



University of Colombo, Sri Lanka

University of Colombo School of Computing

BACHELOR OF SCIENCE IN INFORMATION SYSTEMS

Second Year Examination - Semester II - UCSC AY19 [held in March/ April/May 2023]

IS2110 — Data Structures and Algorithms II

(Two (2) Hours)

00 019

Answer ALL questions

Number of Pages 12

Number of MCQs = 35; Essay Questions = 1

Important Instructions to candidates:

- I. Students should answer in the medium of English language only using the space provided in this question paper.
- II. Note that questions appear on both sides of the paper. If a page or a part of this question paper is not printed, please inform the supervisor immediately.
- III. MCQ should be marked on the **MCQ answer sheet** and the essay question on the **paper** provided.
- IV. Write your **index number** on the answer sheets.
- V. This paper has two (02) parts, **Part I** and **Part II**. Part I consists of **thirty-five (35) MCQ** questions for **seventy (70) marks**. Select the **best suitable answer among the given five (5) choices**. Part II consists of an **essay question for thirty marks (30)**. Answer **ALL** questions.
- VI. Each MCQ question has five (05) answers with **one (01) correct answer**. Each MCQ question is worth two (02) marks. If you **select more than one answer**, you will **receive zero (0) marks** for that particular question. However, there are no negative marks for selecting only one incorrect answer.
- VII. Calculators, mobile phones or any electronic device capable of storing and retrieving data are **not allowed**.

PART I

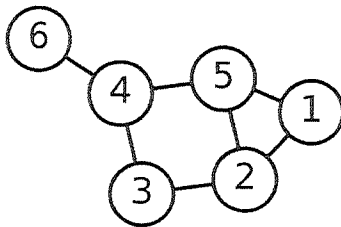
1) What is a **k-partite graph**?

- (a) A graph whose graph vertices can be partitioned into $k/2$ disjoint sets so that no two vertices within the same set are adjacent.
- (b) A graph whose graph vertices can be partitioned into two disjoint sets so that no $k/2$ vertices within the same set are adjacent.
- (c) A graph whose graph vertices can be partitioned into k disjoint trees.
- (d) A graph whose graph vertices can be partitioned into k disjoint sets so that no two vertices within the same set are adjacent.
- (e) A graph whose graph vertices can be partitioned into $k/2$ disjoint trees.

2) What is a **hyperedge** in a graph?

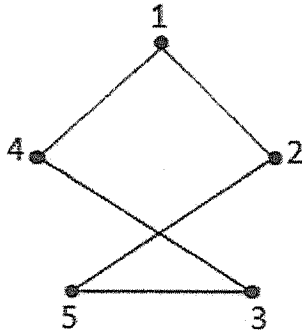
- (a) A particular type of line segment joining two vertices in a polygon, polyhedron, or higher-dimensional polytope
- (b) A particular type of line segment joining two vertices
- (c) A particular type of line segment joining two vertices in a polygon, or higher-dimensional polytope
- (d) A connection between two or more vertices of a hypergraph. A hyperedge connecting just two vertices is simply a usual graph edge
- (e) A connection between two vertices of a hypergraph. A hyperedge connecting just two vertices is simply a usual graph edge

3) What kind of data structure shows by the following figure?



- (a) Undirected graph
- (b) Directed graph
- (c) Multigraph
- (d) Complete Graph
- (e) Singleton graph

- 4) Which **adjacency matrix** shows the correct representation of the following graph.



(a)

	1	2	3	4	5
1		1		1	
2	1				1
3				1	1
4	1		1		
5		1	1		

(b)

	1	2	3	4	5
1		1		1	
2	1				1
3		1			1
4	1		1		
5		1	1		

(c)

	1	2	3	4	5
1		1		1	
2				1	1
3		1			1
4	1		1		
5		1	1		

(d)

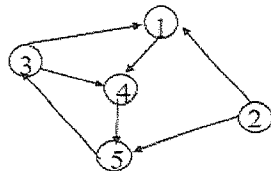
	1	2	3	4	5
1		1		1	
2	1				1
3		1			1
4	1		1		
5		1		1	

(e)

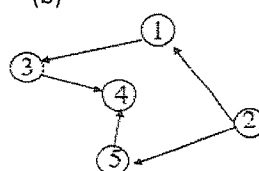
	1	2	3	4	5
1		1		1	
2	1				1
3		1			1
4	1				1
5		1	1		

- 5) Which of the following graph represents a **universal sink**?

