

warmXtrophic Project: Specific Leaf Area (SLA) Analyses

Phoebe Zarnetske

June 29, 2021

Load in packages & data

```
# Clear all existing data
rm(list = ls())

# Load packages
library(tidyverse)
library(bbmle)
library(lmerTest)
library(fitdistrplus)
library(lme4)
library(car)

# Set ggplot2 plotting This code for ggplot2 sets the theme to mostly black and
# white (Arial font, and large font, base size=24)
theme_set(theme_bw(14))
theme_update(axis.text.x = element_text(size = 12, angle = 90), axis.text.y = element_text(size = 12))

# Set working directory to Google Drive
setwd("/Volumes/GoogleDrive/Shared drives/SpaCE_Lab_warmXtrophic/data/")

# Read in data
sla <- read.csv("./L1/SLA/SLA_L1.csv")
```

Check what species are measured at each site

```
unique(sla$species)

## [1] "Dasp" "Popr" "Cest" "Hisp" "Soca" "Ruac"

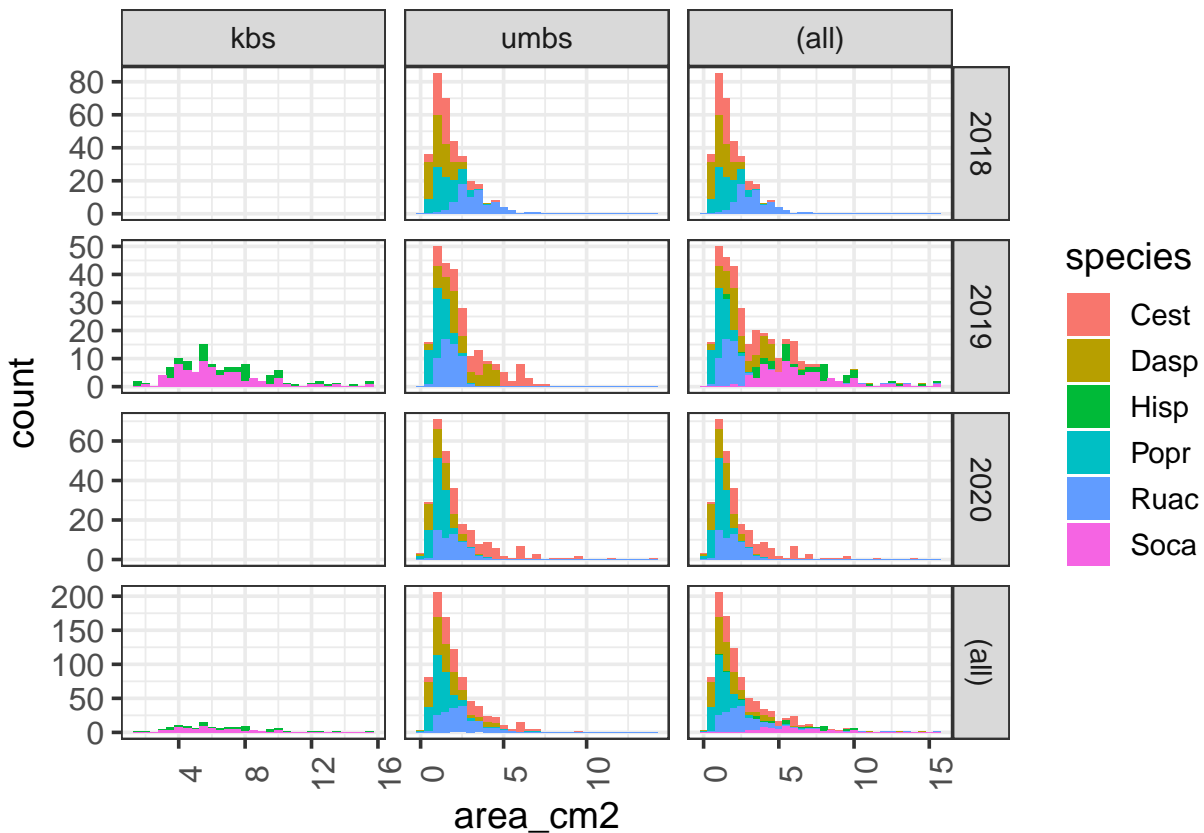
with(sla, table(sla$site, sla$species))

##
##      Cest Dasp Hisp Popr Ruac Soca
## kbs      0   0  41    0   0   73
## umbs  233 205   0  219 185   0
```

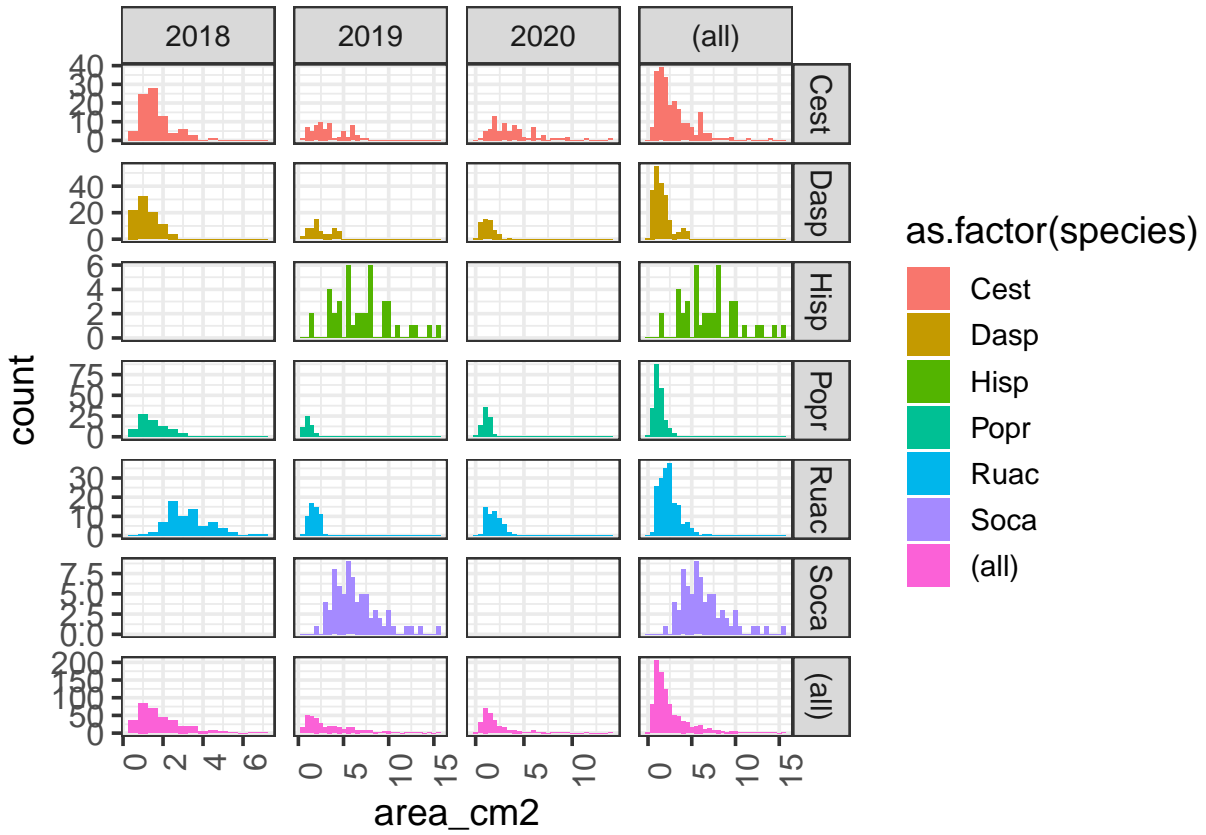
Each species is only at one site, so for now don't make separate dataframes (just use species as fixed effect)

