

## ECE 214 — Final Exam

Estimated time for completion:  $\leq 2$  hour  
10 May 2018

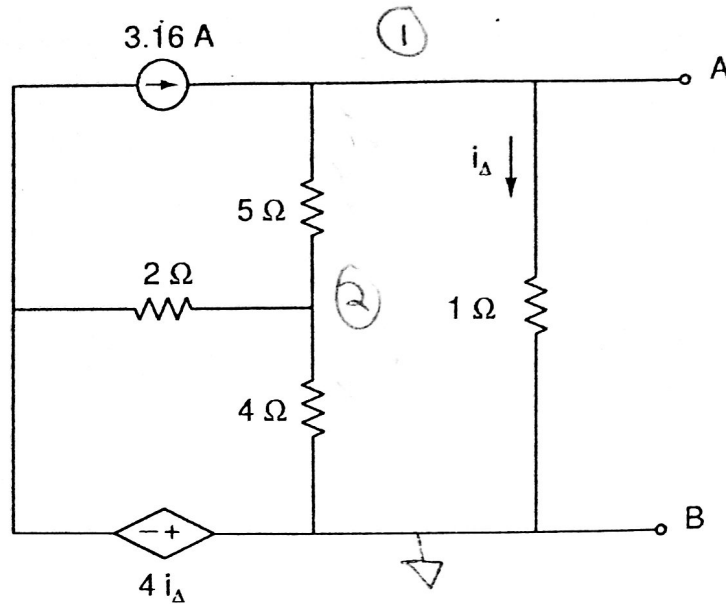
### Rules of the Exam

- Rule 1:** The examination period begins at 10:30 am on Thursday, 10 May 2018, and ends at 12:30 pm on Thursday, 10 May 2018.
- Rule 2:** The exam is worth 20 points.
- Rule 3:** There are three problems each worth seven points, plus one optional extra credit problem worth three points.
- Rule 4:** The exam is closed book and closed notes. You may use your ECE 214 Laboratory Notebook, a ruler, and a calculator.
- Rule 5:** To receive credit for an answer include the units along with the numerical answer.
- Rule 6:** Show all work - answers without supporting work will not receive credit.
- Rule 7:** Do not leave the room until you have completed the exam.

Spencer Goulette  
Name

$\frac{16}{20}$

Problem 1: Consider the circuit below:



Draw the Thévenin Equivalent Circuit with respect to terminals A and B.

