

Optimising SKA1-Mid Scale-Dependent Sensitivity

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Abstract

In this report we study the scale dependent sensitivity of the SKA1-Mid baseline design. We also propose changes to the baseline design that enhance the sensitivity at smaller angular scales (e.g. 0.4-1 arcsec at 650MHz) without compromising the performance at larger scales. The changes we propose are guided by the SKA1-Mid level-zero science requirements [2], which suggest that very long baselines ($> 150\text{km}$) are not necessary to achieve the SKA1-Mid science objectives. In particular, we show that a 254 dish layout with a maximum baseline of 120km improves the SKA1-Mid survey speed by more than 55% and is 3.5 times faster than SKA-SUR (see Table 10) on angular scales 0.4-1 arcsec (over 650-1000MHz), without compromising the performance at larger scales. Such an improvement on these scales could be transformational for other sciences, such as cosmology with weak lensing. Furthermore, this layout spans significantly less space which could potentially reduce trenching and data transport costs. We also show that with a conservative addition of 12 dishes the SKA1-Mid survey speed can be improved by up to 67% on the smaller angular scales.

1 Introduction

The SKA at mid frequencies (SKA-Mid) will be built in two phases, SKA-Mid phase one (SKA1-Mid) and phase two (SKA2-Mid) in South Africa, and SKA-SUR in phase 1 in Australia. The key science goals for SKA1-Mid include the study of the history and role of neutral hydrogen in the Universe from the dark ages to the present-day, the use of pulsars as probes of fundamental physics [1] and continuum and HI surveys to pin down the cosmological model. The large emphasis on key science projects is outlined in several SKA memos, as the baseline design has emerged. It should however be noted that changes which do not compromise the key science cases are possible and such changes could be transformational for other science cases.

In this document, we attempt to gauge the scale-dependent sensitivity of the mid-frequency array described in the *SKA1 System Baseline Design* (BD) document [1]. The performance of this configuration is then compared to two alternative configurations.

The rest of this document is laid out as follows: in subsection 1.2 we discuss the science requirements for SKA1-Mid, then in subsection 1.3 we describe the layouts that we consider. In section 2 we describe our simulation techniques and the metrics we generated from the experiment. Finally, the results and concluding remarks are in section 3.

1.1 SKA1-Mid Baseline Design

The mid-frequency array described in the BD is a 254 dish array with about 36% of the dishes within a radius of 400m (core), 40% of the dishes are between 400m and 4km (outer-core) with the remaining 24% in 3 three spiral arm-like structures starting from about 2km and stretching out to a radius around 100km. Figures 1 and 2 show the BD layout and baseline distribution histogram (\log_{10} space). With about 200 fifteen metre dishes (bar the 64 13.5 metre MeerKAT dishes) within a radius of 4km, this array promises high sensitivity, with noise values around $63\mu\text{Jy beam}^{-1} \text{ hr}^{1/2}$ [1]. However, with three distinct dish-density regions, the resulting full sensitivity (natural weighting) point spread function (PSF) has two pedestals corresponding to the abrupt changes in dish densities from the core to the outer-core and from the outer-core to the spiral arms (see Appendix A). With such a configuration, a uv-weighting that tends towards uniform is required to obtain high resolution and uv-tapering might be also be required to get a well behaved PSF. Leading to significantly lower sensitivity due to the down-weighting of baselines¹. It is therefore important to quantify the scale-dependent sensitivity of this configuration,

¹uniform uv-weighting down-weights the uv-points corresponding to shorter baselines, and hence gives better resolution, while a uv-taper down-weights the edges of the uv-coverage (longer baselines) to decrease sidelobe levels

i.e., what is the sensitivity at different angular scales.

1.2 SKA1-Mid science requirements

In this subsection we outline the scientific rationale for a change in the baseline design, which we believe is as cost neutral as possible given the information we received from the SKA office and which gives a direction which is different for the configuration of SKA-MID. We have based the propositions in this document upon the assessment workshop for the Cosmology working group where extensive discussion have taken place with the pulsar and transient senior scientists, along with direct communication with the Continuum Science SWG, plus several informal discussions between the Cosmology members and the HI/continuum members.

