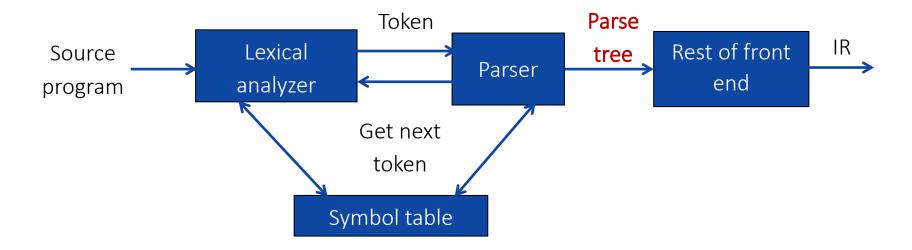
## Module 2 – Syntax Analysis

## Role of parser



- Parser obtains a string of token from the lexical analyzer and reports syntax error if any otherwise generates syntax tree.
- There are two types of parser:
  - 1. Top-down parser
  - 2. Bottom-up parser

- A context free grammar (CFG) is a 4-tuple  $G = (V, \Sigma, S, P)$  where,
  - *V* is finite set of non terminals,
  - $\Sigma$  is disjoint finite set of terminals,
  - *S* is an element of *V* and it's a start symbol,
  - *P* is a finite set formulas of the form  $A \to \alpha$  where  $A \in V$  and  $\alpha \in (V \cup \Sigma)^*$

#### Nonterminal symbol:

- → The name of syntax category of a language, e.g., noun, verb, etc.
- The It is written as a single capital letter, or as a name enclosed between < ... >, e.g., A or <Noun>
  <Noun Phrase> → <Article><Noun>
  - <a href="#"><Article> → a | an | the</a>
  - <Noun> → boy | apple

- A context free grammar (CFG) is a 4-tuple  $G = (V, \Sigma, S, P)$  where,
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  - *S* is an element of *V* and it's a start symbol,
  - *P* is a finite set formulas of the form  $A \rightarrow \alpha$  where  $A \in V$  and  $\alpha \in P$
- ► Terminal symbol:
  - → A symbol in the alphabet.
  - → It is denoted by lower case letter and punctuation marks used in language.

```
<Noun Phrase> → <Article><Noun> <Article> → a | an | the <Noun> → boy | apple
```

- A context free grammar (CFG) is a 4-tuple  $G = (V, \Sigma, S, P)$  where,
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  - *P* is a finite set formulas of the form  $A \rightarrow \alpha$  where  $A \in V$  and  $\alpha \in (V \cup \Sigma)^*$
- Start symbol:
  - First nonterminal symbol of the grammar is called start symbol.

```
<Noun Phrase> → <Article><Noun> <Article> → a | an | the <Noun> → boy | apple
```

- A context free grammar (CFG) is a 4-tuple  $G = (V, \Sigma, S, P)$  where,
  - *V* is finite set of non terminals,
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  - *P* is a finite set formulas of the form  $A \rightarrow \alpha$  where  $A \in V$  and  $\alpha \in (V \cup \Sigma)^*$

#### Production:

→ A production, also called a rewriting rule, is a rule of grammar. It has the form of

A nonterminal symbol → String of terminal and nonterminal symbols

```
<Noun Phrase> → <Article><Noun>
<Article> → a | an | the
<Noun> → boy | apple
```

## Example: Grammar

Write terminals, non terminals, start symbol, and productions for following grammar.

$$E \rightarrow E \cap E \mid (E) \mid -E \mid id$$
  
 $O \rightarrow + \mid -\mid *\mid /\mid \uparrow$ 

Terminals:  $id + - * / \uparrow ()$ 

Non terminals: E, O

Start symbol: E

Productions:  $E \rightarrow E O E | (E) | -E | id$ 

O → + | - | \* | / | ↑

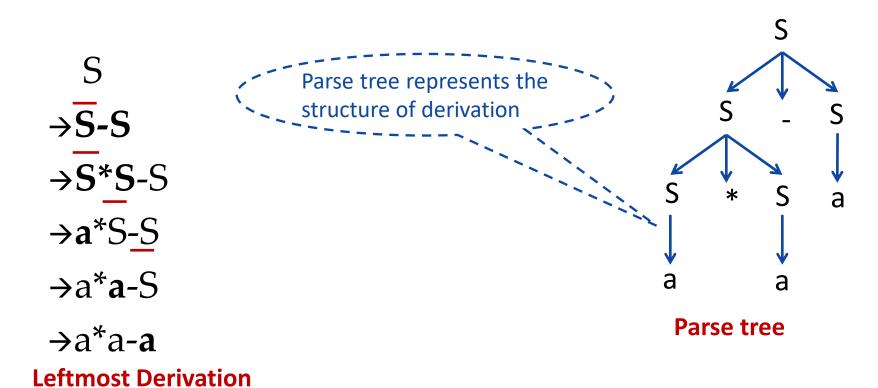
# Derivation & Ambiguity

#### Derivation

- Derivation is used to find whether the string belongs to a given grammar or not.
- Types of derivations are:
  - 1. Leftmost derivation
  - 2. Rightmost derivation

#### Leftmost derivation

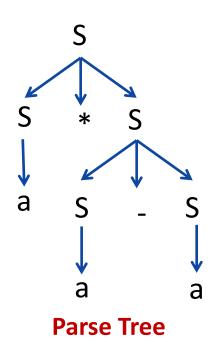
- A derivation of a string *W* in a grammar *G* is a left most derivation if at every step the left most non terminal is replaced.
- Grammar:  $S \rightarrow S + S \mid S S \mid S \mid S \mid S \mid S \mid a$  Output string:  $a^*a a$



## Rightmost derivation

- A derivation of a string W in a grammar G is a right most derivation if at every step the right most non terminal is replaced.
- It is all called canonical derivation.
- Grammar:  $S \rightarrow S + S \mid S S \mid S \mid S \mid S \mid S \mid a$  Output string:  $a^*a a$





#### Exercise: Derivation

1. Perform leftmost derivation and draw parse tree.

```
S\rightarrowA1B
A\rightarrow0A | \epsilon
B\rightarrow0B | 1B | \epsilon
Output string: 1001
```

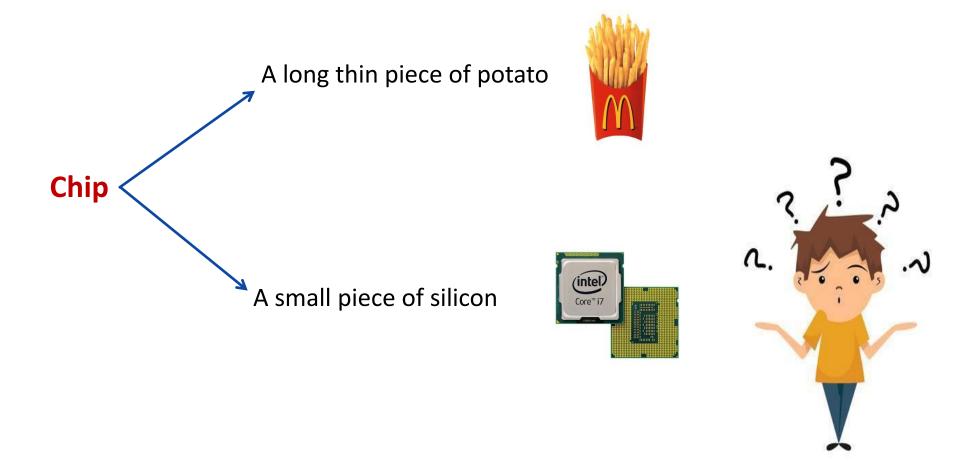
2. Perform leftmost derivation and draw parse tree.

```
S \rightarrow 0S1 \mid 01 Output string: 000111
```

3. Perform rightmost derivation and draw parse tree.

## Ambiguity

• Ambiguity, is a word, phrase, or statement which contains more than one meaning.