Data exploration - some different ways of visualizing these data

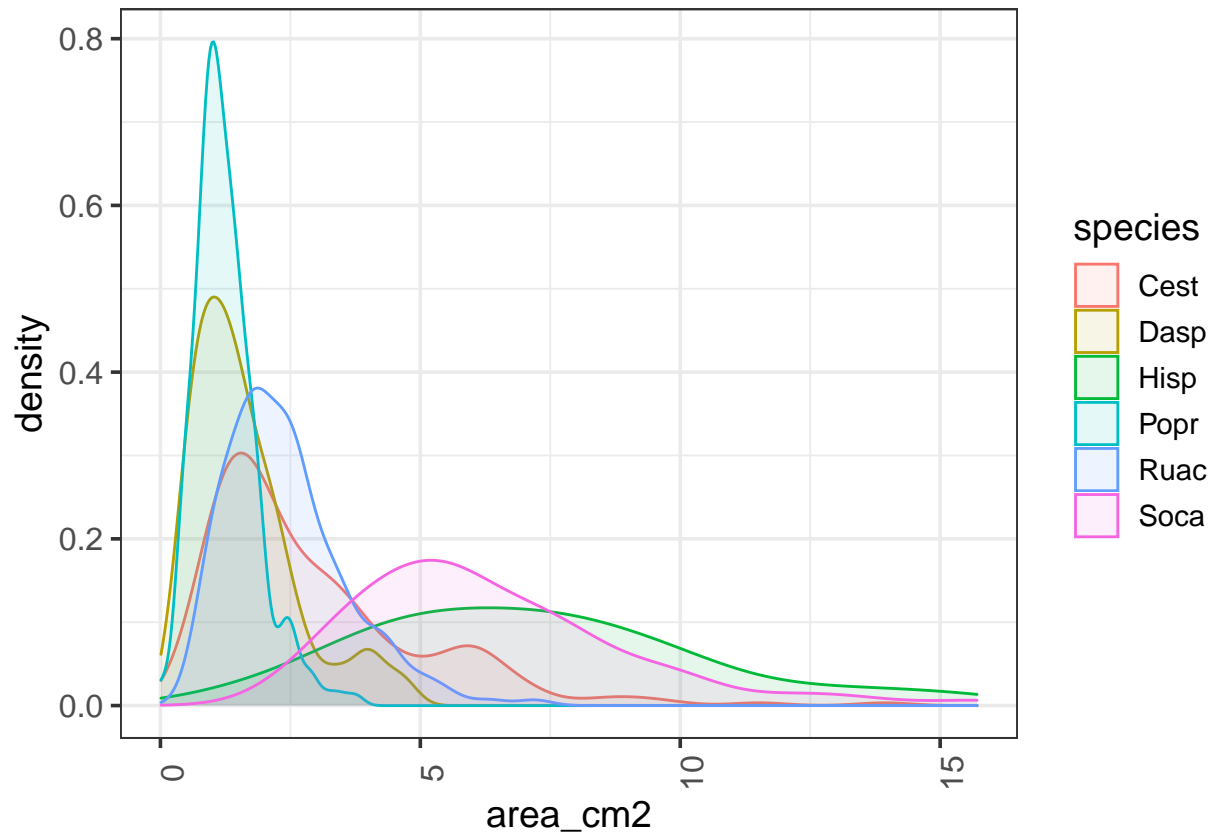
```
ggplot(sla, aes(area_cm2, fill = species)) + geom_histogram(binwidth = 0.5) + facet_grid(year ~ site, margins = TRUE, scales = "free")
```



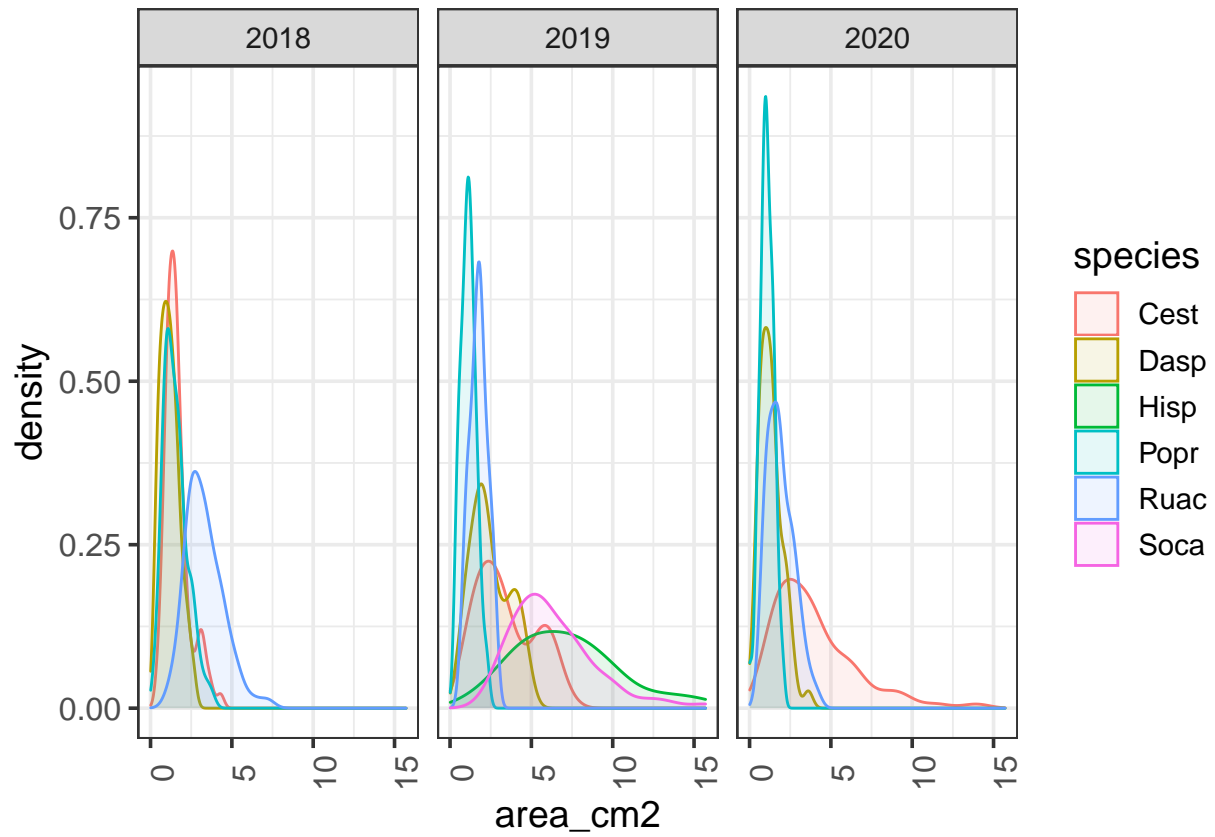
```
ggplot(sla, aes(area_cm2, fill = as.factor(species))) + geom_histogram(binwidth = 0.5) + facet_grid(species ~ year, margins = TRUE, scales = "free")
```