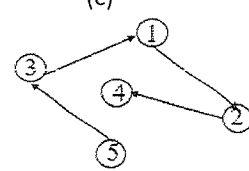
(a)



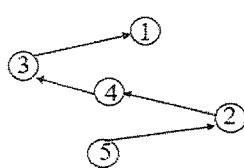
(b)



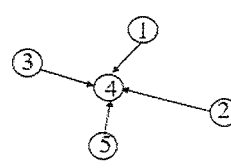
(c)



(d)



(e)



6) What can **Breadth First Search** in graphs be effectively used for?

- (a) To find the shortest path between two nodes
- (b) For topological sorting
- (c) To find the outdegree of a vortex
- (d) For solving sudoku puzzle
- (e) For scheduling problems

7) What can **Depth First Search** in graphs be effectively used for?

- (a) To find Minimum Spanning Tree
- (b) In Peer to Peer Networks
- (c) To find the indegree of a vortex
- (d) To test if a graph is Bipartite
- (e) To find Strongly Connected Components

8) What is a **Strongly connected component**?

- (a) An edge with both ends as the same vertex
- (b) A closed walk which does not repeat edges or vertices except for the starting and ending vertex
- (c) A leaf vertex with degree one.
- (d) The portion of a directed graph in which there is a path from each vertex to another vertex
- (e) A closed walk which repeat edges or vertices except for the starting and ending vertex

9) What is a disadvantage of **Open addressing Hash Table Organization**?

- (a) The use of outer hashing function
- (b) Consider a static set of keys
- (c) Overhead of multiple linked lists
- (d) Two parameters which govern performance need to be estimated
- (e) Maximum number of elements must be known

10) What is the **folding technique** in hashing function does?

- (a) Divide the key into several parts and perform an arithmetic operation (such as summation) on the parts.
- (b) Only a part of the key is used to compute the address.
- (c) The key is transformed into another number base.

- (d) The key is squared and the middle part/mid part of the result is used as the address.
(e) Multiply the key by a constant.

11)

What is the *running time* of **Depth First Search** in a graph?

- | | |
|-------------------|-------------------|
| (a) $O(V+E)$ | (d) $O(\log n)$ |
| (b) $O(n)$ | (e) $O(n \log n)$ |
| (c) $O(\log n^2)$ | |

12)

"Explore if possible, Backtrack otherwise" is a feature of,

- | |
|--------------------------|
| (a) Breadth First Search |
| (b) Depth first search |
| (c) Insertion sort |
| (d) Interpolation search |
| (e) linear search |

13)

What could be the possible *missing step* of the following source code related to **Breadth First Search**?

```
while Q ≠ ∅  
    do u ← DEQUEUE(Q)  
    for each v ∈ Adj[u]  
        do if color[v] = WHITE  
            then color[v] ← GRAY  
                d[v] ← d[u] + 1  
                p[v] ← u  
                _____  
    color[u] ← BLACK
```

- | |
|-------------------------|
| (a) do color[u] ← WHITE |
| (b) ENQUEUE(Q, v) |
| (c) color[s] ← GRAY |
| (d) p[u] ← null |
| (e) Q ← {s} |

- 14) What could be the possible *missing step* of the following source code related to **Depth First Search**?

```
DFS-Visit(u) {  
    color[u] ← GRAY //vertex u has been discovered  
    d[u] ← time ← time + 1  
    for each v ∈ Adj[u] //explore edge (u,v)  
        do if color[v] = WHITE  
            then p[v] ← u  
  
    color[u] → BLACK //blacken u; it is finished  
    f[u] ← time ← time + 1  
}
```

- (a) time ← time + 1
- (b) u ← pop(S)
- (c) DFS-Visit(v)
- (d) push(v, S)
- (e) color[v] = GRAY

- 15) What is the main advantage of **Adjacency Matrix Representation** of Graphs?