## Ambiguity

- In formal language grammar, ambiguity would arise if identical string can occur on the RHS of two or more productions.
- Grammar:

$$N1 \rightarrow \alpha$$
 $N2 \rightarrow \alpha$ 

• α can be derived from either N1 or N2



## Ambiguous grammar

• Ambiguous grammar is one that produces <u>more than one leftmost</u> or more then one rightmost derivation for the same sentence.

• Grammar:  $S \rightarrow S + S \mid S + S \mid (S) \mid a$ Output string: a+a\*a **→**S\*S  $\rightarrow$ S+S  $\rightarrow a+\overline{S}$  $\rightarrow$ S+S\*S  $\rightarrow$ a+S\*S  $\rightarrow$ a+S\*S  $\rightarrow$ a+a\*S  $\rightarrow$ a+a\*S  $\rightarrow$ a+a\*a  $\rightarrow$ a+a\*a

• Here, Two leftmost derivation for string a+a\*a is possible hence, above grammar is ambiguous.

## Exercise: Ambiguous Grammar

Check Ambiguity in following grammars:

- 1.  $S \rightarrow aS \mid Sa \mid \epsilon$  (output string: aaaa)
- 2. S $\rightarrow$  aSbS | bSaS |  $\epsilon$  (output string: abab)
- 3.  $S \rightarrow SS + | SS^* |$  a (output string:  $aa + a^*$ )
- 4.  $\langle \exp \rangle \rightarrow \langle \exp \rangle + \langle \text{term} \rangle | \langle \text{term} \rangle$  $\langle \text{term} \rangle \rightarrow \langle \text{term} \rangle^* \langle \text{letter} \rangle | \langle \text{letter} \rangle$  $\langle \text{letter} \rangle \rightarrow a | b | c | ... | z (output string: a+b*c)$
- 5. Prove that the CFG with productions:  $S \rightarrow a \mid Sa \mid bSS \mid SSb \mid SbS$  is ambiguous (Hint: consider output string yourself)

# Left recursion & Left factoring

#### Left recursion

• A grammar is said to be left recursive if it has a non terminal A such that there is a derivation  $A \rightarrow A\alpha$  for some string  $\alpha$ .



## Examples: Left recursion elimination

$$E \rightarrow E + T \mid T$$

$$E \rightarrow TE'$$

$$E' \rightarrow +TE' \mid \epsilon$$

$$T \rightarrow T^*F \mid F$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT' \mid \epsilon$$

$$X \rightarrow X\%Y \mid Z$$

$$X \rightarrow ZX'$$

$$X' \rightarrow \% Y X' \mid \varepsilon$$

#### Exercise: Left recursion

- A→Abd | Aa | a
   B→Be | b
- 2.  $A \rightarrow AB \mid AC \mid a \mid b$
- 3. S→A | B
   A→ABC | Acd | a | aa
   B→Bee | b
- 4. Exp→Exp+term | Exp-term | term

## Left factoring

Left factoring is a grammar transformation that is useful for producing a grammar suitable for predictive parsing.

```
S\rightarrowaAB | aCD

S\rightarrowaS'

S'\rightarrowAB | CD

A\rightarrow xByA | xByAzA | a

A\rightarrow xByAA' | a

A'\rightarrow \in | zA

A\rightarrowaAB | aA | a

A\rightarrowaA'

A'\rightarrowAB | A | \epsilon

A'\rightarrowAB | A | \epsilon

A'\rightarrowAB | \epsilon
```

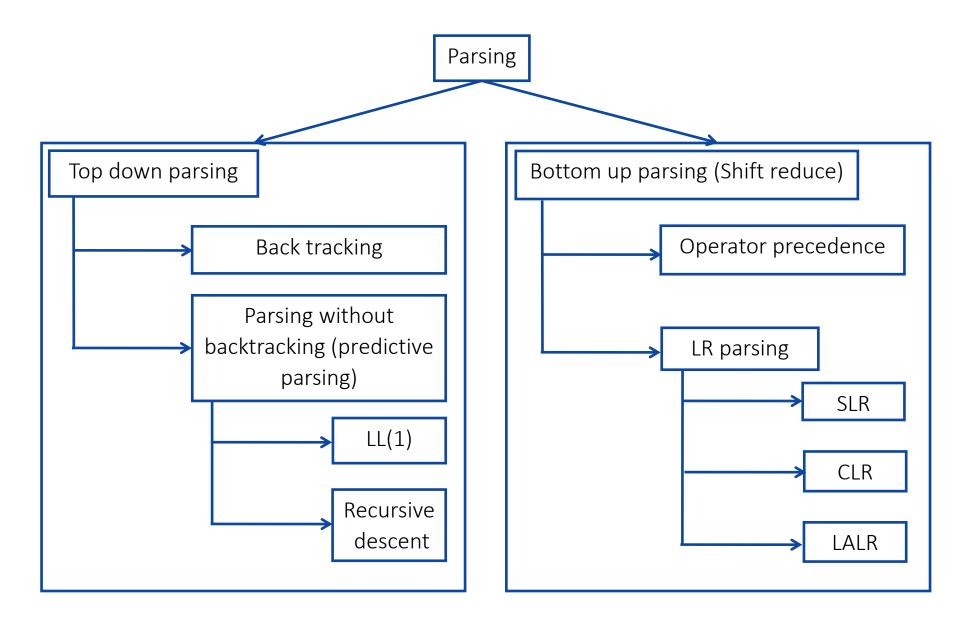
## Exercise

- 1. S→iEtS | iEtSeS | a
- 2.  $A \rightarrow ad \mid a \mid ab \mid abc \mid x$

## Parsing

- Parsing is a technique that takes input string and produces output either a parse tree if string is valid sentence of grammar, or an error message indicating that string is not a valid.
- Types of parsing are:
- 1. Top down parsing: In top down parsing parser build parse tree from top to bottom.
- 2. Bottom up parsing: Bottom up parser starts from leaves and work up to the root.

## Classification of parsing methods



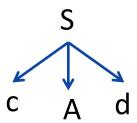
## Backtracking

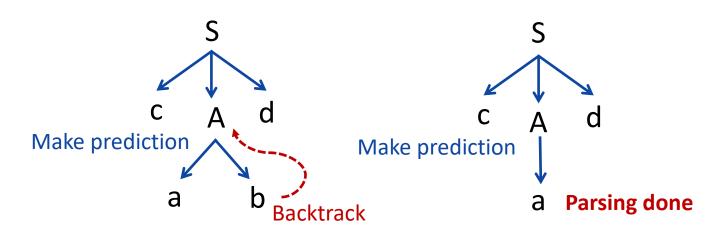
• In backtracking, expansion of nonterminal symbol we choose one alternative and if any mismatch occurs then we try another alternative.