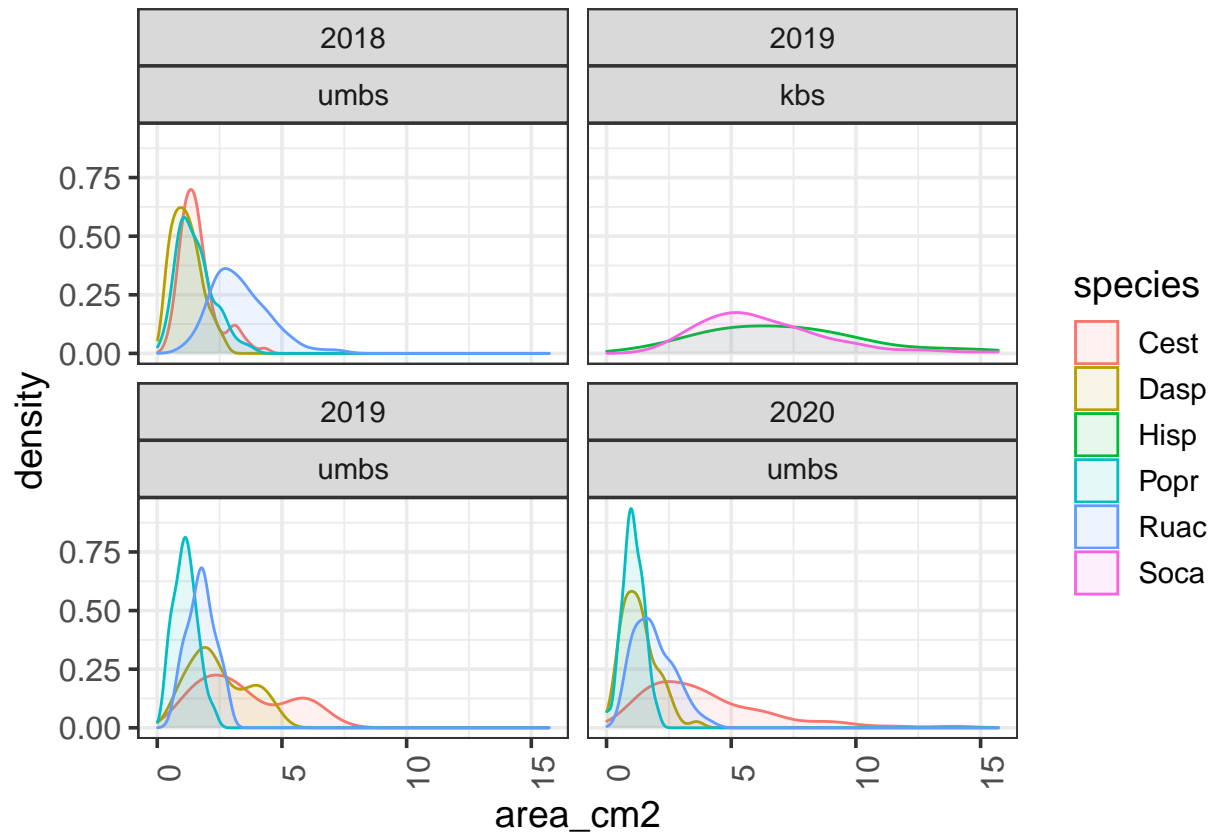
```
ggplot(sla, aes(area_cm2, fill = species, color = species)) + geom_density(alpha = 0.1)
```



```
ggplot(sla, aes(area_cm2, fill = species, color = species)) + geom_density(alpha = 0.1) +  
  facet_wrap(~year)
```

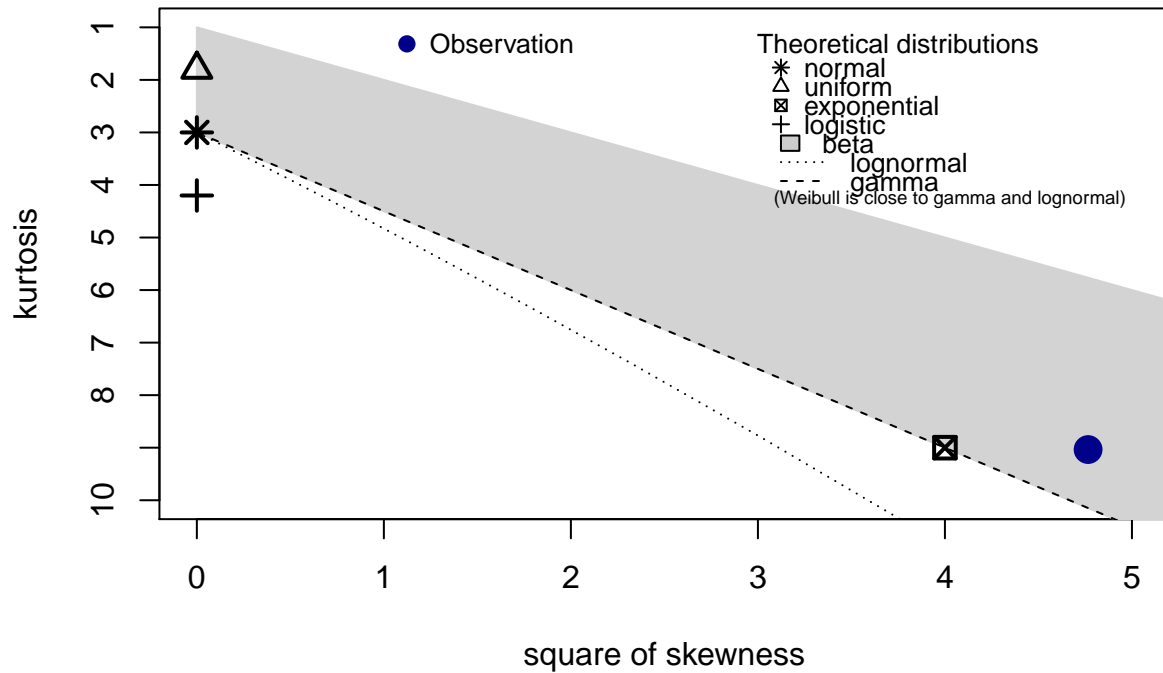


```
ggplot(sla, aes(area_cm2, fill = species, color = species)) + geom_density(alpha = 0.1) +  
  facet_wrap(~year + site)
```



```
# Exploring distributions for these right-skewed data: See:
# http://www.di.fc.ul.pt/~jpn/r/distributions/fitting.html
descdist(sla$area_cm2, discrete = FALSE)
```

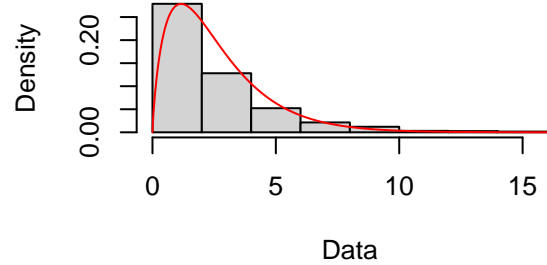
Cullen and Frey graph



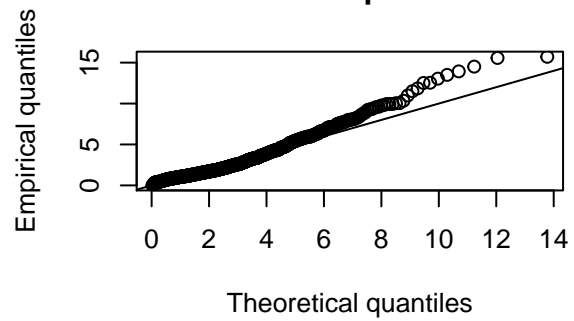
```
## summary statistics
## -----
## min: 0.01  max: 15.71
## median: 1.8
## mean: 2.607322
## estimated sd: 2.277138
## estimated skewness: 2.183
## estimated kurtosis: 9.035438

# Gamma distribution is an option
fit.gamma <- fitdist(sla$area_cm2, "gamma")
plot(fit.gamma)
```

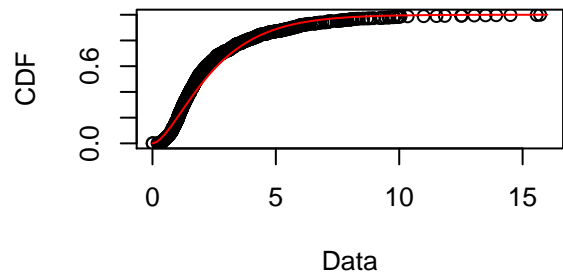
Empirical and theoretical dens.



