

Package ‘cia’

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Title Causal inference assistant (CIA)

Version 0.2.0

Description A library for performing causal inference within the structural causal modelling framework. Structure learning is performed using partition MCMC (Kuipers & Moffa, 2017) and several additional functions have been added to help with causal inference.

References Kuipers and Moffa (2017) <doi:10.1080/01621459.2015.1133426>, Scutari (2010) <doi:10.18637/jss.v035.i03>, Suter et al. (2023) <doi:10.18637/jss.v105.i09>.

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BNLearnScorer	<i>BNLearnScorer</i>
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Description

A thin wrapper on the bnlearn::score function.

Usage

```
BNLearnScorer(node, parents, ...)
```

Arguments

node	Name of node to score.
parents	The parents of node.
...	The ellipsis is used to pass other parameters to the scorer.

Examples

```
data <- bnlearn::learning.test
BNLearnScorer('A', c('B', 'C'), data = data)
BNLearnScorer('A', c(), data = data)
BNLearnScorer('A', vector(), data = data)
BNLearnScorer('A', NULL, data = data)
BNLearnScorer('A', c('B', 'C'), data = data, type = "bde", iss = 100)
BNLearnScorer('A', c('B', 'C'), data = data, type = "bde", iss = 1)
```

CachedScorer	<i>This builds the score cache. It can be used for problems where the score only changes as a function of (node, parents).</i>
--------------	--

Description

This builds the score cache. It can be used for problems where the score only changes as a function of (node, parents).

Usage

```
CachedScorer(scorer, max_size = NULL, nthreads = 1)
```

Arguments

scorer	A scorer.
max_size	Not implemented. Maximum number of scores to store in the cache. If the total number of combinations is greater than this number then the cache follows a least recently used replacement policy.
nthreads	The number of threads used to create the cache.

Examples

```
scorer <- CreateScorer(data = bnlearn::learning.test)
cached_scorer <- CachedScorer(scorer)
cached_scorer('A', c('B', 'C'))
```

CalculateAcceptanceRates	<i>Calculate acceptance rates.</i>
--------------------------	------------------------------------

Description

This makes the assumption that the proposal has saved a variable "proposal_used" and mcmc has saved a variable 'accept'.

Usage

```
CalculateAcceptanceRates(chains, group_by = NULL)
```

Arguments

chains	MCMC chains.
group_by	Vector of strings that are in c("chain", "proposal_used"). Default is NULL which will return the acceptance rates marginalised over chains and the proposal used.

Value

Summary of acceptance rates per grouping.

CalculateEdgeProbabilities*Calculate pairwise edge probabilities marginalised over the graph structure.*

Description

Calculate the probability of a given edge (E) given the data which is given by,

$$p(E|D) = \sum_G p(E|G)p(G|D)$$

.

Usage

```
CalculateEdgeProbabilities(x, ...)
```

Arguments

x	A chain(s) or collection object where states are DAGs.
...	Extra parameters sent to the methods. For a dag collection you can choose to use method='sampled' for MCMC sampled frequency (which is our recommended method) or method='score' which uses the normalised scores.

Value

p_edge An adjacency matrix representing the edge probabilities.

CalculateFeatureProbability*Collect feature probability marginalised over states.*

Description

Calculate the feature (f) probability whereby $p(f|D) = \sum_{G \in \mathcal{G}} p(G|D)p(f|G)$.

Usage

```
CalculateFeatureProbability(x, p_feature, ...)
```

Arguments

x	A chain(s) or collection object.
p_feature	A function that takes an adjacency matrix and collection object and returns a numeric value equal to $p(f G)$. Therefore, it must be of the form $p_feature(dag)$.
...	Extra parameters sent to the methods. For a dag collection you can choose to use method='sampled' for MCMC sampled frequency (which is our recommended method) or method='score' which uses the normalised scores.

Value

p_post_feature A numeric value representing the posterior probability of the feature.

CalculateNodeMoveNeighbourhood

Calculate neighbourhood for node move.

Description

Calculate neighbourhood for node move.

Usage

CalculateNodeMoveNeighbourhood(partitioned_nodes)

Arguments

partitioned_nodes
Labelled partition.

CalculateSplitJoinNeighbourhood

Calculate neighbourhood for the split or join proposal.

Description

The number of split combinations prescribed by KP15 is ambiguous when a partition element has only 1 node. A split for a partition element with 1 node results in a proposal to stay still, as such I remove that proposal.

Usage

CalculateSplitJoinNeighbourhood(partitioned_nodes)

Arguments

partitioned_nodes
Labelled partition.

