

CSE 4200 Homework 2- Spencer Wallace

Summary:

All parts completed successfully. Because I was able to complete all parts, I am giving myself a full score **60/60**.

Part 1) (10 points) For each of the following triplets of points, find the normal vectors manually to the plane (if it exists) that passes through the triplet. Show your steps.

- a. **P1**(1, 1, 1), **P2**(1, 2, 1), **P3**(3, 0, 4)

$$A = P2 - P1 = (1, 2, 1) - (1, 1, 1) = (0, 1, 0)$$

$$B = P3 - P1 = (3, 0, 4) - (1, 1, 1) = (2, -1, 3)$$

$$n = A \times B$$

$$\begin{vmatrix} 0 & 1 & 0 \\ 2 & -1 & 3 \end{vmatrix} = i(3-0) - j(0-0) + k(0-2) = 3i - 2k = \mathbf{(3, 0, -2)}$$

$$\begin{vmatrix} 2 & -1 & 3 \end{vmatrix}$$

$$n = n/|n| = (3, 0, -2)/(3^2+0+(-2)^2)^{1/2} = (3, 0, -2)/(13^{1/2}) = \mathbf{(0.832, 0, -0.555)} \leq \text{normalized}$$

- b. **P1**(6, 3, -4), **P2**(0, 0, 0), **P3**(2, 1, -1)

$$A = P2 - P1 = (0, 0, 0) - (6, 3, -4) = (-6, -3, 4)$$

$$B = P3 - P1 = (2, 1, -1) - (6, 3, -4) = (-4, -2, 3)$$

$$n = A \times B$$

$$\begin{vmatrix} -6 & -3 & 4 \\ -4 & -2 & 3 \end{vmatrix} = i(-9 - -8) - j(-18 - -16) + k(12 - 12) = -i - 2j = \mathbf{(-1, -2, 0)}$$

$$\begin{vmatrix} -4 & -2 & 3 \end{vmatrix}$$

$$n = n/|n| = (-1, -2, 0)/((-1)^2+2^2+0)^{1/2} = (-1, -2, 0)/(5^{1/2}) = \mathbf{(-0.447, -0.894, 0)} \leq \text{normalized}$$

(You may check your answer using the program you wrote in the lab.)

Find the normalized normal to the plane $5x - 3y + 6z = 7$ and determine if the points $P1 = (1, 5, 2)$ and $P2 = (-3, -1, 2)$ are on the same side of the plane.

$$n = n/|n| = (5, -3, 6)/(5^2 + (-3)^2 + 6^2)^{1/2} = (5, -3, 6)/(70^{1/2}) = \left(\frac{5}{\sqrt{70}}, \frac{-3}{\sqrt{70}}, \frac{6}{\sqrt{70}} \right)$$

Part 2) (10 points) Find the normalized normal at the point (1, 2, 3) for each of the following two cases:

- a) A sphere: $x^2 + y^2 + z^2 = 14$

$$(1, 2, 3) - (0, 0, 0) = (1, 2, 3)$$

$$n = n/|n| = (1, 2, 3)/(1^2+2^2+3^2)^{1/2} = \left(\frac{1}{\sqrt{14}}, \frac{2}{\sqrt{14}}, \frac{3}{\sqrt{14}} \right)$$

- b) A plane: $3x - 4y + 2z - 1 = 0$

“For a plane, one perpendicular direction is the same for every point on the surface” – Notes pt.6

$$n = n/|n| = (3, -4, 2)/(9+16+4)^{1/2} = \left(\frac{3}{\sqrt{29}}, \frac{-4}{\sqrt{29}}, \frac{2}{\sqrt{29}} \right)$$

Part 3) (10 points) A robust method to find the normal to any polygon with N vertices is called the Newell's method.

a) Apply the Newell's method to a. of Question 1, and see whether you get the same answer.

(1,1,1) (1,2,1) (3,0,4)

$$N_x = (1-2)*(1+1) + (2-0)*(1+4) + (0-1)*(4+1) = -2 + 10 - 5 = 3$$

$$N_y = (1-1)*0 + (1-4)*(1+3) + (4-1)*(3+1) = 0 + -12 + 12 = 0$$

$$N_z = (1-1)*0 + (1-3)*(2+0) + (3-1)*(0+1) = 0 + -4 + 2 = -2$$

Using Newell's method does give the same answer ✓

b) Find the normal to the polygon (0, 0, 3), (3, 0, 0), (2, 2, -1), (-1, 5, -1), (1, 1, 1)

$$N_x = (0-0)*0 + (0-2)*(0+ -1) + (2-5)*(-1+ -1) + (5-1)*(0) + (1-0)*(1+3) = 0 + 2 + 6 + 0 + 4 = 12$$

