

Xiaolong Pan

Gender: Male

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Education

- Bachelor of Sciences, 09/2018-06/2023
Huazhong University of Science and Technology, China
- Master in pure mathematics, 09/2023-06/2025, Advisor: Professor Ming Lu
Sichuan University, China
- PhD in pure mathematics, 09/2025-now, Advisor: Professor Ming Lu
Sichuan University, China

Research Interests

- Geometric representation theory, focusing on quantum groups, Hall algebras, quiver varieties, and categorification

Languages

- Chinese, English

Publications and preprints

- (with Ming Lu) *Dual canonical bases of quantum groups and \imath quantum groups*, arXiv:2504.19073.
This paper discusses the two realizations of \imath quantum groups via \imath Hall algebras and dual quantum Grothendieck rings of quiver varieties. Perverse sheaves provide the dual canonical bases for \imath quantum groups of type ADE with integral and positive structure constants. A new construction of the dual canonical bases of \imath quantum groups in the setting of \imath Hall algebras is presented, through which one can deduce the invariance of dual canonical bases under braid group actions and Fourier transformations. It is also proved that the dual canonical basis of quantum groups coincides with the double canonical basis defined by Berenstein and Greenstein.
- (with Jiayi Chen, Ming Lu, Shiquan Ruan, and Weiqiang Wang) *\imath Quantum groups and \imath Hopf algebras I: foundation*, arXiv:2511.11291.
The notion of \imath Hopf algebra, a new associative algebra structure defined on a Hopf algebra equipped with a Hopf pairing, is introduced in this paper. The \imath Hopf algebra on a Borel quantum group endowed with a τ -twisted Hopf pairing is shown to be a quasi-split universal \imath quantum group. In particular, the Drinfeld double quantum group is realized as the \imath Hopf algebra on the double Borel. This \imath Hopf approach allows us to develop connections between Lusztig's braid group action and relative braid group action.
- (with Jiayi Chen, Ming Lu, Shiquan Ruan, and Weiqiang Wang) *\imath Quantum groups and \imath Hopf algebras II: dual canonical bases*, submitted.

The iHopf framework enables us to construct the dual canonical basis of a universal iquantum group of arbitrary finite type, which are shown to be preserved by the ibraid group action. Again, the dual canonical basis for the Drinfeld double quantum group constructed via iHopf algebra on the double Borel is identified with Berenstein-Greenstein's double canonical basis.

- (with Ming Lu, Weiqiang Wang and Weinan Zhang) *Braid group action and quasi-split affine iquantum groups III*, arXiv:2511.00882

This paper deals with the Drinfeld presentation of quasi-split affine iquantum groups $\tilde{\mathbf{U}}^i$ of type $\text{AIII}_{2r}^{(\tau)}$. This type distinguishes itself among all quasi-split affine types in having 3 relative root lengths. Various basic real and imaginary v -root vectors for $\tilde{\mathbf{U}}^i$ are constructed, giving rise to affine rank one subalgebras of $\tilde{\mathbf{U}}^i$ associated with simple roots in the finite relative root system. We establish the relations among these v -root vectors and show that they provide a Drinfeld presentation of $\tilde{\mathbf{U}}^i$.

Participation in conferences

- Conference on Representation Theory, Geometry and Categorification, June 2024, Beijing Institute of Technology, Beijing, China
- International Conference on Representations of Algebras (ICRA 21, 2024), August 2024, Shanghai Jiao Tong University, Shanghai, China
- The International Conference on Representation Theory, June 2025, Nanjing University, Nanjing, China