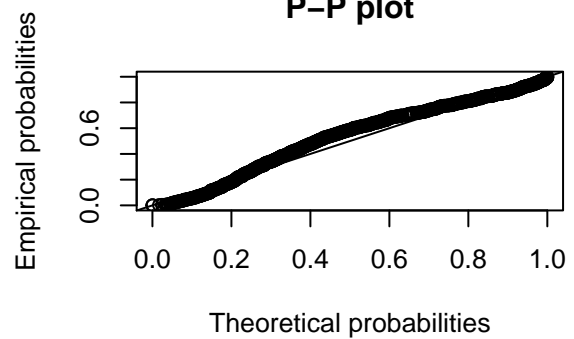
Q-Q plot



Empirical and theoretical CDFs

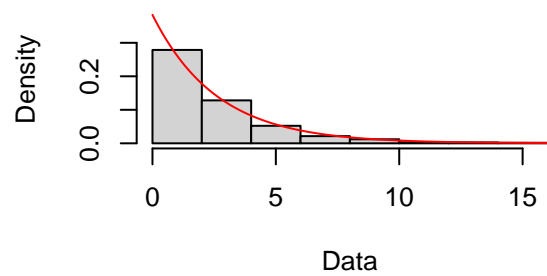


P-P plot

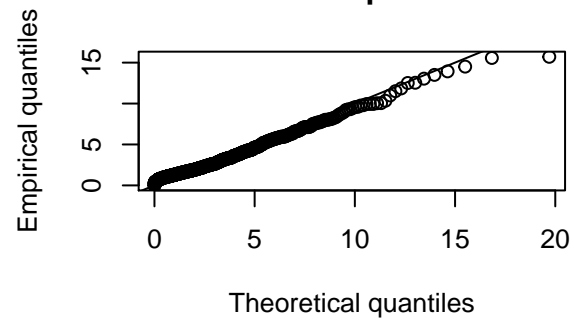


```
# Exponential distribution is another option
fit.exp <- fitdlist(sla$area_cm2, "exp")
plot(fit.exp)
```

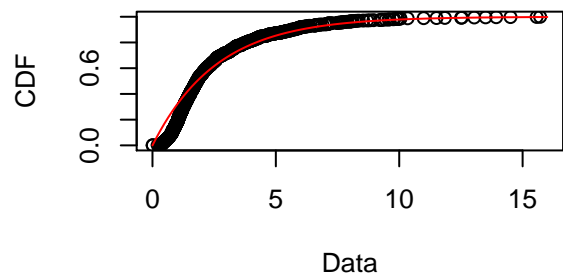

Empirical and theoretical dens.



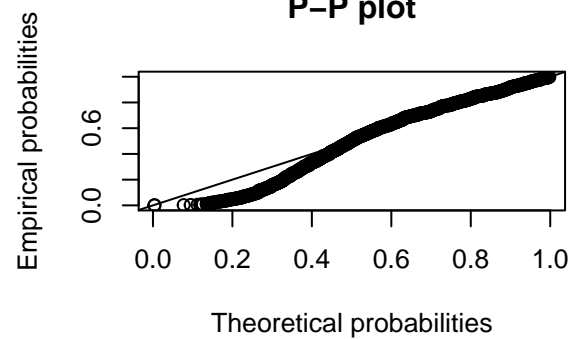
Q-Q plot



Empirical and theoretical CDFs

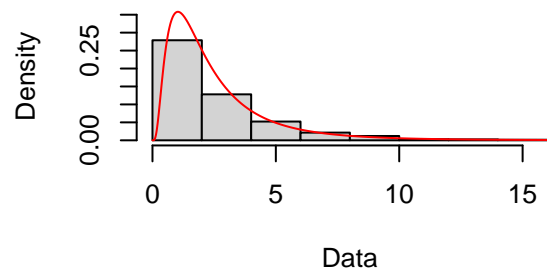


P-P plot

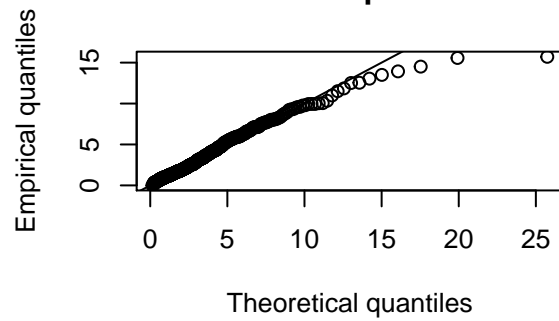


```
# Lognormal distribution is another option  
fit.ln <- fitdist(sla$area_cm2, "lnorm")  
plot(fit.ln)
```

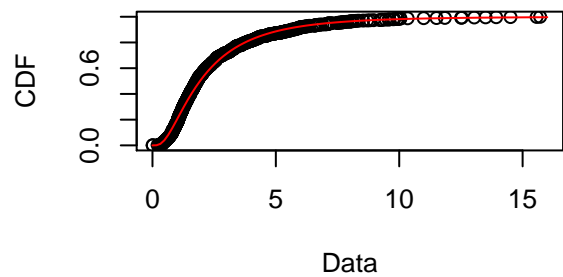
Empirical and theoretical dens.



