

Masa Loai Melhem

Final Assignment 1

Q₁ (a) state and explain the following

- Source coding Theorem

⇒ Source coding theorem is This is also known as Noiseless coding theorem or Shannon's first theorem.

⇒ establishes the limits to possible data compression, and the operational meaning of Shannon entropy.

- Channel coding Theorem

⇒ channel coding theorem is systematic redundancy can be introduced into the transmitted signal so that channels can be used with improved reliability.

This is called channel coding or Error control coding.

⇒ answers the question of how much band width is left for data communication while using the most efficient code.

(b) compute the source entropy of the following text.

"Sometimes the inspiration you need to achieve your dreams can be found in a few simple words of wisdom."

$\times 102$

\Rightarrow Source entropy $\Rightarrow H(S)$

$$H(S) = \sum p_k \log_2 \frac{1}{p_k}$$

« أول شيء كتابة كل عنصر واحتماله »

s 7/104

b 1/104

o 9/104

f 3/104

m 5/104

w 3/104

e 11/104

l 1/104

t 4/104

فراخي 18/104

i 8/104

" 2/104

h 2/104

n 6/104

p 2/104

r 4/104

a 5/104

y 2/104

u 3/104

d 5/104

c 2/104

v 1/104

« 2 »

* Probability :

$$\frac{1}{1024} \quad 3$$

$$\frac{2}{1024} \quad 5$$

$$\frac{3}{1024} \quad 3$$

$$\frac{4}{1024} \quad 2$$

$$\frac{5}{1024} \quad 3$$

$$\frac{6}{1024} \quad 1$$

$$\frac{7}{1024} \quad 1$$

$$\frac{8}{1024} \quad 1$$

$$\frac{9}{1024} \quad 1$$

$$\frac{11}{1024} \quad 1$$

$$\frac{18}{1024} \quad 1$$

« 3 »

$$* H(S) = \sum P_k \log_2 \frac{1}{P_k}$$

$$= 3 \left[\frac{1}{104} \log_2 \frac{104}{1} \right] + 5 \left[\frac{2}{104} \log_2 \frac{104}{2} \right]$$

$$+ 3 \left[\frac{3}{104} \log_2 \frac{104}{3} \right] + 2 \left[\frac{4}{104} \log_2 \frac{104}{4} \right]$$

$$+ 3 \left[\frac{5}{104} \log_2 \frac{104}{5} \right] + 1 \left[\frac{6}{104} \log_2 \frac{104}{6} \right]$$

$$+ 1 \left[\frac{7}{104} \log_2 \frac{104}{7} \right] + 1 \left[\frac{8}{104} \log_2 \frac{104}{8} \right]$$

$$+ 1 \left[\frac{9}{104} \log_2 \frac{104}{9} \right] + 1 \left[\frac{11}{104} \log_2 \frac{104}{11} \right]$$

$$+ 1 \left[\frac{18}{104} \log_2 \frac{104}{18} \right]$$

$$= 0.19328 + 0.54819 + 0.44268 + 0.361572$$

$$+ 0.6315 + 0.237 + 0.262 + 0.2846$$

$$+ 0.3055 + 0.3427 + 0.4379$$

$$= 4.0469 \text{ bits/symbol}$$

((4))

(C) Describe the relative merits and demerits of the following source coding schemes.

- (i) Huffman coding
- (ii) Lempe - Ziv coding.

« وصف المزايا والعيوب النسبية لمخططات تشفير المصدر التالية »

* advantages of Huffman coding *

1. Huffman coding would adapt automatically to choose the best code for each specific input, and the code might be quite different from one text to the next.
2. they are prefix codes.
3. Another advantage of Huffman coding is that you can use it for any alphabet starting from {0,1} finished Chinese hieroglyphs, while Morse is defined only for English letters.

* disadvantages of Huffman coding *

1. The requirement of knowledge of statistics of the source can not be always known priori (in advance)
بمقارنته معرفة أي احتمالية بشكل مسبق بالنسبة لـ 0 و 1
2. does not fully represent relationship between words and phrases.
تخزين الكلمات في الجمل وميل
3. Huffman coding process is not unique.

