NLP - Assignment#1 Yuqian Zhang

(a) What is the cosine similarity of D1 and D2, not using idf weighting? Solution: By using the common choice:

$$sim(A,B) = \frac{\sum_{i} a_{i} \times b_{i}}{\sqrt{\sum_{i} a_{i}^{2}} \times \sqrt{\sum_{i} b_{i}^{2}}}$$

$$sim (D1,D2) = (2*2+1*0+0*1)/5 = 4/5$$

idf1 = log(2/2) = 0

(b) What is the cosine similarity if idf weighting is used? Solution:

$$\begin{aligned} & \text{idf2=log(2/1) = 1} \\ & \text{idf3=log(2/1) = 1} \\ & \text{D1:} \end{aligned} \qquad & \text{D2:} \\ & \text{w1= tf1 *idf1 = (2)*0=0} \\ & \text{w2= tf2 *idf2 = (1)*1=1} \end{aligned} \qquad & \text{w2= tf2 *idf2 = (0)*1=0} \\ & \text{w3= tf3 *idf3 = (0)*1=0} \end{aligned}$$

$$(d1,d2) = \frac{\sum (wd1(j)*wd2(j))}{\sqrt{\sum wd1(j)^2}*\sqrt{\sum wd2(j)^2}}$$

Applying all data in D1 and D2 to the formula above, sim (D1,D2)=(0+0+0)/((1)*(1))=0

```
(c) D3= [meow squeak] added
Solution:
   D1 = [woof woof meow]
   D2 = [woof woof squeak]
   D3= [meow squeak]
  W = [woof meow squeak] (n=3)
  V1 = [ 2, 1, 0 ]
  V2 = [ 2, 0, 1 ]
  V3 = [ 0, 1, 1 ]
  idf1=log(3/2)
   idf2 = log(3/2)
   idf3 = log(3/2)
D1:
w1 = tf1 * idf1 = (2) * log(3/2)
w2 = tf2 * idf2 = (1)* log(3/2)
w3 = tf3 * idf3 = (0)* log(3/2)=0
D2:
w1 = tf1 * idf1 = (2)* log(3/2)
w2 = tf2 * idf2 = (0)* log(3/2)=0
w3 = tf3 * idf3 = (1)* log(3/2)
D3:
w1 = tf1 * idf1 = (0) * log(3/2) = 0
w2 = tf2 * idf2 = (1)* log(3/2)
w3 = tf3 * idf3 = (1)* log(3/2)
(d1,d2) = \frac{\sum (wd1(j)*wd2(j))}{\sqrt{\sum wd1(j)^2}*\sqrt{\sum wd2(j)^2}}
```

Applying all data in D1,D2,D3 to the formula above, sim (D1,D2)= $(4*(\log(3/2)^2)/(5*\log(3/2)^2)=4/5$ sim (D1,D3)= $(1*(\log(3/2)^2)/(10^{1/2}*(\log(3/2)^2)=1/10^{1/2}$ sim (D2,D3)= $(1*(\log(3/2)^2)/(10^{1/2}9*((\log(3/2)^2)=1/10^{1/2})$

6.1 Assume the following likelihoods for each word being part of a positive or negative movie review, and equal prior probabilities for each class.

| | pos | neg |
|---------|------|------|
| I | 0.09 | 0.16 |
| always | 0.07 | 0.06 |
| like | 0.29 | 0.06 |
| foreign | 0.04 | 0.15 |
| films | 0.08 | 0.11 |

What class will Naive bayes assign to the sentence "I always like foreign films."?

Solution:

Set test sentence S = " I always like foreign films"

 $P(-)P(S|-) = \frac{1}{2} *0.16*0.06*0.06*0.15*0.11 = 4.75*10^{-6}$

 $P(+)P(S|+) = \frac{1}{2}*0.09*0.07*0.29*0.04*0.08=2.92*10^{-6}$

The model thus predicts the class negative for the test sentence.

- **6.2** Given the following short movie reviews, each labeled with a genre, either comedy or action:
 - 1. fun, couple, love, love comedy
 - 2. fast, furious, shoot action
 - 3. couple, fly, fast, fun, fun comedy
 - 4. furious, shoot, shoot, fun action
 - 5. fly, fast, shoot, love action

and a new document D:

fast, couple, shoot, fly

compute the most likely class for D. Assume a naive Bayes classifier and use add-1 smoothing for the likelihoods.

Solution:

| Cat | Documents |
|-----|-----------------------------|
| С | fun, couple, love, love |
| С | couple, fly, fast, fun, fun |
| Α | fast, furious, shoot |
| Α | furious, shoot, shoot, fun |
| Α | fly, fast, shoot, love |
| | C C |

Test ? fast, couple, shoot, fly

The prior P(c) for the two classes:

$$P(C) = 2/5$$
 $P(A) = 3/5$

$$P("fast" | C) = (1+1)/(9+7) \qquad P("fast" | A) = (2+1)/(11+7) \\ P("couple" | C) = (2+1)/(9+7) \qquad P("couple" | A) = (0+1)/(11+7) \\ P("shoot" | C) = (0+1)/(9+7) \qquad P("shoot" | A) = (4+1)/(11+7) \\ P("fly" | C) = (1+1)/(9+7) \qquad P("fly" | A) = (1+1)/(11+7)$$

$$P(C)P(S|C) = (2/5)*(2*3*1*2)/16^4 = 7.324*10^(-5)$$

$$P(A)P(S|A) = (3/5)*(3*1*5*2)/18^4 = 17.147*10^{-5}$$

The model thus predicts the class 'Action' for the test sentence.

| Q3. | |
|---|--|
| Sentence: Seeking sentence Seeking np Seeking n Seeking art Found art = The Seeking n Seeking art Found art = The Seeking adj Found adj = old Seeking n Found n = cat Found np = The old cat Seeking vp Seeking v Found v = chases Found vp = chases Found sentence = The old cat chases Seeking v Found v = chases Found r Seeking v Found r Found n = mouse | The old cat chases mouse. + + + + + + + ==== |
| Found np = mouse | ==== |
| Found vp = chases mouse | ========= |
| Found sentence = The old cat chases | mouse |
| Seeking art | + |
| Seeking art | + |
| 0 parse(s) obtained | |
| · | |
| Seeking sentence Seeking np Seeking n Seeking art Found art = My Seeking n | My rabbit is jumping. + + + + + + + + === |