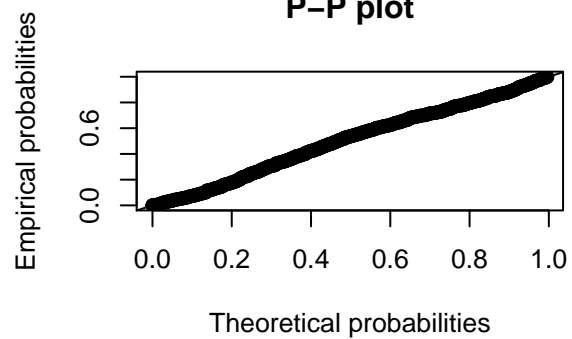
Q-Q plot



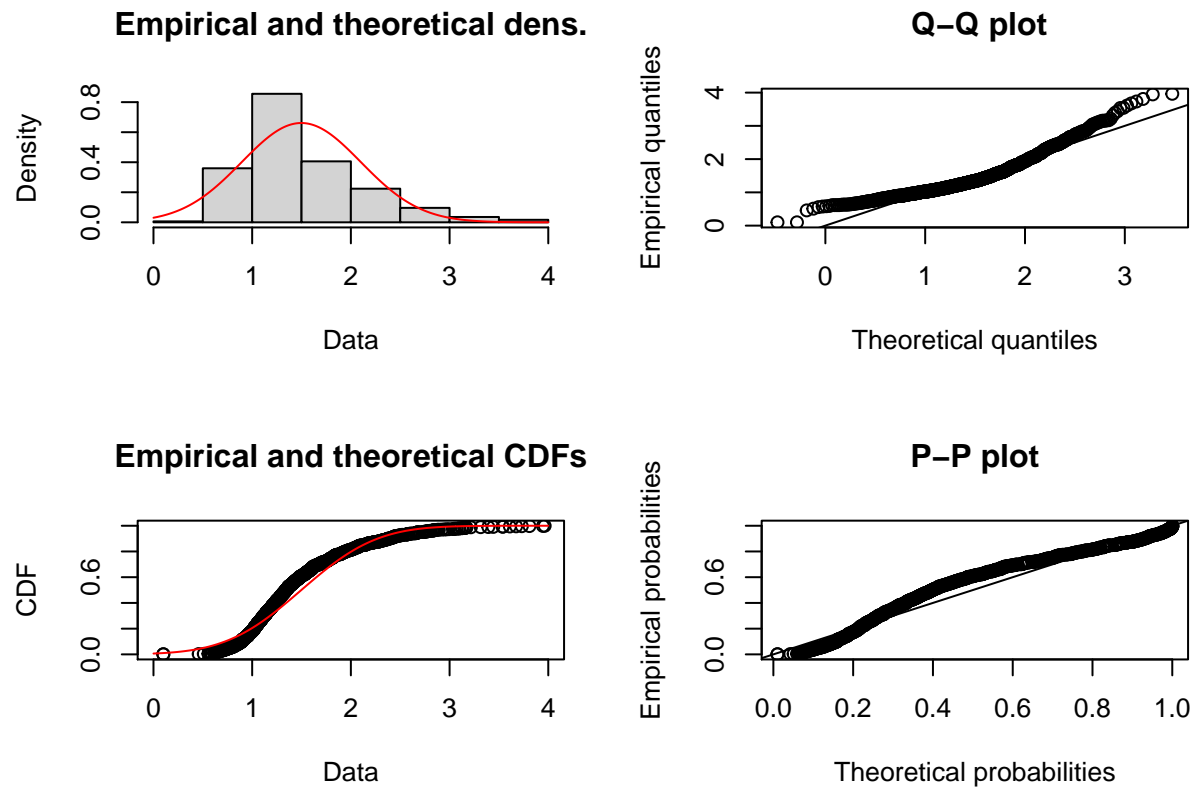
Empirical and theoretical CDFs



P-P plot

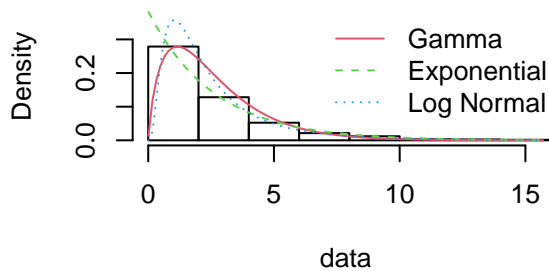


```
# Square root transformed normal distribution  
fit.sr <- fitdist(sqrt(sla$area_cm2), "norm")  
plot(fit.sr)
```

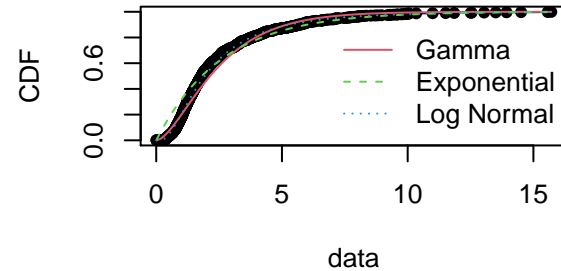


```
par(mfrow = c(2, 2))
plot.legend <- c("Gamma", "Exponential", "Log Normal")
denscomp(list(fit.gamma, fit.exp, fit.ln), legendtext = plot.legend)
cdfcomp(list(fit.gamma, fit.exp, fit.ln), legendtext = plot.legend)
qqcomp(list(fit.gamma, fit.exp, fit.ln), legendtext = plot.legend)
ppcomp(list(fit.gamma, fit.exp, fit.ln), legendtext = plot.legend)
```