ليست دائماً غالباً فلانم أفحص

4. Requires great amount of memory

* advantages of Lempel - Ziv coding *

1. Simpler to implement than Huffman coding.

2. Lempel - Ziv coding is efficient because it does not need to pass the string table to the decompression.

3. There is no need to analyze the incoming text

← لا حاجة لتحليل النص الوارد
بـ uniquely decodable من متتاليات لا يفسد

* disadvantages of Lempel ziv coding *

أوقف وفسد الشيفرة

1. The method is good at text files but not good at other types of files,

2. The amount of storage needed is indeterminate as it depends on the total length of all the strings.

(d)

00010 11100 10100101

1 2 3 4 5 6 7 8 9

0 1 00 01 011 10 010 1100 101

0010 0011 1001 0100 1000 1100 1101

1 1 4 2 4 6 6

الطول متساوية واخر اثنين يختلفو بأخر بيت

(e)

prefix codes

تعريفين

① a code in which no code word is the prefix of any code word is called "a prefix-free code".

② set of binary sequence, probability such that no sequence in probability is a prefix of any other sequence in probability.

Kraft inequality

* the Kraft inequality gives necessary and sufficient condition for the existence of a prefix code or a uniquely decodable code.

((7))

Q2:-

[a] (i) mutual information

for two variables x, y the mutual inform $I(x, y)$ is the amount of certainty Regarding x that we learned after observing

$$\begin{aligned} I(x, y) &= H(x) - H(x|y) \\ &= H(x, y) - H(y|x) - H(y|y) \\ &= H(x) - H(y|x) \\ &= I(y|x) \end{aligned}$$

(2) Channel capacity

is the max rate at which information could be transmitted without loss of information and it's known as Shannon's channel capacity

$$C = W \log(1 + S/N)$$

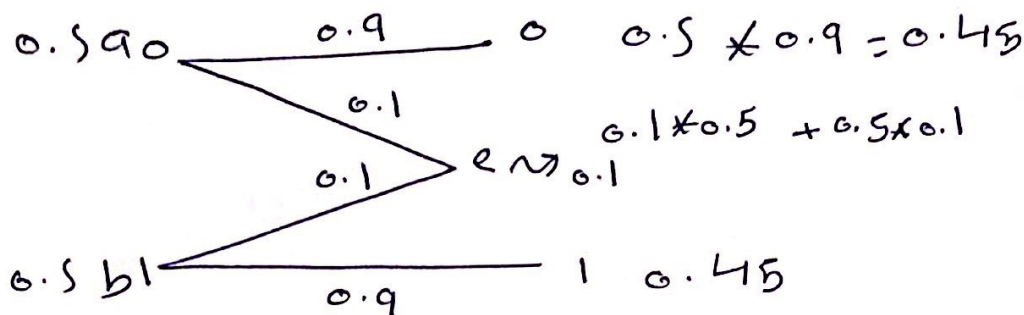
(7)

Q2

b

$$\alpha = 0.1$$

$$\text{let } p(\alpha) = 0.5$$



$$C = I(X, Y) = H(Y) - H(Y/X)$$

$$H(Y) = \sum p_y \log \frac{1}{p_y}$$

$$= 2 \left[0.45 \log_2 \frac{1}{0.45} \right] + \left(0.1 \log \frac{1}{0.1} \right)$$

$$= 1.03667 + 0.3322$$

$$H(Y) = 1.36887 \text{ bit/symbol}$$

$$H(Y/X) = \sum p_x \cdot H(Y/X)$$

$$= 2 \left(0.5 \left(0.9 \log \frac{1}{0.9} + 0.1 \log \frac{1}{0.1} \right) \right)$$