• Grammar:  $S \rightarrow cAd$ 

 $A \rightarrow ab \mid a$ 

Input string: cad





### Exercise

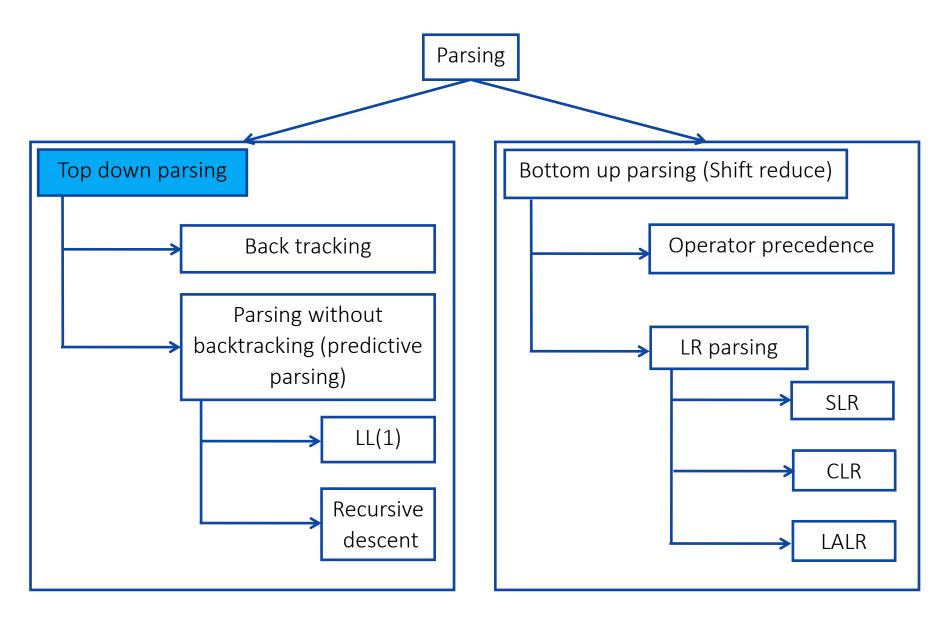
1.  $E \rightarrow 5+T \mid 3-T$ 

 $T \rightarrow V \mid V^*V \mid V^+V$ 

 $V \rightarrow a \mid b$ 

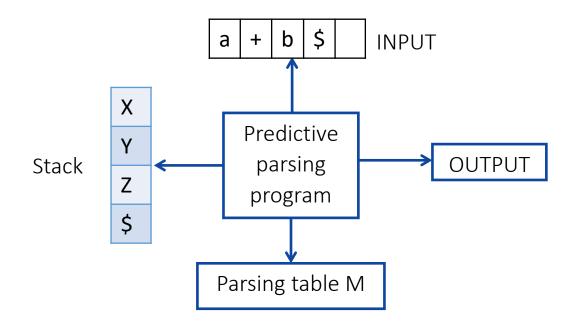
String: 3-a+b

## Parsing Methods



## LL(1) parser (predictive parser)

- LL(1) is non recursive top down parser.
  - 1. First L indicates input is scanned from left to right.
  - 2. The second L means it uses leftmost derivation for input string
  - 3. 1 means it uses only input symbol to predict the parsing process.



## LL(1) parsing (predictive parsing)

Steps to construct LL(1) parser

- 1. Remove left recursion / Perform left factoring (if any).
- 2. Compute FIRST and FOLLOW of non terminals.
- 3. Construct predictive parsing table.
- 4. Parse the input string using parsing table.

## Rules to compute first of non terminal

- 1. If  $A \to \alpha$  and  $\alpha$  is terminal, add  $\alpha$  to FIRST(A).
- 2. If  $A \rightarrow \in$ , add  $\in$  to FIRST(A).
- 3. If X is nonterminal and  $X \rightarrow Y_1 Y_2 \dots Y_k$  is a production, then place a in FIRST(X) if for some i, a is in FIRST(Yi), and  $\epsilon$  is in all of  $FIRST(Y_1), \dots, FIRST(Y_{i-1})$ ; that is  $Y_1 \dots Y_{i-1} \Rightarrow \epsilon$ . If  $\epsilon$  is in  $FIRST(Y_j)$  for all  $j = 1, 2, \dots, k$  then add  $\epsilon$  to FIRST(X).

Everything in  $FIRST(Y_1)$  is surely in FIRST(X) If  $Y_1$  does not derive  $\epsilon$ , then we do nothing more to FIRST(X), but if  $Y_1 \Rightarrow \epsilon$ , then we add  $FIRST(Y_2)$  and so on.

## Rules to compute first of non terminal

#### Simplification of Rule 3

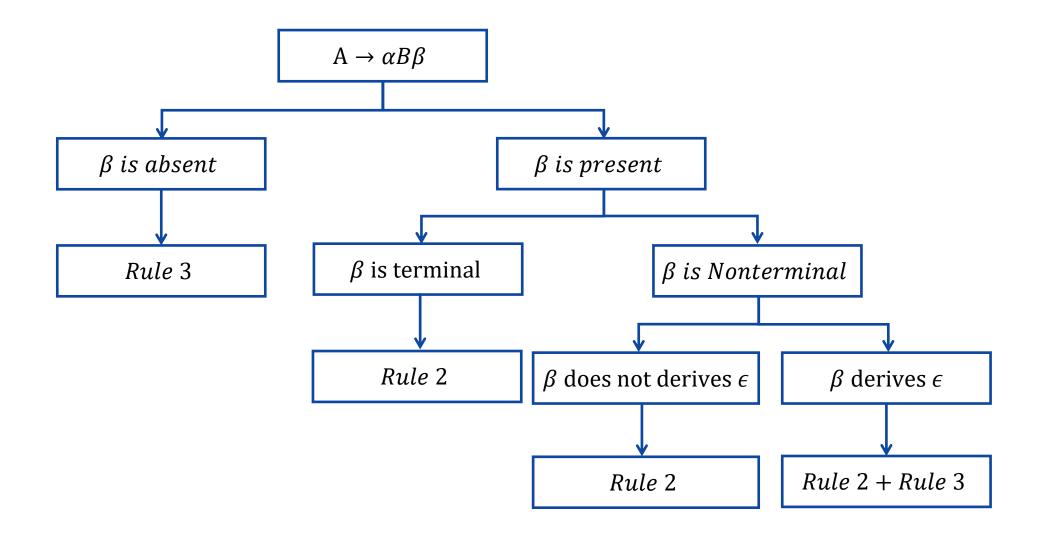
```
If A \to Y_1 Y_2 \dots Y_K,
```

- If  $Y_1$  does not derives  $\in$  then,  $FIRST(A) = FIRST(Y_1)$
- If  $Y_1$  derives  $\in$  then,  $FIRST(A) = FIRST(Y_1) - \epsilon U FIRST(Y_2)$
- If  $Y_1 \& Y_2$  derives  $\in$  then,  $FIRST(A) = FIRST(Y_1) - \epsilon \ U \ FIRST(Y_2) - \epsilon \ U \ FIRST(Y_3)$
- If  $Y_1$ ,  $Y_2$  &  $Y_3$  derives  $\in$  then,  $FIRST(A) = FIRST(Y_1) \epsilon U FIRST(Y_2) \epsilon U FIRST(Y_3) \epsilon U FIRST(Y_4)$
- If  $Y_1$ ,  $Y_2$ ,  $Y_3$ ..... $Y_K$  all derives  $\in$  then,  $FIRST(A) = FIRST(Y_1) \epsilon U FIRST(Y_2) \epsilon U FIRST(Y_3) \epsilon U FIRST(Y_4) \epsilon U \dots FIRST(Y_k)$ (note: if all non terminals derives  $\in$  then add  $\in$  to FIRST(A))

## Rules to compute FOLLOW of non terminal

- 1. Place \$in follow(S). (S is start symbol)
- 2. If  $A \to \alpha B\beta$ , then everything in  $FIRST(\beta)$  except for  $\epsilon$  is placed in FOLLOW(B)
- 3. If there is a production  $A \rightarrow \alpha B$  or a production  $A \rightarrow \alpha B\beta$  where  $FIRST(\beta)$  contains  $\epsilon$  then everything in FOLLOW(A) = FOLLOW(B)

## How to apply rules to find FOLLOW of non terminal?



## Rules to construct predictive parsing table

- 1. For each production  $A \rightarrow \alpha$  of the grammar, do steps 2 and 3.
- 2. For each terminal a in  $first(\alpha)$ , Add  $A \rightarrow \alpha$  to M[A, a].
- 3. If  $\epsilon$  is in  $first(\alpha)$ , Add  $A \to \alpha$  to M[A, b] for each terminal b in FOLLOW(B). If  $\epsilon$  is in  $first(\alpha)$ , and \$ is in FOLLOW(A), add  $A \to \alpha$  to M[A, \$].
- 4. Make each undefined entry of M be error.