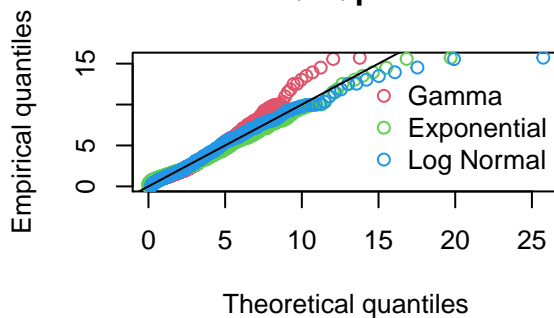
Histogram and theoretical densities



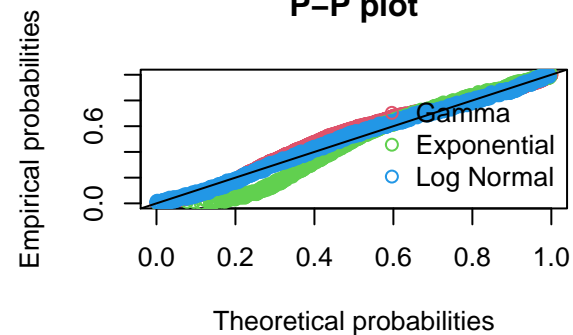
Empirical and theoretical CDFs



Q-Q plot



P-P plot



```
# Goodness of fit comparisons across fits (can't include the sqrt normal bc it
# becomes diff response values)
gofstat(list(fit.gamma, fit.exp, fit.ln), fitnames = c("Gamma", "Exponential", "Log Normal"))

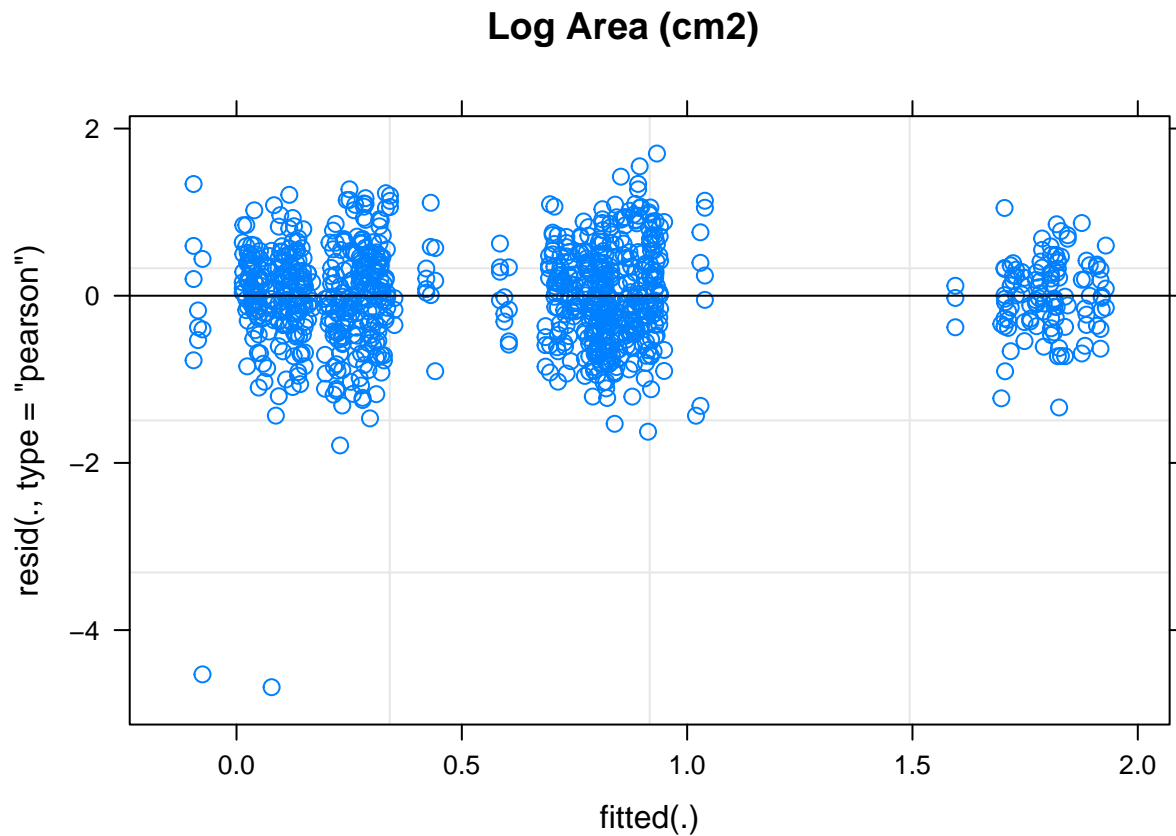
## Goodness-of-fit statistics
##
##      Gamma Exponential Log Normal
## Kolmogorov-Smirnov statistic 0.09305212 0.1658967 0.04205516
## Cramer-von Mises statistic 2.45538794 5.9902005 0.39592631
## Anderson-Darling statistic 13.42273156 37.9638617 2.46661286
##
## Goodness-of-fit criteria
##
##      Gamma Exponential Log Normal
## Akaike's Information Criterion 3582.421 3746.315 3521.768
## Bayesian Information Criterion 3592.147 3751.178 3531.493
# Lognormal is a winner so far
```

Determining appropriate distribution in mixed effects model

```
# See Ben Bolker's site for details on fitting glms:
# https://bbolker.github.io/mixedmodels-misc/glmmFAQ.html Fixed effects: warming,
# year, insecticide Random effect = plot (bc observations are nested within plot)
# Fit with ML bc we are interested in estimating fixed effects more than random
# effects See
# https://uoftcoders.github.io/rcourse/lec08-linear-mixed-effects-models.html for
```

```
# more details
m1 <- lmer(log(area_cm2) ~ state + species + year + insecticide + (1 | plot), data = sla,
  REML = FALSE)

# Check Assumptions: (1) Linearity: if covariates are not categorical (year
# isn't) (2) Homogeneity: Need to Check by plotting residuals vs predicted
# values.
par(mfrow = c(1, 2))
plot(m1, main = "Log Area (cm2)")
```



```
# Homogeneity of variance is ok here (increasing variance in resids is not
# increasing with fitted values) Check for homogeneity of variances (true if
# p>0.05). If the result is not significant, the assumption of equal variances
# (homoscedasticity) is met (no significant difference between the group
# variances).
leveneTest(residuals(m1) ~ sla$state)
```

```
## Warning in leveneTest.default(y = y, group = group, ...): group coerced to
## factor.
```

```
## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value Pr(>F)
## group  1  6.5179 0.01083 *
##      954
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```

# Assumption not met
leveneTest(residuals(m1) ~ sla$species)

## Warning in leveneTest.default(y = y, group = group, ...): group coerced to
## factor.

## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value    Pr(>F)
## group  5  6.4297 6.918e-06 ***
##      950
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

# Assumption not met - not surprising given the differences among species
leveneTest(residuals(m1) ~ sla$insecticide)

## Warning in leveneTest.default(y = y, group = group, ...): group coerced to
## factor.

## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value Pr(>F)
## group  1  0.1397 0.7087
##      954

# Assumption met
leveneTest(residuals(m1) ~ sla$plot)

## Warning in leveneTest.default(y = y, group = group, ...): group coerced to
## factor.

## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value Pr(>F)
## group 23  0.9514  0.528
##      932

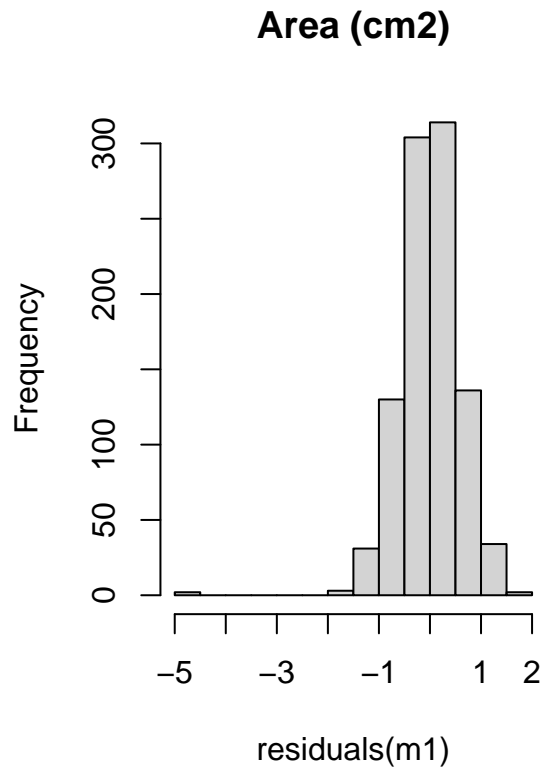
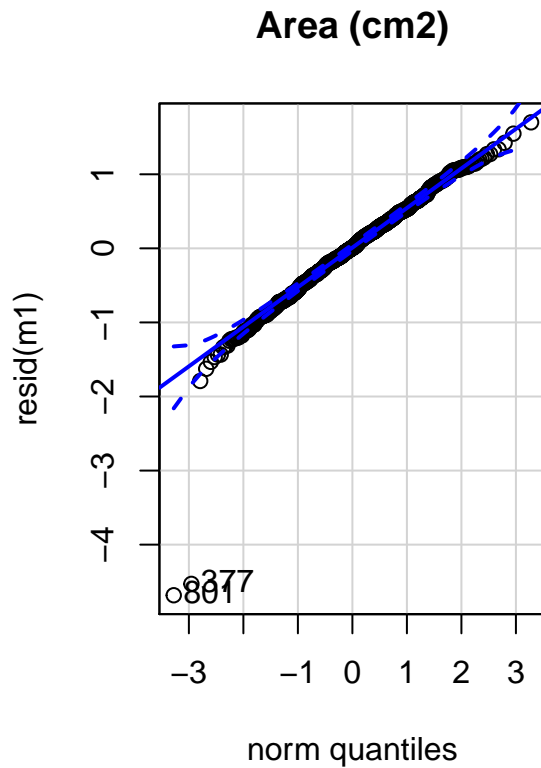
# Assumption met

# (3) Normality of error term: need to check by histogram, QQplot of residuals,
# could do Kolmogorov-Smirnov test. Check for normal residuals
qqPlot(resid(m1), main = "Area (cm2)")

## [1] 801 377

hist(residuals(m1), main = "Area (cm2)")

