

## TMUA Coordinate Geometry

### **Syllabus**

Equation of a straight line; parallel and perpendicular lines; equation of a circle; circle theorems.

- 1a) Find the coordinates of the point lying between A (2,3) and B (8, - 3) which divides the line segment AB in the ratio 1:2.
- b) Find the x-coordinate of the point where the perpendicular bisector of the line segment joining the points (2,-6) and (5,4) cuts the x-axis.
- c) The perpendicular bisector of the line segment joining the points (3,-5) and (1,1) passes through the point with coordinates (11, $a$ ). Find the value of  $a$ .
- d) The straight line  $L_1$  passes through points A (13,5) and B (9,2) and D.  
The straight line  $L_2$  passes through points C (2,3) and D and is perpendicular to  $L_1$   
Find the coordinates of D.
- e) Find the shortest distance between the parallel lines with equations:  
 $x + 2y = 10$  and  $x + 2y = 20$

- f) A line  $L$  has equation  $y = 4 - 3x$ . A second line is perpendicular to  $L$  and passes through  $(-2,0)$ . Find the area of the region enclosed by the two lines and the  $x$ -axis.
- g) The points  $A$ ,  $B$  and  $C$  have coordinates  $(0,3)$  and  $(2, -1)$  and  $(k,1)$  respectively.  $AB$  and  $BC$  are perpendicular. Find the area of the triangle  $ABC$ .
- h) The straight line  $L$  passes through points  $(2,5)$  and  $(-2,3)$  and meets the coordinate axes at  $P$  and  $Q$ . Find the area of a square with side  $PQ$ .
- i) The points  $A$  and  $B$  have coordinates  $(-1,4)$  and  $(3, -2)$  respectively. A line  $L$  is perpendicular to  $AB$  and passes through  $B$ . Find the area of the region enclosed by  $L$  and the coordinate axes.

- j) The points  $A$  and  $B$  have coordinates  $(-4,5)$  and  $(0,4)$  respectively.  
The point  $C$  lies on the straight line through  $A$  and  $B$  such that the distance  $AB$  is the same as the distance  $BC$ . Find the coordinates of  $C$ .
- k) The points  $A$  and  $B$  have coordinates  $(1,4\sqrt{3})$  and  $(-3 + \sqrt{3},3)$  respectively.  
The straight line  $L$  through  $A$  and  $B$  meets the  $x$ -axis at  $C$ .  
Calculate the acute angle between  $L$  and the  $x$ -axis
- l) The points  $A$  and  $B$  have coordinates  $(8,2)$  and  $(11,3)$  respectively.  
The point  $C$  lies on the straight line with equation  $x + y = 14$   
Given that the distance  $AC$  is twice as large as the distance  $AB$ , find the two possible sets of coordinates of  $C$ .

- 2a) The straight line segment joining the points  $(6,-3)$  and  $(14,9)$  is a diameter of a circle. What is the equation of the circle?
- b) The straight line segment joining the points  $(-4,3)$  and  $(0,5)$  is a chord of a circle with centre on the line with equation  $y = 3x + 5$ . What is the equation of the circle?
- c) Find the equation of the tangent to the circle  $x^2 + y^2 - 8x - 14y + 40 = 0$  at the point  $(8,4)$
- d) A tangent to the circle  $x^2 + y^2 = 36$  passes through the point  $(10,0)$  and crosses the positive  $y$ -axis. What is the coordinate of the point where the tangent meets the  $y$ -axis?
- e) Find the radius of the circle with equation  $2x^2 + 2y^2 + 12x - 4y + 13 = 0$

- f) A circle has equation  $x^2 + y^2 - 10x - 12y + 56 = 0$  and  $C$  is the centre of the circle.  
The tangent to the circle at  $A (6,4)$  meets the  $y$ -axis at  $B$ . Find the area of triangle  $ABC$ .
- g) A circle has centre  $(8,k)$  where  $k$  is a constant.  
The straight line with equation  $y = 3x - 12$  is tangent to the circle at  $(5,3)$ .  
Find the equation of the circle.
- h) A circle has centre  $(5,6)$ .  
The straight line which passes through  $(1,8)$  and  $(10,11)$  is a tangent to the circle.  
Find the radius of the circle.
- i) A circle has equation  $x^2 + y^2 + 2x - 4y + 1 = 0$ .  
The straight line with equation  $y = mx$  is a tangent to the circle.  
Find the difference in the possible values of  $m$ .

- j) A circle has centre at the origin and radius  $R$ .  
The circle fits wholly inside the circle with equation  $x^2 + y^2 - 10x - 24y = 231$ .  
Find the range of possible value of  $R$ .
- k) A circle is drawn inside a regular hexagon so that the circle touches each side of the hexagon.  
What fraction of the hexagon is covered by the circle?
- l) Find the shortest distance between the circle  $x^2 + y^2 + 6x + 8y = 75$  and the origin.
- m) Find the shortest distance between the line  $x + 2y = 2$   
and the circle  $x^2 + y^2 - 6x - 8y + 21 = 0$
- n) Find the shortest distance between the two circle with equations:  
 $(x - 5)^2 + (y - 9)^2 = 45$  and  $(x + 1)^2 + (y + 3)^2 = 5$

- o) The two circles with equations below have exactly one point in common.

$$(x + 1)^2 + (y - 5)^2 = 36 \quad \text{and} \quad (x - 8)^2 + (y + 7)^2 = r^2$$

Find the two possible values of  $r$

- p) The two circles with equations below have exactly one point in common.

$$(x + r)^2 + (y + r)^2 = 4r^2 \quad \text{and} \quad (x - r)^2 + (y - 2)^2 = r^2$$

Find the value of  $r$

- q) Circle  $C_1$  has equation  $(x + 2)^2 + (y - 2)^2 = 7$

Circle  $C_2$  has equation  $(x - 6)^2 + (y - 2)^2 = 7$

The straight line  $L$  is a tangent to both circles and has a positive gradient.

The angle between  $L$  and the x-axis is  $\theta$ . Find  $\cos \theta$

- r) Circle  $C_1$  has equation  $x^2 + y^2 - 10x - 10y + 41 = 0$

Circle  $C_2$  has centre  $(k, 5)$  and touches both  $C_1$  and the y-axis

Find the difference between the two possible values of  $k$ .