## Example-1: LL(1) parsing

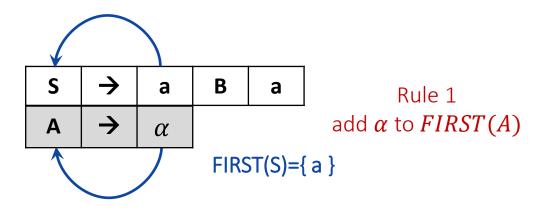
S→aBa B→bB | ∈

Step 1: Not required

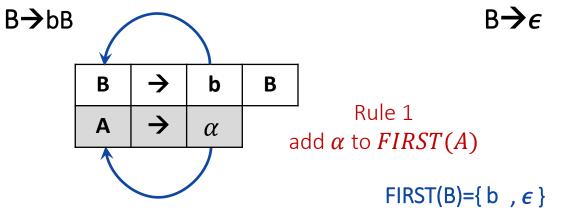
Step 2: Compute FIRST

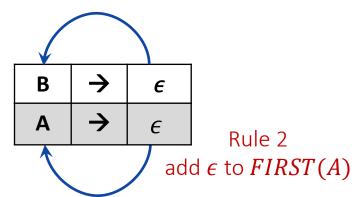
First(S)

S→aBa



First(B)





NT	First
S	
В	

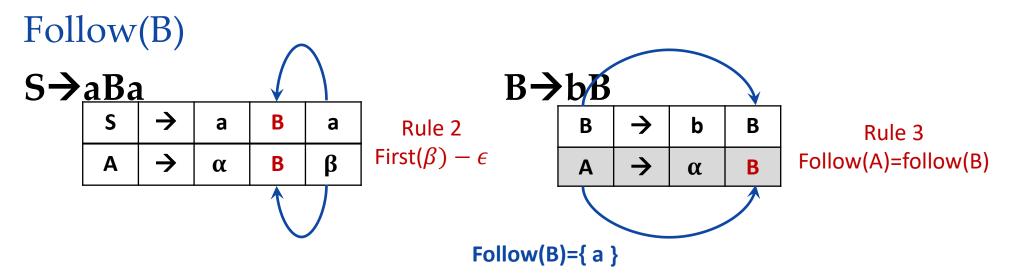
## Example-1: LL(1) parsing

```
S→aBa
B→bB | ∈
```

Step 2: Compute FOLLOW

Follow(S)

Rule 1: Place \$ in FOLLOW(S)



NT	First	Follow
S	{a}	
В	$\{b,\!\epsilon\}$	

Step 3: Prepare predictive parsing table

NT	Input Symbol			
	а	b	\$	
S				
В				

S→aBa
a=FIRST(aBa)={ a }
M[S,a]=S→aBa

Rule: 2  

$$A \rightarrow \alpha$$
  
 $a = first(\alpha)$   
 $M[A,a] = A \rightarrow \alpha$ 

NT	First	Follow
S	{a}	<b>{\$}</b>
В	$\{b,\!\epsilon\}$	{a}

Step 3: Prepare predictive parsing table

NT	Input Symbol			
	а	b	\$	
S	S→aBa			
В				

B→bB
a=FIRST(bB)={ b }
M[B,b]=B→bB

Rule: 2  

$$A \rightarrow \alpha$$
  
 $a = first(\alpha)$   
 $M[A,a] = A \rightarrow \alpha$ 

NT	First	Follow
S	{a}	{\$}
В	$\{b,\!\epsilon\}$	{a}

Step 3: Prepare predictive parsing table

NT	Input Symbol				
	а	b	\$		
S	S→aBa				
В		B→bB			

$B \rightarrow \epsilon$	
b=FOLLOW(B)={ a }	
M[B,a]=B→ $\epsilon$	

Rule: 3  

$$A \rightarrow \alpha$$
  
 $b = follow(A)$   
 $M[A,b] = A \rightarrow \alpha$ 

NT	First	Follow
S	{a}	<b>{\$}</b>
В	$\{b,\!\epsilon\}$	{a}

```
S \rightarrow aB \mid \epsilon

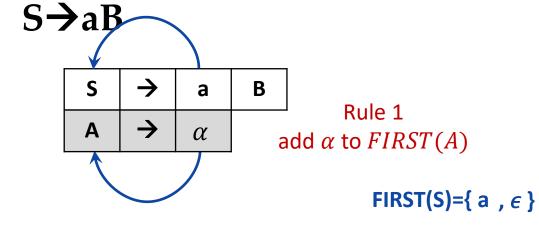
B \rightarrow bC \mid \epsilon

C \rightarrow cS \mid \epsilon
```

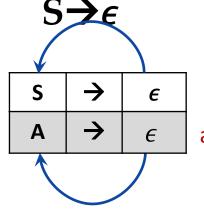
Step 1: Not required

Step 2: Compute FIRST

#### First(S)



NT	First
S	
В	
С	



Rule 2 add  $\epsilon$  to FIRST(A)

```
S \rightarrow aB \mid \epsilon

B \rightarrow bC \mid \epsilon

C \rightarrow cS \mid \epsilon
```

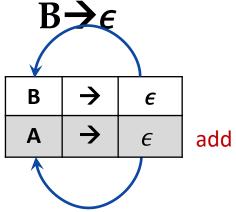
Step 1: Not required

Step 2: Compute FIRST

First(B)

B	<b>≯</b> b¢				
	В	$\rightarrow$	b	С	Dula 4
	Α	<b>→</b>	α	ā	Rule 1 $lpha$ to $FIRST(A)$
				•	FIRST(B)={ b , $\epsilon$

NT	First
S	$\{a,\epsilon\}$
В	
С	



```
S \rightarrow aB \mid \epsilon

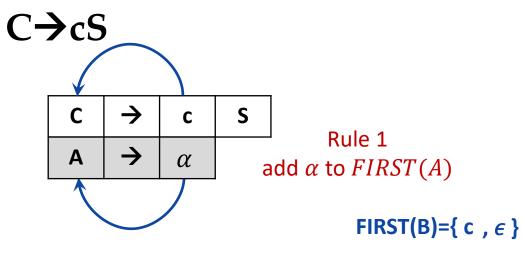
B \rightarrow bC \mid \epsilon

C \rightarrow cS \mid \epsilon
```

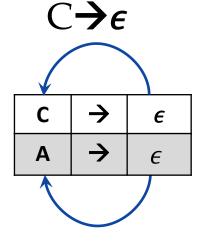
Step 1: Not required

Step 2: Compute FIRST

#### First(C)



NT	First
S	$\{a,\epsilon\}$
В	$\{b,\!\epsilon\}$
С	

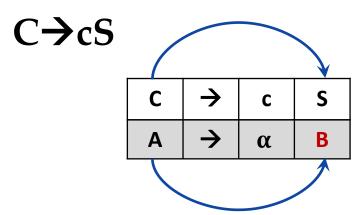


#### Step 2: Compute FOLLOW

Follow(S)

Rule 1: Place \$ in FOLLOW(S)

