## TMUA Practice - Coordinate Geometry

The line y = mx + 4 where m > 0 is the normal to the curve  $y = 6 - x^2$  at the point (p,q). 1) What is the value of p?

A 
$$\frac{\sqrt{2}}{6}$$

A 
$$\frac{\sqrt{2}}{6}$$
 B  $-\frac{\sqrt{2}}{6}$  C  $\sqrt{\frac{3}{2}}$  D  $\pm \sqrt{\frac{3}{2}}$  E  $\sqrt{\frac{5}{2}}$ 

$$\binom{C}{\sqrt{\frac{3}{2}}}$$

$$D \pm \sqrt{\frac{3}{2}}$$

$$E \sqrt{\frac{5}{2}}$$

$$\frac{dy}{dx} = -2x \quad At (p_1q) \frac{dy}{dx} = -2p$$

$$9 = mp + 4$$
  
 $9 = 6 - p^2$   
 $mp + 4 = 6 - p^2$   
 $p^2 + mp - 2 = 0$ 

Find the shortest distance between the line y = 2x - 1 and the curve  $y = x^2 + 5$ 2)

$$\bigcirc$$
B $\sqrt{5}$ 

$$\frac{1}{100} \sqrt{5}$$
 C  $\sqrt{\frac{5}{2}}$  D 3 E 5

$$\frac{dy}{dx} = 2x = 2$$

$$\frac{dx}{dx} = \frac{2x - 1 = -\frac{x}{2} + \frac{13}{2}}{2} \qquad (1,6) \qquad (3,5)$$

$$\frac{dx}{dx} = \frac{15}{2} \qquad (6-5)^2 + (1-3)^2$$

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$$\frac{dy}{dx} = 2x = 3$$

$$3C = 1 \qquad (1/6)$$

$$3C = -\frac{1}{2}(3C - 1)$$

$$y - 6 = -\frac{1}{2} (x - 1)$$
 $y = -\frac{13}{2}$ 

$$2x - 1 = -\frac{\alpha}{2} + \frac{13}{2}$$
So 15

$$\frac{5x}{2} = \frac{15}{2}$$

$$x = 3$$

$$x = 3$$

$$(3,5)$$

$$\sqrt{(b-s)^2+(1-s)^2}$$

A line is drawn normal to the curve  $y = \frac{2}{x}$  at the point where x = 1. 3)

This line cuts the x-axis at P and y-axis at Q. Find the length of PQ.

$$A = \frac{3}{2}$$

A 
$$\frac{3}{2}$$
 B  $\frac{3}{2}\sqrt{5}$  C  $\sqrt{\frac{15}{2}}$  D  $2\sqrt{5}$ 

$$C \sqrt{\frac{15}{2}}$$

D 
$$2\sqrt{5}$$

$$\frac{dy}{dx} = -\frac{2}{x^2}$$

$$\frac{dy}{dx} = -2$$

$$\frac{1}{2}$$

$$y - 2 = \frac{1}{2}(x - 1)$$
 $y = \frac{3}{2} + \frac{3}{2}$ 

$$Q \left( O , \frac{3}{2} \right)$$

$$\frac{1}{2} = \frac{2}{2} \times \frac{1}{2}$$

$$\frac{1}{2} = \frac{3}{2} \times \frac{1}{2}$$

$$\frac{3}{2} \times \frac{1}{2}$$

4) The line y = mx + 2 passes through the points  $(5, log_3p)$  and  $(log_3p, 2)$ 

What is the difference between the possible values of p?



- B 3  $C \frac{2}{5}$  D 2
- E 10

$$log_3 p = 5m + 2$$
  
 $2 = m (5m+z) + 2$   
 $m=0$   $m=-\frac{2}{5}$ 

$$log_3 p = 5m + 2$$
  $Z = mlog_3 p + 2$   
 $2 = m(5m+2) + 2$   $log_3 p = 2$   $log_3 p = 0$   
 $m = 0$   $m = -\frac{2}{5}$   $p = 9$   $p = 1$   $9 - 1 = 8$ 

- 5) The line segment joining the points (2,2) and (6,8) is a diameter of a circle.

This circle is translated by 3 units in the positive x-direction, then reflected in the x-axis, and then enlarged by a scale factor of 2 about the centre of the resulting circle.

Find the equation of the final circle.

A 
$$(x-7)^2 + (y-5)^2 = 26$$

A 
$$(x-7)^2 + (y-5)^2 = 26$$
 B  $(x-7)^2 + (y+5)^2 = 26$ 

C 
$$(x-1)^2 + (y-5)^2 = 52$$
 D  $(x-1)^2 + (y+5)^2 = 52$ 

D 
$$(x-1)^2 + (y+5)^2 = 52$$

$$(E)(x-7)^2 + (y+5)^2 = 52$$
  $F(x-1)^2 + (y-5)^2 = 26$ 

$$F (x-1)^2 + (y-5)^2 = 26$$

Midpoint = 
$$(4,5)$$
  $\Gamma = \sqrt{2^2 + 3^2} = \sqrt{13}$   
 $(x-4)^2 + (y-5)^2 = 13$   
3 units the x-direction  $(x-7)^2 + (y-5)^2 = 13$ 

$$(y-5)^2 + (y-5)^2 = 13$$

reflected in 
$$\alpha$$
-axis 
$$(\alpha-7)^2 + (y+5)^2 = 13$$
 enlarged S.F. 2 
$$(\alpha-7)^2 + (y+5)^2 = 52$$

A point *P* lies on the curve with equation 
$$x^2 + y^2 - 6x + 8y = 24$$

What is the difference between the greatest and least possible values of the length *OP*, where *O* is the origin.