$$N_y = (3-0)*(0+3) + (0- -1)*(3+2) + (-1- -1)*0 + (-1- 1)*(-1+1)*0 + (1-3)*(1+0) = 9 + 5 + -2 = 12$$

$$N_z = (0-3)*(0) + (3-2)*(0+2) + (2- -1)*(2+5) + (-1- 1)*(5+1) + (1- 0)*(1+0) = 0 + 2 + 21 + -12 + 1 = 12$$

$$\mathbf{N} = (12, 12, 12)$$

Part 4) (10 points) Let vectors $\mathbf{A} = (2, -1, 1)^T$ and $\mathbf{B} = (1, 1, -1)^T$. Find

a. the angle between \mathbf{A} and \mathbf{B} ,

$$\text{angle} = \cos^{-1}(\mathbf{A} \cdot \mathbf{B} / (|\mathbf{A}| |\mathbf{B}|))$$

$$\mathbf{A} \cdot \mathbf{B} = 2 + -1 + -1 = 0$$

(check that bottom isn't 0 to check for undefined)

$$|\mathbf{A}| = (4 + 1 + 1)^{1/2} = 6^{1/2}$$

$$|\mathbf{B}| = (1 + 1 + 1)^{1/2} = 3^{1/2}$$

$$\text{angle} = \cos^{-1}(0) = 90 \text{ degrees or } 1/2\pi$$

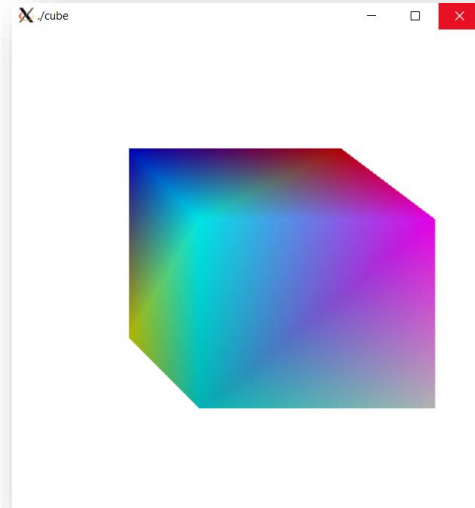
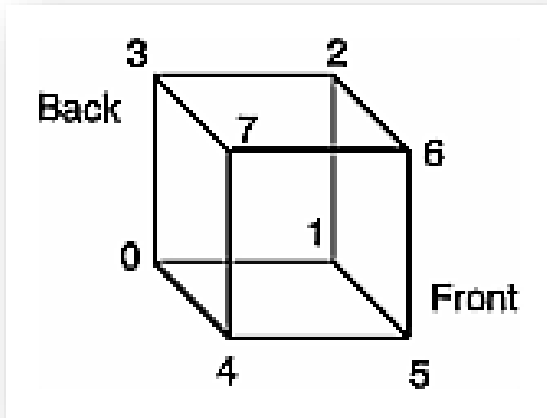
b. a unit vector perpendicular to both \mathbf{A} and \mathbf{B} .

$$\mathbf{A} \times \mathbf{B} = \begin{vmatrix} 2 & -1 & 1 \\ 1 & 1 & -1 \end{vmatrix} = (1 - 1)\mathbf{i} - (-2 - 1)\mathbf{j} + (2 - -1)\mathbf{k} = (0, 3, 3)^T$$

$$\begin{vmatrix} 1 & 1 & -1 \end{vmatrix}$$

$$\mathbf{V} = \mathbf{v} / |\mathbf{v}| = (0, 3, 3) / (0+9+9)^{1/2} = (0, 0.707, 0.707)^T$$

Part 5) (10 points) Use **glDrawElements()** to draw the following cube with each face having a different color.



