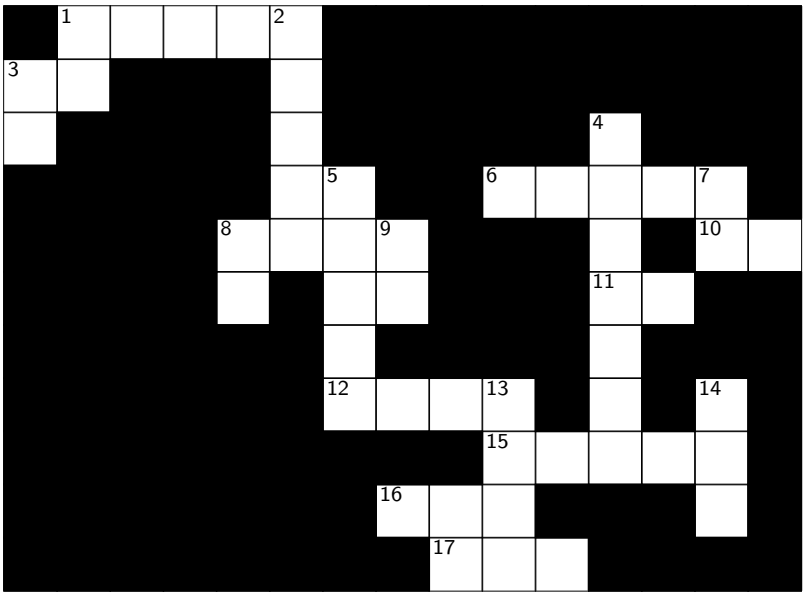
THE UK UNIVERSITY INTEGRATION BEE 2021/22

$$\int$$

ROUND TWO

Saturday, 20 November 2021

Sponsored by



Across

1. Smallest palindrome bigger than 17 ACROSS $\cdot$ (8 DOWN $+ 1)^2$

3. $\int_0^2 f(x)\mathrm{d}x$ where $3\int_1^2 f(x)\mathrm{d}x - 5\int_0^1 f(x)\mathrm{d}x = 17$ and $21\int_0^1 f(x)\mathrm{d}x - 7\int_1^2 f(x)\mathrm{d}x = 35$

6. $\dfrac{1 + 16\text{ ACROSS}^{\,4} + (16\text{ ACROSS } + 1)^4}{1 + 16\text{ ACROSS}^{\,2} + (16\text{ ACROSS } + 1)^2}$

8. The year the Riemann Integral was first published

10. $\lim\limits_{n\to\infty}\int_0^{14} \arctan(x^n)\mathrm{d}x$ to 2 significant figures

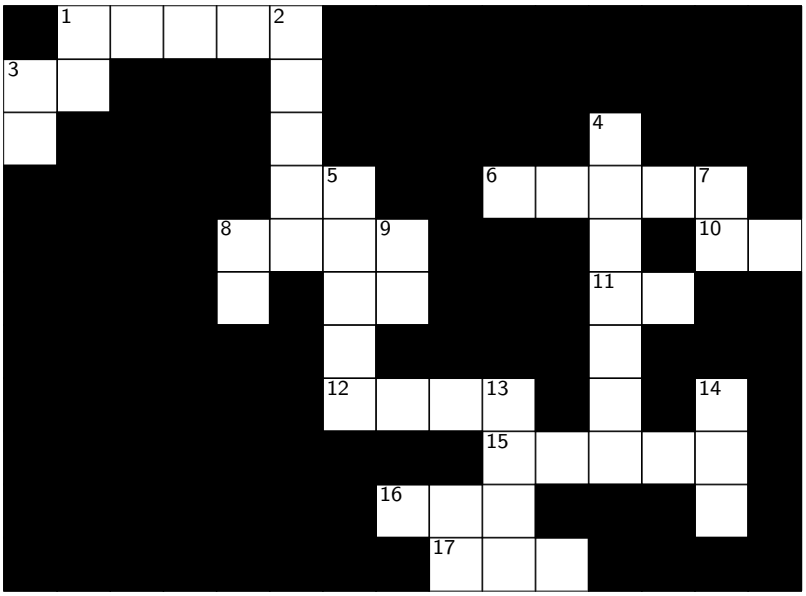
11. Sum of the three smallest numbers

12. A Fibonacci number

15. $\dfrac{1 + 310^2 + 310^4}{1 + 310 + 310^2}$

16. 7 DOWN $\times$ 10 ACROSS $-$ 10

17. A power of 7



Down

1. $\dfrac{16 \text{ ACROSS } + 1}{3}$

2. The nearest integer to $\dfrac{279^4+4}{279^2+2\cdot 279+2} + \displaystyle\int_0^\infty \frac{\ln(\sqrt{1+x})}{x\sqrt{x}}\mathrm{d}x$

3. The x^{th} triangular number where x is $7^{9 \text{ DOWN}} \mod 7$ DOWN

5. The largest n such that $I_n = \displaystyle\int_0^1 \frac{x^n}{1+x}\mathrm{d}x > \frac{1}{6 \text{ ACROSS} - 1}$

6. Palindromic number whose product of digits is 252 and whose digit sum is x mod 9 where x is a solution of the quadratic $x^2 - 7$ DOWN $+ 32 = 0$

7. $\displaystyle\int_0^1 f(x)\mathrm{d}x$ where $5\displaystyle\int_0^2 f(x)\mathrm{d}x + 4\int_0^1 f(x)\mathrm{d}x = 143$ and $7\displaystyle\int_0^2 f(x)\mathrm{d}x + 11\int_1^2 f(x)\mathrm{d}x = 210$

8. The expected number of coin flips to get three heads in a row on a fair coin

9. 14 DOWN - 16 ACROSS

13. The year the Lebesgue Integral was published

14. $f(6)$ where f is such that $f(x) + \displaystyle\int_2^5 f(t)\mathrm{d}t = 12x^2$