6)

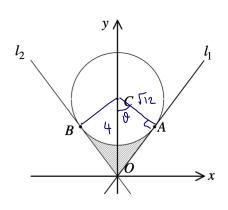
A 2 B 7 
$$\bigcirc$$
 10 D 12 E 14  $(x-3)^2-9+(y+4)^2-16=24$  Centre  $(3,-4)$   $r=7$ 

$$(x-3)^2 + (y+4)^2 = 49$$

$$DC = \sqrt{3^2 + 4^2} = 5$$

The diagram shows a circle with equation  $x^2 + (y - 4)^2 = 12$  and lines  $l_1$  and  $l_2$  which are 7) tangents to the circle at A and B.

Find the area of the shaded region enclosed by the circle and the lines  $l_1$  and  $l_2$ .



$$DA = \sqrt{16 - 12}$$
= 2

$$\cos \theta = \frac{\sqrt{12}}{4} = \frac{\sqrt{3}}{2}$$

A 
$$\pi - 2$$

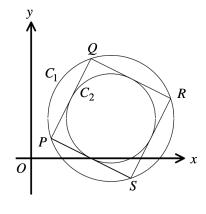
B 
$$2\sqrt{3} - \pi$$

$$C \frac{3\pi}{2}$$

B 
$$2\sqrt{3} - \pi$$
 C  $\frac{3\pi}{2}$  D  $4\sqrt{3} - 2\pi$  E  $2\sqrt{3} + \pi$ 

E 
$$2\sqrt{3} + \pi$$

The diagram shows a square PQRS with vertices at the points P(1,1), Q(3,5), R(7,3) S(5,-1). 8) The square is circumscribed by the circle C<sub>1</sub> and inscribed by the circle C<sub>2</sub> Find the area of the annulus between these two circles.



Midpoint PR = 
$$(4,2)$$
 = Centre  
radius  $C_1 = \sqrt{1^2 + 3^2} = \sqrt{10}$   
(centre to Q)  
radius  $C_7 = \sqrt{1^2 + 2^2} = \sqrt{5}$   
(centre to  
nid QR Aree =  $10\pi - 5\pi = 5\pi$   
 $(5,4)$ 

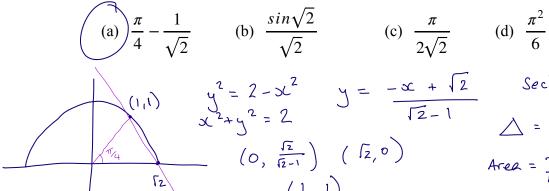
A 
$$(\sqrt{10} - \sqrt{5})\pi$$
 B  $2\pi$  C  $5\pi$  D  $\frac{5\pi}{2}$  E  $\sqrt{5}\pi$ 

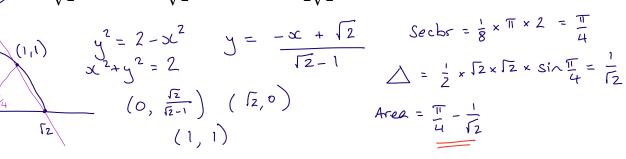
$$C$$
  $5\pi$ 

$$D \frac{5\pi}{2}$$

E 
$$\sqrt{5}\pi$$

Find the area bounded by the graphs  $y = \sqrt{2 - x^2}$  and  $x + (\sqrt{2} - 1)y = \sqrt{2}$ 9)





$$(0, \frac{\sqrt{2}}{(2-1)}) (\sqrt{2}, 0)$$

- 10) The lines given by the following equations are perpendicular.

① 
$$(1+\sqrt{3})y = px + 5$$
 ②  $y = (2-\sqrt{3})x + 8$ 

$$y = (2 - \sqrt{3})x + 8$$

What is the value of 
$$p$$
? Cracke-t  $\bigcirc$ :  $\bigcirc$   $\bigcirc$   $\bigcirc$   $\bigcirc$  2- $\sqrt{3}$ 

$$\widehat{A}$$
  $-5-3\sqrt{3}$ 

B 
$$-5 + 3\sqrt{3}$$

C 
$$5 - 3\sqrt{3}$$

D 
$$5 + 3\sqrt{3}$$

$$P = \frac{1+\sqrt{3}}{\sqrt{3}-2} \times \frac{(\sqrt{3}+2)}{(\sqrt{3}+2)} = \frac{3\sqrt{3}+5}{3-4} = -3\sqrt{3}-5$$

Let a and b be positive real numbers such that  $a \le b$ 11)

Given that  $x^2 + y^2 \le 1$ then the largest value that ax + by can equal is:

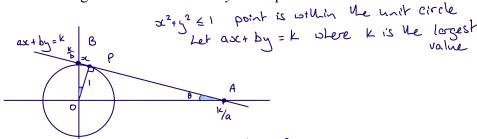
A 
$$a+b$$

$$\mathbf{B}$$

C 
$$\sqrt{a^2+b^2}$$

$$D \qquad a^2 + ab + b^2$$

$$E \qquad \frac{1}{a} + \frac{1}{b}$$



$$\triangle OPA$$
  $Sin \theta = \frac{1}{14/A} = \frac{q}{16}$ 

$$\triangle OPB \quad \cos \theta = \frac{1}{14/A} = \frac{b}{16}$$

$$\triangle$$
 ops  $\cos \theta = \frac{1}{14\sqrt{b}} = \frac{1}{14}$ 

using 
$$\sin^2\theta + \cos^2\theta = 1$$

$$\frac{a^2}{k^2} + \frac{b^2}{k^2} = 1 \qquad k^2 = a^2 + b^2$$

$$k = \sqrt{a^2 + b^2}$$