`CalculateStayStillNeighbourhood`*Calculate neighbourhood for staying still.*

Description

Calculate neighbourhood for staying still.

Usage`CalculateStayStillNeighbourhood(partitioned_nodes)`**Arguments**`partitioned_nodes`

A labelled partition.

`CalculateSwapAdjacentNodeNeighbourhood`*Calculate neighbourhood for swapping nodes.*

Description

Calculate neighbourhood for swapping nodes.

Usage`CalculateSwapAdjacentNodeNeighbourhood(partitioned_nodes)`**Arguments**`partitioned_nodes`

Labelled partition.

`CalculateSwapNodeNeighbourhood`*Calculate neighbourhood for swapping nodes.*

Description

Calculate neighbourhood for swapping nodes.

Usage`CalculateSwapNodeNeighbourhood(partitioned_nodes)`**Arguments**`partitioned_nodes`

Labelled partition.

CheckBlacklistObeyed *Check blacklist obeyed.*

Description

If an edge between two nodes is blacklisted in Partition MCMC the adjacent partition element cannot be the only direct node for it's blacklisted child.

Usage

```
CheckBlacklistObeyed(partitioned_nodes, blacklist = NULL, nodes = NULL)
```

Arguments

partitioned_nodes	Labelled partition.
blacklist	A data.frame of (parent, child) pairs representing edges that cannot be in the DAG.
nodes	A vector of node names to check. Default is to check all child nodes in the blacklist.

CheckWhitelistObeyed *Check whitelist is obeyed.*

Description

Check whitelist is obeyed.

Usage

```
CheckWhitelistObeyed(partitioned_nodes, whitelist = NULL, nodes = NULL)
```

Arguments

partitioned_nodes	Labelled partition.
whitelist	A data.frame of (parent, child) pairs representing edges that must be in the DAG.
nodes	A vector of node names to check. Default is to check all child nodes in the whitelist.

CollectUniqueObjects *Collect unique objects.*

Description

Get the unique set of states along with their log score.

Usage

CollectUniqueObjects(x)

Arguments

x A cia_chains or cia_chain object.

Details

This gets the unique set of states in a cia_object referred to as objects (\mathcal{O}). Then it estimates the probability for each state using two methods. The log_sampling_prob uses the MCMC sampled frequency to estimate the posterior probability.

An alternative method to estimate the posterior probability for each state uses the state score. This is recorded in the log_norm_state_score vector. This approach estimates the log of the normalisation constant assuming $\tilde{Z}_{\mathcal{O}} = \sum_s^S p(\mathcal{O}_s) p(D|\mathcal{O}_s)$ where $\{\mathcal{O}_1, \mathcal{O}_2, \mathcal{O}_3, \dots, \mathcal{O}_S\}$ is the set of unique objects in the chain. This assumes that you have captured the most probable objects, such that $\tilde{Z}_{\mathcal{O}}$ is approximately equal to the true evidence $Z = \sum_{G \in \mathcal{G}} p(G) p(D|G)$ where the sum across all possible DAGs (\mathcal{G}). This also makes the assumption that the exponential of the score is proportional to the posterior probability, such that

$$p(G|D) \propto p(G)p(D|G) = \prod_i \exp(\text{score}(X_i, \text{Pa}_G(X_i)|D))$$

where $\text{Pa}_G(X_i)$ is the parents set for node X_i .

After the normalisation constant has been estimated we then estimate the log probability of each object as,

$$\log(p(\mathcal{O}|D)) = \log(p(\mathcal{O})p(D|\mathcal{O})) - \log(\tilde{Z}_{\mathcal{O}}).$$

Preliminary analysis suggests that the sampling frequency approach is more consistent across chains when estimating marginalised edge probabilities, and therefore is our preferred method. However, more work needs to be done here.

Value

dag_collection: A list with entries:

- state: List of unique states.
- log_evidence_state: Numeric value representing the evidence calculated from the states.
- log_state_score: Vector with the log scores for each state.
- log_sampling_prob: Vector with the log of the probability for each state estimated using the MCMC sampling frequency.

CreateScorer	<i>Scorer constructor.</i>
--------------	----------------------------

Description

Scorer constructor.

Usage

```
CreateScorer(
  scorer = BNLearnScorer,
  ...,
  max_parents = Inf,
  blacklist = NULL,
  whitelist = NULL,
  cache = FALSE,
  nthreads = 1
)
```

Arguments

scorer	A scorer function that takes (node, parents) as parameters. Default is BNLearn-Scorer.
...	Parameters to pass to scorer.
max_parents	The maximum number of allowed parents. Default is infinite.
blacklist	A boolean matrix of (parent, child) pairs where TRUE represents edges that cannot be in the DAG. Default is NULL which represents no blacklisting.
whitelist	A boolean matrix of (parent, child) pairs where TRUE represents edges that must be in the DAG. Default is NULL which represents no whitelisting.
cache	A boolean to indicate whether to build the cache. The cache only works for problems where the scorer only varies as a function of (node, parents). Default is FALSE.
nthreads	Number of threads used to construct cache.

