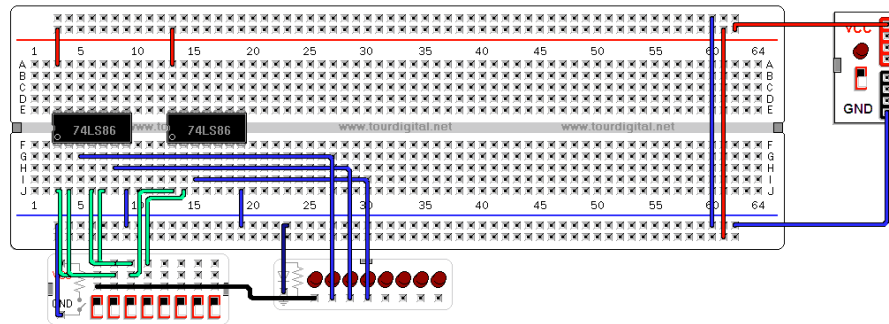
$$= \bar{A}\bar{B}(\bar{C}\bar{D} + \bar{C}D + C\bar{D} + CD) + A\bar{B}(\bar{C}\bar{D} + \bar{C}D + C\bar{D} + CD)$$

$$= \bar{A}\bar{B}(\bar{C}(\bar{D}+D) + C(\bar{D}+D)) + A\bar{B}(\bar{C}(\bar{D}+D) + C(\bar{D}+D))$$

$$= \bar{A}\bar{B}(\bar{C} + C) + A\bar{B}(\bar{C} + C)$$

$$= \bar{C}\bar{D} + \bar{C}D$$

## 2.2. Parte Practica



### 3. De Código BCD a 7 Segmentos

#### 3.1. Parte Teórica

ABCD	a	b	c	d	e	f	g
0000	1	1	1	1	1	1	0
0001	0	1	1	0	0	0	0
0010	1	1	0	1	1	0	1
0011	1	1	1	1	0	0	1
0100	0	1	1	0	0	1	1
0101	1	0	1	1	0	1	1
0110	1	0	1	0	1	1	1
0111	1	1	1	0	1	1	1
1000	1	1	1	1	1	1	1
1001	1	1	1	0	1	1	1
1010	x	x	x	x	x	x	x
1011	x	x	x	x	x	x	x
1100	x	x	x	x	x	x	x
1101	x	x	x	x	x	x	x
1110	x	x	x	x	x	x	x
1111	x	x	x	x	x	x	x

$$a = \sum (0, 2, 3, 5, 7, 8, 9) + \Phi (10-15)$$

$$c = \sum (0, 1, 3, 4, 5, 6, 7, 8, 9) + \Phi (10-15)$$

$a = \bar{B}D + A + C + BD$

$c = A + B + D + \bar{C}$

$b = A + \bar{B} + \bar{C}D$

$d = A + \bar{B}D + B\bar{C}D + \bar{B}C + \bar{C}D$

$$e = \Sigma(0, 2, 6, 8) + \Phi(10-15)$$

CD \ AB	AB			
	00	01	11	10
00	1	0	x	1
01	0	0	1	0
11	0	x	1	x
10	1	1	x	x

$$e = \bar{B}\bar{D} + C\bar{D}$$

$$f = \Sigma(0, 4, 5, 6, 8, 9) + \Phi(10-15)$$

CD \ AB	AB			
	00	01	11	10
00	1	1	x	1
01	0	1	x	1
11	0	0	x	x
10	0	x	x	x

$$f = \bar{C}\bar{D} + B\bar{C} + A$$

$$g = \Sigma(2, 3, 4, 5, 6, 8, 9) + \Phi(10-15)$$

CD \ AB	AB			
	00	01	11	10
00	0	1	1	1
01	0	1	1	1
11	1	0	x	x
10	1	1	x	x

$$g = C\bar{D} + \bar{B}C + A + B\bar{C}$$

## 3.2. Parte Practica