$$V_1 - 3.16 + \frac{V_1 + 8.44V_1 + 7.022}{5} = 0$$

$$5V_1 - 15.8 + 9.44V_1 + 7.022 = 0$$

$$V_1 = 0.608 \text{ V}$$

$$V_2 = -12.2 \text{ V}$$

$$V_{TH} = 0.608 \text{ V}$$

KCL @ ①

$$\frac{V_1}{1} - 3.16 + \frac{V_1 - V_2}{5} = 0$$

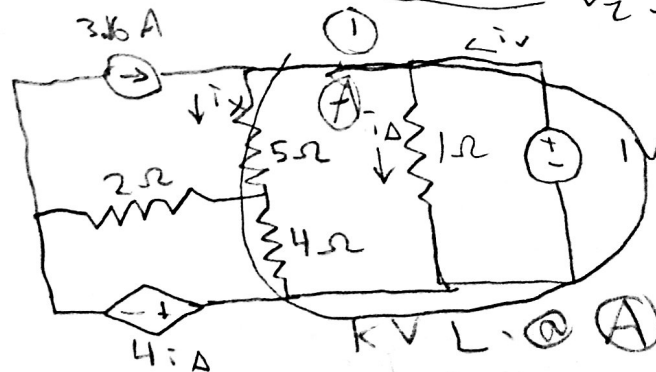
KCL @ ②

$$\frac{V_2 - V_1}{5} + 3.16 + 4V_1 + \frac{V_2}{4} = 0$$

$$-4V_1 + 4V_2 + 63.2 + 80V_1 + 5V_2 = 0$$

$$9V_2 + 76V_1 + 63.2 = 0$$

$$V_2 = -8.44V_1 - 7.022$$



Ohm's Law

$$\frac{1\text{V}}{1\Omega} = i_\Delta$$

$$i_\Delta = 1\text{A}$$

KCL @ ①

$$i_x + i_\Delta - i_v - 3.16 = 0$$

$$3.29 + 1 - i_v - 3.16 = 0$$

$$i_v = 1.13$$

KVL @ ①

$$1\text{V} = i_x 5\Omega + (i_x - 3.16 - 4)4$$

$$1\text{V} = 5i_x + 4i_x - 28.64$$

$$29.64 = 9i_x$$

$$i_x = 3.29\text{A}$$

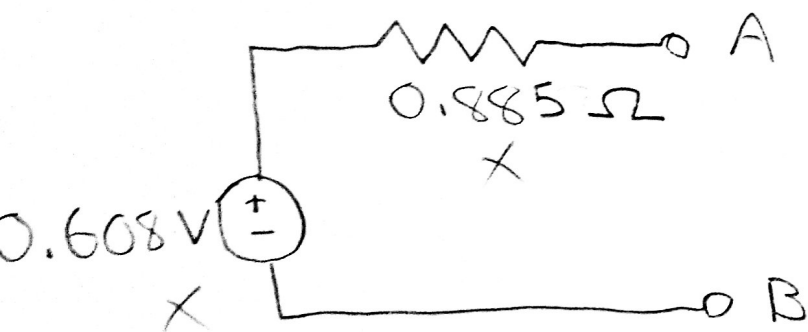
$$R_{TH} = \frac{1\text{V}}{1.13} = 0.885\Omega$$

DRAWING ON NEXT PAGE

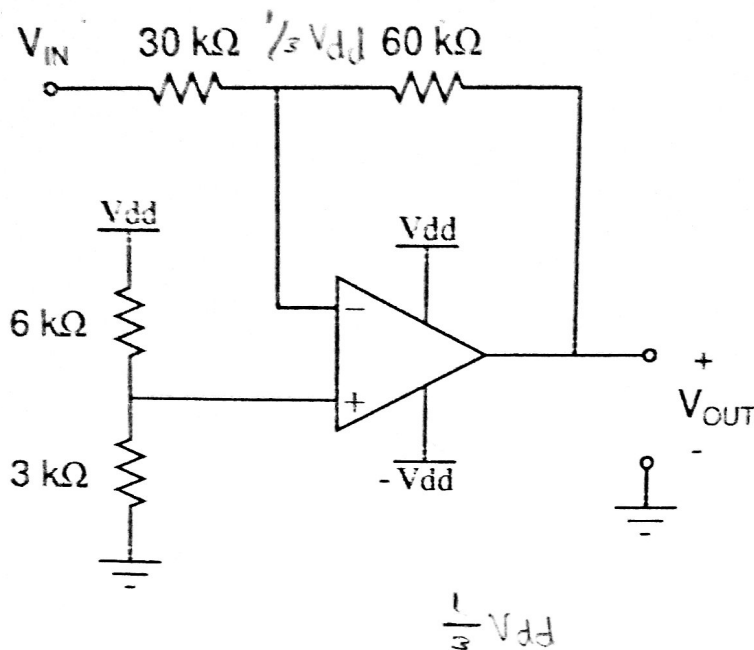
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Name: \_\_\_\_\_

Thévenin Equivalent Circuit



Assume the OpAmp is ideal with  $V_{dd} = 9\text{ V}$ .



1. What is the function of this circuit?

- ☒ (a) inverting amplifier with DC offset
- (b) non-inverting amplifier with DC offset
- (c) comparator
- ✓ (d) Schmitt trigger
- (e) inverting integrator
- (f) inverting integrator with DC offset

$$\frac{1/3 V_{dd}}{30\text{ k}} \cdot 90\text{ k}$$

$V_{dd}$

2.  $V_{IN}$  is a triangular waveform with 1 V peak-to-peak voltage and 4.5 V DC offset. What type of waveform is  $V_{OUT}$ ?