1.2.1 Highlights of requirements of each science area

Pulsar science: the pulsar search science is mainly dependent on the core of SKA-MID. One of the key factor being the instantaneous sensitivity which depends on the number of antennas in the core. Furthermore if the antennas are moved out of the core, the synthesised beam would be reduced which increases the pulsar search time. During the discussions in the SWG, it was our understanding that an increase of the core area of around 10% would be a minor perturbation in the overall pulsar search, although one in which computation costs increase (see Pulsar SWG for more details).

Cosmology: in what concerns the baseline distribution in this document we have four aspects which we would like to highlight: Cosmology with continuum and HI galaxy surveys, weak gravitational lensing and intensity mapping.

- **Cosmology with HI surveys:** The key requirement for HI surveys for cosmology is to have a large survey speed coupled with baselines which do not resolve out the flux of the galaxies being observed. Given the sizes of galaxies and the fact that we would like a significant amount of the flux not to be resolved out, the baselines of most interest are baselines below around 5km. Hence an outer core is the most important aspect of a telescope for such science. However losing a small amount of sensitivity compared to the baseline design in this region of uv space is not critical and was discussed at the Cosmology science assessment workshop, and in fact we find that we do not lose any sensitivity in this regime for our preferred configuration.
- **Cosmology with weak lensing:** Here the main aspect is a high sensitivity at scales which can measure the structure and shape of the galaxies in continuum. Given the size of galaxies, this requires significant sensitivity at scales which correspond to 0.5 to 1 arcsec. The current baseline design has a natural sensitivity very close to the JVLA at the scales of interest, something that will only damage the scientific reputation of the SKA. For these reasons having a larger number of antennas in the spiral arms out to around 70-80 km is beneficial for this science and the lack of those baselines would simply make such a survey unfeasible. Such studies also have to be done with SKA-MID as SKA-SUR does not have enough antennas to produce reliable maps as the number of UV tracks is much lower than SKA-MID. This is intrinsically due to the fact that the sensitivity of SKA-SUR is coming from PAFs and not from extra collecting area.
- **HI and continuum morphologies:** In the current baseline design there is a lack of sensitivity in the baselines which one would need to study morphologies of the detected continuum and HI galaxies. The baselines needed for morphological studies of galaxies are similar to the baselines needed for the weak lensing experiment with weak lensing, and therefore should be advantageous for galaxy evolution studies which are central to the goals of the HI and Continuum SWGs.
- **Cosmology with intensity mapping surveys:** Intensity mapping requires very short baselines and would benefit from having several clusters of antennas placed either in the core or in the outer core. This arrangement is not incompatible with the configuration proposed here and is briefly discussed below.

1.2.2 General rationale

Cost Neutral proposal: We propose here a baseline change outlined in this document. The scientific rationale is that baselines larger than $\sim 80 - 90$ km are expensive given that the signal needs significant boosting to reach the main correlator, and the extra trenching and the key fact that none of the main science goals are directly affected by a modest reduction of the maximum baseline (the science case that we believe to have the most stringent requirement for high resolution is the 40mas at ν 14GHz for the Cradle of Life) . This cost saving should allow for extra antennas to be placed in the spiral arms. We have estimated (after informally enquiring with individuals at the SKA office) this cost saving to allow for an extra 12 antennas.

We also note here that we have assumed an approximate cost neutrality for the SKA-Mid in isolation. If we were to consider a solution where the whole of the mid-frequency SKA1 as cost neutral (i.e. not interfering

with SKA-Low baseline costing) then a significant number of additional dishes could be distributed within our proposed configurations which would substantially increase the imaging capability, the survey speed and the sheer volume of science that could be carried out with the SKA at mid-frequencies, but which could not be carried out with a separate site solution for SKA-Mid. We assume such studies will be incorporated into the new science case for the SKA, but do not consider them here.