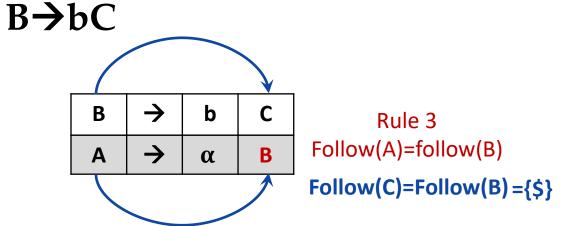
Follow(S)={ \$ }

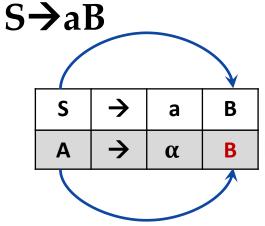


Rule 3
Follow(A)=follow(B)

Follow(S)=Follow(C)={\$}

S→aB	E
B→bC	<b> </b> €
C→cS	E





NT	First	Follow
S	{a, <i>∈</i> }	
В	$\{b,\!\epsilon\}$	
С	{c, <i>€</i> }	

Rule 3
Follow(A)=follow(B)

Follow(B)=Follow(S)={\$}

$$S \rightarrow aB \mid \epsilon$$
  
 $B \rightarrow bC \mid \epsilon$   
 $C \rightarrow cS \mid \epsilon$ 

 $M[S,a]=S \rightarrow aB$ 

Step 3: Prepare predictive parsing table

N Input Symbol				
T	а	b	С	\$
S				
В				
С				

Rule: 2
$$A \rightarrow \alpha$$

$$a = \text{first}(\alpha)$$

$$a = FIRST(aB) = \{a\}$$

$$M[A,a] = A \rightarrow \alpha$$

NTFirstFollowS
$$\{a, \epsilon\}$$
 $\{\$\}$ B $\{b, \epsilon\}$  $\{\$\}$ C $\{c, \epsilon\}$  $\{\$\}$ 

$$S \rightarrow aB \mid \epsilon$$
  
 $B \rightarrow bC \mid \epsilon$   
 $C \rightarrow cS \mid \epsilon$ 

Step 3: Prepare predictive parsing table

N		Input Sy	/mbol	
T	а	b	С	\$
S	S→aB			
В				
С				

$$S \rightarrow \epsilon$$
  
b=FOLLOW(S)={ \$ }  
M[S,\$]=S $\rightarrow \epsilon$ 

Rule: 3  

$$A \rightarrow \alpha$$
  
 $b = follow(A)$   
 $M[A,b] = A \rightarrow \alpha$ 

NT
 First
 Follow

 S
 
$$\{a\}$$
 $\{\$\}$ 

 B
  $\{b,\epsilon\}$ 
 $\{\$\}$ 

 C
  $\{c,\epsilon\}$ 
 $\{\$\}$ 

$$S \rightarrow aB \mid \epsilon$$
  
 $B \rightarrow bC \mid \epsilon$   
 $C \rightarrow cS \mid \epsilon$ 

 $M[B,b]=B\rightarrow bC$ 

Step 3: Prepare predictive parsing table

N	Input Symbol			
T	а	b	С	\$
S	S→aB			S <b>→</b> €
В				
С				

Rule: 2
$$A \rightarrow \alpha$$

$$a = \text{first}(\alpha)$$

$$a = FIRST(bC) = \{b\}$$

$$M[A,a] = A \rightarrow \alpha$$

NT	First	Follow
S	{a}	{\$}
В	$\{b,\!\epsilon\}$	{\$}
С	$\{c,\epsilon\}$	{\$}

$$S \rightarrow aB \mid \epsilon$$
  
 $B \rightarrow bC \mid \epsilon$   
 $C \rightarrow cS \mid \epsilon$ 

Step 3: Prepare predictive parsing table

N	I Input Symbo		mbol	
Т	а	b	С	\$
S	S→aB			S <b>→</b> €
В		B→bC		
С				

B→
$$\epsilon$$
  
b=FOLLOW(B)={\$}  
M[B,\$]=B→ $\epsilon$ 

Rule: 3  

$$A \rightarrow \alpha$$
  
 $b = follow(A)$   
 $M[A,b] = A \rightarrow \alpha$ 

NT
 First
 Follow

 S
 
$$\{a\}$$
 $\{\$\}$ 

 B
  $\{b,\epsilon\}$ 
 $\{\$\}$ 

 C
  $\{c,\epsilon\}$ 
 $\{\$\}$ 

$$S \rightarrow aB \mid \epsilon$$
  
 $B \rightarrow bC \mid \epsilon$   
 $C \rightarrow cS \mid \epsilon$ 

 $C \rightarrow cS$ 

 $a=FIRST(cS)=\{c\}$ 

 $M[C,c]=C\rightarrow cS$ 

Step 3: Prepare predictive parsing table

N	Input Symbol			
T	а	p	С	\$
S	S→aB			S→e
В		B→bC		$B \rightarrow \epsilon$
С				

Rule: 2  

$$A \rightarrow \alpha$$
  
 $a = first(\alpha)$   
 $M[A,a] = A \rightarrow \alpha$ 

NTFirstFollowS
$$\{a\}$$
 $\{\$\}$ B $\{b,\epsilon\}$  $\{\$\}$ C $\{c,\epsilon\}$  $\{\$\}$ 

$$S \rightarrow aB \mid \epsilon$$
  
 $B \rightarrow bC \mid \epsilon$   
 $C \rightarrow cS \mid \epsilon$ 

 $C \rightarrow \epsilon$ 

Step 3: Prepare predictive parsing table

N	Input Symbol			
T	a	b	С	\$
S	S→aB			S→e
В		B→bB		$B \rightarrow \epsilon$
С			C→cS	

 $b=FOLLOW(C)=\{ \} \}$ 

 $M[C,\$]=C\rightarrow\epsilon$ 

Rule: 3  

$$A \rightarrow \alpha$$
  
 $b = follow(A)$   
 $M[A,b] = A \rightarrow \alpha$ 

**First** 

 $\{b,\epsilon\}$ 

 $\{c,\epsilon\}$ 

{a}

NT

S

В

**Follow** 

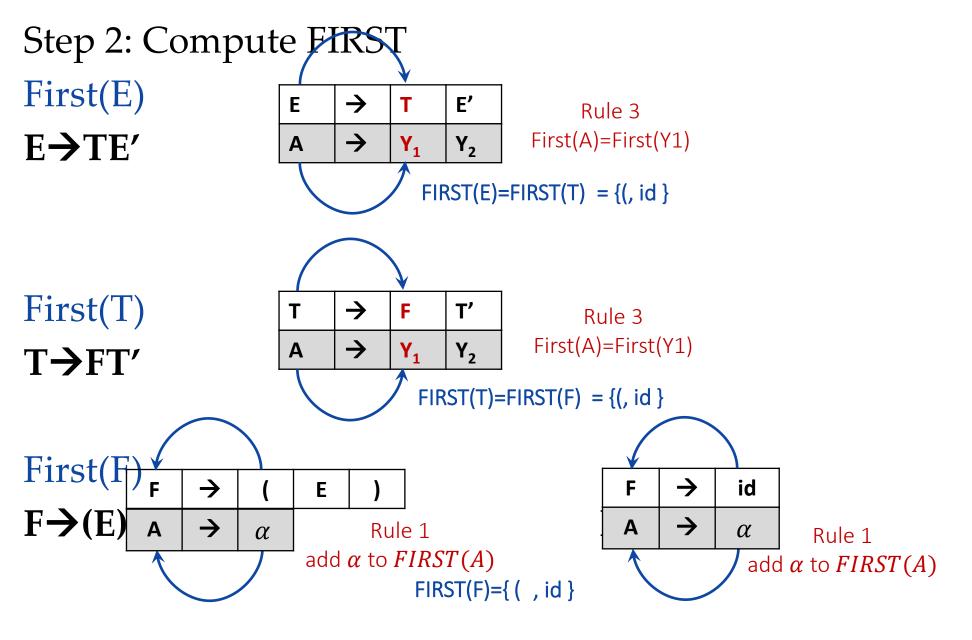
{\$}

**{\$**}

**{\$**}

tep 3: Prepare predictive parsing tales 
$$S \rightarrow AB$$
  $S \rightarrow AB$   $S \rightarrow AB$   $S \rightarrow AB$   $S \rightarrow AB$ 

```
E \rightarrow E + T \mid T
T \rightarrow T^*F \mid F
F\rightarrow (E) \mid id
Step 1: Remove left recursion
            E \rightarrow TE'
            E' \rightarrow +TE' \mid \epsilon
            T \rightarrow FT'
            T' \rightarrow *FT' \mid \epsilon
            F \rightarrow (E) \mid id
```



