









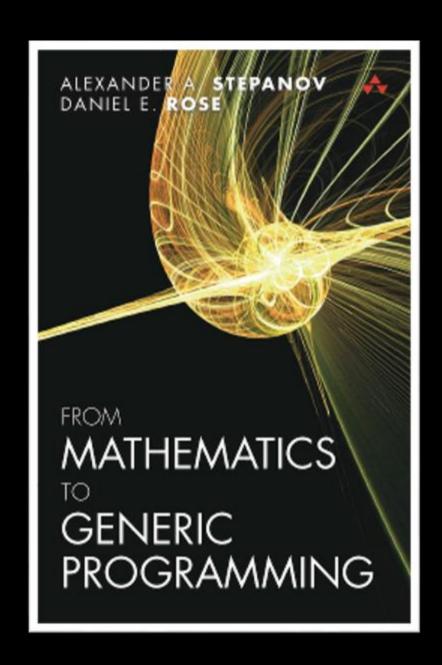


Discord Link: https://discord.gg/nxwbTHd

Github Repo: https://github.com/codereport/FM2GP-2025

code_report: Twitter | BlueSky | Mastodon

CoC: https://berlincodeofconduct.org/



From Mathematics to Generic Programming

Chapter 7/3

- 1. What This Book Is About
- 2. The First Algorithm
- 3. Ancient Greek Number Theory
- 4. Euclid's Algorithm
- 5. The Emergence of Modern Number Theory
- 6. Abstraction in Mathematics
- 7. Deriving a Generic Algorithm
- 8. More Algebraic Structures
- 9. Organizing Mathematical Knowledge
- **10.Fundamental Programming Concepts**
- 11. Permutation Algorithms
- 12.Extensions of GCD
- 13.A Real-World Application

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Deriving a Generic Algorithm 111 **Untangling Algorithm Requirements** 111 Requirements on A 113 116 Requirements on N 7.3 **New Requirements** 118 7.4 **Turning Multiply into Power** 119 Generalizing the Operation 121 7.6 7.7 **Computing Fibonacci Numbers** 124 Thoughts on the Chapter 7.8 127

Reduction

The power algorithm is not the only important algorithm defined on semigroups. Another key algorithm is *reduction*, in which a binary operation is applied successively to each element of a sequence and its previous result.

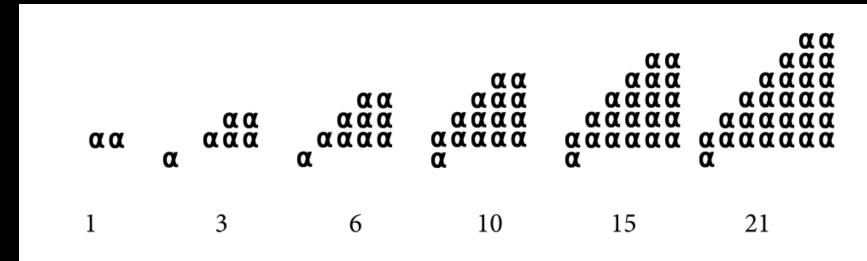
Two commonly seen examples of this in mathematics are the summation (Σ) function for additive semigroups and the product (Π) function for multiplicative semigroups. We can generalize this to an arbitrary semigroup.

This generalized version of reduction was invented in 1962 by computer scientist Ken Iverson in his language APL. In APL terminology, the / represented the reduction operator. For example, summation of a sequence is expressed as

+ / 1 2 3

The idea of reduction has appeared in many contexts since then. John Backus, inventor of the first high-level programming language, included a similar operator called *insert* in his language FP in 1977. (He called operators "functional forms.") An early paper on generic programming, "Operators and Algebraic Structures," by Kapur, Musser, and Stepanov, extended the idea to parallel reduction in 1981 and clarified the relationship to associative operations. The language Common Lisp, popular in the 1980s for artificial intelligence applications, included a reduce function. Google's MapReduce system, and its open-source variant Hadoop, is a current practical application of these ideas.

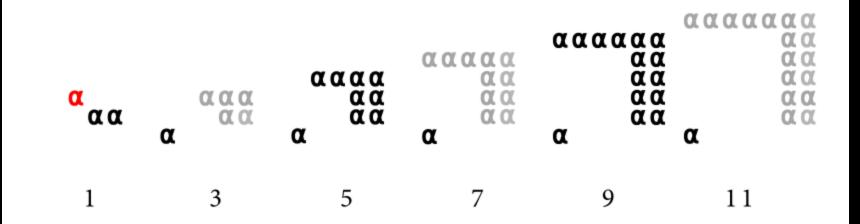
3 **Ancient Greek Number Theory 17** Geometric Properties of Integers 3.2 **Sifting Primes** 20 Implementing and Optimizing the Code 23 3.3 3.4 **Perfect Numbers** 28 3.5 **32** The Pythagorean Program 3.6 A Fatal Flaw in the Program 34 38 Thoughts on the Chapter 3.7



Oblong numbers are those that look like this:

ααα	α	ααα ααα ααα	αααα αααα αααα αααα			
2		6	12	20	30	42

~~~~~~~



Combining the first *n* gnomons creates a familiar shape—a square:

| α α<br>α | ααα<br><b>α</b> αα<br><b>α</b> | αααα<br>αααα<br>αααα<br>αααα | ααααα<br>ααααα<br>ααααα<br>ααααα |    |    |
|----------|--------------------------------|------------------------------|----------------------------------|----|----|
| 1        | 4                              | 9                            | 16                               | 25 | 36 |

## discussion