A proposal that should be encompassing of all science cases: The rationale that the array has significant UV coverage all the way up to 70-80 km baselines to cover the above science cases would suggest a smooth transition from the core to the outer core to the spiral arms. This is obtained by a slight puffing up of the core as suggested it be possible by the pulsar/transient team. The number of antennas in the core is preserved in our proposal. This transitions to the outer core which is slightly reduced as the main science for the outer core is the HI detection for cosmology and galaxy evolution. We propose this sacrifice as the science loss here is minimal for a loss of around 9 antennas. We further propose to reduce the spiral arms as no science directly needs those large baselines and instead move the spiral arms with the extra 21 antennas which were sacrificed from the outer core (9) plus the antennas which could be purchased from a cost effective reduction of the maximum baseline.

This arrangement is very beneficial for HI and continuum morphological studies, furthermore it produces a survey speed which allows weak lensing experiments to be possible with SKA-1. It does not strongly affect HI and pulsar science as a whole and allows for better imaging capabilities with SKA-MID. We believe that this is beneficial for the project compared to the baseline design. Furthermore we suggest that several clusters of around 6 antennas, depending on the exact masking of roads/environments, be placed in the core/outer core as to increase the sensitivity for intensity mapping. We do not investigate this here as we believe it will only cause a minor perturbation in the survey speed and sensitivities that we discuss here.

1.2.3 Specific layout implementation:

The general scientific requirements for SKA1[2] (SRD) published by the SPO in March 2014 suggest that (at least for SKA1-Mid), an array with a maximum baseline of around 100km is required. Therefore, we seek a layout with the shortest possible maximum baseline that does at least as well as the “second generation” baseline design in the resolution range 0.4-1 arcsec over 650, 800 and 1000MHz while not significantly compromising the performance at the larger angular scales. Moreover, as stated previously, having a layout which performs just as well as (or better) than the baseline layout but which covers significantly less space translates to a reduction in trenching and data transport costs, which presents an opportunity to re-invest the funds somewhere else, therefore we consider the conservative addition of 12 dishes. However, we note that improvements on the scales of interest are still possible without these 12 additional dishes. In the next section we present two alternative layouts, these layouts have maximum baselines of 120km. The scale dependent sensitivity of these layouts is compared to the SKA1-Mid and SKASUR baseline layouts in section 2.

1.3 Background on Layouts

The following SKA1-Mid layouts are under consideration here:

REF2A100B173 The Second-generation layout (254 dishes) produced by Robert Braun (September 2013)².

This layout has a maximum baseline of 173km. In this report, we also refer to this layout as REF2.

Wi-jAkBl This is the REF2 layout with the core “puffed up” by 10%, with i dishes moved from the outer core to the spiral arms and j extra dishes added to the spiral arms. The spacing in the arms is then optimised to get more sensitivity on the longer (> 50 km) baselines (See baseline distribution histograms in Figure 2). Each spiral arm stretches out to k kilometres and the maximum baseline length is about l kilometres.

The details of the layouts are tabulated in Table 1, and Figure 1 shows the layouts and Figure 2 shows the baseline distribution histogram for the different layouts. Figure 5 shows the uv-coverage for the different layouts at 1.1GHz for declinations -50,-30,-10 degrees and for 8hr tracks. At this point no optimisation has been done on the antenna distributions and we emphasise that further improvements can be and should be made.

Table 1: Breakdown of the layouts under consideration.

REF2A100B173 [254 dishes]	SKA dishes	MeerKAT dishes	Both	%
Core	70	30	100	39.4
Outer-core	60	34	94	37.0
Spiral-arms	60	0	60	23.6
W9-0A72B120 [254 dishes]				
Core	70	30	100	39.4
Outer-core	51	34	85	33.5
Spiral-arms	69	0	69	27.1
W9-12A60B120 [266 dishes]				
Core	70	30	100	37.6
Outer-core	51	34	85	32.0
Spiral-arms	81	0	81	30.4

²We assume this to be the baseline layout.

