

### Developed by gAGE: Research group of Astronomy & GEomatics Technical University of Catalonia (UPC)

### **Tutorial 3**

# Differential Positioning with code measurements

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Slides associated to *gLAB* version 2.0.0



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### Aim of this tutorial

- ★ This tutorial is devoted to analysing and assessing the differential positioning with code pseudorange measurements. Four different permanent receivers and two baselines 280km and 51km are considered.
- ★ The atmospheric effects on differential positioning are the subject of the first session. The differential tropospheric and ionospheric delays are analysed for the two baselines considered and the absolute and differential user solution are computed and assessed.
- ↑ The ephemeris error on differential positioning is the subject of the second session. A 2000 metres of Along-Track error is simulated by manipulating the broadcast message, and the impact of this error on range and user domains is assessed for absolute and differential positioning. A theoretical expression to predict the range error on a given baseline is also verified in the last part of this session.
- ▶ Detailed guidelines for self-learning students are provided in this tutorial and in its associated notepad text file.
- ▲ All software tools (including *gLAB*) and associated files for the laboratory session are included in the CD-ROM or USB stick associated with this tutorial.



### **OVERVIEW**

### > Introduction: gLAB processing in command line

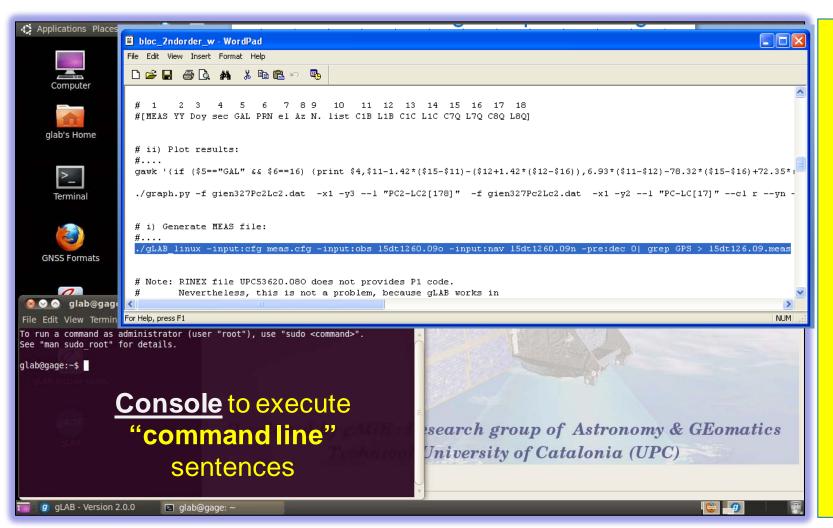
### **△ Session A: Atmospheric effects**

- A1 Differential positioning of EBRE-CREU receivers (Long baseline: 288 km)
- A2 Differential positioning of GARR-MATA receivers (Short baseline: 51 km)

#### **▲ Session B: Orbit error effects**

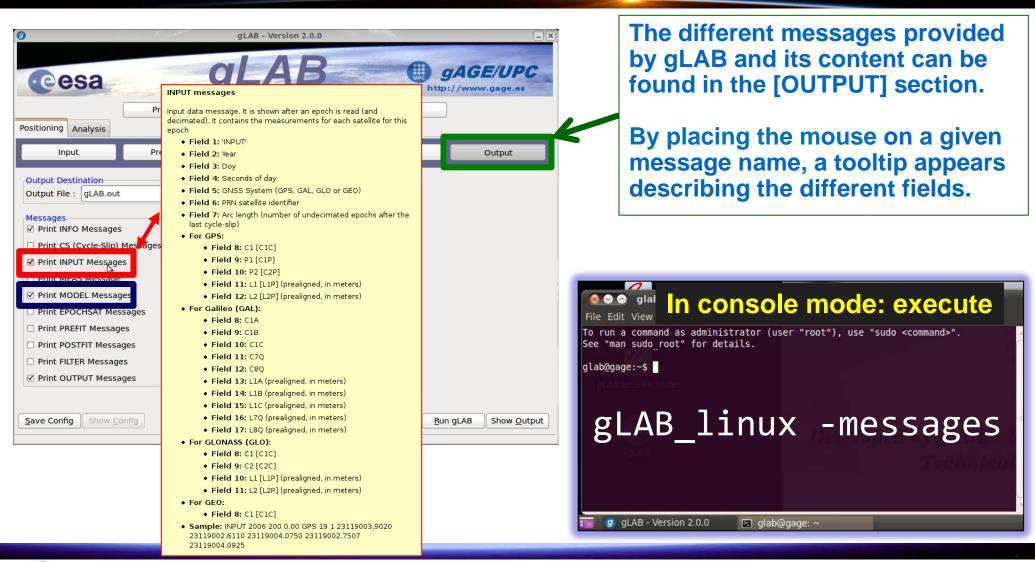
- B1 Differential positioning of EBRE-CREU receivers (Long baseline: 288 km)
- B2 Differential positioning of GARR-MATA receivers (Short baseline: 51 km)
- B3 Range domain orbit error.

### gLAB processing in command line



A "notepad" with the command line sentence is provided to facilitate the sentence writing: just paste" from notepad to the working terminal.

### gLAB processing in command line



### **OVERVIEW**

### ▲ Introduction: gLAB processing in command line

- > Session A: Atmospheric effects
  - A1 Differential positioning of EBRE-CREU receivers (Long baseline: 288 km)
  - A2 Differential positioning of GARR-MATA receivers (Short baseline: 51 km)

#### **▲ Session B: Orbit error effects**

- B1 Differential positioning of EBRE-CREU receivers (Long baseline: 288 km)
- B2 Differential positioning of GARR-MATA receivers (Short baseline: 51 km)
- B3 Range domain orbit error.

# Session A Atmospheric effects on differential positioning with code measurements

### Session A: Atmospheric effects

### **Toulouse ESCO** LLIV **CREU** SBAR CASS SONA BELL PLAN OMATA Barcelona OREUS OGARR **EBRE**



GARR-MATA: 51 km

EBRE-CREU: 288 km

### Session A: Atmospheric effects

#### **Data sets**:

#### Measurement files:

CREU0770.100, EBRE0770.100, GARR0770.100, MATA0770.100

Orbit and clocks files: brdc0770.10n.

#### Receiver coordinates:

```
MATA 4776835.5870 202618.9947 4207574.6304 41.539929530 2.428858625 123.6209 GARR 4796983.5767 160309.1177 4187340.3773 41.292941528 1.914040080 634.6040 EBRE 4833520.1197 41537.2015 4147461.6263 40.820888849 0.492363266 107.8284 CREU 4715420.3054 273177.8809 4271946.7957 42.318843076 3.315603563 133.4780
```

**Note:** the receivers were not moving (**static receivers**) during the data collection.

### **OVERVIEW**

- ▲ Introduction: gLAB processing in command line
- > Session A: Atmospheric effects
  - A1 Differential positioning of EBRE-CREU receivers (Long baseline: 288 km)
  - A2 Differential positioning of GARR-MATA receivers (Short baseline: 51 km)
- **▲ Session B: Orbit error effects** 
  - B1 Differential positioning of EBRE-CREU receivers (Long baseline: 288 km)
  - B2 Differential positioning of GARR-MATA receivers (Short baseline: 51 km)
  - B3 Range domain orbit error.

#### **Model Components computation**

 The script "ObsFile1.scr" generates a data file "STA.obs" with the following content

```
1 2 3 4 5 6 7 8 9 10 11 12 13 14 [sta sat DoY sec P1 L1 P2 L2 Rho Trop Ion Elev Azim Prefit]
```

Run this script for EBRE and CREU receivers:

```
ObsFile1.scr EBRE0770.100 brdc0770.10n ObsFile1.scr CREU0770.100 brdc0770.10n
```

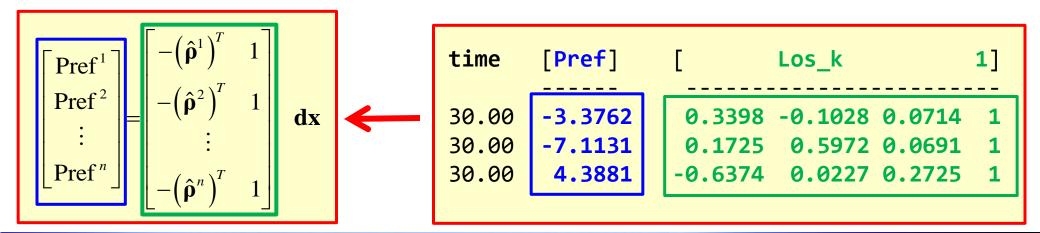
 Generate the navigation equations system for absolute positioning for each receiver and compute the user solution (see next two slides).

Justify that the next sentence builds the navigation equations system for absolute positioning: \_\_\_\_\_\_\_

```
See file content in previous slide
```

```
[Prefit] = [Los_k 1] * [dx]
```

```
cat EBRE.obs | gawk 'BEGIN{g2r=atan2(1,1)/45}{e=$12*g2r;a=$13*g2r;
printf "%8.2f %8.4f %8.4f %8.4f %1i \n".
$4, $14, -cos(e)*sin(a),-cos(e)*cos(a),-sin(e),1}'> EBRE.mod
```



The program kalman.f implements the kalman filter for code positioning (see source code).

The INPUT file is the file **EBRE.mod** generated in the previous slide.

The OUTPUT is the **user solution** file:

1 2 3 4 5 [time dE dN dU, dt]

The filter configuration is done by the namelist kalman.nml.

- The namelist kalman\_wn.nml configures the filter to process the coordinates and clock as white nose (i.e. Kinematic solution).
- The namelist kalman\_ct.nml configures the filter to process the coordinates as constants and clock as white nose (i.e. static solution).

The program is executed as:

```
cp kalman.nml_wn kalman.nml
cat EBRE.mod | kalman > EBRE.pos
```



Using the files EBRE.obs and CREU.obs, follow the next steps:

- 1. Build the navigation equations system for each receiver, for absolute positioning.
- 2. Compute the user solutions in kinematic mode.
- 3. Plot the results and compare the positioning errors.