$$= 2 \left(0.5 \times 0.13667 + 0.1 \times 3.349 \right)$$

$$= 2(0.0683) + 0.3349$$

Q2 b

$$H(Y/X) = 0.8064$$

$$C = I(Y/X) = H(Y) - H(Y/X)$$

$$= 1.36887 - 0.8064$$

$$I(Y/X) = 0.5432 \text{ bit/symbol}$$

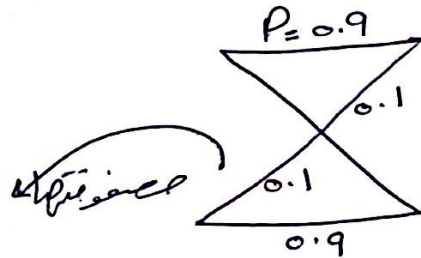
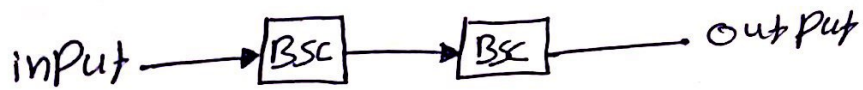
(8)

Q2

C

* البوك الى عنا ~~بوك~~ ممانه لـ BSC

* الـ بـ بـ بـ بـ بـ بـ بـ بـ بـ بـ BSC = 0.1 = cross

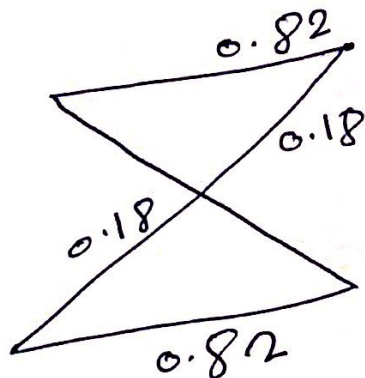


$$P = \begin{bmatrix} p & q \\ q & p \end{bmatrix}$$

$$P = \begin{bmatrix} 0.9 & 0.1 \\ 0.1 & 0.9 \end{bmatrix} * \begin{bmatrix} 0.9 & 0.1 \\ 0.1 & 0.9 \end{bmatrix}$$

first BSC second

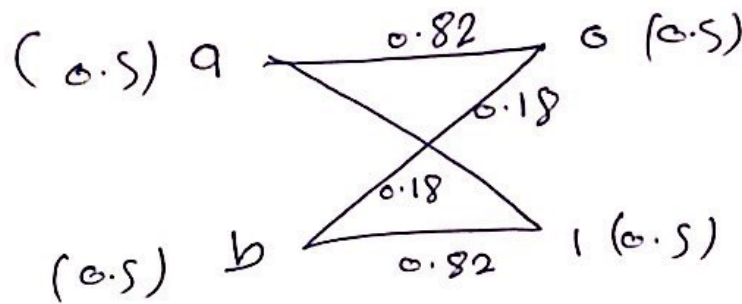
$$P = \begin{bmatrix} 0.82 & 0.18 \\ 0.18 & 0.82 \end{bmatrix}$$



(9)

Q2 Capacity

D



let $P = 0.5$

$$P(0) = 0.5 \times 0.82 + 0.5 \times 0.18$$

$$\boxed{P(0) = 0.5}$$

$$P(1) = 0.5 \times 0.18 + 0.5 \times 0.82$$

$$\boxed{P(1) = 0.5}$$

$$C = I(Y, X) = H(Y) - H(Y/X)$$

$$H(Y) = \sum p_y \log \frac{1}{p_y}$$

$$= (0.5 \times \log \frac{1}{0.5}) + (0.5 \times \log \frac{1}{0.5})$$

$$= 0.5 + 0.5 = 1 \text{ Bit/sym}$$

$$H(Y/X) = \sum p_x H(Y/X)$$

$$= 2 \times 0.5 (0.82 \log \frac{1}{0.82} + 0.18 \log \frac{1}{0.18})$$

$$= 2(0.5(0.23475 + 0.44528))$$

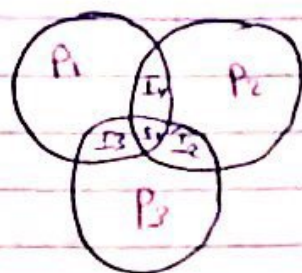
$$\boxed{H(Y/X) = 0.68003 \text{ bit/sym}}$$

$$C = H(Y) - H(Y/X) = 1 - 0.68003$$

(10)

$$\boxed{C = 0.31997 \text{ Bit/sym}}$$

Q4]