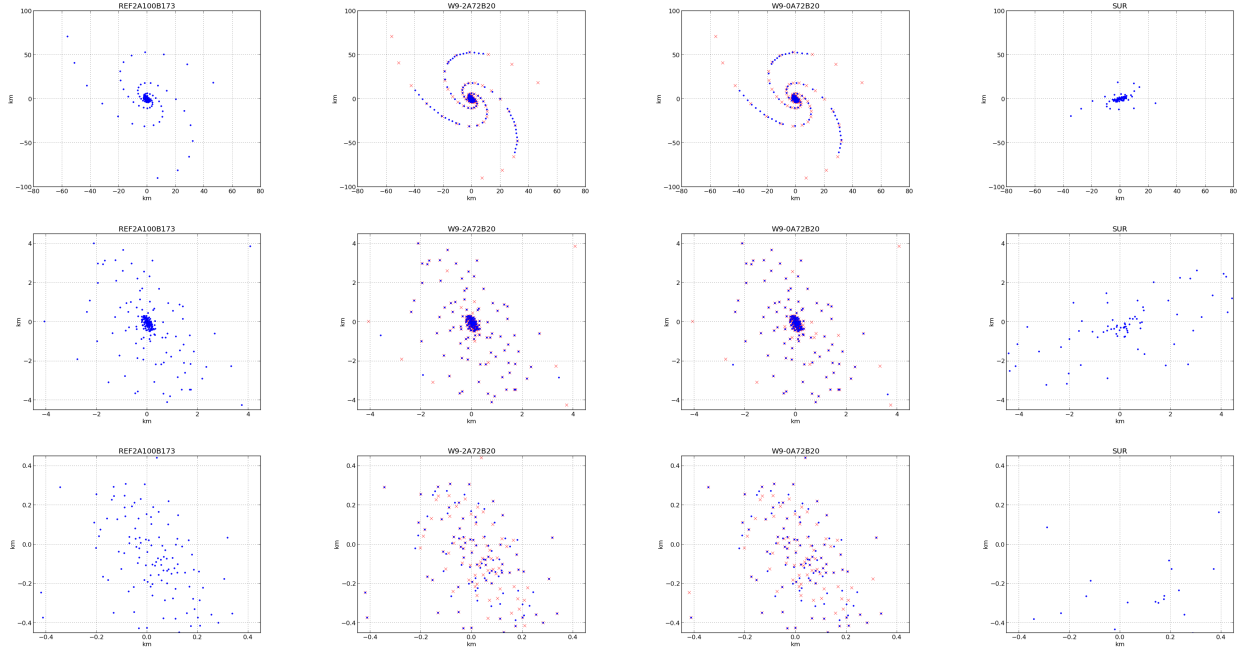


Figure 1: Antenna layouts, REF2 plotted as a reference (red crosses)

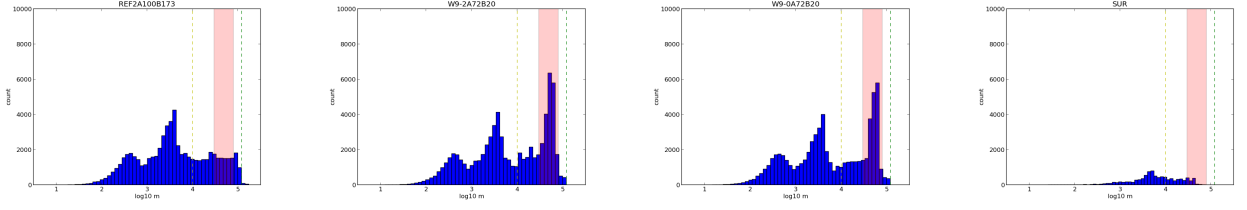


Figure 2: Baseline distribution with the uv-distance in \log_{10} km . Yellow and green dashed lines mark 10 and 120 kilometres respectively, and the pink strip represents baselines from 30-80km.