### 1.- Building the navigation equations system for absolute positioning:

```
cat EBRE.obs | gawk 'BEGIN{g2r=atan2(1,1)/45}{e=$12*g2r;a=$13*g2r;
printf "%8.2f %8.4f %8.4f %8.4f %1i \n",
$4, $14, -cos(e)*sin(a),-cos(e)*cos(a),-sin(e),1 }'> EBRE.mod
```

#### 2.- Computing the user solution for absolute positioning:

```
cp kalman.nml_wn kalman.nml
cat EBRE.mod | kalman > EBRE.pos
```

#### 3.- Plotting results:

```
graph.py -f EBRE.pos -x1 -y2 -s.- -l "North error"
    -f EBRE.pos -x1 -y3 -s.- -l "East error"
    -f EBRE.pos -x1 -y4 -s.- -l "UP error"
    --xl "time (s)" --yl "error (m)" --yn -8 --yx 8
    -t "EBRE: Standard Point Positioning"
```



### 1.- Building the navigation equations system for absolute positioning:

```
cat CREU.obs | gawk 'BEGIN{g2r=atan2(1,1)/45}{e=$12*g2r;a=$13*g2r;
printf "%8.2f %8.4f %8.4f %8.4f %1i \n",
$4, $14, -cos(e)*sin(a),-cos(e)*cos(a),-sin(e),1 }'> CREU.mod
```

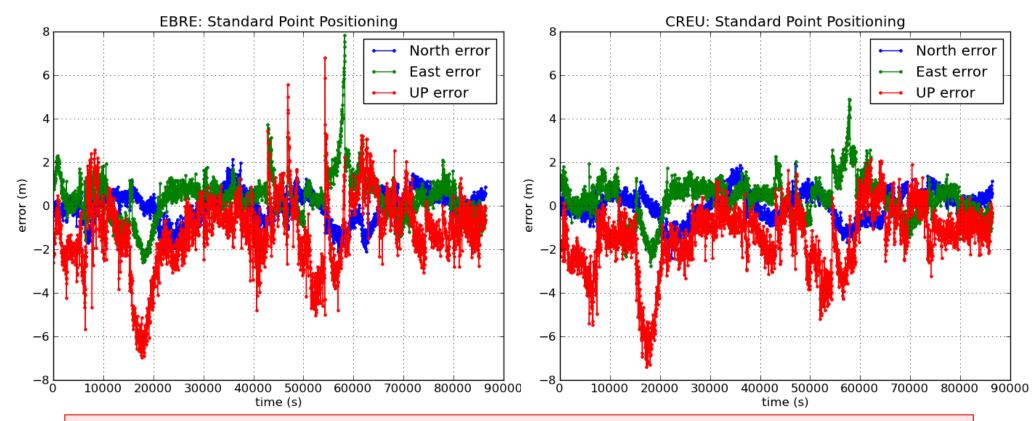
#### 2.- Computing the user solution for absolute positioning:

```
cp kalman.nml_wn kalman.nml
cat CREU.mod | kalman > CREU.pos
```

#### 3.- Plotting results:

```
graph.py -f CREU.pos -x1 -y2 -s.- -l "North error"
   -f CREU.pos -x1 -y3 -s.- -l "East error"
   -f CREU.pos -x1 -y4 -s.- -l "UP error"
   --xl "time (s)" --yl "error (m)" --yn -8 --yx 8
   -t "CREU: Standard Point Positioning"
```





#### **Questions:**

- •What is the expected accuracy of the computed coordinates (in absolute positioning)?
- Why are the patterns seen for the receivers EBRE and CREU are so similar?



The script **Dobs.scr** computes the single difference of measurements files **sta1.obs** (<u>reference station</u>) and **sta2.obs** (<u>user</u>).

It can be executed by the sentence: Dobs.scr sta1.obs sta2.obs

The output file (**D\_sta1\_sta2.obs**) has the following content:

1 2 3 4 5 6 7 8 9 10 11 12 13 14 [sta2 sat DoY sec DP1 DL1 DP2 DL2 DRho DTrop DIon El2 Az2 DPrefit]

Where:  $D(o) = (o)_{sta2} - (o)_{sta1}$ 

EL2 and AZ2 are the satellite azimuth and elevation from sta2.

In our case, executing: Dobs.scr EBRE.obs CREU.obs
the OUTPUT file D\_EBRE\_CREU.obs is generated.

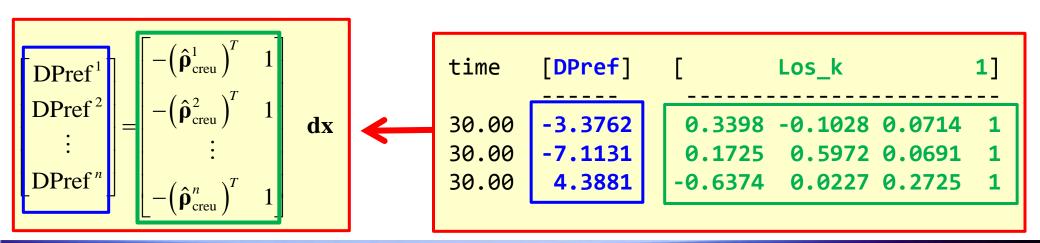


Justify that the next sentence builds the navigation equations system for differential positioning of CREU (user) relative to EBRE (reference station):

```
Question: Is this combination equivalent to use $14? Why?
```

$$[DPrefit] = [Los_k 1]*[dx]$$

```
cat D_EBRE_CREU.obs | gawk 'BEGIN{g2r=atan2(1,1)/45}{e=$12*g2r;a=$13*g2r;
    printf "%8.2f %8.4f %8.4f %8.4f %8.4f %1i \n",
$4,$5-$9-$10-$11 ,-cos(e)*sin(a),-cos(e)*cos(a),-sin(e),1 }'> D_EBRE_CREU.mod
```



### Using the files EBRE.obs and CREU.obs, follow the next steps:

- Compute the single differences of measurements and model components.
- 2. Build the navigation equations system for the differential positioning of CREU receiver (user) relative to EBRE (reference station).
- 3. Compute the user solution in kinematic mode and in static mode.
- 4. Plot the results and discuss the positioning error found.

- 1. Computing the single differences of measurements and model components.

  Dobs.scr EBRE.obs CREU.obs
- 2.- Building the navigation equations system for differential positioning:

```
cat D_EBRE_CREU.obs | gawk 'BEGIN{g2r=atan2(1,1)/45}{e=$12*g2r;a=$13*g2r;
    printf "%8.2f %8.4f %8.4f %8.4f %8.4f %1i \n",
$4,$5-$9-$10-$11,-cos(e)*sin(a),-cos(e)*cos(a),-sin(e),1}'> D_EBRE_CREU.mod
```

3.- Computing the user solution for differential positioning:



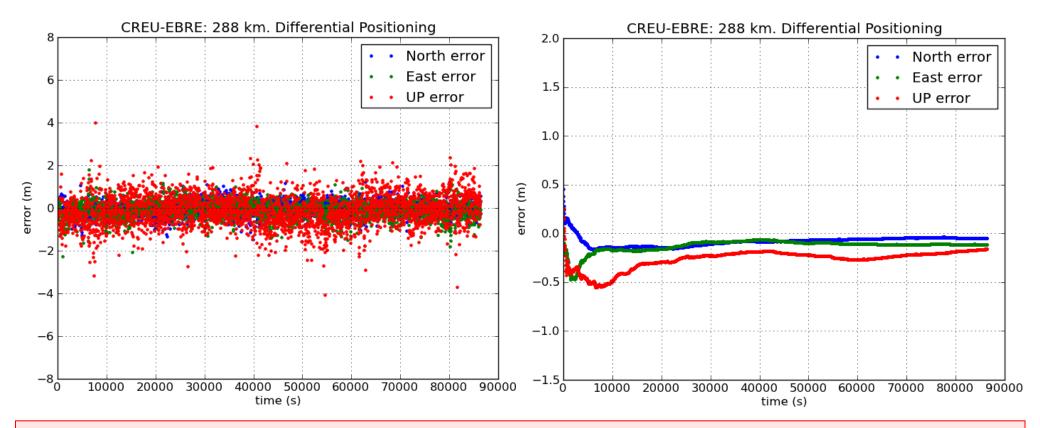
#### 4.- Plotting results:

#### - kinematic mode:

```
graph.py -f EBRE_CREU.posK -x1 -y2 -s. -l "North error"
   -f EBRE_CREU.posK -x1 -y3 -s. -l "East error"
   -f EBRE_CREU.posK -x1 -y4 -s. -l "UP error"
   --xl "time (s)" --yl "error (m)" --yn -8 --yx 8
   -t "CREU-EBRE: 288 km: Differential Positioning"
```

#### - Static mode:

```
graph.py -f EBRE_CREU.posS -x1 -y2 -s. -l "North error"
    -f EBRE_CREU.posS -x1 -y3 -s. -l "East error"
    -f EBRE_CREU.posS -x1 -y4 -s. -l "UP error"
    --xl "time (s)" --yl "error (m)" --yn -8 --yx 8
    -t "CREU-EBRE: 288 km: Differential Positioning"
```



#### **Questions:**

- •Looking at these results, justify intuitively why the errors are reduced in differential positioning.
- •Why is the error lower in static than in kinematic mode?



Analyze the effect of the differential ionosphere on the differential positioning of CREU relative to EBRE station:

#### Follow the next steps:

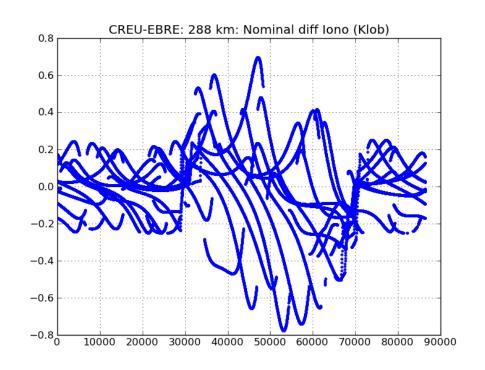
- 1. Using file **D\_EBRE\_CREU.obs** plot the differential ionospheric correction (from Klobuchar model) between EBRE and CREU.
- 2. Repeat the previous process, but without applying the ionospheric correction. Compare the results

#### Plotting the Klobuchar differential ionospheric correction:

```
graph.py -f D_EBRE_CREU.obs -x4 -y'11' --yn -0.8 --yx 0.8 -t "CREU-EBRE: 288 km: Nominal diff Iono (Klob)"
```

#### **Question:**

Justify the pattern seen in the nominal (Klobuchar) ionospheric corrections.



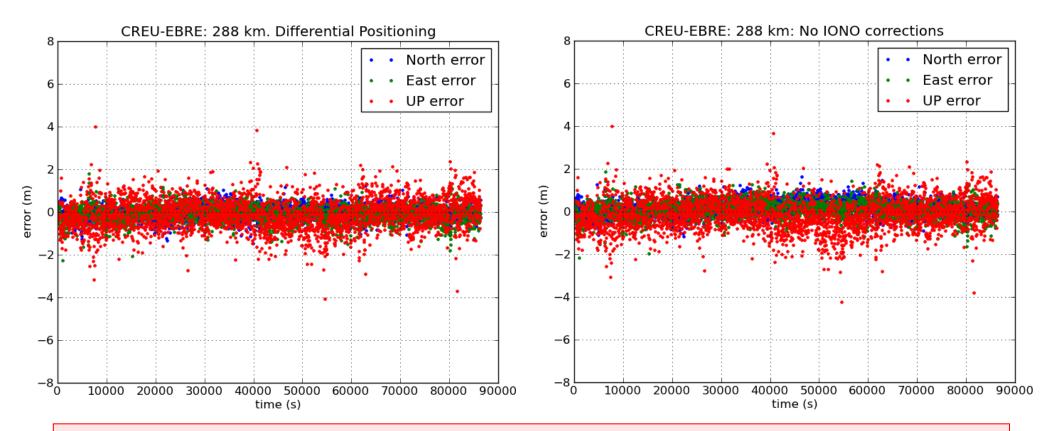
### Computing the differential solution, but without using ionospheric corrections:

1.- Building the navigation equations system for differential positioning, but without using the ionospheric corrections:

```
cat D_EBRE_CREU.obs | gawk 'BEGIN{g2r=atan2(1,1)/45}{e=$12*g2r;a=$13*g2r;
    printf "%8.2f %8.4f %8.4f %8.4f %8.4f %1i \n",
    $4,$5-$9-$10,-cos(e)*sin(a),-cos(e)*cos(a),-sin(e),1}'> D_EBRE_CREU.mod
```

2.- Computing the user solution for differential positioning:

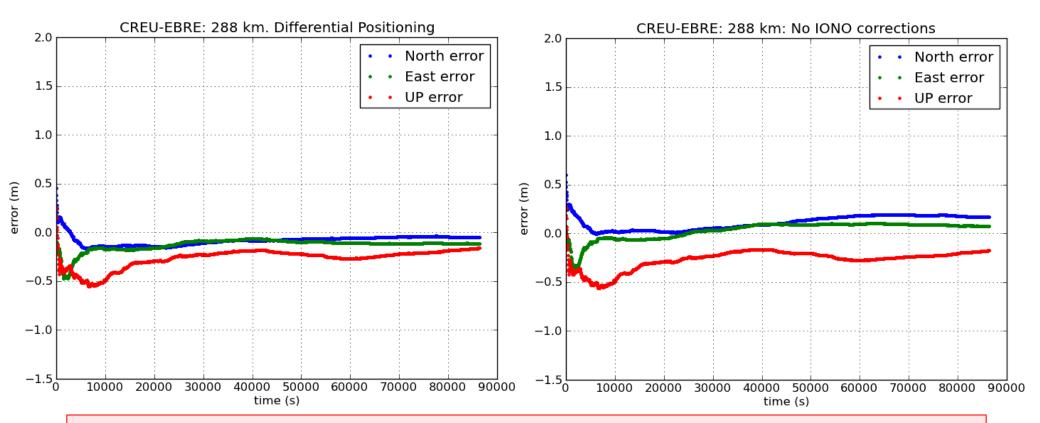




#### **Question:**

Taking into account the previous plot of the differential ionospheric corrections (slide #26), discuss the effect seen on the position domain.





#### **Question:**

Discuss the pattern seen in the figure. Why is the effect of the differential ionospheric error is higher in these static positioning results?



Analyze the effect of the differential Troposphere on the differential positioning of CREU relative to EBRE station:

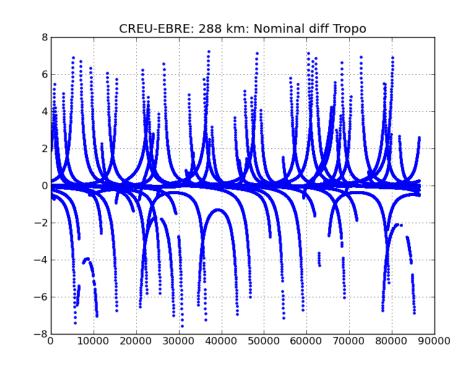
### Follow the next steps:

- 1. Using file **D\_EBRE\_CREU.obs** plot the differential trpospheric correction (from nominal model) between EBRE and CREU.
- 2. Repeat the previous process, but without applying the tropospheric correction. Compare the results

#### Plotting the nominal differential tropospheric correction:

```
graph.py -f D_EBRE_CREU.obs -x4 -y'10' --yn -8 --yx 8
-t "CREU-EBRE: 288 km: Nominal diff Tropo"
```

Question:
Justify the pattern seen in the nominal tropospheric corrections.



### Computing the differential solution, but without using tropospheric corrections:

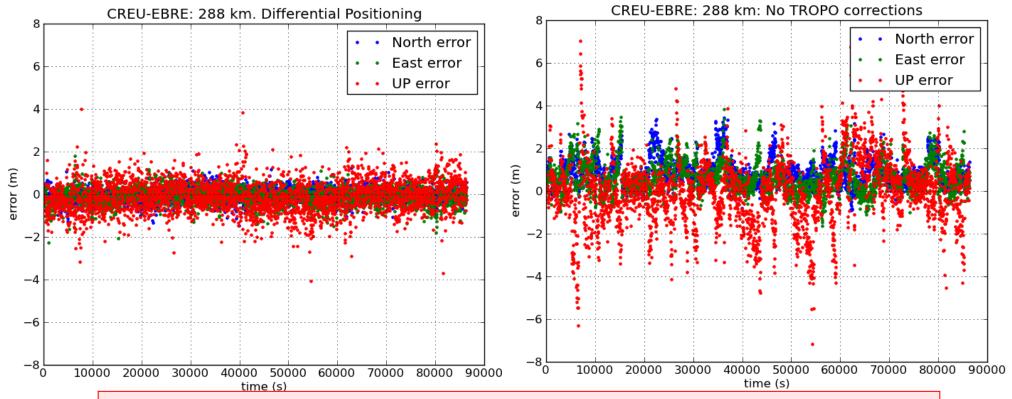
1.- Building the navigation equations system for differential positioning, but without using the tropospheric corrections:

```
cat D_EBRE_CREU.obs | gawk 'BEGIN{g2r=atan2(1,1)/45}{e=$12*g2r;a=$13*g2r;
    printf "%8.2f %8.4f %8.4f %8.4f %8.4f %1i \n",
    $4,$5-$9-$11,-cos(e)*sin(a),-cos(e)*cos(a),-sin(e),1}'> D_EBRE_CREU.mod
```

2.- Computing the user solution for differential positioning:

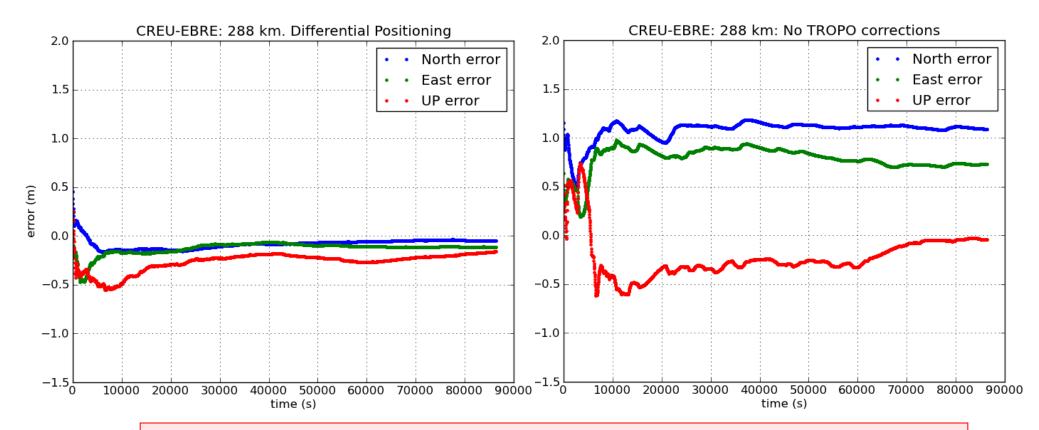
cat D\_EBRE\_CREU.mod | kalman > EBRE\_CREU.posS





#### **Questions:**

- Which error source has the higher impact on the position domain higher the ionosphere or the troposphere?
- Which is easier to model?



#### Question:

• Compare the results with those of the previous case, when not considering the ionospheric error.

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  - A2 Differential positioning of GARR-MATA receivers (Short baseline: 51 km)
- **▲ Session B: Orbit error effects** 
  - B1 Differential positioning of EBRE-CREU receivers (Long baseline: 288 km)
  - B2 Differential positioning of GARR-MATA receivers (Short baseline: 51 km)
  - B3 Range domain orbit error.

### A.2. Differential positioning of GARR\_MATA receivers (Short baseline: 51 km)

Repeat the previous exercise, but using the permanent receivers **GARR** and **MATA**, with only **51 km of baseline**.

#### **Model Components computation**

 The script "ObsFile1.scr" generates a data file "STA.obs" with the following content

```
1 2 3 4 5 6 7 8 9 10 11 12 13 14 [sta sat DoY sec P1 L1 P2 L2 Rho Trop Ion Elev Azim Prefit]
```

Run this script for GARR and MATA receivers:

```
ObsFile1.scr GARR0770.100 brdc0770.10n
ObsFile1.scr MATA0770.100 brdc0770.10n
```

• Generate the navigation equations system for absolute positioning for each receiver and compute the user solution (see next two slides).



Using the files GARR.obs and MATA.obs, follow the next steps:

- 1. Build the navigation equations system for each receiver, for absolute positioning.
- 2. Compute the user solutions in kinematic mode.
- 3. Plot the results and compare the positioning errors.

### 1.- Building the navigation equations system for absolute positioning:

```
cat GARR.obs | gawk 'BEGIN{g2r=atan2(1,1)/45}{e=$12*g2r;a=$13*g2r;
printf "%8.2f %8.4f %8.4f %8.4f %1i \n",
$4, $14, -cos(e)*sin(a),-cos(e)*cos(a),-sin(e),1 }'> GARR.mod
```

#### 2.- Computing the user solution for absolute positioning:

```
cp kalman.nml_wn kalman.nml
cat GARR.mod | kalman > GARR.pos
```

#### 3.- Plotting the results:

```
graph.py -f GARR.pos -x1 -y2 -s.- -l "North error"
   -f GARR.pos -x1 -y3 -s.- -l "East error"
   -f GARR.pos -x1 -y4 -s.- -l "UP error"
   --xl "time (s)" --yl "error (m)" --yn -8 --yx 8
   -t "GARR: Standard Point Positioning"
```

### 1.- Building the navigation equations system for absolute positioning:

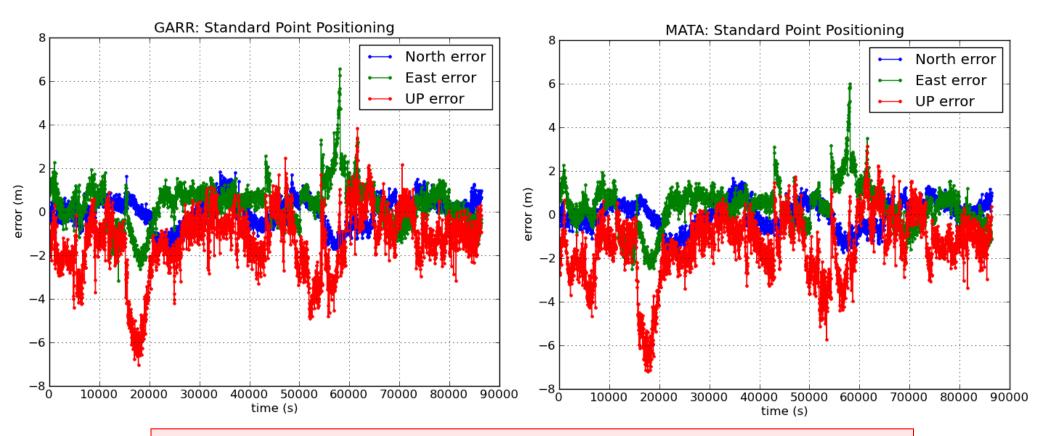
```
cat MATA.obs | gawk 'BEGIN{g2r=atan2(1,1)/45}{e=$12*g2r;a=$13*g2r;
    printf "%8.2f %8.4f %8.4f %8.4f %8.4f %1i \n",
    $4, $14, -cos(e)*sin(a),-cos(e)*cos(a),-sin(e),1 }'> MATA.mod
```

#### 2.- Computing the user solution for absolute positioning:

```
cp kalman.nml_wn kalman.nml
cat MATA.mod | kalman > MATA.pos
```

#### 3.- Plotting the results:

```
graph.py -f MATA.pos -x1 -y2 -s.- -l "North error"
   -f MATA.pos -x1 -y3 -s.- -l "East error"
   -f MATA.pos -x1 -y4 -s.- -l "UP error"
   --xl "time (s)" --yl "error (m)" --yn -8 --yx 8
   -t "MATA: Standard Point Positioning"
```



#### **Questions:**

- Compare the results with the previous case with a baseline of 280 km.
- Are the patterns even more similar now? Why?