Examples

```
scorer <- CreateScorer(data = bnlearn::asia)
```

DAGtoCPDAG	<i>Convert DAG to CPDAG.</i>
------------	------------------------------

Description

Convert DAG to CPDAG.

Usage

```
DAGtoCPDAG(x)
```

Arguments

`x` A matrix, `cia_chain`, or `cia_chains` object. When it is a chain(s) object the state must be an adjacency matrix.

Value

`x` Returns same object type converted to a CPDAG.

DefaultProposal	<i>Default proposal constructor.</i>
-----------------	--------------------------------------

Description

Default proposal constructor.

Usage

```
DefaultProposal(p = c(0.33, 0.33, 0.165, 0.165, 0.01), verbose = TRUE)
```

Arguments

`p` Probability for each proposal in the order (split_join, node_move, swap_node, swap_adjacent, stay_still).

`verbose` Boolean flag to record proposal used.

FindChangedNodes	<i>Find nodes with changed parent combinations between different labelled partitions.</i>
------------------	---

Description

TODO: This is quite slow. From the proposal we should be able to determine the nodes that need to be rescored rather than finding them using this function.

Usage

```
FindChangedNodes(old_partitioned_nodes, new_partitioned_nodes, scorer)
```

Arguments

`old_partitioned_nodes` Labelled partition.

`new_partitioned_nodes` Labelled partition.

`scorer` Scorer object.

Value

Vector of changed nodes.

Examples

```

scorer = CreateScorer()

old_dag <- UniformlySampleDAG(LETTERS[1:5])
old_partitioned_nodes <- GetPartitionedNodesFromAdjacencyMatrix(old_dag)

new_dag <- UniformlySampleDAG(LETTERS[1:5])
new_partitioned_nodes <- GetPartitionedNodesFromAdjacencyMatrix(new_dag)

changed_nodes <- FindChangedNodes(old_partitioned_nodes, new_partitioned_nodes, scorer)

```

FlattenChains	<i>Flatten list of chains.</i>
---------------	--------------------------------

Description

Flatten list of chains.

Usage

```
FlattenChains(chains)
```

Arguments

chains	MCMC chains.
--------	--------------

GetEmptyDAG	<i>Get an empty DAG given a set of nodes.</i>
-------------	---

Description

Get an empty DAG given a set of nodes.

Usage

```
GetEmptyDAG(nodes)
```

Arguments

nodes	A vector of node names.
-------	-------------------------

Value

An adjacency matrix with elements designated as (parent, child).

`GetIncrementalScoringEdges`*Get the score of the empty DAG*

Description

Get the score of the empty DAG

Usage

```
GetIncrementalScoringEdges(scorer, cutoff = 0)
```

Arguments

scorer	A scorer object.
cutoff	A score cutoff.

Value

A Boolean matrix of (parent, child) pairs for blacklisting..

`GetLowestPairwiseScoringEdges`*Preprocessing for blacklisting. Get the lowest pairwise scoring edges.*

Description

Get the lowest c pairwise scoring edges represented as a blacklist matrix. This blacklisting procedure is motivated by Koller & Friedman (2003). This is rarely used now as we found that it blacklists edges that have significant dependencies but are not in the top n edges. We prefer the `GetIncrementalScoringEdges` method.

Usage

```
GetLowestPairwiseScoringEdges(scorer, n_retain)
```

Arguments

scorer	A scorer object.
n_retain	An integer representing the number of edges to retain.

Value

A boolean matrix of (parent, child) pairs for blacklisting.

References

1. Koller D, Friedman N. Being Bayesian about network structure. A Bayesian approach to structure discovery in Bayesian networks. *Mach Learn.* 2003;50(1):95–125.

GetMAP	<i>Get the maximum a posteriori state.</i>
--------	--

Description

Get the maximum a posteriori state.

Usage

GetMAP(x)

Arguments

x	A collection of unique objects. See CollectUniqueObjects.
---	---

Value

maps A list with the adjacency matrix for the map and it's posterior probability. It is possible for it to return multiple DAGs. The list has elements;

- state: List of MAP DAGs.
- log_p: Numeric vector with the log posterior probability for each state.

GetNodePartition	<i>Get a node's partition element number.</i>
------------------	---

Description

Get a node's partition element number.