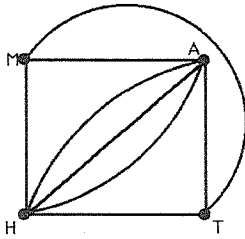
- (a) Has a quick way to determine the vertices adjacent to another vertex
- (b) Can quickly determine if there is an edge between two vertices
- (c) Memory required is $O(V + E)$
- (d) Preferred when the graph is sparse
- (e) Perform well for Directed graphs

- 16) What is the main advantage of **Adjacency List Representation** of Graphs?

- (a) Perform well for Directed graphs
- (b) Preferred when the graph is dense
- (c) Memory required is $O(V + 2E)$
- (d) Can quickly determine if there is an edge between two vertices
- (e) Has a quick way to determine the vertices adjacent to another vertex

17)

What is the **degree** of the vertex H?

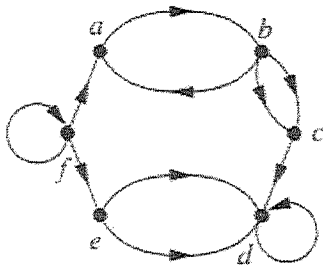


- (a) 3
- (b) 5
- (c) $5/3$

- (d) $2+3/2$
- (e) 10

18)

What is the best explanation for the graph given below?

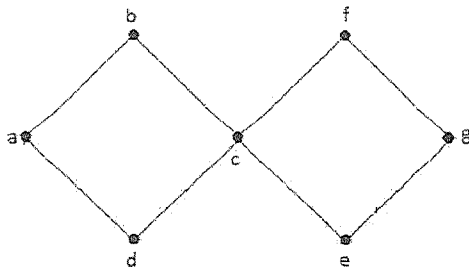


- (a) Directed multigraph
- (b) Simple graph
- (c) Complete graph

- (d) Disconnected Graph
- (e) Regular Graph

19)

What is the best explanation for the graph given below?



- (a) Regular Graph
- (b) Wheel graph
- (c) Complete graph
- (d) Cyclic Graph
- (e) Circuit

20) Which of the following statement is *false* regarding tree structures?

- (a) Trees contain no cycles
- (b) Has $V-1$ number of edges
- (c) Addition of any new edge to a tree creates exactly one cycle.
- (d) A tree need not be a graph but a graph must be a tree.
- (e) Trees represent relations of a hierarchical type.

21) Which of the following statement is *false* regarding **Jump Search**?

- (a) Works only for sorted arrays
- (b) The optimal size of a block to be jumped is (\sqrt{V}) .
- (c) The time complexity of Jump Search is between Linear Search and Binary Search.
- (d) Jump search may traverse back-and-forth few times before finding the search element.
- (f) The time complexity of Jump Search $O(\sqrt{V})$.

22) A **compression map hash function** is defined as:

$$h(k) = k \bmod m$$

if $m = 101$, what are the expected hash values for

{300, 305, 310, 400, 405, 410, 500, 505, 510}

- (a) {0, 5, 10, 0, 5, 10, 0, 5, 10}
- (b) {99, 3, 8, 98, 2, 7, 97, 1, 6}
- (c) {98, 2, 7, 97, 1, 6, 96, 0, 5}
- (d) {97, 1, 6, 96, 0, 5, 95, 99, 4}
- (e) {1, 6, 11, 1, 6, 11, 1, 6, 11}

23) In a **Radix Transformation** hashing function base 11 is used and $m=99$. What is the output hash value of $(453)_{10}$?

- (a) 382
- (b) 85
- (c) 84
- (d) 271
- (e) 57

- 24) Based on the **Pigeonhole Principle**, find the *minimum* number of students in a class such that three of them are born in the same month?

- | | |
|--------|--------|
| (a) 36 | (d) 27 |
| (b) 37 | (e) 25 |
| (c) 12 | |

- 25) **Perfect hashing** is a hashing technique which,

- | |
|---|
| (a) Provides $O(1)$ memory access to perform a search in a worst case |
| (b) Create a three-level hashing scheme with universal hashing at each level |
| (c) Is an open-addressing technique |
| (d) Successively examine the hash table until an empty slot is found to insert the key. |
| (e) A sequence of probe depends on the key being inserted. |

- 26) A **greedy strategy** usually progresses in,

- | |
|---|
| (a) A bottom-up fashion |
| (b) A top-down fashion |
| (c) Following divide and conquer approach |
| (d) Following decrease and conquer approach |
| (e) The virtual memory of a computer system |

- 27) Which is *not* an application of **Greedy algorithms**?

