

# THERMAL EXPANSION

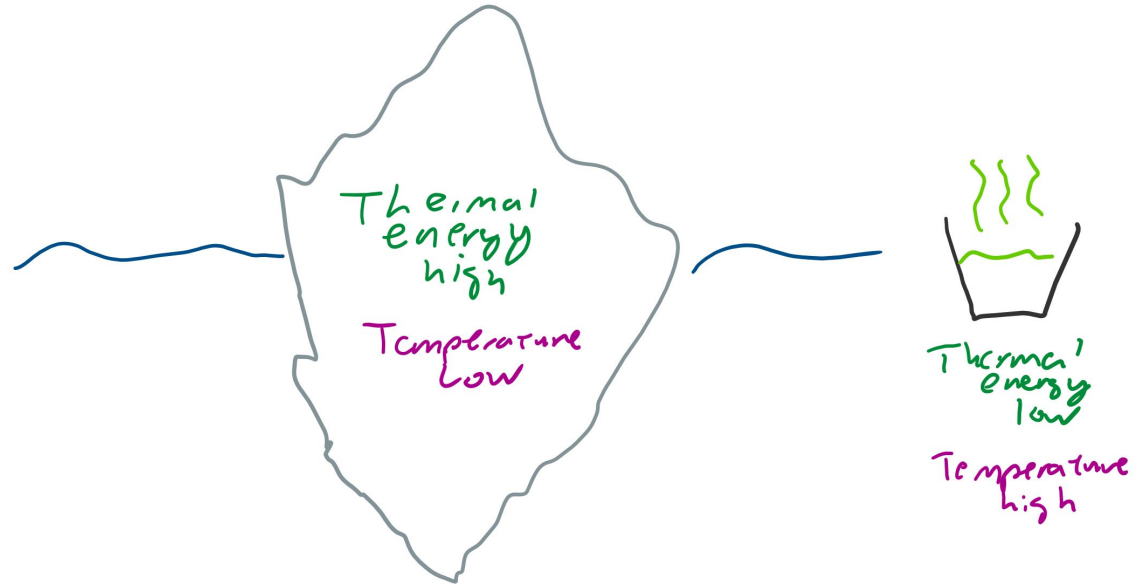
**When the solid turn to solid but bigger**

REVIEW

# TEMPERATURE

The average amount of energy the particles have

Opposed to thermal energy: the total amount of energy a sample has



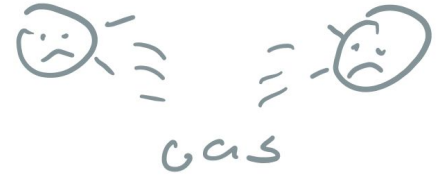
SOLIDS?

# STRUCTURE

Strongly connected particles

To weaken bonds, takes energy (like how it takes energy to pull apart two magnets)

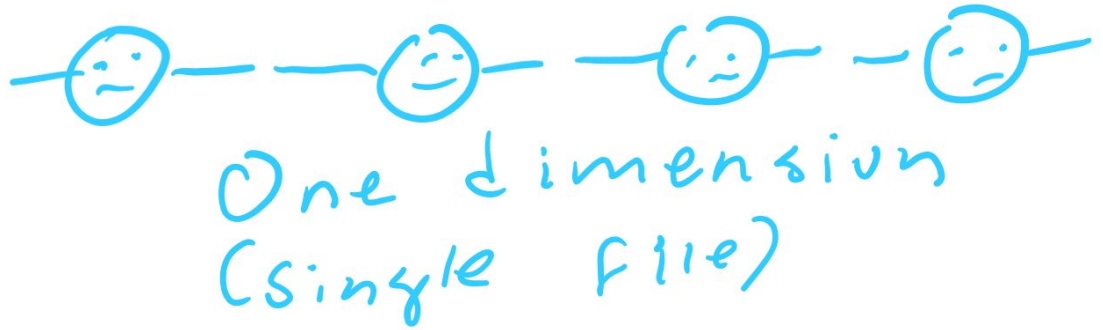
When energy given, bonds stretch



# THERMAL EXPANSION

# DIMENSIONS?

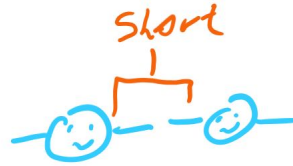
We will talk about 1D  
(one dimension) so  
the particles can  
only stretch in one  
direction