Usage

GetNodePartition(partitioned_nodes, node)

Arguments

partitioned_nodes	Labelled partition.
node	Node name.

Value

Node's partition element number.

GetNumberOfPartitions *Get number of partitions.*

Description

Calculate the number of partitions for a given labelled partition. This is ‘m’ in Kuipers & Moffa (2015).

Usage

GetNumberOfPartitions(partitioned_nodes)

Arguments

partitioned_nodes
 Labelled partition.

GetOrderedPartition *Get ordered labelled partition.*

Description

Calculate the ordered partition. Denoted as lambda in Kuipers & Moffa (2015).

Usage

GetOrderedPartition(partitioned_nodes)

Arguments

partitioned_nodes
 Labelled partition.

Value

Ordered partition.

GetParentCombinations	<i>Get parent combinations for a given node.</i>
-----------------------	--

Description

Get parent combinations for a given node.

Usage

```
GetParentCombinations(partitioned_nodes, node, scorer)
```

Arguments

partitioned_nodes	Labelled partition.
node	Node name.
scorer	A scorer object.

Value

List of parent combinations.

GetParentsKey	<i>Get parents key.</i>
---------------	-------------------------

Description

TODO: The in function is quite slow. May need to make this a for loop in C++.

Usage

```
GetParentsKey(parents, nodes)
```

Arguments

parents	A character vector of the parent nodes.
nodes	A character vector for all nodes.

`GetPartiallyIncrementalEdges`*Get partially incremental scoring edges.*

Description

Get the positive incremental scoring edges after conditioning on all other variables.

Usage

```
GetPartiallyIncrementalEdges(scorer, cutoff = 0)
```

Arguments

scorer A scorer object.

cutoff A cutoff value for the blacklist. Less than this value is blacklisted.

`GetPartitionedNodesFromAdjacencyMatrix`*Map DAG to a labelled partition.*

Description

This partitions nodes into levels of outpoints as explained in Section 4.1 of Kuipers & Moffa 2015. This takes an adjacency matrix and returns a data.frame of (partition, node) pairs

Usage

```
GetPartitionedNodesFromAdjacencyMatrix(adjacency)
```

Arguments

adjacency Adjacency matrix.

Value

Labelled partition for the given adjacency matrix.

GetPartitionNodes	<i>Get nodes in a partition element.</i>
-------------------	--

Description

Get nodes in a partition element.

Usage

```
GetPartitionNodes(partitioned_nodes, elements)
```

Arguments

partitioned_nodes	Labelled partition.
elements	An integer or vector of integers for the partition element number.

GetRestrictedNodes	<i>Get nodes that have restricted parents.</i>
--------------------	--

Description

Get nodes that have restricted parents.

Usage

```
GetRestrictedNodes(list)
```

Arguments

list	A black or white list.
------	------------------------

GetRestrictedParents	<i>Get black or white listed parents.</i>
----------------------	---

Description

Get black or white listed parents.

Usage

```
GetRestrictedParents(node, listed = NULL)
```

Arguments

node	The name of the node to get white or black listed parents.
listed	A black or white list.

LogSumExp	<i>Log-Sum-Exponential calculation using the trick that limits underflow issues.</i>
-----------	--

Description

Log-Sum-Exponential calculation using the trick that limits underflow issues.

Usage

LogSumExp(x)

Arguments

x A vector of numeric.

Value

Log-Sum-Exponential (LSE) of x.

MutilateGraph	<i>This creates a mutilated graph in accordance with an intervention.</i>
---------------	---

Description

This creates a mutilated graph in accordance with an intervention.

Usage

MutilateGraph(grain_object, intervention)

Arguments

grain_object A grain object.

intervention A list of nodes and their corresponding intervention distribution represented as a vector of unconditional probabilities.

Value

A grain object. Please note that any evidence set within the grain object will not be passed to the new object.

Examples

```
# This creates a mutilated graph in accordance with turning the sprinkler
# on in the wet grass example (i.e, do(S = 'yes')).
yn <- c("yes", "no")
p.R <- gRain::cptable(~R, values=c(.2, .8), levels=yn)
p.S_R <- gRain::cptable(~S:R, values=c(.01, .99, .4, .6), levels=yn)
p.G_SR <- gRain::cptable(~G:S:R, values=c(.99, .01, .8, .2, .9, .1, 0, 1), levels=yn)
wet.cpt <- gRain::grain(gRain::compileCPT(p.R, p.S_R, p.G_SR))

mut_graph <- MutilateGraph(wet.cpt, list(S = c(1.0, 0.0)))

# You can then use querygrain to perform an intervention query. For example,
# p(G | do(S = 'yes')) is given by,
gRain::querygrain(mut_graph, 'G')

# You can also perform an observational query for a node not affected
# by the intervention. For example, p(R | do(S = 'yes')) = p(R) is given by,
gRain::querygrain(mut_graph, 'R')
```

NodeMove

*Node move proposal.***Description**

Node move proposal.