### Using the files GARR.obs and MATA.obs, follow the next steps:

- Compute the single differences of measurements and model components.
- 2. Build the navigation equations system for the differential positioning of MATA receiver (user) relative to GARR (reference station).
- 3. Compute the user solution in kinematic mode and in static mode.
- 4. Plot the results and discuss the positioning error found.

1. Computing the single differences of measurements and model components.

Dobs.scr GARR.obs MATA.obs

2.- Building the navigation equations system for differential positioning:

```
cat D_GARR_MATA.obs | gawk 'BEGIN{g2r=atan2(1,1)/45}{e=$12*g2r;a=$13*g2r;
    printf "%8.2f %8.4f %8.4f %8.4f %8.4f %1i \n",
$4,$5-$9-$10-$11,-cos(e)*sin(a),-cos(e)*cos(a),-sin(e),1}'> D_GARR_MATA.mod
```

3.- Computing the user solution for differential positioning:



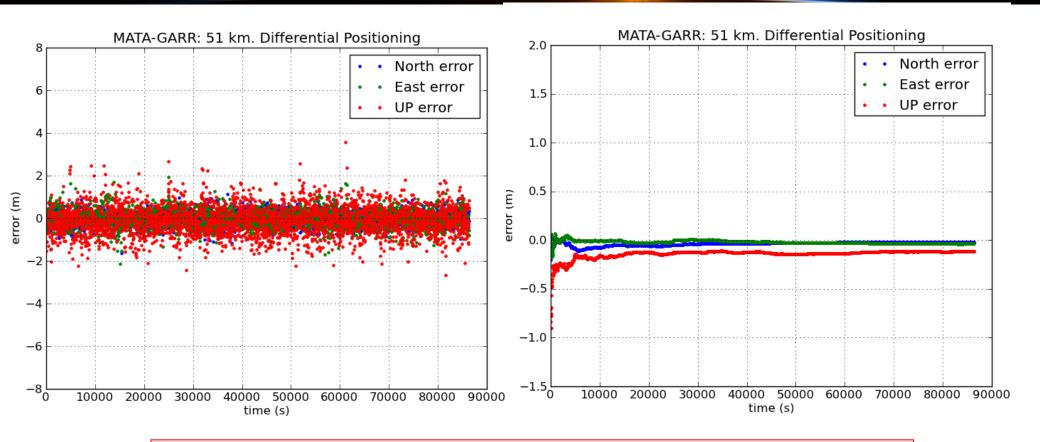
#### 4.- Plotting the results:

#### - Kinematic mode:

```
graph.py -f GARR_MATA.posK -x1 -y2 -s. -l "North error"
   -f GARR_MATA.posK -x1 -y3 -s. -l "East error"
   -f GARR_MATA.posK -x1 -y4 -s. -l "UP error"
   --xl "time (s)" --yl "error (m)" --yn -8 --yx 8
   -t "GARR_MATA: 51 km: Differential Positioning"
```

#### - Static mode:

```
graph.py -f GARR_MATA.posS -x1 -y2 -s. -l "North error"
    -f GARR_MATA.posS -x1 -y3 -s. -l "East error"
    -f GARR_MATA.posS -x1 -y4 -s. -l "UP error"
    --xl "time (s)" --yl "error (m)" --yn -8 --yx 8
    -t "GARR_MATA: 51 km: Differential Positioning"
```



#### **Questions:**

- Compare the results with the previous case with a baseline of 280 km.
- Are we reaching a similar level of accuracy? Why?



Analyze the effect of the differential ionosphere on the differential positioning of MATA relative to GARR station:

### Follow the next steps:

- 1. Using file **D\_GARR\_MATA.obs** plot the differential ionospheric correction (from Klobuchar model) between EBRE and CREU.
- 2. Repeat the previous process, but without applying the ionospheric correction. Compare the results

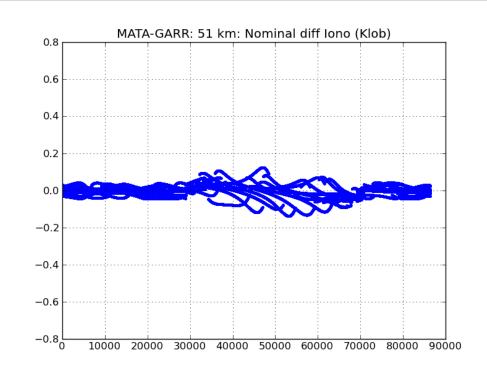
#### Plotting the Klobuchar differential ionospheric correction:

```
graph.py -f D_GARR_MATA.obs -x4 -y'11' --yn -0.8 --yx 0.8 -t "GARR-MATA: 51km: Nominal diff Iono (Klob)"
```

#### **Question:**

Justify the pattern seen in the nominal (Klobuchar) ionospheric corrections.

Compare the plot with that of the 280km baseline (slide #26). Do the results perform as expected?



### Computing the differential solution, but without using ionospheric corrections:

1.- Building the navigation equations system for differential positioning, but without using the ionospheric corrections:

```
cat D_GARR_MATA.obs | gawk 'BEGIN{g2r=atan2(1,1)/45}{e=$12*g2r;a=$13*g2r;
    printf "%8.2f %8.4f %8.4f %8.4f %8.4f %1i \n",
    $4,$5-$9-$10,-cos(e)*sin(a),-cos(e)*cos(a),-sin(e),1}'> D_GARR_MATA.mod
```

2.- Computing the user solution for differential positioning:

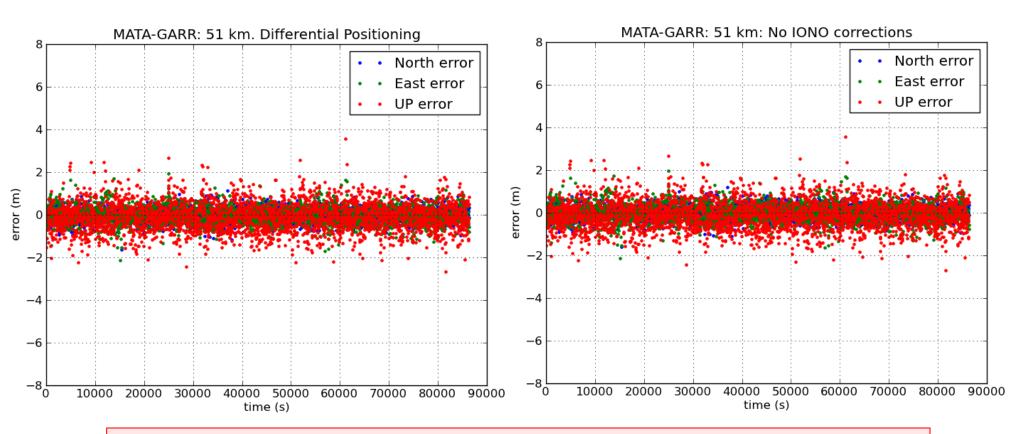
```
Kinematic:
```

```
cp kalman.nml_wn kalman.nml
cat D_GARR_MATA.mod | kalman > GARR_MATA.posK
```

#### Static:

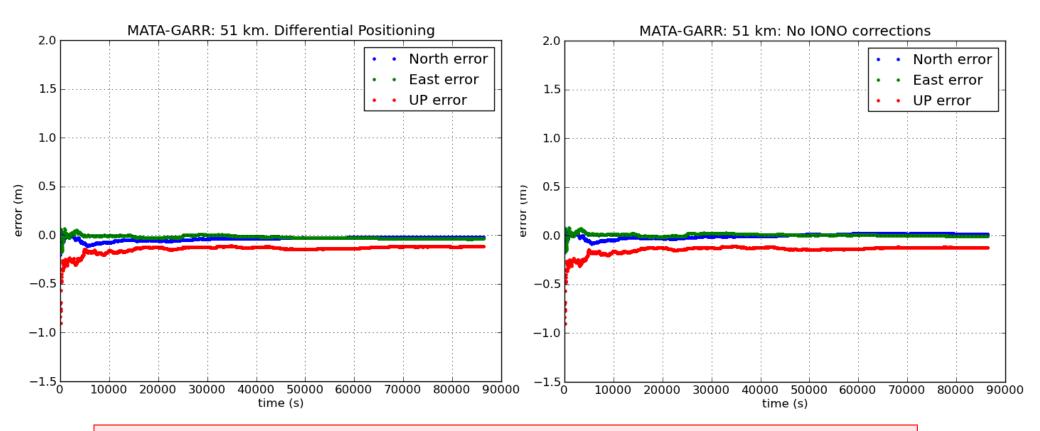
```
cp kalman.nml_ct kalman.nml
cat D_GARR_MATA.mod | kalman > GARR_MATA.posS
```





#### Question:

• Do the results confirm the expected effect of neglecting the ionospheric corrections for this baseline (using code measurements ) at the user level?



#### Question:

• Do the results confirm the expected effect of neglecting the ionospheric corrections for this baseline (using code measurements ) at the user level?

Analyze the effect of the differential Troposphere on the differential positioning of MATA relative to GARR station:

### Follow the next steps:

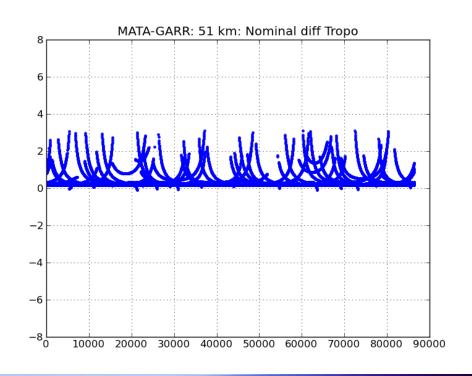
- 1. Using file **D\_GARR\_MATA.obs** plot the differential trpospheric correction (from nominal model) between EBRE and CREU.
- 2. Repeat the previous process, but without applying the tropospheric correction. Compare the results.

#### Plotting the nominal differential tropospheric correction:

```
graph.py -f D_GARR_MATA.obs -x4 -y'10' --yn -8 --yx 8
-t "GARR_MATA: 51km: Nominal diff Tropo"
```

#### **Question:**

Justify the pattern seen in the nominal tropospheric corrections. Compare the plot with that of the 280km baseline (slide #31). Do the results perform as expected?