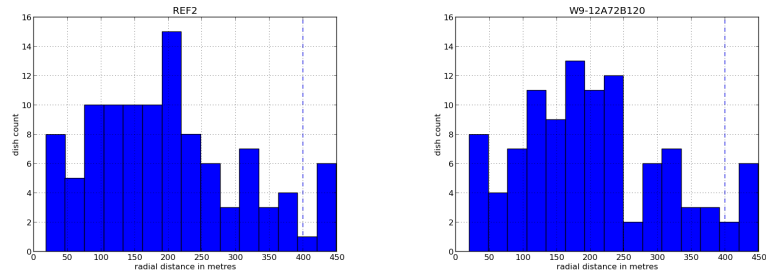


Figure 3: Dish density histograms (row 1) of the core for the layouts under consideration. The dashed line marks 400m. The core of the W-9-12 layouts is the same, therefore we only need to plot one of these.

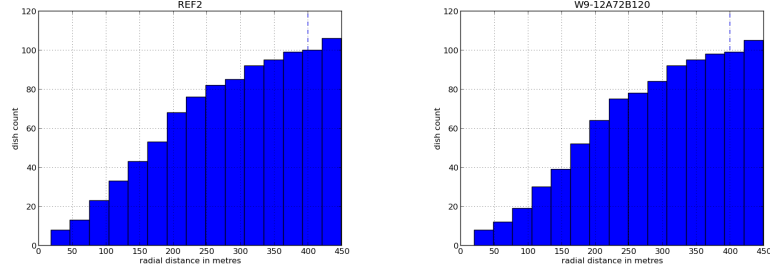


Figure 4: Cumulative dish density histograms (row 1) of the core for the layouts under consideration. The dashed line marks 400m. The core of the W-9-12 layouts is the same, therefore we only need to plot one of these.