Code

```
[007463307@csusb.edu@jb359-4 hw2]$ cat cube.cpp
```

```
#include <stdio.h>
#define GL_GLEXT_PROTOTYPES
#include <GL/gl.h>
#include <GL/glu.h>
#include <GL/glx.h>
#include <GL/glex.h>
#include <GL/glut.h>
```

```
GLfloat cube[] = {
    //back
    125, 175, 0.7, 0.7, 0, //0
    350, 175, 0.7, 0, 0.7, //1
    350, 375, 0.7, 0, 0, //2
    125, 375, 0, 0, 0.7, //3
    //front
    200, 100, 0, 0.7, 0.7, //4
    450, 100, 0.7, 0.7, 0.7, //5
    450, 300, 0.9, 0, 0.9, //6
    200, 300, 0, 0.9, 0.9, //7
};
```

```
GLubyte front[] = {4,5,6,7};
```

```
GLubyte right[] = { 1,2,6,5};
GLubyte left[] = {0,4,7,3};
GLubyte back[] = {0,3,2,1};
GLubyte top[] = {2,3,7,6};
GLubyte bottom[] = {0,1,5,4};
```

```
unsigned int vbo; //vertex buffer object
unsigned int ind;
//initialization
void init( void )
{
    glClearColor( 1.0, 1.0, 1.0, 0.0 ); //get white background color
    glColor3f( 0.0f, 0.0f, 0.0f ); //set drawing color
    gluOrtho2D( 0.0, 500.0, 0.0, 500.0 );
    glGenBuffers ( 1, &vbo ); //handle to vertex buffer object
    glBindBuffer ( GL_ARRAY_BUFFER, vbo );
    glBufferData ( GL_ARRAY_BUFFER, sizeof ( cube ), cube, GL_STATIC_DRAW );
}
```

```
void display( void )
{
    glClear( GL_COLOR_BUFFER_BIT ); //clear screen
    glEnableClientState(GL_VERTEX_ARRAY);
    glEnableClientState(GL_COLOR_ARRAY);
    glVertexPointer(2, GL_FLOAT, 5*sizeof(GLfloat), 0);
    glEnable(GL_CULL_FACE);
    glCullFace(GL_BACK);

    glColorPointer ( 3, GL_FLOAT, 5*sizeof(GLfloat), (void*)(2*sizeof(GLfloat)));
    glDrawElements ( GL_POLYGON, 4, GL_UNSIGNED_BYTE, front );

    // glColorPointer ( 3, GL_FLOAT, 3*sizeof(float), right);
    //glColor3f(0.7,0.7,0);
    glDrawElements ( GL_POLYGON, 4, GL_UNSIGNED_BYTE, right );

    //glColorPointer ( 3, GL_FLOAT, 3*sizeof(float), left);
    // glColor3f(0.7,0,0.7);
    glDrawElements ( GL_POLYGON, 4, GL_UNSIGNED_BYTE, left );

    //glColorPointer ( 3, GL_FLOAT, 3*sizeof(float), back);
    //glColor3f(0.7,0,0);
    glDrawElements ( GL_POLYGON, 4, GL_UNSIGNED_BYTE, back );
}
```

```
//glColorPointer ( 3, GL_FLOAT, 3*sizeof(float), top);  
//glColor3f(0,0.7,0.7);  
glDrawElements ( GL_POLYGON, 4, GL_UNSIGNED_BYTE, top );
```

```
//glColorPointer ( 3, GL_FLOAT, 3*sizeof(float), bottom);  
//glColor3f(0,0.7,0);  
glDrawElements ( GL_POLYGON, 4, GL_UNSIGNED_BYTE, bottom );
```

```
glDisableClientState ( GL_VERTEX_ARRAY );  
glDisableClientState ( GL_COLOR_ARRAY );  
glFlush(); //send all output to screen  
}
```

```
void keyboard ( unsigned char key, int mousex, int mousey )  
{  
    switch ( key ) {  
        case 27: // escape  
            exit ( -1 );  
    }  
    glutPostRedisplay();  
}
```

```
void specialKey ( int key, int mousex, int mousey )  
{  
    switch ( key ) {  
        case GLUT_KEY_UP:  
            break;  
        case GLUT_KEY_DOWN:  
            break;  
        case GLUT_KEY_LEFT:  
            break;  
        case GLUT_KEY_RIGHT:  
            break;  
    }  
    glutPostRedisplay();  
}
```

```
void myMouse( int button, int state, int x, int y )  
{  
    glFlush(); //send all output to screen  
}
```

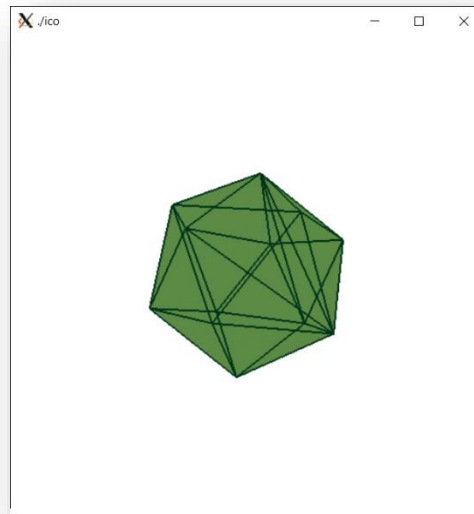
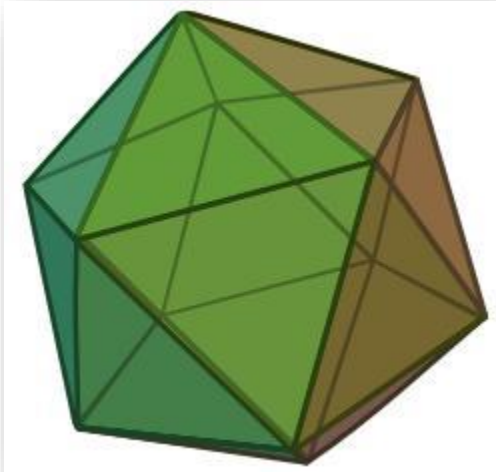
```

/* Main Loop
 * Open window with initial window size, title bar,
 * RGBA display mode, depth buffer.
 */
int main(int argc, char** argv)
{
    glutInit(&argc, argv);    //initialize toolkit
    glutInitDisplayMode (GLUT_SINGLE| GLUT_RGB ); //set display mode
    glutInitWindowSize(500, 500);    //set window size on screen
    glutInitWindowPosition( 100, 150 ); //set window position on screen
    glutCreateWindow(argv[0]);    //open screen widow
    init();
    glutDisplayFunc (display);    //points to display function
    glutKeyboardFunc ( keyboard );
    // glutSpecialFunc( specialKey );
    glutMouseFunc( myMouse );

    glutMainLoop();    //go into perpetual loop
    return 0;
}

