THE UK UNIVERSITY INTEGRATION BEE 2021/22

 \int

ROUND ONE

Friday, 15 October 2021











Sponsored by



$$1. \int \sqrt{x} \sqrt[3]{x} \sqrt[4]{x} \sqrt[5]{x} \cdots dx$$

2.
$$\int_0^{2\pi} \cos^{420}(x) dx$$

3.
$$\int_0^{\frac{\pi}{2}} \frac{\sqrt{\cos \theta}}{(\sqrt{\cos \theta} + \sqrt{\sin \theta})^5} d\theta$$

4.
$$\int_0^1 \frac{\sin(\ln x)}{\ln x} dx$$

5.
$$\int_0^4 \frac{\ln(x)}{\sqrt{4x - x^2}} dx$$

6.
$$\int_0^\infty \left(\frac{\ln x}{1+x}\right)^2 dx$$

7.
$$\int_0^\infty \frac{\ln(x)}{x^2 + 2x + 2} dx$$

$$8. \int_{-\infty}^{\infty} \frac{\mathrm{d}x}{\left(x^3 + \frac{1}{x^3}\right)^2}$$

9.
$$\int \frac{x-1}{(x+1)\sqrt{x^3+x^2+x}} dx$$

$$10. \int_0^{\frac{\pi}{2}} \frac{x}{\sin(x)} \mathrm{d}x$$

11.
$$\int_{1}^{\infty} \left(\frac{\ln x}{x} \right)^{2011} dx$$

12.
$$\int_0^\infty \frac{\sin x}{x^n} dx \ (0 < n < 2)$$

13.
$$\int_0^{\frac{\pi}{2}} \frac{\cos x}{(1 + \sqrt{\sin(2x)})^2}$$

14.
$$\int_0^{\frac{\pi}{2}} \ln(7997 \sin^2 \theta + 7945 \cos^2 \theta)$$

15.
$$\int \frac{\mathrm{d}x}{\csc x + 1}$$

16.
$$\int_0^{\frac{\pi}{2}} \frac{\{\tan(x)\}}{\tan(x)} dx$$
, where $\{x\}$ is the fractional part of x

17.
$$\int_0^{\frac{\pi}{2}} \frac{\sin^3 x}{2 + \sin x} dx$$

$$18. \int \sqrt{\frac{1}{x} - 1} dx$$

19.
$$\int_0^{2\pi} e^{3\cos\theta} \cos(3\sin\theta) d\theta$$

$$20. \int \sqrt{x^2 - 1} dx$$

$$21. \int_0^a \frac{x dx}{\cos(x)\cos(a-x)}$$

$$22. \int_0^1 \frac{\arctan x}{1+x} \mathrm{d}x$$

$$23. \int_0^{\frac{\pi}{2}} \frac{\ln(\cos x)}{\sin x} \mathrm{d}x$$

$$24. \int \frac{x \arcsin x}{\sqrt{1-x^2}} dx$$

25.
$$\int_0^\infty \frac{\arctan(x)}{x(\log(x)^2 + 1)} dx$$

26.
$$\int_{1}^{e} \frac{x - \ln x + 1}{x(x+1)^{2} + x \ln^{2} x} dx$$

$$27. \int_0^\infty \frac{\cos(ax)}{x^2 + b^2} \mathrm{d}x$$

$$28. \int_1^\infty \frac{\mathrm{d}x}{x + x^{\sqrt{2}}}$$

29.
$$\int_0^\infty \lfloor x \rfloor e^{-x} dx$$

30.
$$\int_0^1 \frac{\arctan(x^2)}{1+x^2} dx$$

31.
$$\int_0^1 \frac{dx}{1 + |\frac{1}{x}|}$$

32.
$$\int_0^\infty \frac{\cos(ax) - \cos(bx)}{x^2} dx$$

33.
$$\int_0^{2\pi} e^{\cos x} \cos(\sin x) \cos(5x) dx$$

$$34. \int_{-\infty}^{\infty} \frac{\mathrm{d}x}{\cosh^2(x)}$$

35.
$$\int_0^e W(x) dx$$
, where W is the Lambert W function, the solution to $W(x)e^{W(x)} = x$

$$36. \int_0^1 \frac{\arctan^2 x}{x} dx$$

$$37. \int_0^{\frac{\pi}{2}} \cos x^{\sin x^{\cos x}} - \sin x^{\cos x^{\sin x}} dx$$

38.
$$\int_3^5 \ln \Gamma(x) dx$$

39.
$$\int \frac{dx}{\sin^4(x) + \cos^4(x)}$$

$$40. \int_0^\infty \frac{\cos(\ln x)}{(1+x)^2} \mathrm{d}x$$