- | |
|-----------------------------------|
| (a) Pathfinding |
| (b) Fractional knapsack problem |
| (c) Huffman Coding |
| (d) Strongly connected components |
| (e) Coin problem |

- 28) As shown in the table below, there are 6 activities with corresponding start and end time, the objective is to compute an execution schedule having the maximum number of non-conflicting activities. What is the possible **activity execution schedule** using **greedy approach**?

Start Time (s)	Finish Time (f)	Activity Name
5	9	a1

1	2	a2
3	4	a3
0	6	a4
5	7	a5
8	9	a6

- (a) a2, a3, a5, a6
- (b) a2, a3, a4, a5
- (c) a1, a2, a5, a6
- (d) a1, a3, a2, a6
- (e) a4, a5, a1, a6

29) **Huffman's greedy algorithm** can be effectively used for,

- (a) Lossless data compression
- (b) Hashing large set of numbers
- (c) Appointing shorter codes for the data which appear with lower frequency
- (d) Finding strongly connected components
- (e) Finding cycles in graphs

30) The main difference between the **divide and conquer algorithms** and **Decrease and Conquer** algorithms is,

- (a) Decrease and conquer is a greedy approach while divide and conquer is not
- (b) There is only one subproblem in decrease and conquer techniques while divide and conquer has many
- (c) Length of coding
- (d) Decrease and conquer uses threads while divide and conquer uses processes.
- (e) Decrease and conquer cannot be used for sorting while divide and conquer is mainly used for sorting.

31) Which algorithm **cannot** be considered as an implementation of the **decrease and conquer approach**?

- (a) Insertion Sort
- (b) Depth First Search
- (c) Topological Sorting

- (d) Binary Search
- (e) Merge sort

32) What is the time complexity of **topological sort** using depth-first search?

- (a) $O(n)$
- (b) $O(\log n)$
- (c) $O(V^2)$
- (d) $O(n^2)$
- (e) $O(V+E)$

33) What is the time complexity of the **insertion sort** algorithm?

- (a) $O(n)$
- (b) $O(\log n)$
- (c) $O(V^2)$
- (d) $O(n^2)$
- (e) $O(V+E)$

34) What can be the missing step in the following **binary search** implementation?

```
while (l < r)
    _____
    if K = A[m] then
        return m
    else if K < A[m] then
        r = m-1
    else
        l = m+1
return -1
```

- (a) $m = [(l+r)/2]$
- (b) $m = [(l+r)]$
- (c) $m = m+1$

- (d) $m = m-1$
 (e) $m = \lfloor (1-r) \rfloor$

35)

What can be the missing step in the following **insertion sort** implementation?

INSERTION-SORT (A)

for $j = 2$ to $A.length$

$key = A[j]$

$i = j - 1$

while $i > 0$ and $A[i] > key$

$i = i - 1$

$A[i+1] = key$

- (a) $A[i] = A[i+1]$
 (b) $A[i+1] = A[i]$
 (c) $A[j] = A[j+1]$
 (d) $A[j+1] = A[j]$
 (e) $j=j+1$

Part II

Use separate answer sheets to answer this question.

Q1

- a. With a proper example discuss how you would insert keys {15, 38, 29, 25, 30, 43, 48, 53} to a hash table using **Coalesced Chaining** method ($m=9$). Make necessary assumptions if needed. (9 marks)
- b. Briefly describe how **Hashing** can be effectively used in the following application areas: (9 marks)
 - i. Dictionary
 - ii. Board Games
 - iii. Unix Shell
- c. Compare and contrast **divide and conquer algorithms** and **greedy algorithms** on problem-solving. (6 marks)
- d. Briefly describe the following three variations of **decrease and conquer algorithms** (6 marks)
 - i. Decrease by a constant
 - ii. Decrease by a constant factor
 - iii. Variable size decrease

(6 marks)