

Discussion 3: Algorithm V1 & Experiment on Cases

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Algorithm Version 1

Algorithm 1 Algorithm Version1: Learn Multiphase RF Incrementally

Require: Loop L , depthBound db

Ensure: $\text{result} \in \{\text{FIN}, \text{INF}, \text{UNKNOWN}\}$, a list of RFs rf_list

```
1:  $i := 0, \text{result} := \text{UNKNOWN}, \text{rf\_list} := []$ 
2: while  $i < db$  and  $\text{result} == \text{UNKNOWN}$  do
3:    $\text{result}, \text{rf} = \text{LearnRankerBounded}(L)$ 
4:   if  $\text{result} == \text{INF}$  or  $\text{result} == \text{FIN}$  then
5:      $\text{rf\_list.append}(\text{rf})$ 
6:     return  $\text{result}, \text{rf\_list}$ 
7:   else
8:      $\text{result}, \text{rf} = \text{LearnRankerNoBound}(L)$ 
9:      $\text{rf\_list.append}(\text{rf})$ 
10:  end if
11:   $L = \text{ConjunctConstraint}(L, \text{rf})$ 
12:   $i += 1$ 
13: end while
14: return  $\text{UNKNOWN}, \text{rf\_list}$ 
```

Case 1: Multiphase

Example

while($x > 0$ or $y > 0$) do $x' = x + y - 1$; $y' = y - 1$

is a loop ranked by 2-phase multiphase ranking function: $\langle y, x \rangle$

Result of the algorithm: $\langle 0.9971y, 0.639x + 0.6774 \rangle$

```
-----START INCREMENTAL LEARNING-----
-----INCREASE TIMES: 0
-----LEARN BOUNDED
Failed to prove it is terminating

-----LEARN UNBOUNDED
Found Ranking Part: 0.9971 * x[1]^1

-----INCREASE TIMES: 1
-----LEARN BOUNDED
Found Ranking Function: 0.639 * x[0]^1 + 0.6774 * 1

-----LEARNING MULTIPHASE SUMMARY-----
MULTIPHASE DEPTH: 2
LEARNING RESULT: FINITE
-----RANKING FUNCTIONS-----
0.9971 * x[1]^1
0.639 * x[0]^1 + 0.6774 * 1
```

Case 2: Multiphase plus Branch

Example

while($x > 0$ or $y > 0$) do

If $y > 0$: $x' = x$; $y' = y - 1$; else: $x' = x - 1$; $y' = y$;

is a loop with 2-phase multiphase ranking function $\langle y, x \rangle$

Use template $ax + by + c$ to run:

```
-----LEARNING MULTIPHASE SUMMARY-----  
MULTIPHASE DEPTH: 4  
LEARNING RESULT: UNKNOWN  
-----RANKING FUNCTIONS-----  
0.992 * x[0]^1 + 0.9955 * x[1]^1  
0.9756 * x[0]^1 + 0.9756 * x[1]^1  
0.9756 * x[0]^1 + 0.9756 * x[1]^1
```

where the learn unbound part always generating $x + y$ as a decreasing function.

Way to solve the problem

Try a different template when learning failed.

If we try $by + c$ as the first template and $ax + by + c$ as the second:

```
-----LEARNING MULTIPHASE SUMMARY-----  
MULTIPHASE DEPTH: 2  
LEARNING RESULT: FINITE  
-----RANKING FUNCTIONS-----  
1.0 * x[1]^1  
0.9804 * x[0]^1 + 0.6667 * 1
```

We have to modify our algorithm to by adding back-tracking to try different templates when we fail to learn a ranking function out.

Case 3: Split Technique

Example

`while($x > 0$ or $y > 0$) do $x' = x + y; y' = y - 1$`

This is a false example for multiphase ranking function $\langle y, x \rangle$ for when $y < 0$

$$x - x' = -y > 0$$

not δ .

By setting the conjuncted formula to $y < -0.1, -y > 0.1$. The multiphase ranking function is $\langle y + 0.1, x \rangle$

Case 4: Not all cases can be solved

Example

`while($x \geq 1$ and $y \geq 1$ and $x \geq y$ and $2^B y \geq x$) do`
 `$x' = 2x; y' = 3y$`

According to "On Multiphase" paper, this loop has a multiphase ranking function:

$$\langle x - 2^B y, x - 2^{B-1} y, \dots, x - y \rangle$$

We ran a experiment on $B = 2$. But failed to learn the RF out.

```
-----LEARNING MULTIPHASE SUMMARY-----  
MULTIPHASE DEPTH: 5  
LEARNING RESULT: UNKNOWN  
-----RANKING FUNCTIONS-----  
- 0.1905 * x[0]^1 - 0.3809 * x[1]^1  
- 0.1905 * x[0]^1 - 0.3809 * x[1]^1  
- 0.1905 * x[0]^1 - 0.3809 * x[1]^1  
- 0.1905 * x[0]^1 - 0.3809 * x[1]^1
```

Reason: the first guess is incorrect.

Algorithm Version 2

Algorithm 2 Algorithm Version2: Learn Multiphase RF Backtracking

Require: Loop L , depthBound db , templateList $tpList$

Ensure: $result \in \{FIN, INF, UNKNOWN\}$, a list of RFs rf_list

```
1:  $i = 1$ 
2: while  $i \leq db$  and  $result == UNKNOWN$  do
3:    $rf\_list = []$ 
4:    $result, rf\_list = \text{train\_backtracking\_loopbody}(L, rf\_list,$ 
      $tpList, 0, 1, i)$ 
5:   if  $result \neq UNKNOWN$  then
     return  $result, rf\_list$ 
6:   end if
7: end while
```

Algorithm Version 2 Continue

Algorithm 3 Algorithm Version2: Learn Multiphase RF Backtracking

```
train_backtracking_loopbody( $L$ , rf_list, tpList, tempId,  
currentDepth, maxDepth):
```

Use dfs to learn multiphase ranking function, if for one layer the learning result is UNKNOWN, backtrack one depth and change the template.

TODOs

- ▶ Implement the algorithm that extract guard to be the ranking function.
- ▶ Find more cases and explore the advantage of our methods, and do some large scale experiment.