

Hybrid Quantum Computing

Phys 309: Quantum Computing

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Good stories have a good beginning!



The founding members (fathers and mother) of quantum science

Image taken during one of the Solvay conferences, when quantum theory was still an infant

but...

Was this story a good one?

Confusion:

Bohr Vs Einstein

Heisenberg Vs Schrodinger

World war...

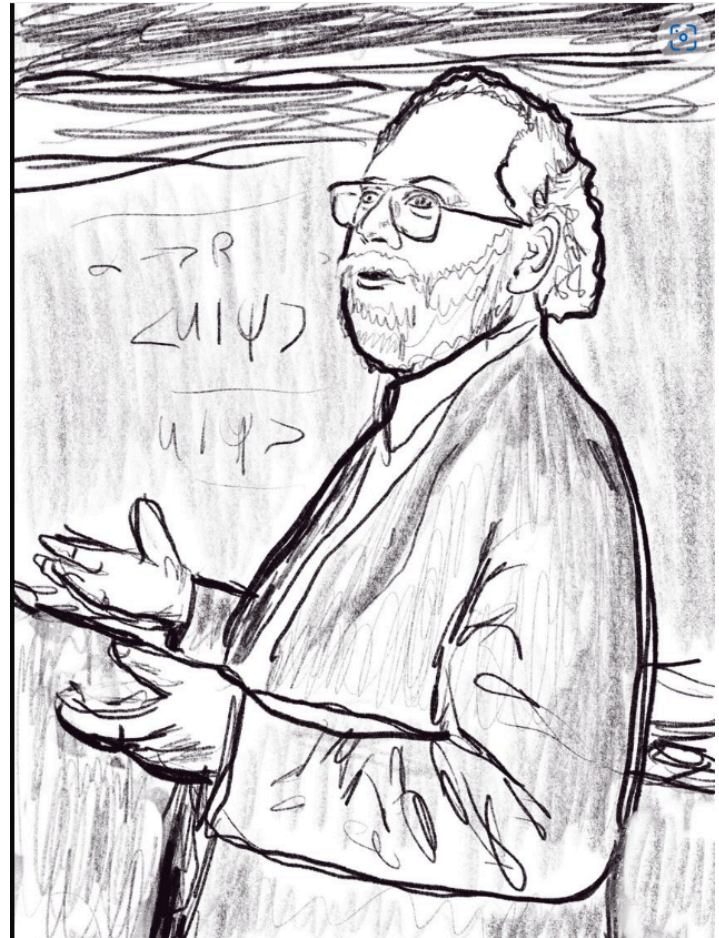
Overall, no large public interest...

1994

Peter Shor

Discrete log algorithm

AKA Shor's factoring algorithm



1995



Groover Search Algorithm

Potential usecase in everyday life and general computer science algorithms

More people's interest aroused

not so fast ...

Decoherence and noise (Shor 1997)

TBT: Back to the 80's and early 90's

R. P. Feynman, Seth Lloyd

Quantum simulation

Ideas on how to circumvent noise and decoherence

Quantum Algorithms skyrocketed

Up until now ...

Realizing quantum computation proves to be hard due to interaction with environment

Remedy??