### Computing the differential solution, but without using tropospheric corrections:

1.- Building the navigation equations system for differential positioning, but without using the tropospheric corrections:

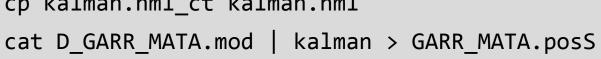
```
cat D_GARR_MATA.obs | gawk 'BEGIN{g2r=atan2(1,1)/45}{e=$12*g2r;a=$13*g2r;
    printf "%8.2f %8.4f %8.4f %8.4f %8.4f %1i \n",
    $4,$5-$9-$11,-cos(e)*sin(a),-cos(e)*cos(a),-sin(e),1}'> D_GARR_MATA.mod
```

2.- Computing the user solution for differential positioning:

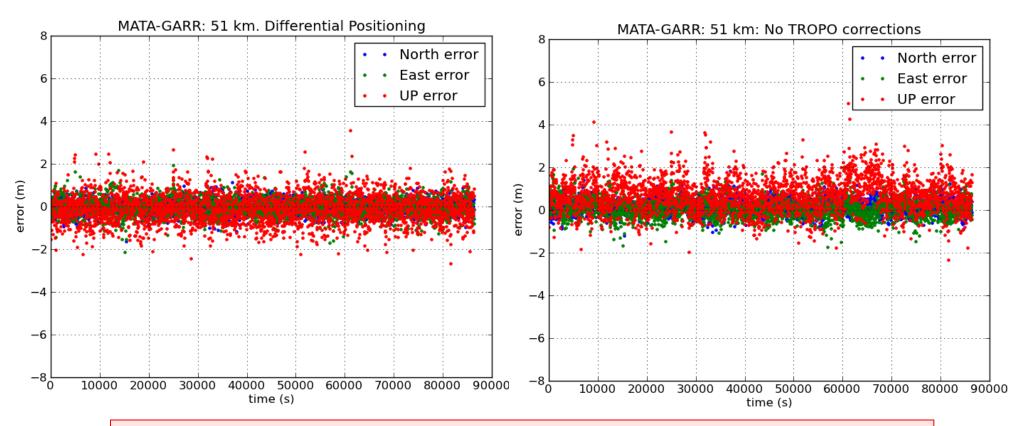
```
Kinematic:
cat D_GARR_MATA.mod | kalman > GARR_MATA.posK

cp kalman.nml_ct kalman.nml
```



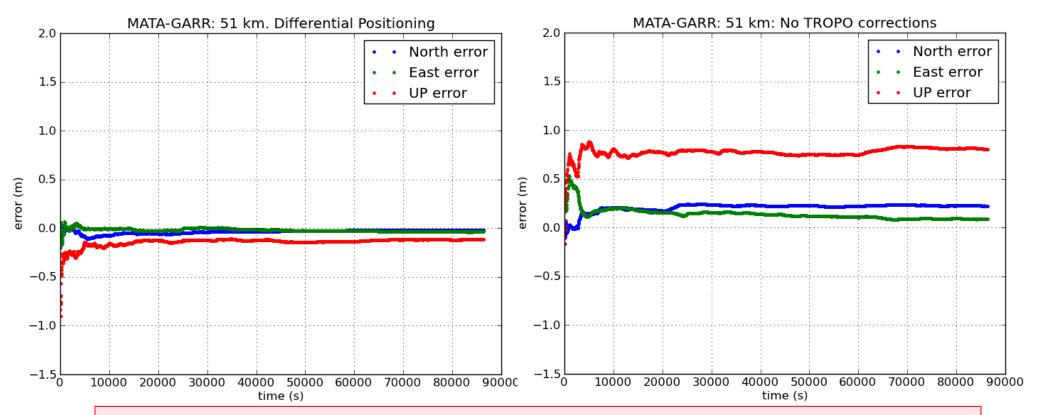






#### Question:

• Do the results confirm the expected effect of neglecting the tropospheric corrections for this baseline (using code measurements ) at the user level?



#### **Question:**

- Discuss the error found at the user level for the 50 Km of baseline.
- Is the error level similar to the error seen with the 280km of baseline (slide 34#)?
- Should the tropospheric corrections still be applied for these baselines?



### **OVERVIEW**

### ▲ Introduction: gLAB processing in command line

### Session A: Atmospheric effects

- A1 Differential positioning of EBRE-CREU receivers (Long baseline: 288 km)
- A2 Differential positioning of GARR-MATA receivers (Short baseline: 15 km)

#### Session B: Orbit error effects

- B1 Differential positioning of EBRE-CREU receivers (Long baseline: 288 km)
- B2 Differential positioning of GARR-MATA receivers (Short baseline: 15 km)
- B3 Range domain orbit error.

### **Session B**

# Differential positioning Orbit errors

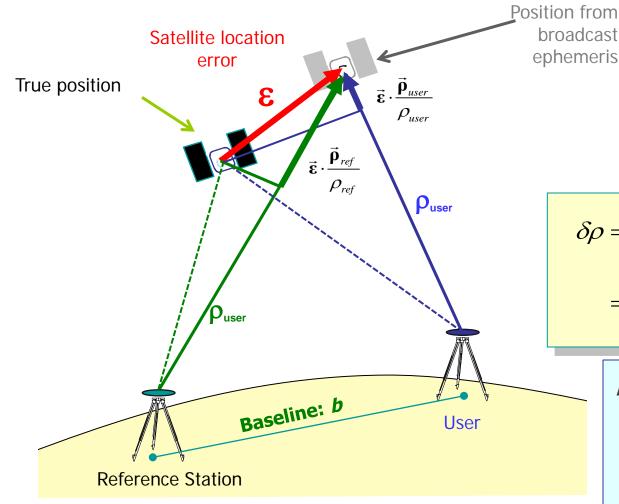
### B. Orbit error effect on Differential positioning.

The target of this exercise is to asses the satellite orbit error on absolute and differential positioning.

This will be done by modifying the broadcast orbit parameters to generate an Along-track orbit error of about 2000m and, positioning two receivers with these corrupted orbits.

The user positioning error using the original and the corrupted orbits will be compared for absolute and differential positioning, with the receivers and baselines used in the previous session.

### **Ephemeris Errors and Geographic decorrelation**



Differential range error due to satellite obit error

$$\delta \rho = \vec{\mathbf{\epsilon}} \cdot \frac{\vec{\boldsymbol{\rho}}_{user}}{\rho_{user}} - \vec{\mathbf{\epsilon}} \cdot \frac{\vec{\boldsymbol{\rho}}_{ref}}{\rho_{ref}}$$

$$\delta \rho = -\frac{b \sin \phi}{\rho} \vec{\mathbf{e}}^T \cdot \hat{\mathbf{u}} = -\vec{\mathbf{e}}^T \cdot (\sin \phi \, \hat{\mathbf{u}}) \frac{b}{\rho}$$
$$= -\vec{\mathbf{e}}^T \left( \mathbf{I} - \hat{\boldsymbol{\rho}} \cdot \hat{\boldsymbol{\rho}}^T \right) \frac{\mathbf{b}}{\rho} \quad \text{Where: } \mathbf{b} = b \, \hat{\mathbf{b}} \text{ is the baseline vector}$$

#### A conservative bound:

 $\delta \rho < \frac{b}{\rho} \varepsilon$ 

with a baseline b = 20km

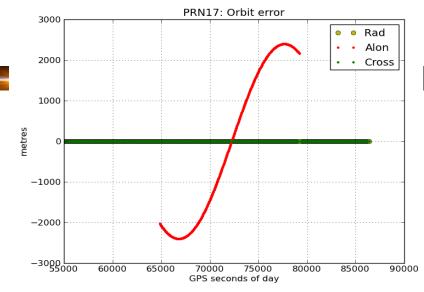
$$\delta \rho < \frac{20}{20000} \varepsilon = \frac{1}{1000} \varepsilon$$

#### **B.** Orbit error effect.

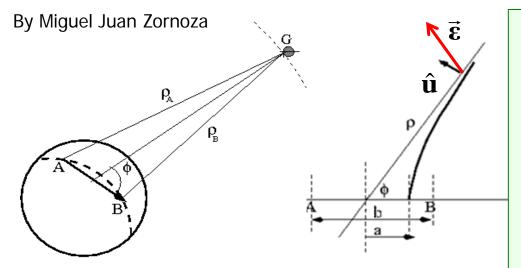
#### Injecting an error to broadcast orbits:

Along-track Error (PRN17)

The following ephemeris block of PRN17 is modified In order to simulate an Along-track error of about 2000m. The corrupted file is renamed as: brdc0770.10nERR







 $a = (\rho_R - \rho_A)/2$ : hyperboloid semiaxis

b/2: focal length

where 
$$a = \frac{1}{2}b\cos\phi$$

Note: in this 3D problem  $\phi$  is NOT the elevation of ray.

Differential range error  $\delta \rho$  produced by an orbit error  $arepsilon_{\scriptscriptstyle \parallel}$  parallel to vector  $\hat{\mathbf{u}}$ 

Let 
$$\delta \varepsilon \equiv \varepsilon_{\parallel}$$

$$\delta\rho \equiv \delta(\rho_B - \rho_A) = 2\delta a =$$

$$= 2\frac{\partial a}{\partial \varepsilon} \delta\varepsilon = 2\frac{\partial a}{\partial \phi} \frac{\partial \phi}{\partial \varepsilon} \delta\varepsilon = -b\sin\phi \frac{\partial \phi}{\partial \varepsilon} \delta\varepsilon$$

$$\approx -b\sin\phi \frac{1}{\rho} \delta\varepsilon$$

$$\text{Note: } \vec{\mathbf{e}}_{\parallel} \perp \vec{\mathbf{p}} \Rightarrow \delta\varepsilon \approx \rho \delta\phi$$

- Errors over the hyperboloid (i.e.  $\rho_{\rm\scriptscriptstyle B} - \rho_{\rm\scriptscriptstyle A} = ctt$  ) will not produce differential range errors.
  - The highest error is given by the vector  $\hat{\mathbf{u}}$  , orthogonal to the hyperboloid and over the plain containing the baseline vector **b** and the LoS vector  $\hat{\mathbf{\rho}}$ .

Note:

Being the baseline b much smaller than the distance to the satellite, we can assume that the LoS vectors from A and B receives are essentially identical to  $\rho$ .

That is,  $\rho_{\scriptscriptstyle R} \cong \rho_{\scriptscriptstyle A} \cong \rho$ 

$$\mathbf{u} = \hat{\boldsymbol{\rho}} \times (\hat{\mathbf{b}} \times \hat{\boldsymbol{\rho}}) = \hat{\mathbf{b}} (\hat{\boldsymbol{\rho}}^T \cdot \hat{\boldsymbol{\rho}}) - \hat{\boldsymbol{\rho}} (\hat{\boldsymbol{\rho}}^T \cdot \hat{\mathbf{b}})$$
$$= \mathbf{I} \hat{\mathbf{b}} - (\hat{\boldsymbol{\rho}} \cdot \hat{\boldsymbol{\rho}}^T) \hat{\mathbf{b}} = (\mathbf{I} - \hat{\boldsymbol{\rho}} \cdot \hat{\boldsymbol{\rho}}^T) \hat{\mathbf{b}}$$

Note:  $\mathbf{u} = \sin \phi \,\hat{\mathbf{u}}$ 

Note: being  $\hat{\mathbf{u}}$  a vector orthogonal to the LoS  $\hat{\mathbf{\rho}}$ , thence,  $\varepsilon_{\parallel} = \vec{\mathbf{\epsilon}}^T \hat{\mathbf{u}}$ 

Thence:

$$\delta \rho = -\frac{b \sin \phi}{\rho} \vec{\mathbf{\epsilon}}^T \cdot \hat{\mathbf{u}} = -\vec{\mathbf{\epsilon}}^T \cdot (\sin \phi \, \hat{\mathbf{u}}) \frac{b}{\rho}$$

$$= -\vec{\mathbf{\epsilon}}^T \left( \mathbf{I} - \hat{\boldsymbol{\rho}} \cdot \hat{\boldsymbol{\rho}}^T \right) \frac{\mathbf{b}}{\rho}$$
 Where:  $\mathbf{b} = b \hat{\mathbf{b}}$  is the baseline year

is the baseline vector

### **OVERVIEW**

### ▲ Introduction: gLAB processing in command line

- **△ Session A: Atmospheric effects** 
  - A1 Differential positioning of EBRE-CREU receivers (Long baseline: 288 km)
  - A2 Differential positioning of GARR-MATA receivers (Short baseline: 15 km)
- Session B: Orbit error effects
  - B1 Differential positioning of EBRE-CREU receivers (Long baseline: 288 km)
  - B2 Differential positioning of GARR-MATA receivers (Short baseline: 15 km)
  - B3 Range domain orbit error.

