

Young Tableau, Symmetric Functions, Schubert Polynomials, and Degeneracy Loci

With 0 Figures

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Preface

These are notes for a reading course under Professor [Dave Anderson](#). They begin with a review of some material from Fulton's *Young Tableaux*¹ [[Ful97](#)]. However, the primary focus is Manivel's *Symmetric Functions, Schubert Polynomials, and Degeneracy Loci* [[Man01](#)] which one could see as a quasi-sequel.

¹which throughout these notes will be spelled as “tableaux” or “tableau” with no real consistency.

Chapter 1

[Ful97] Geometry

Solution: [Ful97] §9.1 Ex. 1: Choose a basis $\{e_1, \dots, e_m\}$ so that E can be identified with \mathbb{C}^m . Let $i_1 < \dots < i_{d-1}$ and $j_1 < \dots < j_{d+1}$ be sequences in $[m]$. Apply §9.1 Equation (1) with $k = 1$ to the sequences $j_2 < \dots < j_{d+1}$ and $i_1 < \dots < i_{d-1}, j_1$ by fixing j_1 to be the vector swapped successively with the $j_2 < \dots < j_{d+1}$. Reordering the indices and applying the appropriate sign change yields the desired alternating summation. \square

Bibliography

- [Ful97] William Fulton. *Young Tableaux: With Applications to Representation Theory and Geometry*. Cambridge University Press, 1997. ISBN: 0521567246. DOI: [10.1017/cbo9780511626241](https://doi.org/10.1017/cbo9780511626241).
- [Man01] L. Manivel. *Symmetric Functions, Schubert Polynomials and Degeneracy Loci*. Collection SMF. American Mathematical Society, 2001. ISBN: 9780821821541. URL: <https://books.google.com/books?id=yz7gyKYgIuwC>.