

TMUA Practice - Logarithms and Exponentials

1. Given that  $5^a = 32$  and  $2^b = 125$ , find the value of  $ab$

A  $\frac{\log 5}{\log 2}$

B  $\frac{5}{2}$

C  $\frac{15}{2}$

D 10

E 15

2. Find the product of the real roots of the equation

$$(\log_{10} x^2)^2 + \log_{10} x = 3$$

A  $-\frac{3}{4}$

B  $10^{-1}$

C  $10^{-\frac{1}{4}}$

D  $\frac{3}{4}$

E  $10^{\frac{1}{3}}$

3. Given  $\log_a y = \frac{1}{3}$  and  $\log_8 a = x + 1$  Express  $y$  in terms of  $x$

A  $y = x^{1/3}$

B  $y = x^3 + 2$

C  $y = 2^{x+1}$

D  $y = 8^{x+1}$

E  $y = 2^{x+\frac{1}{3}}$

4. In the following equation  $x \log 9 + \log 28 = \log 12 + x \log 49$  the value of  $x$  is

A  $\frac{\log 7}{\log 3}$       B  $\frac{1}{2}$       C 2      D  $\frac{7}{3}$       E 3

5. Given that  $x$  and  $y$  satisfy the following simultaneous equations

$$\log_y x = 5 \qquad \log_2 x = 2 + \log_2 y$$

what is the value of  $x + y$

A  $\sqrt{2}$       B 2      C  $4\sqrt{2}$       D  $5\sqrt{2}$       E  $2 + \sqrt{2}$

6. Given that  $x$  and  $y$  satisfy the following simultaneous equations

$$\log_2(y - 1) = 1 + \log_2 x \qquad 2\log_3 y = 2 + \log_3 x$$

the sum of the smallest solutions for  $x$  and  $y$  is

A  $\frac{1}{4}$       B  $\frac{5}{4}$       C  $\frac{3}{2}$       D  $\frac{7}{4}$       E 4

7. Find the sum of the real solutions of the equation

$$\log_2 x = \frac{2}{\log_2 x} + 1$$

- A  $\frac{9}{2}$       B 4      C  $\frac{7}{2}$       D 2      E  $\frac{3}{2}$

8. Given that  $6^{4x-3}$  can be written as  $216^a$  what is  $a$  in terms of  $x$

- A  $12x - 9$       B  $\frac{4x-3}{3}$       C  $4x - 1$       D  $\sqrt[3]{4x-3}$

9.  $(\log_{\frac{1}{2}} 2)(\log_{\frac{1}{3}} 3)(\log_{\frac{1}{4}} 4) \dots (\log_{\frac{1}{1000}} 1000)$  is equal to:

- A 2      B 1      C 0      D  $\pm 1$       E -1

10. The following three numbers are consecutive terms in an arithmetic progression

$$\log_{10}2 \qquad \log_{10}(2^x - 1) \qquad \log_{10}(2^x + 3)$$

what is the value of  $x$

- A  $2^5$       B 5      C  $\log_2 5$       D  $\log_5 2$       E  $\log_{10} \frac{5}{2}$

11. The positive real numbers  $a$  and  $b$  satisfy the following simultaneous equations

$$\log_2 4a - \log_2 b = 4 \qquad \log_2 a + \log_2 2b = 3$$

what is the value of  $2a + b$

- A 2      B 4      C 5      D 9      E 12

12. The number of positive solutions  $x$  to the equation

$$\log_2 x = \log_2(x + a) + b \qquad \text{where } a, b \text{ are non-zero real numbers, is}$$

- A zero if  $ab < 1$ , or one if  $ab > 1$   
B one if  $ab < 1$ , or two if  $ab > 1$   
C one if  $ab < 0$ , or zero if  $ab > 0$   
D zero if  $ab < 0$ , or one if  $ab > 0$   
E one if  $ab < 1$ , or zero if  $ab > 1$

13. Let  $a, b, c > 0$ . The equations:  $\log_a b = c$      $\log_b a = c + \frac{3}{2}$      $\log_c a = b$

- A    specify  $a, b$  and  $c$  uniquely
- B    specify  $c$  uniquely but have infinitely many solutions for  $a$  and  $b$
- C    specify  $a$  and  $b$  uniquely but have infinitely many solutions for  $c$
- D    have no solutions for  $a, b$  and  $c$
- E    have infinitely many solutions for  $a, b$  and  $c$

14. The equation  $\log_b((b^x)^x) + \log_a\left(\frac{c^x}{b^x}\right) + \log_a\left(\frac{1}{b}\right)\log_a c = 0$  has a repeated root when:

- A     $b^2 = 4ac$
- B     $b = \frac{1}{a}$
- C     $c = \frac{1}{b}$
- D     $c = \frac{b}{a}$

15. If  $\frac{\log a}{b-c} = \frac{\log b}{c-a} = \frac{\log c}{a-b}$  then  $(a^{b+c})(b^{c+a})(c^{a+b}) =$

- A     $-1$
- B     $1$
- C     $abc$
- D     $0$
- E     $a + b + c$