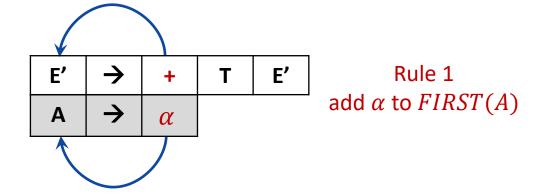
E→TE′
E' <b>→</b> +ΤΕ'   ε
T→FT′
T' <b>→</b> *FT'   ∈
$F \rightarrow (E) \mid id$

NT	First
E	
E'	
Т	
T'	
F	

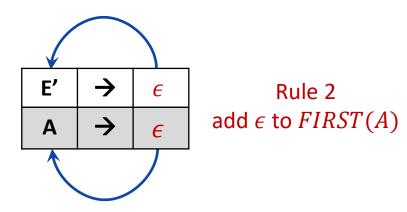
#### Step 2: Compute FIRST

First(E')

$$E' \rightarrow +TE'$$







FIRST(E')= $\{+, \epsilon\}$ 

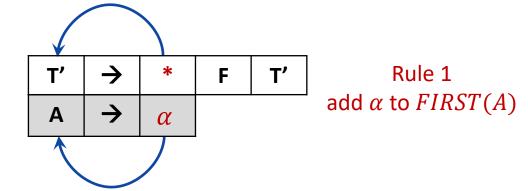
E→TE′
E' <b>→</b> +ΤΕ'   ε
T→FT′
T' <b>→</b> *FT'   ε
$F \rightarrow (E) \mid id$

NT	First	
Е	{ (,id }	
E'		
Т	{ (,id }	
T'		
F	{ (,id }	

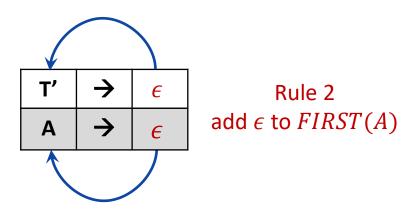
#### Step 2: Compute FIRST

First(T')

 $T' \rightarrow *FT'$ 



 $T' \rightarrow \epsilon$ 



FIRST(T')=
$$\{*, \epsilon\}$$

E→TE′
E' <b>→</b> +ΤΕ'   ε
T→FT′
T' <b>→</b> *FT'   ε
$F \rightarrow (E) \mid id$

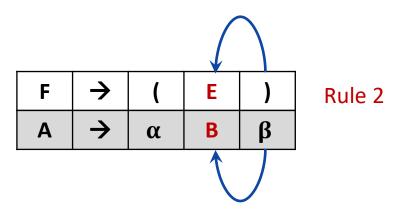
NT	First	
E	{ (,id }	
E'	{ +, <i>ϵ</i> }	
Т	{ (,id }	
T'		
F	{ (,id }	

Step 2: Compute FOLLOW

FOLLOW(E)

Rule 1: Place \$ in FOLLOW(E)

 $F \rightarrow (E)$ 

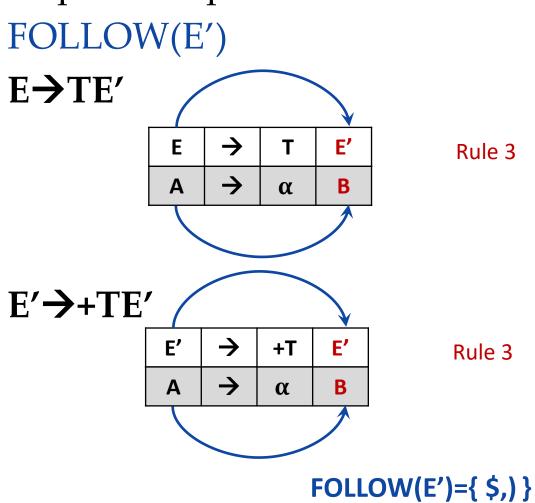


E→TE' E'→+TE' | ∈ T→FT' T'→\*FT' | ∈ F→(E) | id

NT	First	Follow
E	{ (,id }	
E'	{ +, ε }	
Т	{ (,id }	
T'	{ *, ε }	
F	{ (,id }	

FOLLOW(E)={ \$, ) }

Step 2: Compute FOLLOW



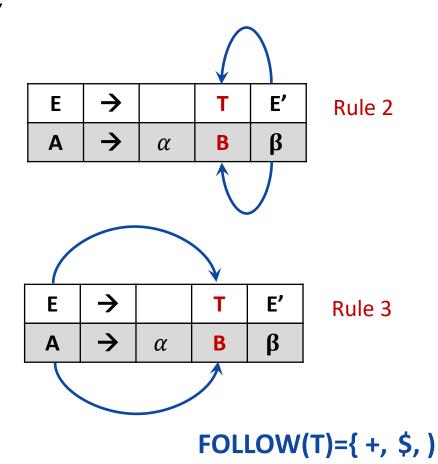
E→TE'	
E'→+TE'	$\epsilon$
T→FT'	
T'→*FT'	E
<b>F</b> →(E)   id	

NT	First	Follow
E	{ (,id }	{ \$,) }
E'	{ +, ε }	
Т	{ (,id }	
T'	{ *, ε }	
F	{ (,id }	

Step 2: Compute FOLLOW

FOLLOW(T)

 $E \rightarrow TE'$ 



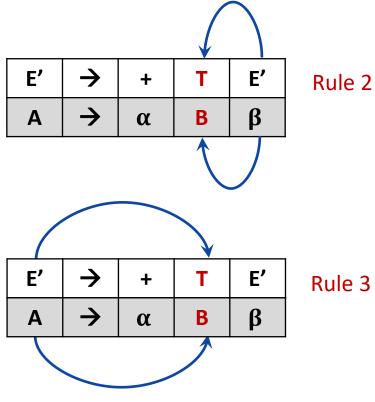
E→TE' E'→+TE' | ∈ T→FT' T'→\*FT' | ∈ F→(E) | id

NT	First	Follow
E	{ (,id }	{ \$,) }
E'	{ +, ε }	{ \$,) }
Т	{ (,id }	
T'	{ *, ε }	
F	{ (,id }	

Step 2: Compute FOLLOW

#### FOLLOW(T)





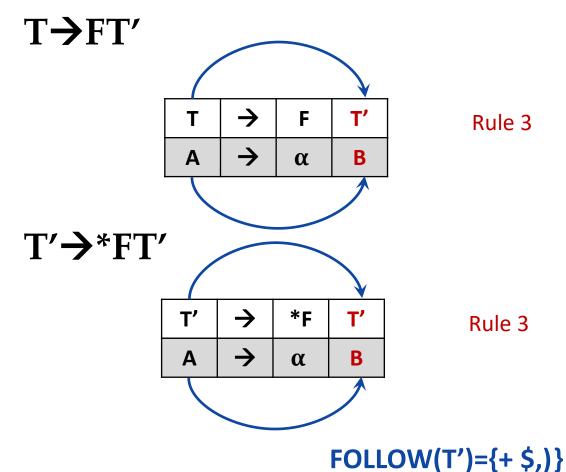
FOLLOW(T)={ +, \$, ) }

E→TE' E'→+TE' | ∈ T→FT' T'→\*FT' | ∈ F→(E) | id

NT	First	Follow
E	{ (,id }	{ \$,) }
E'	{ +, ε }	{ \$,) }
Т	{ (,id }	
T'	{ *, ε }	
F	{ (,id }	