- (a) sinusoidal waveform
- (b) triangular waveform
- ✓ (c) triangular waveform with a DC offset
- (d) square waveform
- (e) square waveform with a DC offset
- ✓ (f) DC output equal to 0 V

$$\frac{1/3 V_{dd} + 3}{30\text{ k}} \cdot 90\text{ k}$$

$V_{dd} + 9\text{ V}$

3.  $V_{IN} = 0\text{ V}$ . What is  $V_{OUT}$ ? 9 V

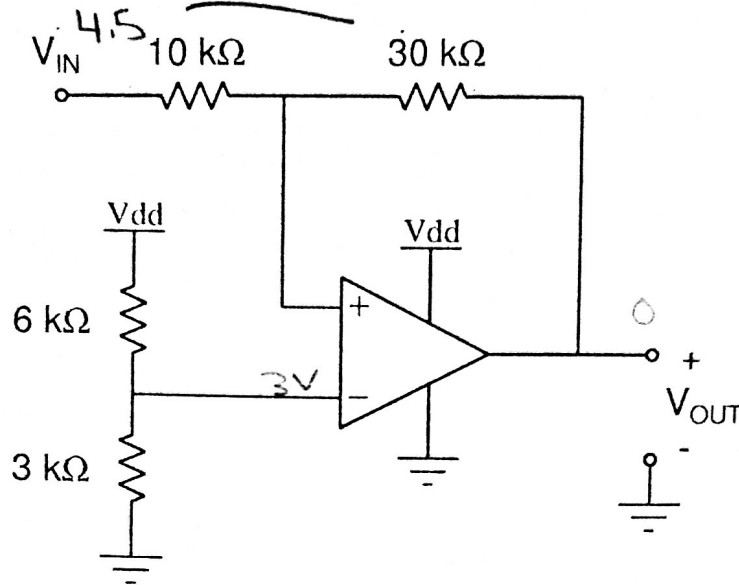
$$\frac{1/3 V_{dd} - 3}{30\text{ k}} \cdot 90\text{ k}$$

$V_{dd} - 9\text{ V}$

4.  $V_{IN} = -3\text{ V}$ . What is  $V_{OUT}$ ? 18 V

5.  $V_{IN} = 3\text{ V}$ . What is  $V_{OUT}$ ? 0 V

Assume the OpAmp is ideal with  $V_{dd} = 9\text{ V}$ .



6. What is the function of this circuit?

- (a) inverting amplifier with DC offset
- (b) non-inverting amplifier with DC offset
- (c) comparator
- ✓ (d) Schmitt trigger
- (e) inverting integrator
- (f) inverting integrator with DC offset

$$\frac{1}{3} V_{dd}$$

7.  $V_{IN}$  is a triangular waveform with 1 V peak to peak voltage and 0 V DC offset. What type of waveform is  $V_{OUT}$ ?

- (a) sinusoidal waveform
- (b) triangular waveform
- (c) triangular waveform with a DC offset
- (d) square waveform
- ✓ (e) square waveform with a DC offset
- ✓ (f) DC output equal to 0 V

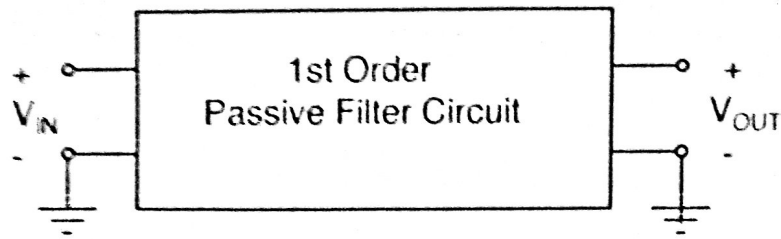
in order to be square waveform,  
input needs to be at least 4V

8. When  $V_{IN} = 0\text{ V}$ , what is  $V_{OUT}$ ? 0V

9. When  $V_{IN} = 4.5\text{ V}$ , what is  $V_{OUT}$ ?  $V_{dd}$

10. When  $V_{IN} = 9\text{ V}$ , what is  $V_{OUT}$ ?  $V_{dd}$

Problem 3: Consider the 1st order ideal passive filter circuit shown below:



For the questions below circle the most correct answer:

1.  $V_{IN}$  is a sine wave with a frequency of 150 kHz and a peak-to-peak voltage of 5 V.  $V_{OUT}$  is a sinusoidal waveform with a frequency of 150 kHz and a peak-to-peak voltage of 2 V. What type of filter could be used to generate  $V_{OUT}$ ?
  - (a) low pass filter
  - (b) high pass filter
  - (c) band reject filter
  - ☒ (d) all of the above
  - (e) none of the above
  
2.  $V_{IN}$  is a square wave with a 50% duty cycle, a frequency of 50 kHz, and a peak-to-peak voltage of 5 V.  $V_{OUT}$  that is a sinusoidal waveform with a frequency of 200 kHz and peak-to-peak voltage of 1 V? What type of filter could be used to generate  $V_{OUT}$ ?
  - (a) low pass filter
  - (b) band pass filter
  - (c) band reject filter
  - (d) high pass filter
  - ☒ (e) none of the above

3.  $V_{IN}$  is a square wave with a 50% duty cycle, a frequency of 50 kHz, and a peak-to-peak voltage of 10 V. The filter is a low pass filter with a cutoff frequency of 100 kHz. What is the relative amplitude of the 7th harmonic to the fundamental at the output of the filter?

- (a) -3.0 dB
- (b) -8.0 dB
- (c) -10.9 dB
- (d) -13.9 dB
- (e) -16.9 dB
- (f) -19.9 dB
- (g) -22.8 dB
- (h) -26.0 dB
- (i) -33.9 dB

(j) none of the above

$$f_{fund} : 0$$

$$filter : 0$$

$$f_{7th} : 20 \log\left(\frac{1}{7}\right)$$

$$filter : -20 \log\left(\frac{350k}{100k}\right)$$

$$relative\ amplitude : 20 \log\left(\frac{1}{7}\right) + -20 \log\left(\frac{350k}{100k}\right) = -27.8\text{ dB}$$

4.  $V_{IN}$  is a square wave with a 50% duty cycle, a frequency of 50 kHz, and a peak-to-peak voltage of 10 V. The filter is a low pass filter with a cutoff frequency of 50 kHz. What is the relative amplitude of the 7th harmonic to the fundamental at the output of the filter?

- (a) -3.0 dB
- (b) -8.0 dB
- (c) -10.9 dB
- (d) -13.9 dB
- (e) -16.9 dB
- (f) -19.9 dB
- (g) -22.8 dB
- (h) -26.0 dB
- (i) -33.9 dB

$$f_{fund} : 0$$

$$filter : -3$$

$$f_{7th} : 20 \log\left(\frac{1}{7}\right)$$

$$filter : -20 \log\left(\frac{350k}{50k}\right)$$

$$relative\ amplitude = 20 \log\left(\frac{1}{7}\right) - 20 \log\left(\frac{350k}{50k}\right) + 3 = -30.8\text{ dB}$$

... pretty sure it is **-30.8 dB**

5.  $V_{IN}$  is a square wave with a 50% duty cycle, a frequency of 50 kHz, and a peak-to-peak voltage of 10 V. The filter is a high pass filter with a cutoff frequency of 50 kHz. What is the peak amplitude of the 7th harmonic at the output of the filter?

- (a) -3.0 dB
- (b) -8.0 dB
- (c) -10.9 dB
- (d) -13.9 dB
- (e) -16.9 dB
- (f) -19.9 dB
- (g) -22.8 dB
- (h) -26.0 dB
- (i) -33.9 dB