# EXPANSION

Average amount of energy between bonds proportional to stretchy

If temperature higher, distance between particles more

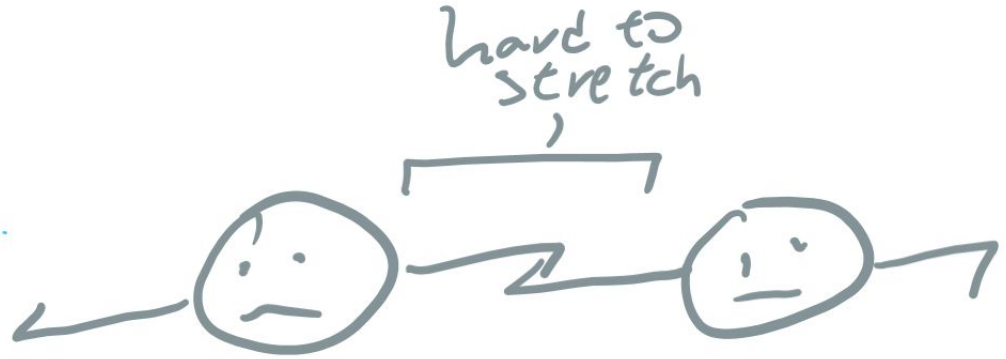




# STRETCHINESS

Some substances stretch (or expand) more when temperature is added

The “stretchiness” of a substance is called the “thermal expansion coefficient”





## HOW TO REMEMBER?

Symbol:  $\alpha$  (alpha)

Is a in Greek

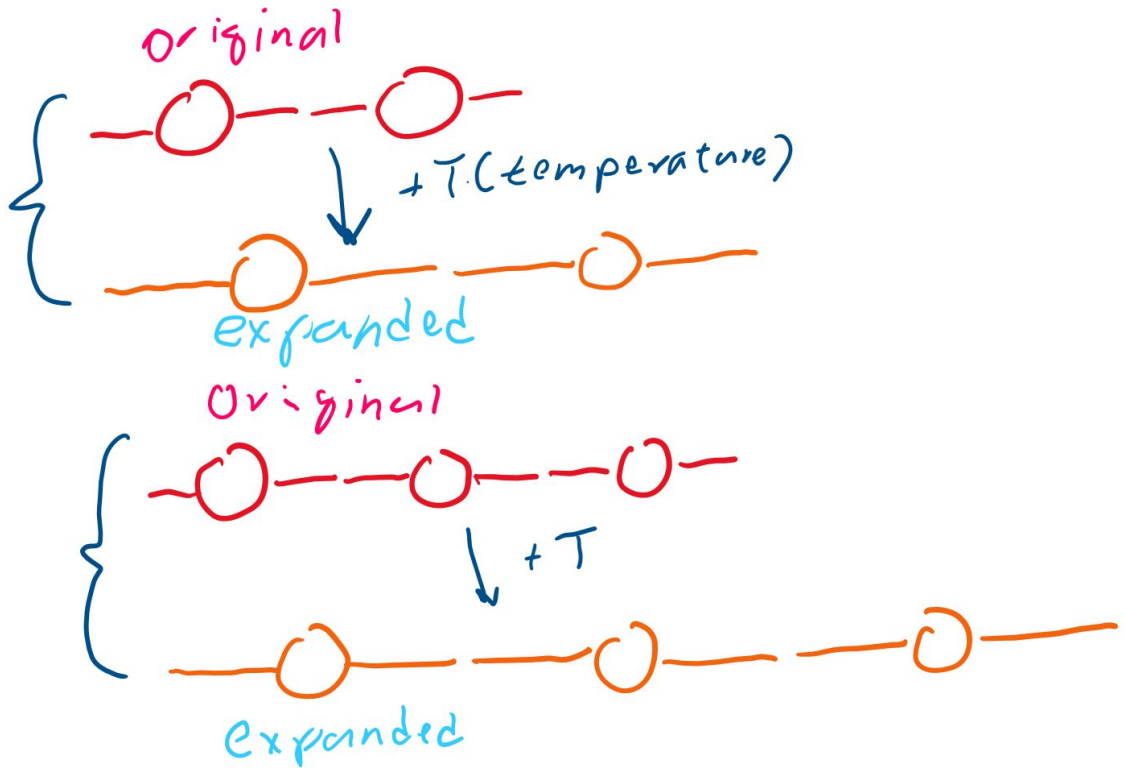
If you stretch  
someone out they'll  
scream aaaaaa