Usage

NodeMove(partitioned_nodes)

Arguments

partitioned_nodes

Labelled partition.

OrderPartitionedNodes *Order partitioned nodes.***Description**

Order partitioned nodes.

Usage

OrderPartitionedNodes(partitioned_nodes)

Arguments

partitioned_nodes

Labelled partition.

Value

Labelled partitioned in descending partition element order.

PartitionMCMC	<i>Transition objects. One step implementation of the tempered partition MCMC. This acts as a constructor.</i>
---------------	--

Description

This is a constructor for a single Tempered Partition MCMC step. The function constructs an environment with the proposal, inverse temperature, and verbose flag. It then returns a function which takes the current_state and a scorer object. This only allows the scores to be raised to a constant temperature for every step.

Usage

```
PartitionMCMC(
  proposal = DefaultProposal(),
  temperature = 1,
  prerejection = TRUE,
  verbose = TRUE
)
```

Arguments

proposal	Proposal function. Default is the DefaultProposal.
temperature	Numeric value representing the temperature to raise the score to.
prerejection	Boolean flag to reject due to the proposal disobeying the black or white lists. Only set to FALSE if you want to understand how often you are proposing states that disobey the black or white lists. Can be useful for debugging or understanding the efficiency of specific proposal distributions.
verbose	Flag to pass MCMC information.

Value

Function that takes the current state and scorer that outputs a new state.

Examples

```
dag <- UniformlySampleDAG(c('A', 'B', 'C', 'D', 'E', 'F'))
partitioned_nodes <- GetPartitionedNodesFromAdjacencyMatrix(dag)

scorer <- list(
  scorer = BNLearnScorer,
  parameters = list(data = bnlearn::learning.test)
)

current_state <- list(
  state = partitioned_nodes,
  log_score = ScoreLabelledPartition(partitioned_nodes, scorer)
)
```

```
pmcmc <- PartitionMCMC(proposal = NodeMove, temperature = 1.0)
pmcmc(current_state, scorer)
```

PartitionSplitJoin	<i>Partition split or join constructor.</i>
--------------------	---

Description

Partition split or join constructor.

Usage

```
PartitionSplitJoin(partitioned_nodes)
```

Arguments

partitioned_nodes	Labelled partition.
-------------------	---------------------

PartitiontoDAG	<i>Sample DAGs from labelled partitions.</i>
----------------	--

Description

Sample DAGs from labelled partitions.

Usage

```
PartitiontoDAG(partitions, scorer)
```

Arguments

partitions	A dagms_chains, cia_chain, or matrix.
scorer	A scorer object.

PlotConcordance	<i>Concordance plot.</i>
-----------------	--------------------------

Description

Concordance plot.

Usage

```
PlotConcordance(x, ...)
```

Arguments

<code>x</code>	A list of adjacency matrices representing edge probabilities, a chains object, or a collections object with states as DAGs.
<code>...</code>	Additional parameter to send to the appropriate method. This includes 'highlight' (defaulted to 0.3) which sets the cutoff difference that is used to highlight the points, and the probability edge estimation 'method' for a <code>cia_collections</code> object.

Examples

```
data <- bnlearn::learning.test
dag <- UniformlySampleDAG(colnames(data))
partitioned_nodes <- GetPartitionedNodesFromAdjacencyMatrix(dag)
scorer <- CreateScorer(scorer = BNLearnScorer, data = data)

results <- SampleChains(300, partitioned_nodes, PartitionMCMC(), scorer, n_parallel_chains = 2)
dags <- PartitiontoDAG(results, scorer)
PlotConcordance(dags)

# OR
p_edge <- CalculateEdgeProbabilities(dags)
PlotConcordance(p_edge)
```

PlotScoreTrace	<i>Plot the score trace.</i>
----------------	------------------------------

Description

Plot the score trace.

Usage

```
PlotScoreTrace(
  chains,
  attribute = "log_score",
  n_burnin = 0,
  same_plot = TRUE,
  col = NULL,
  ...
)
```

Arguments

chains	MCMC chains.
attribute	Name of attribute to plot. Default is "log_score".
n_burnin	Number of steps to remove as burnin.
same_plot	Whether to plot on the same figure or on multiple figures.
col	A string representing a color for a single chain or a vector of strings to cycle through for multiple chains.
...	Extra parameters to pass to the plot and graphics::line functions.

