## THE UK UNIVERSITY INTEGRATION BEE 2022/23

## **ROUND ONE TIEBREAKER**

Monday, 12 December 2022

Sponsored by



$$1. \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{\cos x}{1 + e^x} \mathrm{d}x$$

$$2. \int \sqrt{x\sqrt[3]{x\sqrt[4]{x\sqrt[5]{x\cdots}}}} dx$$

3. 
$$\int_0^1 x^{\frac{1}{\ln x}} dx$$

4. 
$$\int e^{x+e^x} dx$$

5. 
$$\int_0^1 \ln\left(\frac{1+x}{1-x}\right) dx$$

6. 
$$\int_0^\infty \frac{1}{1 + e^{ax}} dx$$

$$7. \int_0^{2\pi} \sin(\sin(x) - x) \mathrm{d}x$$

8. 
$$\int_0^{\frac{\pi}{2}} \frac{\mathrm{d}x}{\tan^{\sqrt{2}}(x) + 1}$$

$$9. \int_0^\infty \frac{\arctan x}{1+x} \frac{\mathrm{d}x}{\sqrt{x}}$$

10. 
$$\int_{1}^{\sqrt{3}} \frac{\arctan x + \operatorname{arccot} x}{x} dx$$

11. 
$$\int \frac{\ln(2x)}{x \ln x} dx$$

12. 
$$\int_{0}^{\infty} x^{2n} e^{-x^2} dx$$

$$13. \int_0^1 \sqrt{-\ln x} \mathrm{d}x$$

14. 
$$\int_0^1 \frac{\ln{(1+x)}}{x} dx$$

$$15. \int_0^\infty \frac{x^2}{e^x - 1} \mathrm{d}x$$

$$16. \int_0^\infty \frac{\ln(x^2+1)}{x^2+1} dx$$

17. 
$$\int_0^\infty e^{-x} \frac{\sin ax}{x} dx$$

18. 
$$\int_0^1 \ln(x) \sin(\ln(x)) dx$$

19. 
$$\int_0^{\frac{\pi}{2}} (\ln(\tan\theta))^2 d\theta$$

$$20. \int_0^{\frac{\pi}{2}} \frac{\cos x}{2 - \sin(2x)} \mathrm{d}x$$