```

Part 6) (10 points) Write a program or programs to reproduce one of the following figures of **icosahedron** and dodecahedron



Code

```
#include <GL/glut.h>
#include <GL/gl.h>
#include <stdlib.h>
using namespace std;

#define a .525731112119133606
#define b .850650808352039932

GLfloat vdata[12][3] =
{
    {-a, 0.0, b}, {a, 0.0, b}, {-a, 0.0,-b}, {a, 0.0,-b},
    {0.0, b, a}, {0.0, b,-a}, {0.0,-b, a}, {0.0,-b,-a},
    {b, a, 0.0}, {-b, a, 0.0}, {b,-a, 0.0}, {-b,-a, 0.0}
};

GLuint tindices[20][3] =
{
    {0,4,1}, {0,9,4}, {9,5,4}, {4,5,8}, {4,8,1},
    {8,10,1}, {8,3,10}, {5,3,8}, {5,2,3}, {2,7,3},
    {7,10,3}, {7,6,10}, {7,11,6}, {11,0,6}, {0,1,6},
    {6,1,10}, {9,0,11}, {9,11,2}, {9,2,5}, {7,2,11}
};

void init(void)
{
    glClearColor(1.0, 1.0, 1.0, 0.0); //get white background color
    glShadeModel(GL_SMOOTH);
    glEnable(GL_SMOOTH);
    glEnable(GL_POINT_SMOOTH);
```

```

glEnableClientState(GL_VERTEX_ARRAY);
glBlendFunc(GL_SRC_ALPHA, GL_ONE_MINUS_SRC_ALPHA);
glEnable( GL_BLEND );

}

void display()
{
    glLoadIdentity();
    gluLookAt(2.0, 2.0, 2.0, 0.0, 0.0, 0.0, 1.0, 0.0);
    glClear(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT);

    glRotatef(25, 0, 0, 1);
    glBegin(GL_TRIANGLES);
        glColor4f(0.3, 0.5, 0.2, 0.7);
    for (int i = 0; i < 20; i++) {
        glVertex3fv(&vdata[tindices[i][0]][0]);
        glVertex3fv(&vdata[tindices[i][1]][0]);
        glVertex3fv(&vdata[tindices[i][2]][0]);
    }
    glEnd();

    glColor4f(0.0, 0.2, 0.1, 1);
    glLineWidth(2.25);
    for (int i = 0; i < 20; i++) {
        glBegin(GL_LINE_LOOP);
        glVertex3fv(&vdata[tindices[i][0]][0]);
        glVertex3fv(&vdata[tindices[i][1]][0]);
        glVertex3fv(&vdata[tindices[i][2]][0]);
    }
    glEnd();
    glFlush();
}

void reshape(int w, int h)
{
    glViewport(0, 0, (GLsizei)w, (GLsizei)h);
    glMatrixMode(GL_PROJECTION);
    glLoadIdentity();
    glFrustum(-1.0, 1.0, -1.0, 1.0, 1.5, 20.0);
    glMatrixMode(GL_MODELVIEW);
}

int main(int argc, char** argv)
{
    glutInit(&argc, argv); //initialize toolkit
    glutInitDisplayMode(GLUT_SINGLE | GLUT_RGB); //set display mode: single buffering, RGB model
    glutInitWindowPosition(500, 150); //set window position on screen
    glutInitWindowSize(500, 500);
    glutCreateWindow(*argv); //open screen window

```



```
init();  
glutDisplayFunc(display); //points to display function  
glutReshapeFunc(reshape);  
glutMainLoop(); //go into perpetual loop  
return 0;  
}
```