

Name: Spencer Smalls

- Make sure you write your name on all pages.
- Detailed descriptions of how you solved the problem will get you maximum partial credit if your final answer is wrong.
- You must provide the correct unit along with your answer in the answer areas. An answer without its unit will be considered incorrect.
- You may only use FE exam approved, so called dumb calculators.
- A table of commonly used constants, parameters and equations is being distributed with the exam.
- Unless noted otherwise, assume room temperature conditions, i.e. $T = 300\text{K}$

Question	Grade	Out of
#1	16	20
#2	20	20
#3	15	15
#4	18	18
#5	15	15
#6	12	12
Total Grade	96	100

Choice of candy: Left Twix

Name: Spencer Grawlette

1. (20 points) Each correct answer is worth +2 points. Indicate if the following statements are True or False:

✓T A pn junction diode is a rectifying device.

✓F A p-type semiconductor has very few holes compared to electrons.

F The I-V characteristics of a pn junction diode are temperature independent.

F T Arsenic (As) is a group V element. It is an acceptor-type dopant in Si, which is a group IV element.

✓T A pn junction diode can be used to regulate voltage.

✓T The resistivity of a semiconductor is related to the drift current.

✓F The depletion region of a pn junction diode will shrink with increasing reverse bias.

F T A pn junction diode can be used to amplify an AC signal.

✓T The electronic properties of a semiconductor are temperature dependent.

✓T Diffusion current in a semiconductor is due to a gradient in the carrier concentration.



Name: Sponner, Caroline

2. Quick calculations (20 points). Each of the questions below are quick calculations, usually requiring a single equation.

- a. A Si diode conducts $I_F = 2$ mA when forward biased with $V_F = 0.7$ V. What is the forward bias voltage if the current decreases to $I_F = 1$ mA? $V_T = 26$ mV, and $\eta = 1$.

$$V_{F_{new}} = V_{F_{prev}} + 26 \ln\left(\frac{1 \text{ mA}}{2 \text{ mA}}\right)$$

$$V_F = \underline{0.682 \text{ V}}$$

- b. A pn junction diode with a built-in potential of $V_{bi} = 0.8$ V has a zero-bias capacitance of $C_{j0} = 2$ nF. What is its junction capacitance at a reverse bias voltage of 16 V?

$$C_j = \frac{C_{j0}}{\sqrt{1 + V_R/V_{bi}}} = \frac{2 \text{ n}}{\sqrt{1 + 16/0.8}}$$

$$C_j = \underline{436 \text{ pF}}$$

- c. What is the forward bias diffusion capacitance of a pn junction diode forward biased with $I_F = 10$ mA and a minority carrier lifetime $\tau = 260$ ns, operating at room temperature?

$$C_d = \frac{\tau}{V_T} I = \frac{260 \text{ ns}}{26 \text{ m}} 10 \text{ m} = 0.0000001$$

$$C_D = \underline{400 \text{ nF}}$$

- d. A p⁺n Si diode has $N_A = 2 \times 10^{18} \text{ cm}^{-3}$ and $N_D = 5 \times 10^{15} \text{ cm}^{-3}$. Calculate the built in potential, V_{bi} , at room temperature. $n_i = 10^{10} \text{ cm}^{-3}$, $V_T = 26$ mV

$$V_{bi} = V_T \ln\left(\frac{N_A N_D}{n_i^2}\right)$$

$$V_{bi} = \underline{838 \text{ mV}}$$

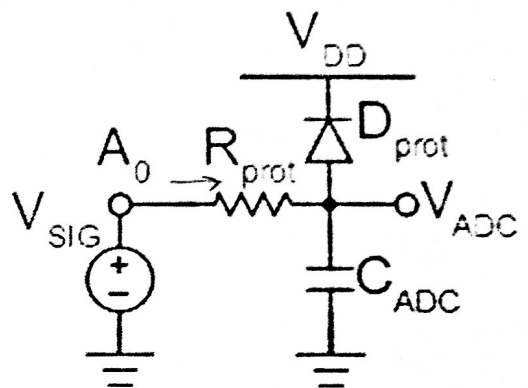
- e. What is the conductivity of an n-type Si sample which is doped with $N_D = 5 \times 10^{15} \text{ cm}^{-3}$? Take $\mu_n = 1200 \text{ cm}^2/\text{Vs}$ and $\mu_p = 450 \text{ cm}^2/\text{Vs}$.