* block code form: $I_1, I_2, I_3, I_4, P_1, P_2, P_3$

$$P_1 = I_4 + I_1 + I_3$$

$$P_2 = I_4 + I_1 + I_2$$

$$P_3 = I_1 + I_2 + I_3$$

1. given the information digits

I_1, I_2, I_3, I_4
1 0 1 1

$$P_1 = 1 + 1 + 1 = 1$$

$$P_2 = 1 + 1 + 0 = 0$$

$$P_3 = 1 + 0 + 1 = 0$$

transmitted code word

1 0 1 1 1 0 0
 $I_1, I_2, I_3, I_4, P_1, P_2, P_3$

2. code rate: $\frac{k}{n} = \frac{4}{7}$

3. received \rightarrow

I_1	I_2	I_3	I_4	P_1	P_2	P_3
1	1	1	1	1	0	0
7	6	5	4	3	2	1

find the transmitted:

$$\begin{matrix} 4 & 3 & 1 \\ 1 & 1 & 0 \end{matrix} \Rightarrow 6$$

\therefore the error occurred in bit 6

10

$$C_1 = P_1 + I_4 + I_1 + I_3 = 1 + 1 + 1 + 1 = 0$$

$$C_2 = P_2 + I_4 + I_1 + I_2 = 0 + 1 + 1 + 1 = 1$$

$$C_3 = P_3 + I_1 + I_2 + I_3 = 0 + 1 + 1 + 1 = 1$$

\therefore Transmitted code word = 101100

B repetition code $(5,1)$
 \downarrow
 $(n,1)$

0 \rightarrow 00000

1 \rightarrow 11111

the received code 11001

1's = 3

0's = 2

number of 1's > number of 0's

\therefore transmitted b.t = 1

$$\text{code rate} = \frac{1}{n} = \frac{1}{5}$$

11

Q3] 6,3 systematic vector block code

$$b_0 = m_0 + m_1 + m_2$$

$$b_1 = m_0 + m_2$$

$$b_2 = m_0 + m_1$$

$$(a) G = [I/P] = \begin{bmatrix} 1 & 0 & 0 & 1 & 1 & 1 \\ 0 & 1 & 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 1 & 1 & 0 \end{bmatrix}$$

$$(b) C = I * G$$

$$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 0 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix}$$

8x3

$$\begin{bmatrix} 1 & 0 & 0 & 1 & 1 & 1 \\ 0 & 1 & 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 1 & 1 & 0 \end{bmatrix}_{3 \times 6}$$

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201710212

$$C = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 & 1 & 0 \\ 0 & 1 & 0 & 1 & 0 & 1 \\ 0 & 1 & 1 & 0 & 1 & 1 \\ 1 & 0 & 0 & 1 & 1 & 1 \\ 1 & 0 & 1 & 0 & 0 & 1 \\ 1 & 1 & 0 & 0 & 1 & 0 \\ 1 & 1 & 1 & 1 & 0 & 0 \end{bmatrix}$$

8x6

$Q_3 \ b$

$$G = \begin{matrix} & c_1 & c_2 & c_3 & c_4 & c_5 & c_6 & c_7 \\ \begin{matrix} x_0 \\ x_1 \\ x_2 \\ x_3 \end{matrix} & \begin{bmatrix} 1 & 0 & 1 & 1 & 0 & 0 & 0 \\ 1 & 1 & 1 & 0 & 1 & 0 & 0 \\ 1 & 1 & 0 & 0 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 & 0 & 0 & 1 \end{bmatrix} \end{matrix}$$

(a) all code vector:-

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$$C_0 = 00000000 \quad d=0$$

$$C_1 = x_0 + x_1 + x_2$$

$$C_2 = x_1 + x_2 + x_3$$

$$C_3 = x_0 + x_1 + x_3$$

$$C_4 = x_0$$

$$C_5 = x_1$$

$$C_6 = x_2$$

$$C_7 = x_3$$

(b) $d_{\min} = 3$