$$f_{fund} : 0$$

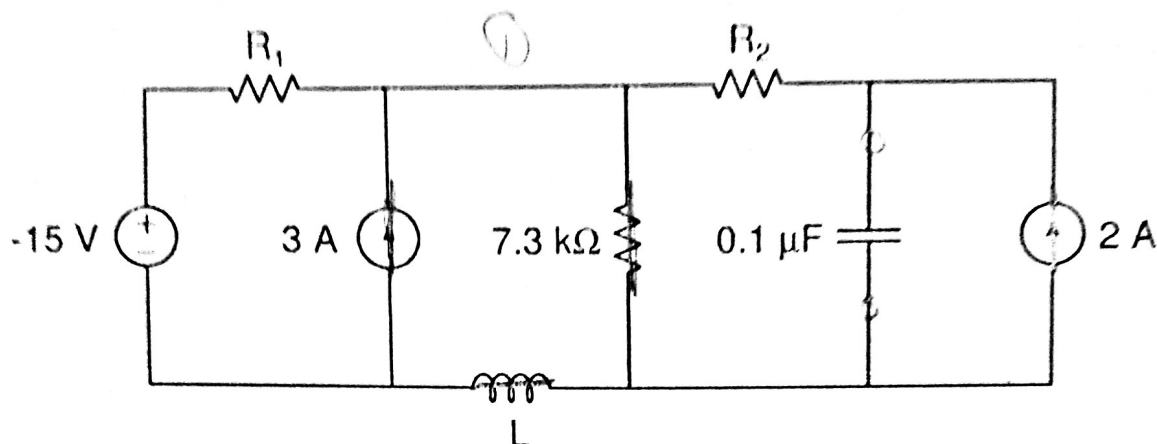
$$filter : -3$$

$$f_{7th} : 20 \log\left(\frac{1}{7}\right)$$

$$filter : 0$$

$$peak\ amplitude = 20 \log\left(\frac{1}{7}\right) = -16.9\text{ dB}$$

**Optional Bonus Problem** In the circuit below, the 3 A source delivers no power and absorbs no power. The circuit dissipates a total of 155 W of power and stores 0.1 mJ of energy.

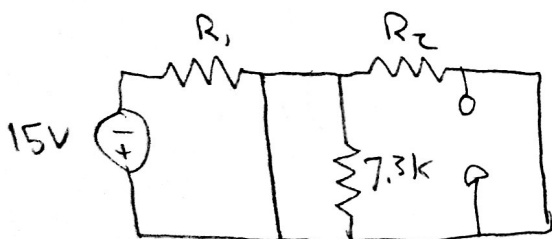


What are:

$$R_1 = 1.45 \Omega \quad \times$$

$$R_2 = 0 \Omega \quad \times$$

$$L = 50 \mu H \quad \times$$



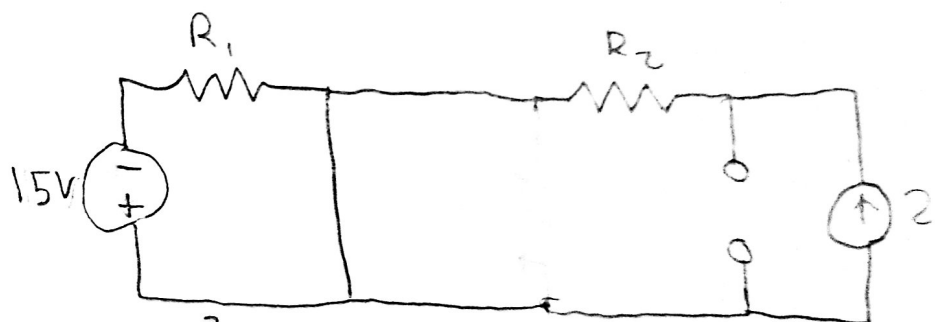
$$\frac{15^2}{R_1}$$

$$3A$$

KCL @ ①

$$-3A + \frac{V_1}{7.3k} + \frac{V_1 + 15}{R_1} = 0$$

$V_1$



$$P_{diss} = \frac{15^2}{R_1} + \frac{2^2}{R_2}$$

$$155 = \frac{225}{R_1} + \frac{4}{R_2} \Rightarrow R_1 = 1.45 \Omega$$

~~just picking a value for  $R_1$~~

$$155 = \frac{225}{3} + 4R_2$$

$$R_2 = 20$$

$$20 \cdot 2 = 40V$$

~~40V across capacitor~~

$$0.1 \cdot 10^{-3} = \frac{1}{2} C V^2 + \frac{1}{2} L I^2$$

$$0.1 \cdot 10^{-3} = \frac{1}{2} \cdot 0.1 \mu \cdot 40^2 + \frac{1}{2} \cdot L \cdot 2^2$$