$$\sigma = q(N_D \mu_n)$$

$$\sigma = \underline{0.96 \text{ } \Omega^{-1} \text{ cm}}$$

Name: Spencer Gault

3. (15 points) The input protection diode D_{prot} in the circuit below is used to limit the voltage at node ADC, representing the analog-to-digital converter of a microcontroller. The diode has $I_s = 1 \text{ nA}$ and an ideality factor of $\eta = 1.3$. The input protection resistor is $R_{\text{prot}} = 10 \text{ k}\Omega$. An external voltage source of $V_{\text{SIG}} = 7 \text{ V}$ is connected to the input pin A0 of the microcontroller. Calculate the voltage at node ADC, V_{ADC} . The supply voltage is $V_{\text{DD}} = 5 \text{ V}$.



$$I_{\text{max}} = \frac{7-5}{10 \text{ k}\Omega} = 200 \mu\text{A}$$

$$V_{D_{\text{prot}}} = V_T \ln\left(\frac{I}{I_s} + 1\right)$$

$$V_{D_{\text{prot}}} = 26 \text{ mV} \cdot 1.3 \ln\left(\frac{200 \mu\text{A}}{1 \text{ nA}} + 1\right)$$

$$V_{D_{\text{prot}}} = 0.4125 \text{ V}$$

$$I_{\text{guess}} = \frac{7-5-0.4125}{10 \text{ k}\Omega} = 159 \mu\text{A}$$

$$V_{D_{\text{prot}}} = 26 \text{ mV} \cdot 1.3 \ln\left(\frac{159 \mu\text{A}}{1 \text{ nA}} + 1\right)$$

$$V_{D_{\text{prot}}} = 0.405 \text{ V}$$

doing another iteration just to check

$$I_{\text{max}} = \frac{7-5-0.405}{10 \text{ k}\Omega} = 159.5 \mu\text{A}$$

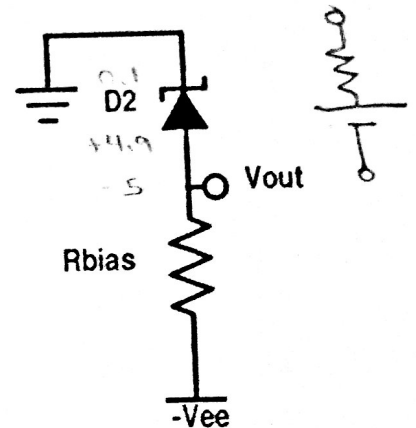
$$\text{so } V_{D_{\text{prot}}} \approx 405 \text{ mV}$$

$$V_{\text{ADC}} = 5 + 405 \text{ mV} = 5.405 \text{ V}$$

$$V_{\text{ADC}} = \underline{5.405 \text{ V}}$$

Name: Spencer Grubbs

4. (18 points) The voltage reference circuit below uses a Zener diode which conducts a current of $I_Z = 1 \text{ mA}$ when biased with $V_Z = 5 \text{ V}$, and has an equivalent resistance of $r_z = 100 \Omega$. The supply voltage is $-V_{cc} = -12 \text{ V}$.
- Calculate the equivalent voltage source V_{z0} of the Zener diode.
 - Calculate the required value of the bias resistor R_{bias} such that $V_{out} = -5.0 \text{ V}$.
 - Draw the equivalent circuit. Calculate V_{out} if the circuit is connected to a -15 V supply instead of a -12 V supply.



a.

$$V_{z0} = V_Z - I_Z r_z$$

$$V_{z0} = 5 \text{ V} - 1 \text{ mA} \cdot 100$$

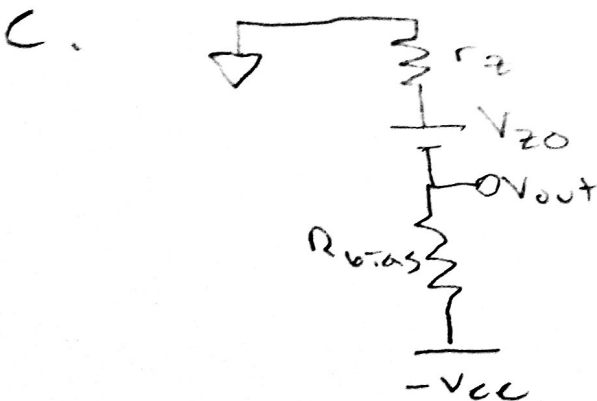
$$V_{z0} = 4.9 \text{ V}$$

b.