PostProcessChains	<i>Analysis of chains. Equilibrium states.</i>
-------------------	--

Description

This allows you to remove a burnin and thin the chains after processing.

Usage

```
PostProcessChains(chains, n_burnin = 0, n_thin = 1)
```

Arguments

chains	MCMC chains.
n_burnin	Number of steps to remove at the start as a burnin. Default is 0.
n_thin	Number of steps between retained states. Default is 1.

ProposeNodeMove	<i>Propose individual node movement.</i>
-----------------	--

Description

This proposes that a single node selected uniformly can either:

1. Move to any current partition.
2. Move to any gap between or at the ends of the partitions.

Any of these moves are possible and are selected uniformly with two exceptions:

1. The selected node cannot move into adjacent gaps if it originated from a single node partition.
2. The selected node cannot move to the immediately higher gap if it originated from a two node partition.

Usage

```
ProposeNodeMove(partitioned_nodes)
```


Arguments

partitioned_nodes
 Labelled partition.

Examples

```
dag <- UniformlySampleDAG(c('A', 'B', 'C', 'D', 'E', 'F'))
partitioned_nodes <- GetPartitionedNodesFromAdjacencyMatrix(dag)
ProposeNodeMove(partitioned_nodes)
```

ProposePartitionSplitJoin

Propose a split or join of two partitions.

Description

This is the ‘Basic Move’ (i.e. algorithm 1) in Kuipers & Moffa (2015). There is a caveat in that the split proposal for a partition with one element is ambiguous, as a split for such a partition element results in a stay still proposal. Such a proposal has been removed.

Usage

```
ProposePartitionSplitJoin(partitioned_nodes)
```

Arguments

partitioned_nodes
 A labelled partition.

Value

A proposed labelled partition.

Examples

```
dag <- UniformlySampleDAG(c('A', 'B', 'C', 'D', 'E', 'F'))
partitioned_nodes <- GetPartitionedNodesFromAdjacencyMatrix(dag)
ProposePartitionSplitJoin(partitioned_nodes)
```

ProposeStayStill	<i>Propose that the partition stays still.</i>
------------------	--

Description

Propose that the partition stays still.

Usage

```
ProposeStayStill(partitioned_nodes)
```

Arguments

partitioned_nodes
A labelled partition.

Value

A proposed labelled partition.

Examples

```
dag <- UniformlySampleDAG(c('A', 'B', 'C', 'D', 'E', 'F'))
partitioned_nodes <- GetPartitionedNodesFromAdjacencyMatrix(dag)
ProposeStayStill(partitioned_nodes)
```

ProposeSwapAdjacentNode	<i>Propose that two nodes swap partition elements.</i>
-------------------------	--

Description

Propose that two nodes swap partition elements.

Usage

```
ProposeSwapAdjacentNode(partitioned_nodes)
```

Arguments

partitioned_nodes
labelled partition.

Value

A proposed labelled partition.

Examples

```
dag <- UniformlySampleDAG(c('A', 'B', 'C', 'D', 'E', 'F'))
partitioned_nodes <- GetPartitionedNodesFromAdjacencyMatrix(dag)
ProposeStayStill(partitioned_nodes)
```

ProposeSwapNode

Propose that two nodes swap partition elements.

Description

Propose that two nodes swap partition elements.

Usage

```
ProposeSwapNode(partitioned_nodes)
```

Arguments

partitioned_nodes
labelled partition.

Value

A proposed labelled partition.

Examples

```
dag <- UniformlySampleDAG(c('A', 'B', 'C', 'D', 'E', 'F'))
partitioned_nodes <- GetPartitionedNodesFromAdjacencyMatrix(dag)
ProposeStayStill(partitioned_nodes)
```

SampleChain

Sample a single chain.

Description

Sample a single chain.

Usage

```
SampleChain(n_results, init_state, transition, scorer, n_thin = 1)
```

Arguments

n_results Number of saved states.
init_state An initial state that can be passed to transition.
transition A transition function.
scorer A scorer object.
n_thin Number of steps between saved states.

Value

chain A `cia_chain` object.

Examples

```
data <- bnlearn::learning.test

dag <- UniformlySampleDAG(colnames(data))
partitioned_nodes <- GetPartitionedNodesFromAdjacencyMatrix(dag)

scorer_1 <- list(
  scorer = BNLearnScorer,
  parameters = list(data = data)
)

results <- SampleChain(10, partitioned_nodes, PartitionMCMC(), scorer_1)
```

SampleChains

Sample multiple chains in parallel.