Repeat the computation of the absolute positioning of receivers **EBRE** and **CREU**, but using the corrupted ephemeris file **brdc0770.10nERR**.

#### **Model Components computation**

 The script "ObsFile1.scr" generates a data file "STA.obs" with the following content

```
1 2 3 4 5 6 7 8 9 10 11 12 13 14 [sta sat DoY sec P1 L1 P2 L2 Rho Trop Ion Elev Azim Prefit]
```

• Run this script for EBRE and CREU receivers. Rename as STA.obsERR the output files

Observed the output files

```
ObsFile1.scr EBRE0770.100 brdc0770.10nERR
mv EBRE.obs EBRE.obsERR
ObsFile1.scr CREU0770.100 brdc0770.10nERR
mv EBRE.obs EBRE.obsERR
```

 Generate the navigation equations system for absolute positioning for each receiver and compute the user solution (see the next two slides).



### 1.- Building the navigation equations system for absolute positioning:

```
cat EBRE.obsERR | gawk 'BEGIN{g2r=atan2(1,1)/45}{e=$12*g2r;a=$13*g2r;
printf "%8.2f %8.4f %8.4f %8.4f %1i \n",
$4, $14, -cos(e)*sin(a),-cos(e)*cos(a),-sin(e),1 }'> EBRE.modERR
```

#### 2.- Computing the user solution for absolute positioning:

```
cp kalman.nml_wn kalman.nml
cat EBRE.modERR | kalman > EBRE.posERR
```

#### 3.- Plotting the results:

```
graph.py -f EBRE.posERR -x1 -y2 -s.- -l "North error"
-f EBRE.posERR -x1 -y3 -s.- -l "East error"
-f EBRE.posERR -x1 -y4 -s.- -l "UP error"
--xl "time (s)" --yl "error (m)" --yn -300 --yx 300
-t "EBRE: SPP: 2000m Along-Track orbit error"
```

### 1.- Building the navigation equations system for absolute positioning:

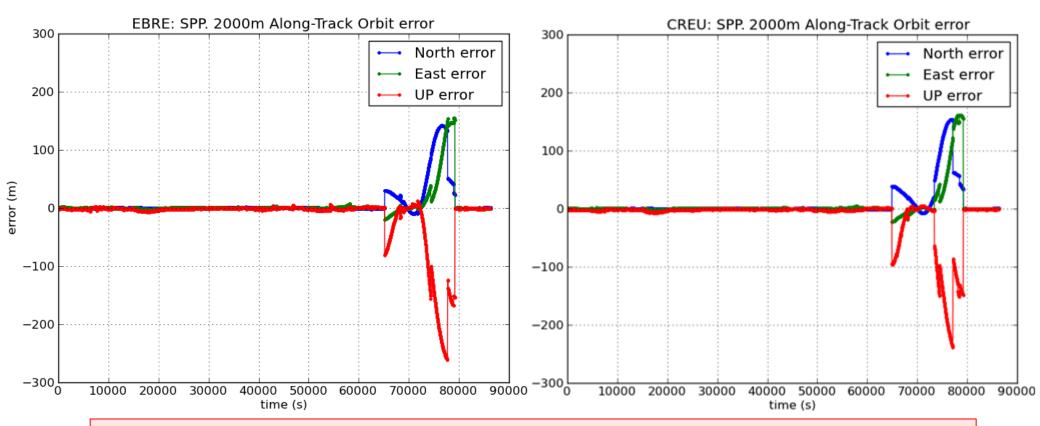
```
cat CREU.obsERR | gawk 'BEGIN{g2r=atan2(1,1)/45}{e=$12*g2r;a=$13*g2r;
    printf "%8.2f %8.4f %8.4f %8.4f %1i \n",
    $4, $14,-cos(e)*sin(a),-cos(e)*cos(a),-sin(e),1 }'> CREU.modERR
```

#### 2.- Computing the user solution for absolute positioning:

```
cp kalman.nml_wn kalman.nml
cat CREU.modERR | kalman > CREU.posERR
```

#### 3.- Plotting the results:

```
graph.py -f CREU.posERR -x1 -y2 -s.- -l "North error"
-f CREU.posERR -x1 -y3 -s.- -l "East error"
-f CREU.posERR -x1 -y4 -s.- -l "UP error"
--xl "time (s)" --yl "error (m)" --yn -300 --yx 300
-t "CREU: SPP: 2000m Along-Track orbit error"
```



#### **Question:**

- Is the impact on user positioning error similar for both receivers?
- From these plots, what is the expected level of error in differential positioning?



Analyse the effect of the 2000m orbit error on the differential positioning of CREU receiver relative to EBRE, with 280km of baseline.

Using the files EBRE.obsERR and CREU.obsERR, follow next steps:

- 1. Compute the single differences of measurements and model components.
- 2. Build the navigation equations system for the differential positioning of CREU receiver (user) relative to EBRE (reference station).
- 3. Compute the user solution in kinematic mode.
- 4. Plot the results and discuss the positioning error found.

1.- Computing the single differences of measurements and model

```
components. Dobs.scr EBRE.obsERR CREU.obsERR mv D_EBRE_CREU.obs D_EBRE_CREU.obsERR
```

2.- Building the navigation equations system for differential positioning:

```
cat D_EBRE_CREU.obsERR | gawk 'BEGIN{g2r=atan2(1,1)/45}{e=$12*g2r;a=$13*g2r;
    printf "%8.2f %8.4f %8.4f %8.4f %8.4f %1i \n",
$4,$5-$9-$10-$11,-cos(e)*sin(a),-cos(e)*cos(a),-sin(e),1}'>D_EBRE_CREU.modERR
```

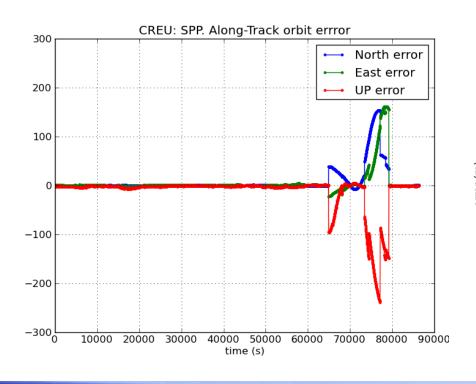
3.- Computing the user solution for differential positioning:

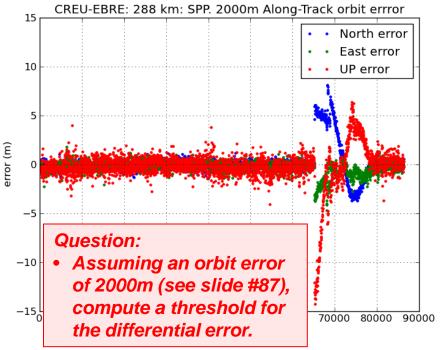
```
Kinematic:
```

```
cp kalman.nml_wn kalman.nml
cat D_EBRE_CREU.modERR| kalman > EBRE_CREU.posKERR
```

### 4.- Plotting results:

```
graph.py -f D_EBRE_CREU.modERR -x1 -y2 -s. -l "North error"
-f D_EBRE_CREU.modERR -x1 -y3 -s. -l "East error"
-f D_EBRE_CREU.modERR -x1 -y4 -s. -l "UP error"
--xl "time (s)" --yl "error (m)" --yn -15 --yx 15
-t "EBRE-CREU 280km: SPP: 2000m Along-Track orbit error"
```





### **OVERVIEW**

### ▲ Introduction: gLAB processing in command line

- **△ Session A: Atmospheric effects** 
  - A1 Differential positioning of EBRE-CREU receivers (Long baseline: 288 km)
  - A2 Differential positioning of GARR-MATA receivers (Short baseline: 15 km)

#### Session B: Orbit error effects

- B1 Differential positioning of EBRE-CREU receivers (Long baseline: 288 km)
- B2 Differential positioning of GARR-MATA receivers (Short baseline: 15 km)
- B3 Range domain orbit error.

### B2. Orbit error: Differential positioning of GARR-MATA receivers (Long baseline: 51 km)

Repeat the computation of the absolute positioning of receivers **GARR** and **MATA**, but using the corrupted ephemeris file **brdc0770.10nERR**.

#### **Model Components computation**

 The script "ObsFile1.scr" generates a data file "STA.obs" with the following content

1 2 3 4 5 6 7 8 9 10 11 12 13 14 [sta sat DoY sec P1 L1 P2 L2 Rho Trop Ion Elev Azim Prefit]

• Run this script for GARR and MATA receivers. Rename as STA. obsERR the output files

ObsEilel.scr GARR0770.100 brdc0770.10nERR

ObsFile1.scr GARR0770.100 brdc0770.10nERR
mv GARR.obs GARR.obsERR
ObsFile1.scr MATA0770.100 brdc0770.10nERR
mv MATA.obs MATA.obsERR

 Generate the navigation equations system for absolute positioning for each receiver and compute the user solution (see next two slides).