Step 2: Compute FOLLOW





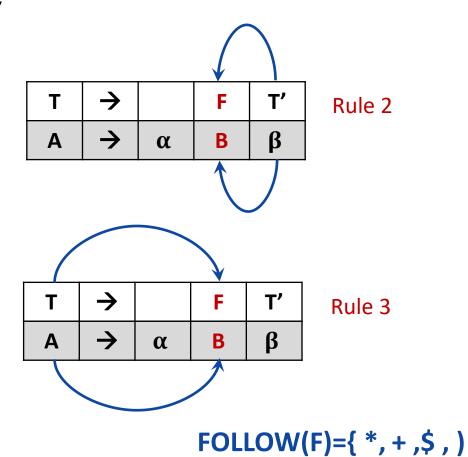
E→TE'	
E'→+TE'	E
T→FT′	
T'→*FT'	E
<b>F</b> →(E)   id	

NT	First	Follow
E	{ (,id }	{ \$,) }
E'	{ +, ε }	{ \$,) }
Т	{ (,id }	{ +,\$,) }
T'	{ *, ε }	
F	{ (,id }	

Step 2: Compute FOLLOW

FOLLOW(F)

 $T \rightarrow FT'$ 



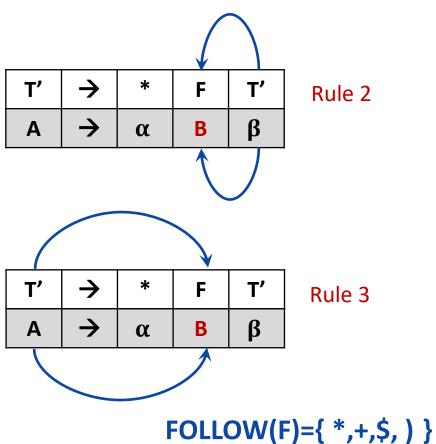
E→TE' E'→+TE' | ∈ T→FT' T'→\*FT' | ∈ F→(E) | id

NT	First	Follow
Е	{ (,id }	{ \$,) }
E'	{ +, ε }	{ \$,) }
Т	{ (,id }	{ +,\$,) }
T'	{ *, ε }	{ +,\$,) }
F	{ (,id }	

Step 2: Compute FOLLOW

#### FOLLOW(F)





NT	First	Follow
E	{ (,id }	{ \$,) }
E'	{ +, ε }	{ \$,) }
Т	{ (,id }	{ +,\$,) }
T'	{ *, ε }	{ +,\$,) }
F	{ (,id }	

Step 3: Construct predictive parsing table

NT			Input Sy	mbol		
	id	+	*	(	)	\$
Е						
E'						
Т						
T'						
F						

E $\rightarrow$ TE'  $A \rightarrow \alpha$   $a = FIRST(TE') = \{ (,id \} \}$   $M[A,a] = A \rightarrow \alpha$   $M[E,(]=E \rightarrow TE']$   $M[E,id]=E \rightarrow TE'$ 

NT	First	Follow
Е	{ (,id }	{ \$,) }
E'	{ +, ε }	{ \$,) }
Т	{ (,id }	{ +,\$,) }
T'	{ *, ε }	{ +,\$,) }
F	{ (,id }	{*,+,\$,)}

Step 3: Construct predictive parsing table

NT		Input Symbol				
	id	+	*	(	)	\$
Е	E→TE′			E→TE′		
E'						
Т						
T'						
F						

Rule: 2  

$$A \rightarrow \alpha$$
  
 $a=FIRST(+TE')=\{+\}$   
 $M[A,a]=A \rightarrow \alpha$   
 $M[E',+]=E' \rightarrow +TE'$ 

NT	First	Follow
Е	{ (,id }	{ \$,) }
E'	{ +, ε }	{ \$,) }
Т	{ (,id }	{ +,\$,) }
T'	{ *, ε }	{ +,\$,) }
F	{ (,id }	{*,+,\$,)}

Step 3: Construct predictive parsing table

NT		Input Symbol				
	id	+	*	(	)	\$
Е	E→TE′			E→TE′		
E'		E′→+TE′				
Т						
T'						
F						

Rule: 3
$$A \rightarrow \alpha$$

$$b = \text{FOLLOW}(E') = \{\$,\}\}$$

$$M[E',\$] = E' \rightarrow \epsilon$$

$$M[E',)] = E' \rightarrow \epsilon$$

NT	First	Follow
Е	{ (,id }	{ \$,) }
E'	{ +, ε }	{ \$,) }
Т	{ (,id }	{ +,\$,) }
T'	{ *, ε }	{ +,\$,) }
F	{ (,id }	{*,+,\$,)}

Step 3: Construct predictive parsing table

NT	Input Symbol					
	id	+	*	(	)	\$
Е	E→TE′			E→TE′		
E'		E′→+TE′			E′ <b>→</b> ε	E′ <b>→</b> ε
Т						
T'						
F						

T $\rightarrow$ FT'  $A \rightarrow \alpha$   $a = FIRST(FT') = \{ (,id \} \}$   $M[A,a] = A \rightarrow \alpha$   $M[T,(]=T \rightarrow FT']$   $M[T,id]=T \rightarrow FT'$ 

E→TE'
E'→+TE'   ∈
T→FT'
T'→*FT'   ∈
F→(E)   id

NT	First	Follow
E	{ (,id }	{ \$,) }
E'	{ +, <i>ϵ</i> }	{ \$,) }
Т	{ (,id }	{ +,\$,) }
T'	{ *, ε }	{ +,\$,) }
F	{ (,id }	{*,+,\$,)}

Step 3: Construct predictive parsing table

NT	Input Symbol					
	id	+	*	(	)	\$
Е	E→TE′			E→TE′		
E'		E′→+TE′			E′ <b>→</b> ε	E' <b>→</b> ε
Т	T→FT′			T→FT′		
T'						
F						

 $T' \rightarrow *FT'$   $a=FIRST(*FT')=\{ * \}$   $M[T',*]=T' \rightarrow *FT'$ 

Rule: 2  $A \rightarrow \alpha$   $a = first(\alpha)$  $M[A,a] = A \rightarrow \alpha$ 

E→TE'
E'→+TE'   ∈
T→FT'
T'→*FT'   ∈
F→(E)   id

NT	First	Follow
Е	{ (,id }	{ \$,) }
E'	{ +, ε }	{ \$,) }
Т	{ (,id }	{ +,\$,) }
T'	{ *, ε }	{ +,\$,) }
F	{ (,id }	{*,+,\$,)}

Step 3: Construct predictive parsing table

NT	Input Symbol							
	id	+	)	\$				
Е	E→TE′			E→TE′				
E'		E'→+TE'			E′ <del>→</del> ε	E′ <b>→</b> ε		
Т	T→FT′			T→FT′				
T'			T′ <b>→</b> *FT′					
F								

$$T' \rightarrow \epsilon$$
  
 $b=FOLLOW(T')=\{+,\$,\}\}$   
 $M[T',+]=T' \rightarrow \epsilon$   
 $M[T',\$]=T' \rightarrow \epsilon$   
 $M[T',\$]=T' \rightarrow \epsilon$   
 $Rule: 3$   
 $A \rightarrow \alpha$   
 $b = follow(A)$   
 $M[A,b] = A \rightarrow \alpha$ 