Ez claps

  
Name: alpha  
Looks like:   
It's a fish!

# LENGTH AND EXPANSION

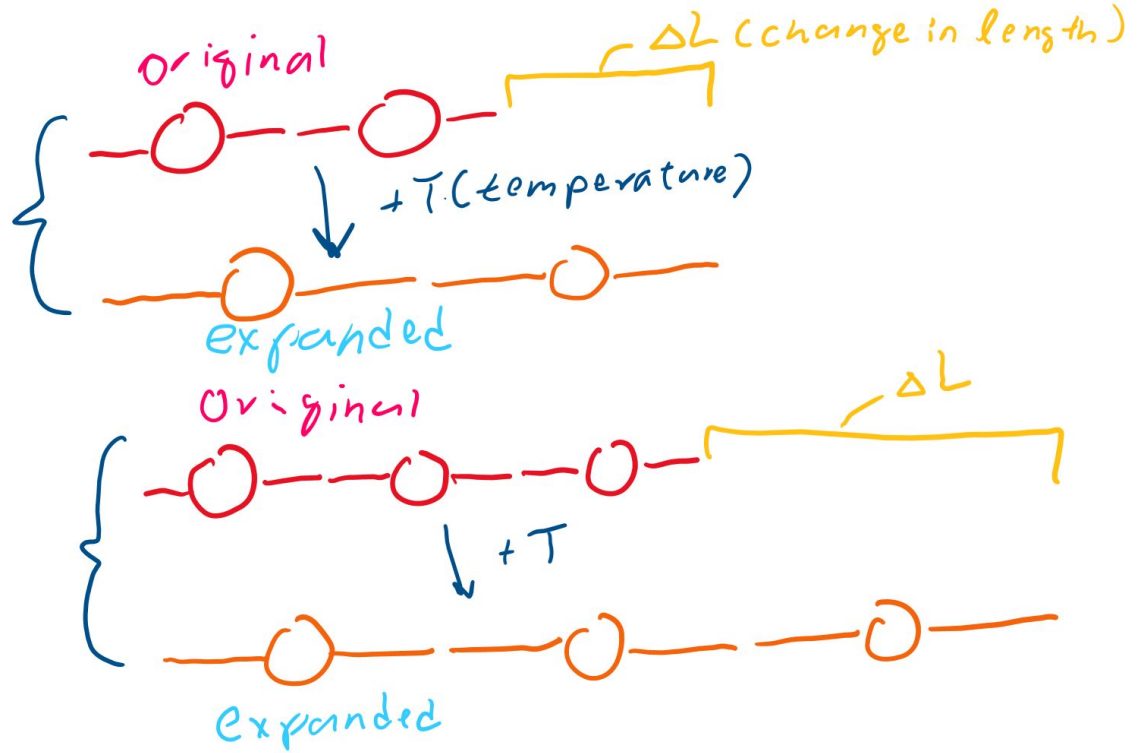
If the average length of bonds increases, which system on the right sees a longer change in length?