### B2. Orbit error: Differential positioning of GARR-MATA receivers (Long baseline: 51 km)

### 1.- Building the navigation equations system for absolute positioning:

```
cat GARR.obsERR | gawk 'BEGIN{g2r=atan2(1,1)/45}{e=$12*g2r;a=$13*g2r;
    printf "%8.2f %8.4f %8.4f %8.4f %1i \n",
    $4, $14, -cos(e)*sin(a),-cos(e)*cos(a),-sin(e),1 }'> GARR.modERR
```

#### 2.- Computing the user solution for absolute positioning:

```
cp kalman.nml_wn kalman.nml
cat GARR.modERR | kalman > GARR.posERR
```

#### 3.- Plotting the results:

```
graph.py -f GARR.posERR -x1 -y2 -s.- -l "North error"
-f GARR.posERR -x1 -y3 -s.- -l "East error"
-f GARR.posERR -x1 -y4 -s.- -l "UP error"
--xl "time (s)" --yl "error (m)" --yn -300 --yx 300
-t "GARR: SPP: 2000m Along-Track orbit error"
```

### B2. Orbit error: Differential positioning of GARR-MATA receivers (Long baseline: 51 km)

### 1.- Building the navigation equations system for absolute positioning:

```
cat MATA.obsERR | gawk 'BEGIN{g2r=atan2(1,1)/45}{e=$12*g2r;a=$13*g2r;
printf "%8.2f %8.4f %8.4f %8.4f %8.4f %1i \n",
$4, $14, -cos(e)*sin(a),-cos(e)*cos(a),-sin(e),1 }'> MATA.modERR
```

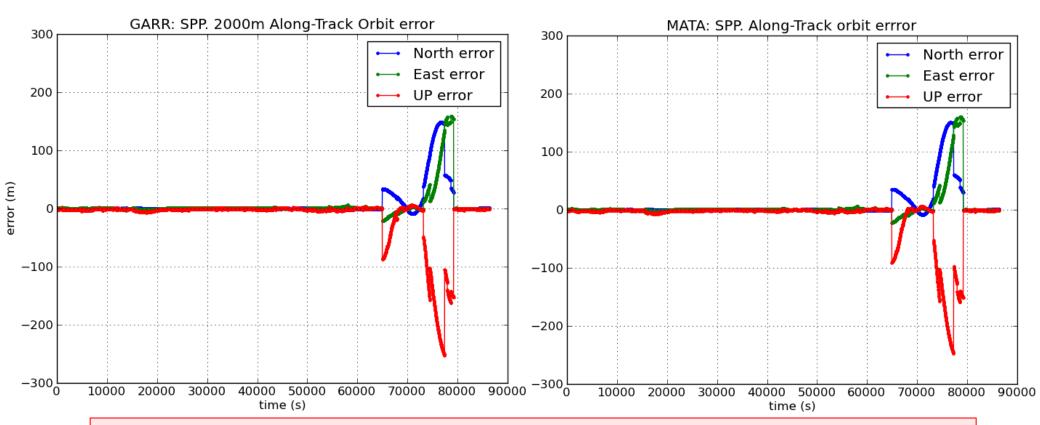
#### 2.- Computing the user solution for absolute positioning:

```
cp kalman.nml_wn kalman.nml
cat MATA.modERR | kalman > MATA.posERR
```

#### 3.- Plotting the results:

```
graph.py -f MATA.posERR -x1 -y2 -s.- -l "North error"
-f MATA.posERR -x1 -y3 -s.- -l "East error"
-f MATA.posERR -x1 -y4 -s.- -l "UP error"
--xl "time (s)" --yl "error (m)" --yn -300 --yx 300
-t "MATA: SPP: 2000m Along-Track orbit error"
```

#### B2. Orbit error: Differential positioning of GARR-MATA receivers (Long baseline: 51 km)



#### **Question:**

- Is the impact on user positioning error similar for both receivers?
- From these plots, what is the expected level of error in differential positioning?



#### B2. Orbit error: Differential positioning of GARR-MATA receivers (Short baseline: 51 km)

Analyse the effect of the 2000m orbit error on the differential positioning of MATA receiver relative to GARR, with 51km of baseline.

Using the files GARR.obsERR and MATA.obsERR, follow the next steps:

- Compute the single differences of measurements and model components.
- Build the navigation equations system for the differential positioning of MATA receiver (user) relative to GARR (reference station).
- Compute the user solution in kinematic mode.
- 4. Plot the results and discuss the positioning error found.

#### B2. Orbit error: Differential positioning of GARR-MATA receivers (Long baseline: 51 km)

- 1. Computing the single differences of measurements and model components.

  Dobs.scr GARR.obsERR MATA.obsERR
- 2.- Building the navigation equations system for differential positioning:

```
cat D_GARR_MATA.obsERR | gawk 'BEGIN{g2r=atan2(1,1)/45}{e=$12*g2r;a=$13*g2r;
    printf "%8.2f %8.4f %8.4f %8.4f %8.4f %1i \n",
$4,$5-$9-$10-$11,-cos(e)*sin(a),-cos(e)*cos(a),-sin(e),1}'>D_GARR_MATA.modERR
```

3.- Computing the user solution for differential positioning:

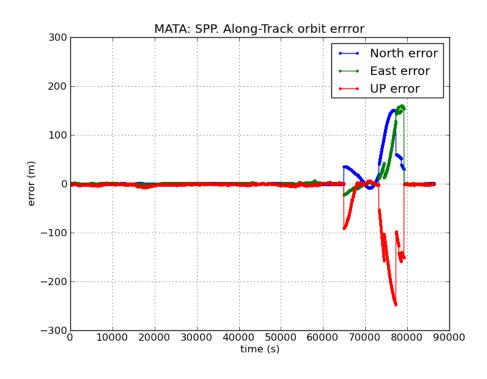
```
Kinematic:
```

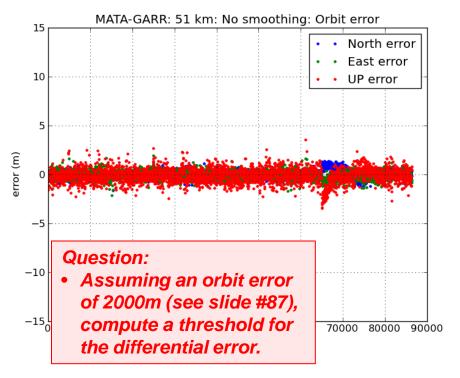
```
cp kalman.nml_wn kalman.nml
cat D_GARR_MATA.modERR| kalman > GARR_MATA.posKERR
```

#### B2. Orbit error: Differential positioning of GARR-MATA receivers (Long baseline: 51 km)

#### 4.- Plotting results:

```
graph.py -f D_GARR_MATA.modERR -x1 -y2 -s. -l "North error"
-f D_GARR_MATA.modERR -x1 -y3 -s. -l "East error"
-f D_GARR_MATA.modERR -x1 -y4 -s. -l "UP error"
--xl "time (s)" --yl "error (m)" --yn -8 --yx 8
-t "GARR_MATA 51km: SPP: 2000m Along-Track orbit error"
```





#### **OVERVIEW**

#### ▲ Introduction: gLAB processing in command line

#### Session A: Atmospheric effects

- A1 Differential positioning of EBRE-CREU receivers (Long baseline: 288 km)
- A2 Differential positioning of GARR-MATA receivers (Short baseline: 15 km)

#### Session B: Orbit error effects

- B1 Differential positioning of EBRE-CREU receivers (Long baseline: 288 km)
- B2 Differential positioning of GARR-MATA receivers (Short baseline: 15 km)
- B3 Range domain orbit error.

Analyze the orbit error of **PRN17** in the Range Domain.

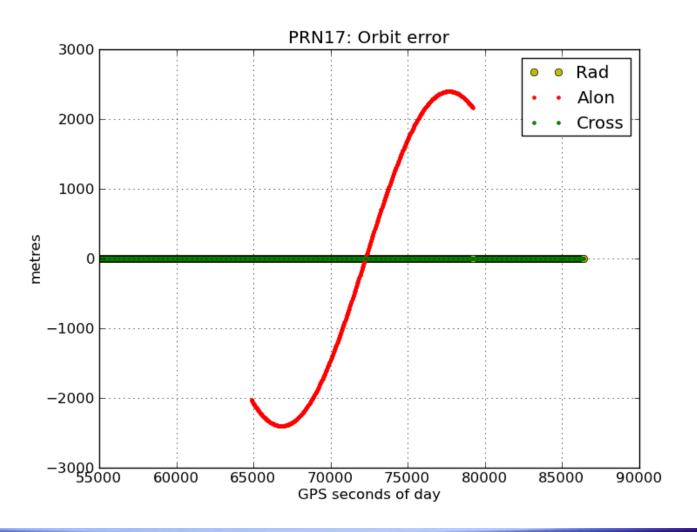
The following procedure is proposed: Using the files **brdc0770.10n** and **brdc0770.10nERR**, follow the next steps:

- 1. Compute the absolute orbit for satellite PNR17 error by comparing the corrupted orbits with the original ones.
- 2. Compute the range error for the receivers EBRE and CREU
- 3. Compute the differential range error between EBRE and CREU
- 4. Compute the predicted range error between EBRE and CREU and compare with the present one.

#### **B.3.1.- Absolute error computation for satellite PRN17:**

Compute the discrepance between the satellite coordinates predicted from files brdc0770.10n and brdc0770.10nERR

#### Plot the results for satellite PRN17:



#### **B.3.2.- Absolute Range error** computation for satellite PRN17 from **EBRE**:

- 1. Using the original orbits **brdc0770.10n**, compute the geometric range between EBRE and satellite PRN17 (i.e **rang.ebre** file).
  - 1.1- Compute the satellite coordinates with the original orbits and generate a file with the following content:

```
[time X Y Z]
```

1.2.- Using the coordinates EBRE=[4833520.1197 41537.2015 4147461.6263], compute the geometric range between EBRE and satellite PRN17:

```
cat xyz.brdc | gawk 'BEGIN{x0=4833520.1197;y0=41537.2015;z0=4147461.6263}
{dx=$2-x0;dy=$3-y0;dz=$4-z0;rho=sqrt(dx**2+dy**2+dz**2);
printf "%s %16.6f \n", $1,rho}' > rang.ebre
```

- 2. Repeat the previous computation using the corrupted orbits file brdc0770.10nERR (i.e. generate the rang.ebreERR file).
  - 2.1- Compute the satellite coordinates with the corrupted orbits and generate a file with the following content:

```
1 2 3 4
[time X Y Z]
```

2.2.- Using the coordinates EBRE=[4833520.1197 41537.2015 4147461.6263], compute the geometric range between EBRE and satellite PRN17:

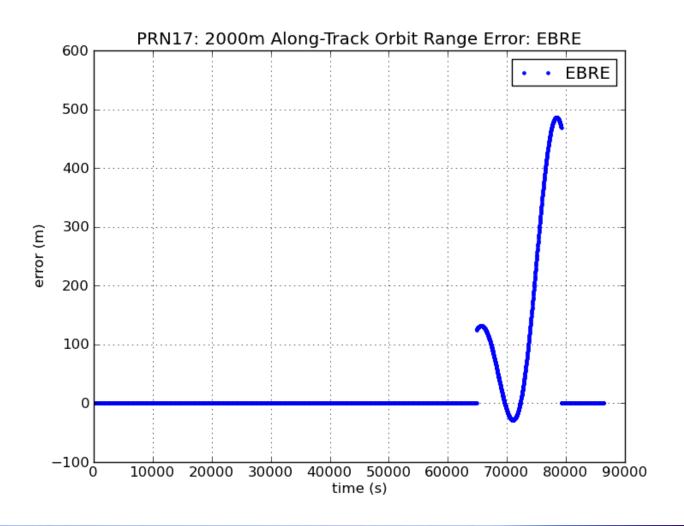
```
cat xyz.brdcERR|gawk 'BEGIN{x0=4833520.1197;y0=41537.2015;z0=4147461.6263}
{dx=$2-x0;dy=$3-y0;dz=$4-z0;rho=sqrt(dx**2+dy**2+dz**2);
printf "%s %16.6f \n", $1,rho}' > rang.ebreERR
```

3. Calculate the discrepancy between the geometric ranges computed using the original and the corrupted orbits:

```
cat rang.ebre rang.ebreERR | gawk '{i=$1*1;if (length(r[i])==0) {r[i]=$2}else{print i,$2-r[i]}' > drang.ebre
```