 $M[T',)=T' \rightarrow \epsilon$ 

E→TE'
E'→+TE'   €
T→FT'
T'→*FT'   ε
$F \rightarrow (E) \mid id$

NT	First	Follow
E	{ (,id }	{ \$,) }
E'	{ +, <i>ϵ</i> }	{ \$,) }
Т	{ (,id }	{ +,\$,) }
T'	{ *, ε }	{ +,\$,) }
F	{ (,id }	{*,+,\$,)}

Step 3: Construct predictive parsing table

NT	Input Symbol							
	id	+	)	\$				
E	E→TE′			E→TE′				
E'		E'→+TE'			E′ <b>→</b> ε	E' <b>→</b> ε		
Т	T→FT′			T→FT′				
T'		T′ <b>→</b> ε	T′ <b>→</b> *FT′		T′ <b>→</b> ε	T′ <b>→</b> ε		
F								

Rule: 2  

$$A \rightarrow \alpha$$
  
 $a = first(\alpha)$   
 $M[A,a] = A \rightarrow \alpha$ 

 $F \rightarrow (E)$   $a=FIRST((E))=\{ ( \}$  $M[F,(]=F \rightarrow (E)$ 

NT	First	Follow
E	{ (,id }	{ \$,) }
E'	{ +, ε }	{ \$,) }
Т	{ (,id }	{ +,\$,) }
T'	{ *, ε }	{ +,\$,) }
F	{ (,id }	{*,+,\$,)}

Step 3: Construct predictive parsing table

NT	Input Symbol							
	id	+	*	(	)	\$		
E	E→TE′			E→TE′				
E'		E′→+TE′			E′ <b>→</b> ε	E′ <b>→</b> ε		
Т	T→FT′			T→FT′				
T'		T′ <b>→</b> ε	T' <b>→</b> *FT'		T′ <b>→</b> ε	T′ <b>→</b> ε		
F				F→(E)				

Rule: 2  

$$A \rightarrow \alpha$$
  
 $a = first(\alpha)$   
 $M[A,a] = A \rightarrow \alpha$ 

F→id

a=FIRST(id)={ id }

M[F,id]=F→id

E→TE'
E'→+TE'   ∈
T→FT′
T'→*FT'   ∈
F→(E)   id

NT	First	Follow
E	{ (,id }	{ \$,) }
E'	{ +, ε }	{ \$,) }
Т	{ (,id }	{ +,\$,) }
T'	{ *, ε }	{ +,\$,) }
F	{ (,id }	{*,+,\$,)}

• Step 4: Make each undefined entry of table be Error

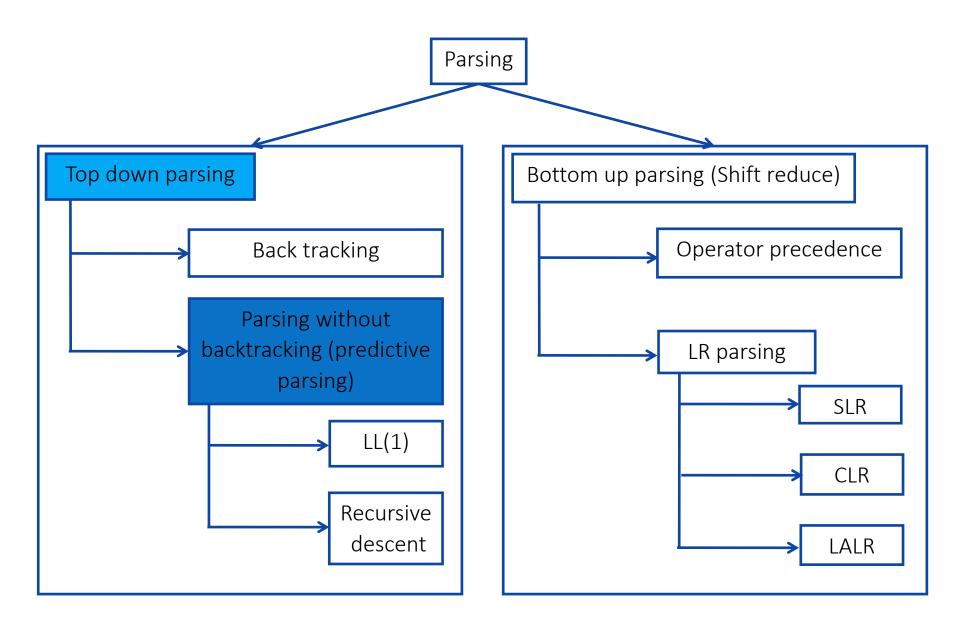
NT	Input Symbol							
	id	+	*	(	)	\$		
Е	E→TE′	Error	Error	E→TE′	Error	Error		
E'	Error	E′→+TE′	Error	Error	E′ <b>→</b> ε	<b>E</b> ′ <b>→</b> ε		
Т	T→FT′	Error	Error	T→FT′	Error	Error		
T'	Error	T′ <b>→</b> ε	T′ <b>→</b> *FT′	Error	T′ <b>→</b> ε	T′ <b>→</b> ε		
F	F→id	Error	Error	F→(E)	Error	Error		

Step 4: Parse the string : id + id \* id \$

STACK	INPUT	OUTPUT
E\$	i <mark>d</mark> +id*id\$	

NT	Input Symbol							
	id	+	*	(	)	\$		
Е	E→TE′	Error	Error	E→TE′	Error	Error		
E'	Error	E'→+TE'	Error	Error	E′ <b>→</b> ε	E′ <b>→</b> ε		
Т	T→FT′	Error	Error	T→FT′	Error	Error		
T'	Error	T′ <b>→</b> ε	T′ <del>→</del> *FT′	Error	T′ <b>→</b> ε	T′ <b>→</b> ε		
F	F→id	Error	Error	F <del>→</del> (E)	Error	Error		

# Parsing methods



# Recursive descent parsing

- A top down parsing that executes a set of recursive procedure to process the input without backtracking is called recursive descent parser.
- There is a procedure for each non terminal in the grammar.
- Consider RHS of any production rule as definition of the procedure.
- As it reads expected input symbol, it advances input pointer to next position.

#### Cont.,

```
void A() {
       Choose an A-production, A \to X_1 X_2 \cdots X_k;
       for (i = 1 \text{ to } k) {
              if (X_i \text{ is a nonterminal})
                     call procedure X_i();
              else if (X_i equals the current input symbol a)
                     advance the input to the next symbol;
              else /* an error has occurred */;
```

# Example: Recursive descent parsing

```
Proceduce Match(token t) ←
                                                          If lookahead=t ←
                              If lookahead='*' ←
lookahead=next_token; <
                                                          Else
     Match(num); ←
                                   Match('*'); ←
                                                            Error();
                                   If lookahead=num 

     T(); ←
                                        Match(num); ←
Else
     Error();
                                        T(); ←
                                                       Procedure Error
If lookahead=$ ←
                                   Else
                                                                Print("Error");
     Declare success; ←
                                        Error();
Else
     Error();
                              Else ←
                                                              E \rightarrow num T
                                   NULL ←
                                                              T \rightarrow * num T \mid \epsilon
                              Success
```

# Example: Recursive descent parsing

```
Proceduce Match(token t)
Procedure E←
                            Procedure T ←
                                                          If lookahead=t ←
                                If lookahead='*' ←
     Else
          Match(num);←
                                     Match('*');
                                                            Error();
                                     If lookahead=num
          T(); ←
     Else
                                         Match(num);
          Error();
                                         T();
                                                        Procedure Error ←
     If lookahead=$ ←
                                     Else
                                                                Print("Error"); ←
          Declare success;
                                          Error();
     Else ←
          Error();←
                                Else ←
                                                              E \rightarrow num T
                                     NULL ←
                                                              T \rightarrow * num T \mid \epsilon
                                 Success
                                                                    Error
```