Description

Sample multiple chains in parallel.

Usage

```
SampleChains(
  n_results,
  init_state,
  transition,
  scorer,
  n_thin = 1,
  n_parallel_chains = 2
)
```

Arguments

<code>n_results</code>	Number of saved states per chain.
<code>init_state</code>	An initial state that can be passed to transition. This can be a single state or a list of states for each parallel chain.
<code>transition</code>	A transition function.
<code>scorer</code>	A scorer object.
<code>n_thin</code>	Number of steps between saved states.
<code>n_parallel_chains</code>	Number of chains to run in parallel. Default is 2.

Value

chains A `cia_chains` object.

Examples

```

data <- bnlearn::learning.test

dag <- UniformlySampleDAG(colnames(data))
partitioned_nodes <- GetPartitionedNodesFromAdjacencyMatrix(dag)

scorer <- list(
  scorer = BNLearnScorer,
  parameters = list(data = data)
)

results <- SampleChains(10, partitioned_nodes, PartitionMCMC(), scorer)

```

SampleDAGFromLabelledPartition

Sample a DAG from a labelled partition.

Description

Sample a single DAG with from the set of DAGs that is consistent with a labelled partition. That is, given a set of DAGs \mathcal{G} that is consistent with a labelled partition Λ then it will sample a given DAG G where $G \in \mathcal{G}$ with probability $p(G|D, \Lambda) = p(G)p(D|G) / \sum_{G \in \mathcal{G}} p(G)p(D|G)$.

Usage

```
SampleDAGFromLabelledPartition(partitioned_nodes, scorer)
```

Arguments

partitioned_nodes	Labelled partition.
scorer	Scorer object.

Value

A list with elements:

- state Adjacency matrix.
- log_score Score of the sampled DAG.

Examples

```

data <- bnlearn::learning.test

dag <- UniformlySampleDAG(colnames(data))
partitioned_nodes <- GetPartitionedNodesFromAdjacencyMatrix(dag)

scorer <- CreateScorer(data = data)

SampleDAGFromLabelledPartition(partitioned_nodes, scorer)

```

ScoreDAG	<i>Score DAG.</i>
----------	-------------------

Description

Score DAG.

Usage

```
ScoreDAG(dag, scorer)
```

Arguments

dag	Adjacency matrix of (parent, child) entries with 1 denoting an edge and 0 otherwise.
scorer	Scorer object.

Value

Log of DAG score.

ScoreDiff	<i>Calculate the difference in log scores between two labelled partitions.</i>
-----------	--

Description

Calculate the difference in log scores between two labelled partitions.

Usage

```
ScoreDiff(
  old_partitioned_nodes,
  new_partitioned_nodes,
  scorer,
  rescore_nodes = NULL
)
```

Arguments

old_partitioned_nodes	A labelled partition.
new_partitioned_nodes	A labelled partition.
scorer	A scorer object.
rescore_nodes	Default is NULL which will determine the

Value

Log of score difference between two labelled partitions.

Examples

```
data <- bnlearn::learning.test

old_dag <- UniformlySampleDAG(names(data))
old_partitioned_nodes <- GetPartitionedNodesFromAdjacencyMatrix(old_dag)

new_dag <- UniformlySampleDAG(names(data))
new_partitioned_nodes <- GetPartitionedNodesFromAdjacencyMatrix(new_dag)

scorer <- list(
  scorer = BNLearnScorer,
  parameters = list(data = data)
)

ScoreDiff(old_partitioned_nodes, new_partitioned_nodes, scorer = scorer)
```

ScoreLabelledPartition

Score labelled partition by adding the log scores for each node.

Description

Score labelled partition by adding the log scores for each node.

Usage

```
ScoreLabelledPartition(partitioned_nodes, scorer)
```

Arguments

partitioned_nodes	
	Labelled partition.
scorer	Scorer object.

Value

Log of the node score.

Examples

```
data <- bnlearn::learning.test

dag <- UniformlySampleDAG(names(data))
partitioned_nodes <- GetPartitionedNodesFromAdjacencyMatrix(dag)

scorer <- list(
  scorer = BNLearnScorer,
  parameters = list(data = data)
)

ScoreLabelledPartition(partitioned_nodes, scorer)
```

ScoreNode	<i>Score node by marginalising over parent combinations.</i>
-----------	--

Description

Score node by marginalising over parent combinations.

Usage

```
ScoreNode(partitioned_nodes, node, scorer)
```

Arguments

partitioned_nodes	Labelled partition.
node	The node name.
scorer	A scorer object.

Value

Log of the node score.