```



```
shapiro.test(resid(m1)) # not normally distributed resids bc p>0.05
```

```
##
## Shapiro-Wilk normality test
##
## data: resid(m1)
## W = 0.9494, p-value < 2.2e-16
```

```
# Outliers
sla[377, ]
```

```
##      plot site      date julian species plant_number area_cm2 mass_g state
## 377   B3 umbs 7/23/2020    205   Popr          2    0.01    0.6 warmed
##      treatment_key insecticide day month year
## 377              WI      insects  23     7  2020
```

```
sla[801, ]
```

```
##      plot site      date julian species plant_number area_cm2 mass_g state
## 801   D2 umbs 7/23/2020    205   Popr          4    0.01    0.97 warmed
##      treatment_key insecticide day month year
## 801              W0 no_insects  23     7  2020
```

```
# Outlier test - yes, these are outliers bc p<0.05
outlierTest(m1)
```

```
##      rstudent unadjusted p-value Bonferroni p
## 801 -8.049862      2.4816e-15  2.3724e-12
## 377 -7.788077      1.7865e-14  1.7079e-11
```

```
# Remove these 2 points
sla1 <- sla[-c(377, 801), ]
m1.nooutlier <- lmer(log(area_cm2) ~ state + species + year + insecticide + (1 |
  plot), data = sla1, REML = FALSE)
shapiro.test(resid(m1.nooutlier)) # normally distributed resids - good!
```

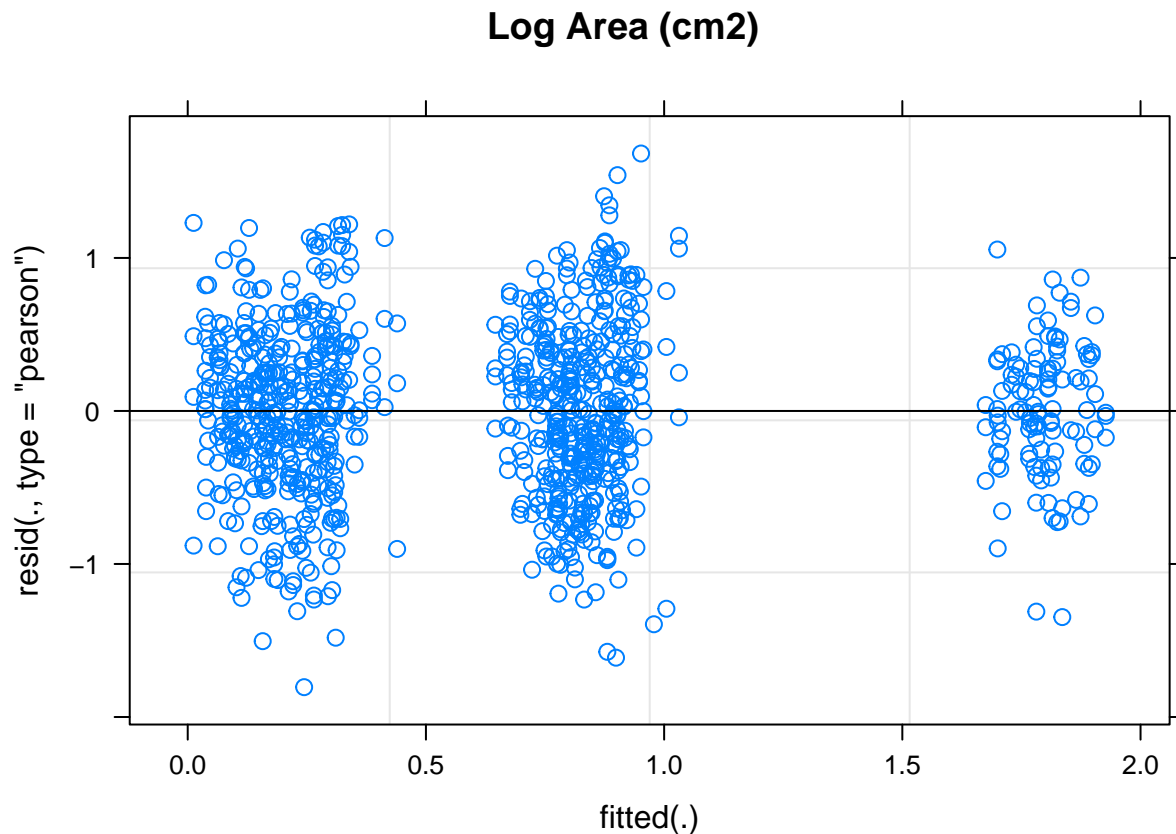
```
##
## Shapiro-Wilk normality test
##
## data: resid(m1.nooutlier)
## W = 0.99863, p-value = 0.6775
```

```
# (4) Normality of random effect: Get the estimate of random effect (e.g., random
# intercepts), and check them as you would check the residual. [***need to do for
# final model]
```

Model exploration determined log normal distribution for SLA and dropping 2 outliers. Proceed with re-checking the distribution and assumptions as above with the outliers removed.

```
# Fixed effects: warming, year, insecticide Random effect = plot (bc observations
# are nested within plot) Fit with ML bc we are interested in estimating fixed
# effects more than random effects See
# https://uoftcoders.github.io/rcourse/lec08-linear-mixed-effects-models.html for
# more details
m2 <- lmer(log(area_cm2) ~ state + species + year + insecticide + (1 | plot), data = sla1,
  REML = FALSE)
```

```
# Check Assumptions: (1) Linearity: if covariates are not categorical (year
# isn't) (2) Homogeneity: Need to Check by plotting residuals vs predicted
# values.
par(mfrow = c(1, 2))
plot(m2, main = "Log Area (cm2)")
```

Homogeneity of variance is ok here (increasing variance in resids is not increasing with fitted values) Check for homogeneity of variances (true if $p > 0.05$). If the result is not significant, the assumption of equal variances (homoscedasticity) is met (no significant difference between the group variances).

```
leveneTest(residuals(m2) ~ sla1$state)
```

```
## Warning in leveneTest.default(y = y, group = group, ...): group coerced to
## factor.
```

```
## Levene's Test for Homogeneity of Variance (center = median)
```

```
##      Df F value Pr(>F)
## group  1  4.3454 0.03738 *
##      952
```

```
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Assumption not met

```
leveneTest(residuals(m2) ~ sla1$species)
```

```
## Warning in leveneTest.default(y = y, group = group, ...): group coerced to
## factor.
```

```
## Levene's Test for Homogeneity of Variance (center = median)
```

```
##      Df F value    Pr(>F)
## group  5  9.4353 8.614e-09 ***
##      948
```

```
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
# Assumption not met - not surprising given the differences among species
leveneTest(residuals(m2) ~ sla1$insecticide)

