

3. Big-O notation

• $O(1)$ $O(5)$ $O(2/N)$

$O(\log N)$

$O(\sqrt{N})$

$O(N)$

$O(N \log N)$

$O(N^{1.5})$

$O(N^2)$ $O(NM)$

$O(N^4)$

$O(2^N)$

$O(\infty)$

• i. $\text{sum} = 0;$

$\text{for } (i=0; i < n; i++)$
 (n times) 1 time n+1 times n times

$\text{sum}++;$

$2n+2$

$$T(n) = \frac{2n+2}{+n} = 3n+2$$

★

complexity is $O(n)$

• $f(n) > T(n)$ for all $n > n_0$

• $n > 3n+2$

$c > 3 + \frac{2}{n}$; set $n_0 = 1$

$c = 3 + \frac{2}{1} = 5$

5. $f(n) > T(n)$ for all $n > 1$

Not
Necessary

ii.

$\text{for } (i=0; i < n; i++)$
 (n times) 1 time n+1 times n times

$2n+2$

$\text{for } (j=0; j < n; j++)$
 (n² times) 1 time n+1 times n times

$2n^2+2n$

$\text{sum}++;$

$$\frac{2n^2+2n}{+n^2} = 3n^2+4n+2$$

★

complexity is $O(n^2)$