$$I_D = \frac{-4.9 - (-5)}{100} = 1 \text{ mA}$$

$$R_{bias} = \frac{-5 - (-12)}{1 \text{ mA}}$$

$$R_{bias} = 7 \text{ k}\Omega$$



$$\Delta V_{out} = \frac{r_d}{r_d + R_L} \Delta V_{supply}$$

$$\Delta V_{out} = \frac{100}{100 + 7\text{k}} (-3) = -0.0422$$

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$$V_{out} = -5 + -0.0422$$

$$V_{out} = -5.0422 \text{ V}$$

(a) $V_{z0} = 4.9 \text{ V}$

(b) $R_{bias} = 7 \text{ k}\Omega$

(c) $V_{out} = -5.0422 \text{ V}$

Name: Spencer Goulette

5. (15 points) An n-type Si cylindrical sample is doped with $N_D = 2 \times 10^{16} \text{ cm}^{-3}$. It has a diameter of $2r = 1 \text{ mm}$, and is $\ell = 10 \text{ mm}$ long. Use the following values: $n_i(300\text{K}) = 10^{10} \text{ cm}^{-3}$, $\mu_n = 1100 \text{ cm}^2/\text{Vs}$, and $\mu_p = 420 \text{ cm}^2/\text{Vs}$. Unit charge is $q = 1.6 \times 10^{-19} \text{ C}$.
- a) What is the conductivity of this sample, from the top surface to the bottom surface?
- b) A 1 V bias voltage is applied between the top and bottom surfaces. Calculate the current flowing through the sample.

a. $N_D \gg N_A$

$$\sigma = q(N_D \mu_n)$$

$$\sigma = 1.6 \cdot 10^{-19} \cdot 2 \cdot 10^{16} \cdot 1100$$

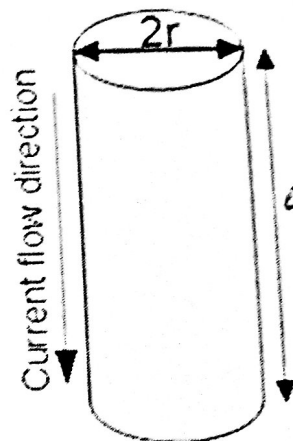
$$\sigma = 3.52 \frac{1}{\Omega \cdot \text{cm}}$$

b. $R = \frac{1}{\sigma} \frac{\ell}{A}$

$$R = \frac{1}{3.52} \frac{1}{\pi (0.05)^2}$$

$$R = 36.2 \Omega$$

$$I = \frac{1}{36.2 \Omega} = 27.6 \text{ mA}$$



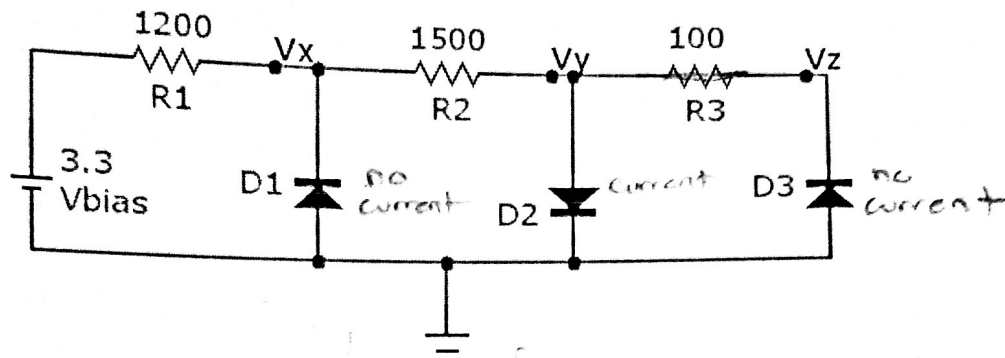
(a) σ $3.52 \frac{1}{\Omega \cdot \text{cm}}$

(b) I 27.6 mA

Name: Spencer Gault

Oct. 26, 2018

6. (10 points) Three identical diodes are used in the circuit in the figure. The only known fact about the diodes is that $I_D = 1 \text{ mA}$ at $V_D = 0.6 \text{ V}$. Calculate the three node voltages, V_x , V_y , V_z if $V_{\text{bias}} = 3.3 \text{ V}$. Explain your reasoning.



$V_y = V_z$ cause no current through 100- Ω resistor.

Assume $V_D = 0.6 \text{ V}$
and current $I_D = 1 \text{ mA}$,

$$\text{so } 3.3 = I_D \cdot 1200 + I_D \cdot 1500 + V_D \quad \text{KV}$$

$$3.3 = 1.2 \text{ V} + 1.5 \text{ V} + 0.6 \text{ V}$$

$$\boxed{V_y = V_z = 0.6 \text{ V}} \quad \text{since diode volt.}$$

$$V_x = 1.5 \text{ V} + 0.6 \text{ V}$$

$$\boxed{V_x = 2.1 \text{ V}}$$

$$\begin{array}{l} V_x \underline{2.1 \text{ V}} \\ V_y \underline{0.6 \text{ V}} \\ V_z \underline{0.6 \text{ V}} \end{array}$$