Examples

```
data <- bnlearn::learning.test

dag <- UniformlySampleDAG(names(data))
partitioned_nodes <- GetPartitionedNodesFromAdjacencyMatrix(dag)

scorer <- list(
  scorer = BNLearnScorer,
  parameters = list(data = data)
)

ScoreNode(partitioned_nodes, 'A', scorer)
```

ScoreTableNode	<i>Calculate score tables for (node, parents) combinations.</i>
----------------	---

Description

Calculate score tables for (node, parents) combinations.

Usage

```
ScoreTableNode(partitioned_nodes, node, scorer)
```


Arguments

partitioned_nodes	Labelled partition.
node	Name of node.
scorer	Scorer object.

Value

List of log_scores for each combination in parent_combinations.

Examples

```
data <- bnlearn::learning.test

dag <- UniformlySampleDAG(names(data))
partitioned_nodes <- GetPartitionedNodesFromAdjacencyMatrix(dag)

scorer <- list(
  scorer = BNLearnScorer,
  parameters = list(data = data)
)

ScoreTableNode(partitioned_nodes, 'A', scorer)
```

StayStill

StayStill proposal.

Description

StayStill proposal.

Usage

```
StayStill(partitioned_nodes)
```

Arguments

partitioned_nodes	Labelled partition.
-------------------	---------------------

SwapAdjacentNode	<i>Swap nodes from adjacent partition elements proposal.</i>
------------------	--

Description

Swap nodes from adjacent partition elements proposal.

Usage

```
SwapAdjacentNode(partitioned_nodes)
```

Arguments

partitioned_nodes
 Labelled partition.

SwapNode	<i>Swap node proposal.</i>
----------	----------------------------

Description

Swap node proposal.

Usage

```
SwapNode(partitioned_nodes)
```

Arguments

partitioned_nodes
 Labelled partition.

toBNLearn	<i>Convert to bnlearn object.</i>
-----------	-----------------------------------

Description

Convert to bnlearn object.

Usage

```
toBNLearn(x)
```

Arguments

x An object that represents a DAG.

Value

bn_obj A bn object.

Examples

```
adj <- UniformlySampleDAG(c('A', 'B', 'C'))
bn_obj <- toBNLearn(adj)
```

togRain	<i>Convert an adjacency matrix or igraph object to a gRain object.</i>
---------	--

Description

Convert an adjacency matrix or igraph object to a gRain object.

Usage

```
togRain(x, ...)
```

Arguments

x An adjacency matrix or an igraph object
 ... extra parameters to gRain compile

Value

gRain_obj A gRain object.

Examples

```
dag <- bnlearn::model2network("[A][C][F][B|A][D|A:C][E|B:F]")
gRain_obj <- togRain(x = dag |> toMatrix(), data = bnlearn::learning.test)
```

toMatrix	<i>Convert network to an adjacency matrix.</i>
----------	--

Description

Convert a bnlearn or igraph object to an adjacency matrix.

Usage

```
toMatrix(network)
```

Arguments

network A network object from bnlearn or igraph.

Value

An adjacency matrix representation of network.

Examples

```
toMatrix(bnlearn::empty.graph(LETTERS[1:6]))
toMatrix(igraph::sample_k_regular(10, 2))
```

UniformlySampleDAG	<i>Uniformly sample DAG given a set of nodes.</i>
--------------------	---

Description

Uniformly sample DAG given a set of nodes.

Usage

```
UniformlySampleDAG(nodes)
```

Arguments

nodes	A vector of node names.
-------	-------------------------

Value

Adjacency matrix with elements designated as (parent, child).

[.cia_chain	<i>Indexing with respect to iterations.</i>
-------------	---

Description

Indexing with respect to iterations.

Usage

```
## S3 method for class 'cia_chain'
x = list()[i, ...]
```

Arguments

x	A cia_chain object.
i	An index.
...	ellipsis for extra indexing parameters.

Value

chain A cia_chain.

[.cia_chains	<i>Index a cia_chains object with respect to iterations.</i>
--------------	--

Description

Index a cia_chains object with respect to iterations.

Usage

```
## S3 method for class 'cia_chains'
x = list()[i, ...]
```

Arguments

x	A cia_chain object.
i	An index to get the cia_chain iterations.
...	ellipsis for extra indexing parameters.

Value

chain A cia_chains object.

[.cia_chains	<i>Index a cia_chains object.</i>
--------------	-----------------------------------

Description

Index a cia_chains object.

Usage

```
## S3 method for class 'cia_chains'
x[[i, ...]]
```

Arguments

x	A cia_chains object.
i	An index to get the cia_chain.
...	ellipsis for extra indexing parameters.

Value

chain A cia_chains object.

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