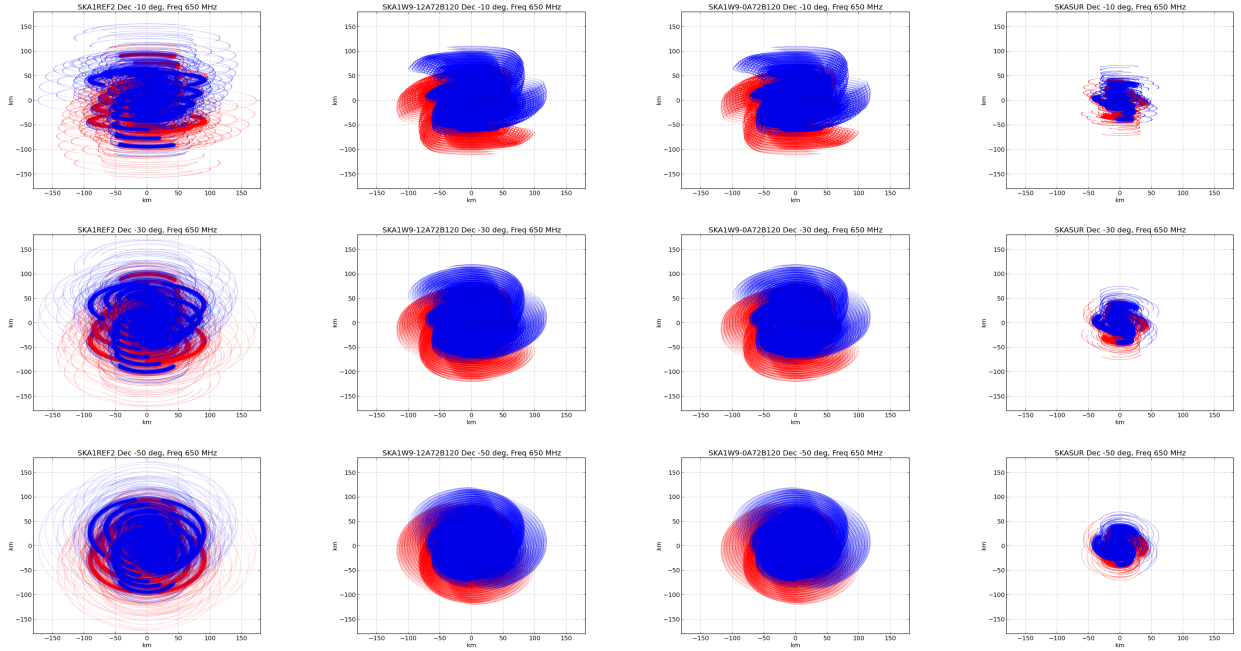


Figure 5: UV-Coverage for 8-hr tracks at 1.1 GHz (50MHz bandwidth) at declinations -50,-30,-10 for the different layouts. Blue indicates uv-points, red indicates conjugate uv-points.

2 The Experiment

Our aim is to investigate the scale-dependent sensitivity of the layouts described in the previous section. We use the `makems` tool to make simulated measurement sets (MS) of 8hr tracks with a 60s integration time for declinations -50, -30 and -10 degrees, at frequencies of 650, 800 and 1000MHz, with a single 50MHz channel. The expected rms noise per real and imaginary part for each visibility is calculated as

$$\sigma_{\text{vis}} = \frac{\text{SEFD}}{\sqrt{2\Delta t \Delta \nu}}. \quad (1)$$

We use the baseline design's SEFD values for the SKA and legacy dishes. The noise for visibilities corresponding to baselines between SKA and legacy dishes is calculated using $\text{SEFD}_{\text{MIX}} = \sqrt{\text{SEFD}_{\text{SKA}} \times \text{SEFD}_{\text{LEGACY}}}$. The MS is then filled with random Gaussian noise using the computed value of the noise for a given integration and bandwidth. We then use the (CASA-derived) `lwimager` tool to make naturally weighted maps of the PSF as well as dirty maps of the noise. The following metrics were generated:

Note: These metrics are generated at different angular scales, this is done by applying an inner-taper³ to taper out baselines that do not fall within a given resolution range, i.e., we only consider uv-points that correspond to a given resolution.

- PSF full width at half maximum (FWHM) size (mean of the FWHM dimensions). This was measured by making high-resolution images of the PSF (0.05 arcsec resolution), and fitting a Gaussian to the PSF. (Table 2). A catalog of PSF cross-sections (full uv-coverage) is provided in Appendix A.

³The weights for the taper are generated using a Butterworth function.

- PSF symmetry (PSF size parameters are obtained as explained above). As a measure of PSF symmetry, we define $\text{PSF}_{\text{sym}} = 1 - \text{FWHM}_{\text{min}}/\text{FWHM}_{\text{maj}}$, then $\text{PSF}_{\text{sym}} = 0$ is perfect symmetry, and the symmetry degenerates as $\text{PSF}_{\text{sym}} \rightarrow 1$ (Table 3).
- Rms pixel noise at different angular scales for 50kHz, 50MHz and 166MHz wide bands (Tables 4 and 6).
- SNR for a $10\mu\text{Jy}$ source at 1000MHz with a spectral index of -0.7 after 8hrs for a 166MHz band (Table 7).
- Average SNR over frequencies 650, 800 and 1000MHz (166MHz band) after 8 hours, for a $10\mu\text{Jy}$ source at 1000MHz with a spectral index of -0.7. $\overline{\text{SNR}}_{10} = \sqrt{\text{SNR}_{650}^2 + \text{SNR}_{800}^2 + \text{SNR}_{1000}^2}$ (Table 8).
- Hours required to reach a mean SNR of 10 (Table 9).
- Average survey speed (SS). These values are calculated using the FOV values in the SRD (PAF FOVs for SKASUR) and the values in Table 7. Note that unlike the SKASUR FOV, the SKA1-Mid FOV changes across the band ($\text{FOV}_{\text{Mid}} \sim \nu^{-2}$). $\overline{\text{SS}} = \sqrt{\text{SS}_{650}^2 + \text{SS}_{800}^2 + \text{SS}_{1000}^2}$, where $\text{SS}_{\text{Freq}} = \text{FOV}_{\text{Freq}} \times \text{SNR}^2$. We consider band 1 for SKA-Mid and band 2 for SKASUR. (Table 10).