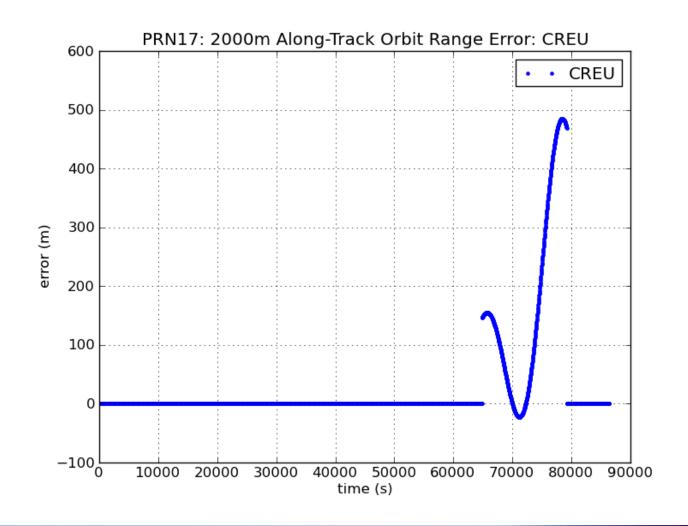
#### 4.- Plot the results

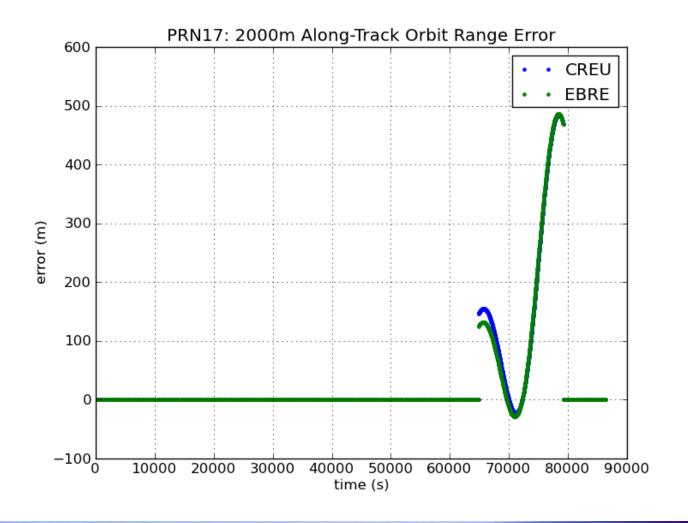
```
graph.py -f drang.ebre -x1 -y2 -l"EBRE"
--xl "time (s)" --yl "error (m)" --yx 600
-t"PRN17: 2000m AT orbit error PRN17: EBRE: Range Error"
```



Absolute Range error computation for satellite PRN17 from CREU:

- Repeat the previous computations of section B.3.2 for the receiver CREU.
- b) Compare in the same plot the results for EBRE and CREU





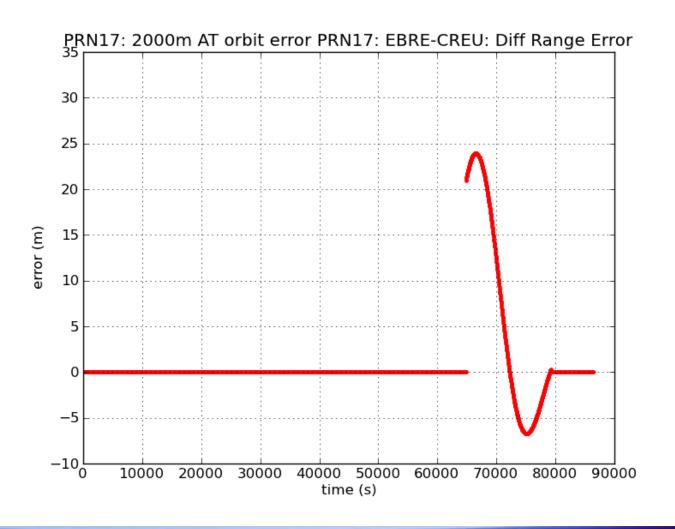
#### **B.3.3 Differential range Error computation**

Using the previous files **drang.ebre** and **drang.creu**, compute the differential range orbit error of PRN17 between the receivers EBRE and CREU

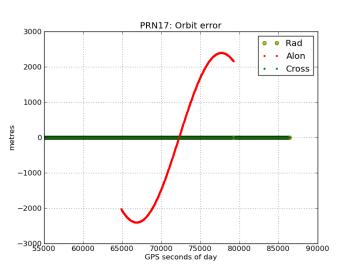
```
cat drang.ebre drang.creu | gawk '{i=$1*1;if (length(r[i])==0) {r[i]=$2}else{printf "%s %16.6f \n", i,$2-r[i]}' > ddrang.creu_ebre
```

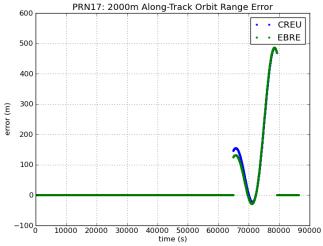
#### Plot the results

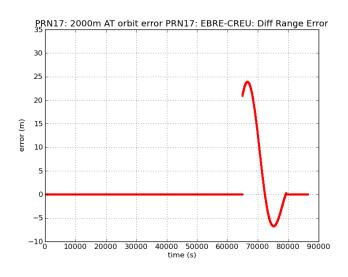
```
graph.py -f ddrang.creu_ebre -x1 -y2 -s. --cl r --yn -10 --yx 35
    --xl "time (s)" --yl "error (m)"
    -t"PRN17: 2000m AT orbit error PRN17: EBRE-CREU: Diff Range Error"
```



#### Results comparison

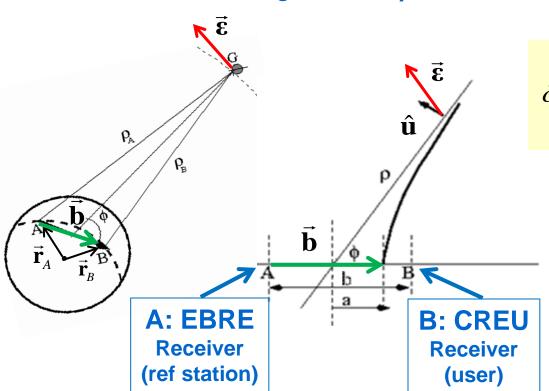






#### **B.3.4.** Prediction of the differential range orbit error

Verify the next expression, which relates the orbit error  $\varepsilon$  with the differential range error  $\delta \rho$ :



$$\delta \rho = -\frac{b}{\rho} \vec{\mathbf{\epsilon}}^T \cdot \mathbf{u} = -\frac{b}{\rho} \vec{\mathbf{\epsilon}}^T \cdot \left[ \hat{\mathbf{b}} - \hat{\boldsymbol{\rho}} \left( \hat{\boldsymbol{\rho}}^T \cdot \hat{\mathbf{b}} \right) \right]$$

#### **Baseline vector**

$$\vec{\mathbf{b}} = \vec{\mathbf{r}}_B - \vec{\mathbf{r}}_A$$

 $\vec{\mathbf{r}}_A = [4833520.1197, 41537.2015, 4147461.6263]$ 

 $\vec{\mathbf{r}}_B = [4715420.3054, 273177.8809, 4271946.7957]$ 

#### The following procedure can be applied:

1.- Compute the orbit error  $\varepsilon$  vector from the original and corrupted orbits:

2.- From previous results, generate a file err.dat with the orbit error ( $\varepsilon$ ) vector and the Line-Of-Sight ( $\rho$ ) from CREU receiver (with coordinates [4715420.3054, 273177.8809, 4271946.7957]), according to format: err.dat=[sec  $\varepsilon_x$   $\varepsilon_y$   $\varepsilon_z$   $\rho_x$   $\rho_y$   $\rho_z$ ]

#### 3.- Using the expression:

$$\delta \rho = -\frac{b}{\rho} \vec{\mathbf{\epsilon}}^T \cdot \mathbf{u} = -\frac{b}{\rho} \vec{\mathbf{\epsilon}}^T \cdot \left[ \hat{\mathbf{b}} - \hat{\boldsymbol{\rho}} \left( \hat{\boldsymbol{\rho}}^T \cdot \hat{\mathbf{b}} \right) \right]$$

**Baseline vector** 

$$\vec{\mathbf{b}} = \vec{\mathbf{r}}_{B} - \vec{\mathbf{r}}_{A}$$

#### and the receivers' coordinates:

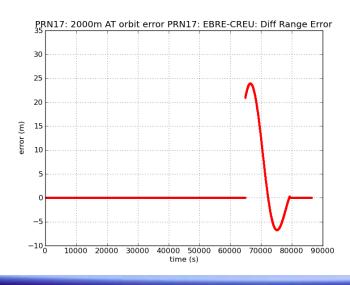
EBRE:  $\vec{\mathbf{r}}_A = [4833520.1197, 41537.2015, 4147461.6263]$ 

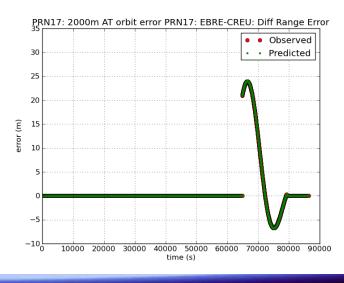
**CREU**:  $\vec{\mathbf{r}}_B = [4715420.3054, 273177.8809, 4271946.7957]$ 

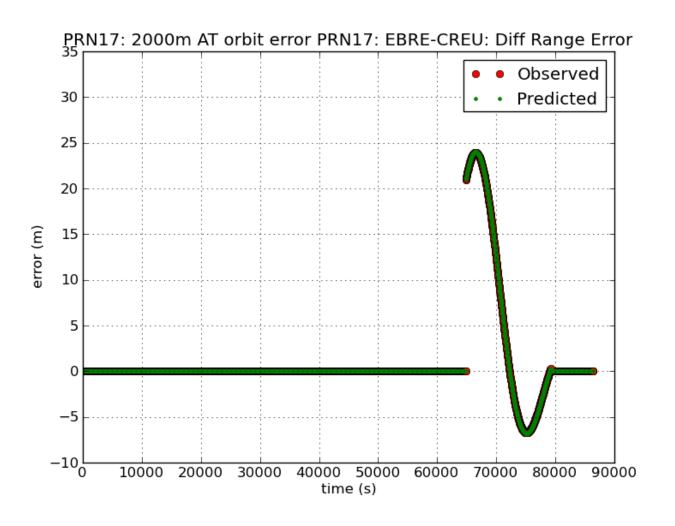
Compute the predicted differential orbit error  $d\rho$  for the receiver CREU relative to EBRE station.

Plot the results and compare with the result found in the previous exercise B.3.3 (i.e. with those of file ddrang.creu\_ebre):

```
graph.py -f ddrang.creu_ebre -x1 -y2 -so --cl r -l "Observed"
   -f rang.err -x1 -y2 -l "Predicted"
   --xl "time (s)" --yl "error (m)"
   -t"PRN17: 2000m AT orbit error PRN17: EBRE-CREU: Diff Range Error"
   --yn -10 --yx 35
```







# Thanks for your attention

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