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Candidate surname	Other names
Pearson Edexcel nternational Advanced Level	cre Number Candidate Number
<b>Monday 11 May</b>	2020
Afternoon (Time: 1 hour 30 minutes)	Paper Reference <b>WFM01/01</b>
Mathematics	
International Advanced Su Further Pure Mathematics	•

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

## Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer all questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
   there may be more space than you need.
- You should show sufficient working to make your methods clear.
   Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

## Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 8 questions in this question paper. The total mark for this paper is 75.
- The marks for each question are shown in brackets
  - use this as a guide as to how much time to spend on each question.

## Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

Turn over ▶







- 1.  $f(x) = x^3 \frac{10\sqrt{x} 4x}{x^2} \qquad x > 0$ 
  - (a) Show that the equation f(x) = 0 has a root  $\alpha$  in the interval [1.4, 1.5]

**(2)** 

(b) Determine f'(x).

**(3)** 

(c) Using  $x_0 = 1.4$  as a first approximation to  $\alpha$ , apply the Newton-Raphson procedure once to f(x) to calculate a second approximation to  $\alpha$ , giving your answer to 3 decimal places.

**(2)** 

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Question 1 continued	
	Q1
(Total 7 marks)	



**2.** The quadratic equation

$$5x^2 - 2x + 3 = 0$$

has roots  $\alpha$  and  $\beta$ .

Without solving the equation,

(a) write down the value of  $(\alpha + \beta)$  and the value of  $\alpha\beta$ 

**(1)** 

- (b) determine, giving each answer as a simplified fraction, the value of
  - (i)  $\alpha^2 + \beta^2$
  - (ii)  $\alpha^3 + \beta^3$

**(4)** 

(c) determine a quadratic equation that has roots

$$(\alpha + \beta^2)$$
 and  $(\beta + \alpha^2)$ 

giving your answer in the form  $px^2 + qx + r = 0$  where p, q and r are integers.

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Question 2 continued		

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3.	$f(z) = z^4 + az^3 + bz^2 + cz + d$	
	where $a$ , $b$ , $c$ and $d$ are integers.	
	The complex numbers $3 + i$ and $-1 - 2i$ are roots of the equation $f(z) = 0$	
	(a) Write down the other roots of this equation.	(2)
	(b) Show all the roots of the equation $f(z) = 0$ on a single Argand diagram.	(2)
	(c) Determine the values of a, b, c and d.	(5)
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Question 3 continu	ed		

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	Q3
(Total 9 marks)	



**4.** (a) Use the standard results for  $\sum_{r=1}^{n} r^2$  and  $\sum_{r=1}^{n} r$  to show that

$$\sum_{r=1}^{n} (2r-1)^2 = \frac{1}{3} n(4n^2 - 1)$$

for all positive integers n.

**(5)** 

(b) Hence find the exact value of the sum of the squares of the odd numbers between 200 and 500

(4)

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Question 4 continued	

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Question 4 continued	
	Q4
(Total 9 marks)	



5. The rectangular hyperbola H has equation xy = 64

The point  $P\left(8p, \frac{8}{p}\right)$ , where  $p \neq 0$ , lies on H.

(a) Use calculus to show that the normal to H at P has equation

$$p^3x - py = 8(p^4 - 1)$$
(5)

The normal to H at P meets H again at the point Q.

(b) Determine, in terms of p, the coordinates of Q, giving your answers in simplest form.

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Question 5 continue	ed		

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- **6.** (i)  $\mathbf{A} = \begin{pmatrix} 1 & 0 \\ 0 & 3 \end{pmatrix}$ 
  - (a) Describe fully the single transformation represented by the matrix **A**.

The matrix **B** represents a rotation of 45° clockwise about the origin.

(b) Write down the matrix **B**, giving each element of the matrix in exact form. (1)

The transformation represented by matrix A followed by the transformation represented by matrix B is represented by the matrix C.

(c) Determine C.

**(2)** 

**(2)** 

(ii) The trapezium T has vertices at the points (-2, 0), (-2, k), (5, 8) and (5, 0), where k is a positive constant. Trapezium T is transformed onto the trapezium T' by the matrix

$$\begin{pmatrix} 5 & 1 \\ -2 & 3 \end{pmatrix}$$

Given that the area of trapezium T' is 510 square units, calculate the exact value of k.

**(5)** 

estion 6 continued	



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Question 6 continued	
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(Total 10 marks)	



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7. The parabola C has equation $y^2 = 4ax$ , where a is a positive cons	tant.
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The line *l* with equation 3x - 4y + 48 = 0 is a tangent to *C* at the point *P*.

(a) Show that a = 9

**(4)** 

(b) Hence determine the coordinates of P.

**(2)** 

Given that the point S is the focus of C and that the line l crosses the directrix of C at the point A,

1)

(c) determine the exact area of triangle PSA.	(4		

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Question 7 continued		

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**8.** (i) Prove by induction that, for  $n \in \mathbb{Z}^+$ 

$$\sum_{r=1}^{n} \frac{2r^2 - 1}{r^2(r+1)^2} = \frac{n^2}{(n+1)^2}$$

(6)

(ii) Prove by induction that, for  $n \in \mathbb{Z}^+$ 

$$f(n) = 12^n + 2 \times 5^{n-1}$$

is divisible by 7

**(6)** 

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Question 8 continued	

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	. Q8
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TOTAL FOR PAPER: 75 MARKS	