

# Homework 4

1. Consider a dataset with following points in 2-dimensional space: (1,1), (2,1), (1,2), (2,2), (7,1), (8,1), (7,2), and (8,2). Show the clustering results using k-means with each of the following initial seed pairs.

- a. seed 1: (3, 2)  
seed 2: (5, 2)

First Iteration:

**seed 1: (1,2),(2,2),(1,1),(2,1) → Mean Center (1.5,1.5)**

**seed 2: (7,2),(8,2),(7,1),(8,1) → Mean Center (7.5,1.5)**

Second Iteration:

No Change

- b. seed 1: (3, 1)  
seed 2: (3, 0)

First Iteration:

seed 1: (1,2),(2,2),(1,1),(2,1),(7,2),(8,2),(7,1),(8,1) → Mean Center (4.5, 1.5)

seed 2: nothing! → Mean Center (3,0)

Second Iteration:

**seed 1: (1,2),(2,2),(1,1),(2,1) → Mean Center (1.5,1.5)**

**seed 2: (7,2),(8,2),(7,1),(8,1) → Mean Center (7.5,1.5)**

Third Iteration:

No Change

- c. seed 1: (4, 1.5)  
seed 2: (15, 1.5)

First Iteration:

seed 1: (1,2),(2,2),(1,1),(2,1),(7,2),(8,2),(7,1),(8,1) → Mean Center (4.5, 1.5)

seed 2: nothing! → Mean Center (15, 1.5)

Second Iteration:

**seed 1: (1,2),(2,2),(1,1),(2,1),(7,2),(8,2),(7,1),(8,1) → Mean Center (4.5, 1.5)**

**seed 2: Nothing! → Mean Center (15, 1.5)**

No change from first

Third Iteration:

Keeps looking for second cluster, but there isn't one.

We assume it keeps repeating and looping through the set of points but never finds a second cluster and therefore goes on forever looking for  $K = 2$  or eventually gives up.

2. Compute participation index (an interest measure for colocation) for the following pairs:

- a. (Burger King, Pizza Hut)  
 $\text{pi}(\text{BK}, \text{PH}) = \min \{ \text{pr}(\text{BK}, (\text{BK}, \text{PH})) , \text{pr}(\text{PH}, (\text{BK}, \text{PH})) \}$   
 $\text{pr}(\text{BK}, (\text{BK}, \text{PH})) = 1/10$   
 $\text{pr}(\text{PH}, (\text{BK}, \text{PH})) = 1/4$   
Therefore...  
 **$\text{pi}(\text{BK}, \text{PH}) = 1/4$**
- b. (Pizza Hut, McDonalds)  
 $\text{pr}(\text{PH}, (\text{PH}, \text{MC})) = 3/4$   
 $\text{pr}(\text{MC}, (\text{PH}, \text{MC})) = 3/13$   
 **$\text{pi}(\text{PH}, \text{MC}) = 3/13$**
- c. (Burger King, McDonalds)  
 $\text{pr}(\text{BK}, (\text{BK}, \text{MC})) = 6/10$   
 $\text{pr}(\text{MC}, (\text{BK}, \text{MC})) = 6/13$   
 **$\text{pi}(\text{BK}, \text{MC}) = 6/13$**