NISQ era: Combine Quantum and Classical Algorithms

That's where we come into the scene

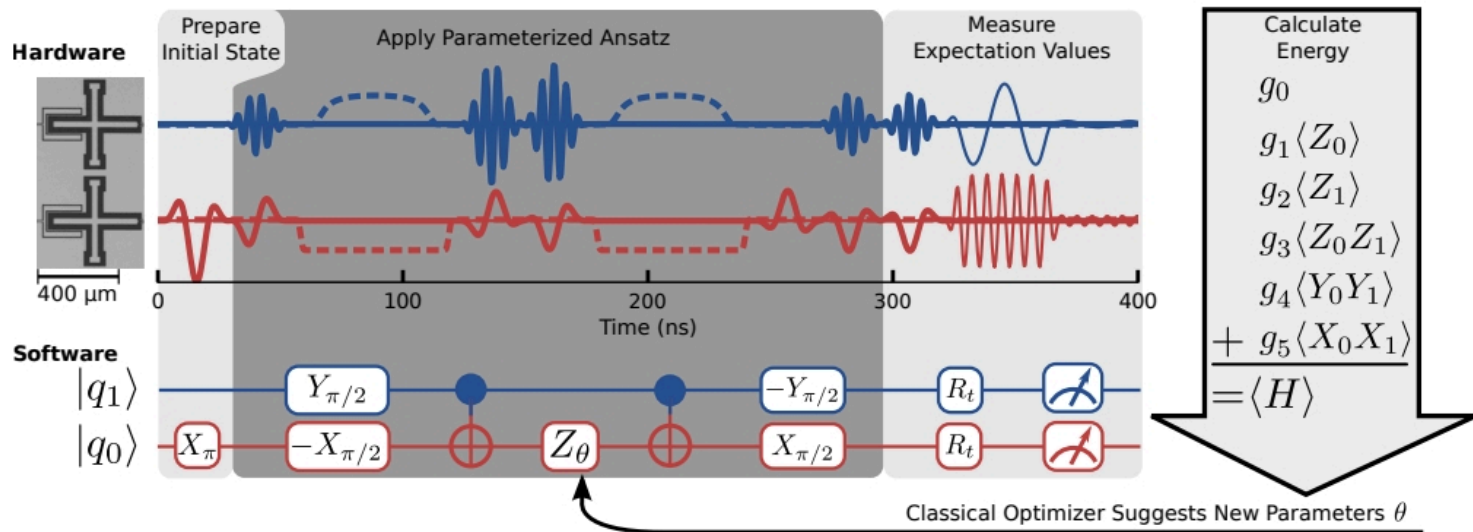
My final paper focuses on this part

Algorithm 1 Hardware-efficient optimization of quantum Hamiltonian problems

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1: Map the quantum Hamiltonian problem to a qubit Hamiltonian  $H$ 
2: Choose a depth  $d$  for the quantum circuit that prepares the trial state
3: Choose a set of variational controls  $\vec{\theta}_1$  that parametrize the starting trial state
4: Choose a number of samples  $S$  for the feedback loop and one  $S_f$  for the final estimation
5: Choose a number of maximal control updates  $k_L$ 
6: while  $E_f$  has not converged do
7:   procedure QUANTUM FEEDBACK LOOP
8:     for  $k = 1$  to  $k_L$  do
9:       Prepare trial states around  $\vec{\theta}_k$  and evaluate  $\langle H \rangle$  with  $S$  samples
10:      Update and store the controls  $\vec{\theta}_k$ 
11:    end for
12:    Evaluate  $E_f = \langle H \rangle$  using the best controls with  $S_f$  samples
13:  end procedure
14:  Increase  $d, k_L, S, S_f$ 
15: end while
16: return  $E_f$ 
```

Abhinav Kandala et al (2017)

A visual representation coming up ...

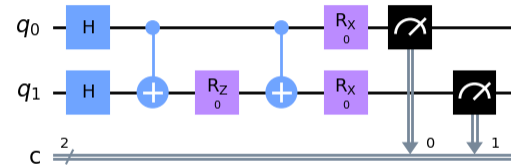


P. J. J. O'Malley et al (2017)

- Hardware (micrograph <- two Xmon transmon qubits):
 - Single qubit rotation performed using microwave pulse sequences
 - DC pulse for two-qubit entangling gates
 - Microwave spectroscopy tones for qubit measurements
- Software
 - Preparation of a Hartree-Fock state
 - Apply unitary coupled cluster ansatz
 - Apply efficient partial tomography to measure the expectation values

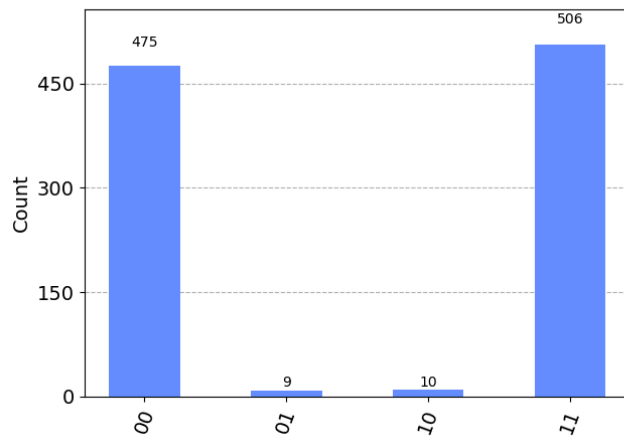
Compute total energy from measurements and provide the result to a classical optimizer to determine the new parameters, repeat b and c till you get optimal results.

Simple modified set-up



Pauli Z matrices used to represent cost hamiltonian, Pauli X matrices used to represent mixing hamiltonian

These gates combined to form circuit shown



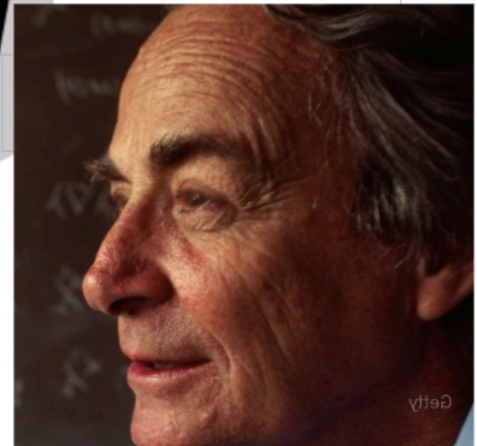
Our algorithm works for a simple case of using Pauli X and Pauli Z to represent our hamiltonian. Again, with different hamiltonians, the expectation is that the algorithm still works but more thought needs to be put in the encoding of data.

A realization of this simple model may be done using ion traps, which provide well defined hamiltonians that can be used to describe the system. This choice gets rid of the disadvantage associated with cooling resources thus bringing us nearer and nearer to quantum computing/simulation actualization.

With more research into decoherence and physical realization of quantum systems, the potential of scalability might be attained. A drawback, however, is that some hamiltonians may take a longer time to minimize, thus making things hard when the simulation involves a bigger number of parameters for these complicated hamiltonians, even with the physical realization available to us.

Final word...

Quantum simulation will give us the ability to explain quantum phenomena, staying consistent with all the known facts and suggest new facts that are yet to be explained.



With these quantum algorithms in place and future discovery of better ways to realize quantum computation, we will eventually realize this idea.

References

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