## Warning in leveneTest.default(y = y, group = group, ...): group coerced to
## factor.

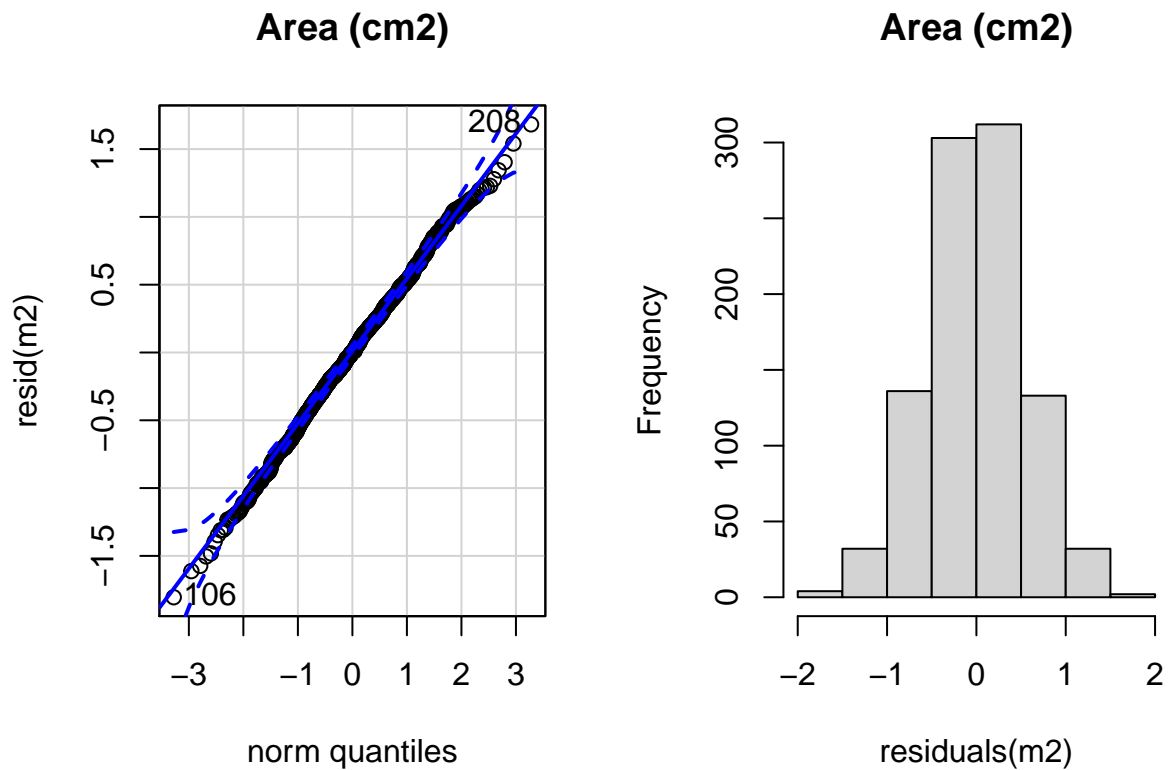
## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value Pr(>F)
## group  1  0.2575  0.612
##      952
# Assumption met
leveneTest(residuals(m2) ~ sla1$plot)

## Warning in leveneTest.default(y = y, group = group, ...): group coerced to
## factor.

## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value Pr(>F)
## group 23  0.6489 0.8956
##      930
# Assumption met

# (3) Normality of error term: need to check by histogram, QQplot of residuals,
# could do Kolmogorov-Smirnov test. Check for normal residuals
qqPlot(resid(m2), main = "Area (cm2)")

## [1] 106 208
hist(residuals(m2), main = "Area (cm2)")
```



```
shapiro.test(resid(m2)) # normally distributed resids bc p>0.05
```

```
##
## Shapiro-Wilk normality test
##
## data: resid(m2)
## W = 0.99863, p-value = 0.6775
```

```
# Outlier test - no, these are no outliers bc p>0.05
outlierTest(m2)
```

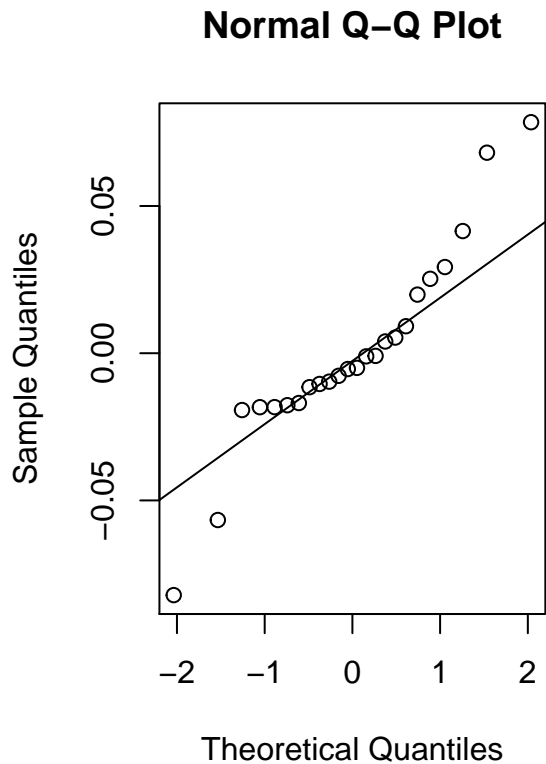
```
## No Studentized residuals with Bonferroni p < 0.05
## Largest |rstudent|:
##      rstudent unadjusted p-value Bonferroni p
## 106 -3.316548      0.00094621      0.90268
```

```
# (4) Normality of random effect: Get the estimate of random effect (e.g., random
# intercepts), and check them as you would check the residual.
```

```
require(lme4)
r_int <- ranef(m2)$plot$(Intercept)`
qqnorm(r_int)
qqline(r_int)
shapiro.test(r_int)
```

```
##
## Shapiro-Wilk normality test
##
## data: r_int
```

```
## W = 0.92594, p-value = 0.07912
# Yes, normally distributed random effect.
```



According to the results above, the outlier removal helps the model meet the assumptions. Proceed with model comparison. Start with investigating the model summary to determine which covariates to drop.

```
summary(m2)
```

```
## Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's
## method [lmerModLmerTest]
## Formula: log(area_cm2) ~ state + species + year + insecticide + (1 | plot)
## Data: sla1
##
##      AIC      BIC    logLik deviance df.resid
## 1592.4   1645.9   -785.2   1570.4      943
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -3.2911 -0.6385  0.0076  0.6769  3.0677
##
## Random effects:
##  Groups   Name                Variance Std.Dev.
##  plot      (Intercept)  0.003531  0.05942
##  Residual                    0.300796  0.54845
## Number of obs: 954, groups:  plot, 24
##
## Fixed effects:
```

```
##               Estimate Std. Error      df t value Pr(>|t|)
## (Intercept)    -52.23690    45.59534  941.48314   -1.146   0.2522
## statewarmed      0.04006     0.04376   24.86614    0.915   0.3688
## speciesDasp     -0.59150     0.05290  945.29635  -11.181 <2e-16 ***
## speciesHisp      1.00608     0.09376  946.00772   10.730 <2e-16 ***
## speciesPopr     -0.73661     0.05198  948.62269  -14.171 <2e-16 ***
## speciesRuac     -0.10312     0.05440  953.99284   -1.896   0.0583 .
## speciesSoca      0.89983     0.07362  935.35538   12.223 <2e-16 ***
## year             0.02628     0.02258  941.48103    1.164   0.2449
## insecticideno_insects 0.06901     0.04342  23.96707    1.589   0.1251
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
##      (Intr) sttwrm spcsDs spcsHs spcsPp spcsRc spcsSc year
## statewarmed -0.014
## speciesDasp -0.065  0.053
## speciesHisp  0.004  0.099  0.267
## speciesPopr -0.005  0.036  0.474  0.270
## speciesRuac -0.023 -0.035  0.450  0.249  0.460
## speciesSoca  0.007  0.014  0.332  0.189  0.338  0.322
## year        -1.000  0.013  0.064 -0.004  0.005  0.022 -0.007
## insctcdn_ns  0.019 -0.017 -0.044  0.016 -0.044 -0.031  0.004 -0.019
# Looks like year and warmed aren't significant - I'm leaving it in for now bc
# the data will change. With fuller data we'd begin model comparison here (will
# pick up here when those data are available). Then run the code below for diff
# models:
# AICctab(m2, m3, weights = T)
```