## ORIGINAL LENGTH

The bottom one!

It had a longer original length, so it was able to stretch a longer distance!



EQUATION

# CHANGE IN LENGTH

More change in temp  
means more change in  
length

More “stretchiness”  
means more change in  
length

Longer original  
length means more  
change in length

$$\Delta L = \alpha \Delta T L_0$$

Diagram illustrating the equation for change in length:

- $\Delta L$ : Change in length (indicated by a blue arrow pointing down to the text "Change in length")
- $\alpha$ : thermal expansion coefficient (indicated by a red arrow pointing up to the text "thermal expansion coefficient")
- $\Delta T$ : Change in temperature (indicated by a purple arrow pointing down to the text "Change in temperature")
- $L_0$ : Original length (indicated by a blue arrow pointing up to the text "Original length")

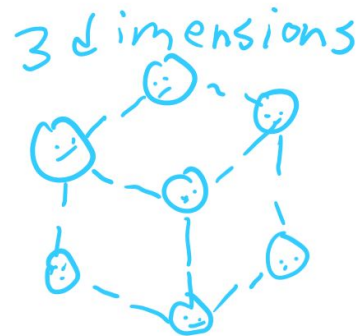
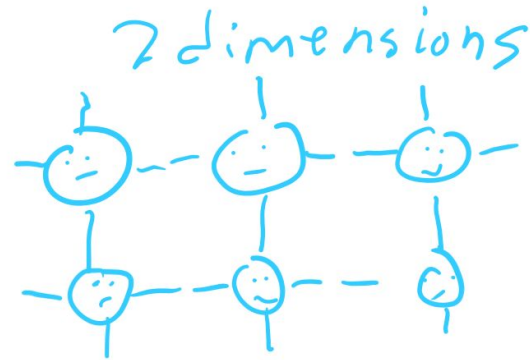
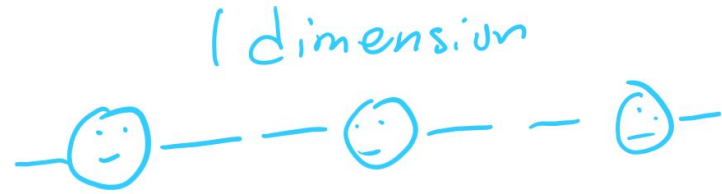
MORE DIMENSION?

## OTHER DIMENSIONS

1D is like a long rod  
(what we were using  
before)

2D is like a flat  
plate

3D is like a cube or  
any shape that is not  
flat





## EQUATIONS

1 dimension

$$\Delta L = 1 \alpha \Delta T L_0 \rightarrow \text{length}$$

2 dimensions

$$\Delta A = 2 \alpha \Delta T A_0 \rightarrow \text{area}$$

3 dimensions

$$\Delta V = 3 \alpha \Delta T V_0 \rightarrow \text{volume}$$

DERIVATION TO 2D (TOO  
HARD, NO NEED TO  
MEMORIZE)

$$\Delta L = L_{\text{final}} - L_{\text{original}}$$

$$L_f - L_0 = \alpha \Delta T L_0$$

$$L_f = \alpha \Delta T L_0 + L_0$$

$$L_f^2 = A_f$$

$$A_f = (\alpha \Delta T L_0 + L_0)^2$$

$$A_f = L_0^2 + 2\alpha \Delta T L_0^2 + \underbrace{\alpha^2 \Delta T^2 L_0^2}_{\text{close enough to 0}}$$

$$A_f = A_0 + 2\alpha \Delta T A_0$$

$$A_f - A_0 = 2\alpha \Delta T A_0$$

$$\Delta A = 2\alpha \Delta T A_0$$

## DERIVATION BORING

Here's the conceptual way to remember it:

In 2D you can stretch in 2 directions

In 3D you can stretch in 3 directions

See? It's like 1D but in more directions!