In appendix B the above mentioned metrics are presented for a 2.5GHz band at 8, 12 and 13.8GHz, at a declination of -30 degrees.

Table 2: FWHM PSF sizes (in arcseconds) for the different layouts at different angular scales. These values are generated at 650, 800 and 1000MHz, for angular scales $\{0.4\text{-}1, 1\text{-}2, 2\text{-}3, 3\text{-}4, 600\text{-}3600\}$ arcsec and are labeled *resbin* $\{1, 2, 3, 4, 5\}$ respectively. This is done for natural weighting at declinations -10, -30 and -50 degrees. For each column, the intensity of the color increases with the value.

(a) DEC=-10, natural weighting

resbin	650MHz					800MHz					1000MHz				
	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5
SKA1REF2	0.65	1.33	2.33	3.35	803.1	0.60	1.33	2.35	3.34	792.3	0.59	1.33	2.35	3.32	777.1
SKA1W9-12A72B120	0.78	1.22	2.35	3.35	804.3	0.70	1.28	2.35	3.32	800.6	0.61	1.32	2.34	3.32	788.1
SKA1W9-0A72B120	0.78	1.21	2.35	3.35	802.2	0.70	1.27	2.36	3.31	796.6	0.60	1.31	2.33	3.33	787.5
SKASUR	0.91	1.46	2.36	3.34	1072	0.93	1.36	2.39	3.36	984.2	0.84	1.35	2.35	3.38	948.6

(b) DEC=-30, natural weighting

resbin	650MHz					800MHz					1000MHz				
	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5
SKA1REF2	0.65	1.34	2.35	3.37	797.3	0.60	1.33	2.35	3.34	790.6	0.59	1.34	2.37	3.33	770
SKA1W9-12A72B120	0.78	1.22	2.37	3.35	800.3	0.69	1.29	2.34	3.31	799.6	0.59	1.33	2.35	3.33	779.7
SKA1W9-0A72B120	0.79	1.21	2.35	3.34	798.1	0.70	1.29	2.35	3.30	795.5	0.59	1.31	2.34	3.37	778.6
SKASUR	0.95	1.46	2.36	3.34	1167	0.97	1.38	2.37	3.40	1019	0.84	1.35	2.36	3.38	933.8

(c) DEC=-50, natural weighting

resbin	650MHz					800MHz					1000MHz				
	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5
SKA1REF2	0.65	1.34	2.34	3.35	799.8	0.60	1.33	2.36	3.34	789.6	0.59	1.34	2.36	3.34	776.9
SKA1W9-12A72B120	0.79	1.22	2.35	3.34	801.5	0.70	1.28	2.35	3.31	795.8	0.60	1.34	2.35	3.34	784.2
SKA1W9-0A72B120	0.79	1.21	2.34	3.35	799.6	0.70	1.28	2.35	3.32	791	0.60	1.32	2.34	3.35	780.1
SKASUR	0.92	1.50	2.36	3.37	1051	0.92	1.37	2.36	3.37	975.9	0.83	1.33	2.38	3.37	948.3

Table 3: PSF symmetry (see section 2) for the different layouts at different angular scales. These values are generated at 650, 800 and 1000MHz, for angular scales $\{0.4-1, 1-2, 2-3, 3-4, 600-3600\}$ arcsec and are labeled *resbin* $\{1, 2, 3, 4, 5\}$ respectively. This is done for natural weighting at declinations -10, -30 and -50 degrees. For each column, the intensity of the color increases with the value.

(a) DEC=-10, natural weighting

resbin	650MHz					800MHz					1000MHz				
	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5
SKA1REF2	0.05	0.02	0.04	0.07	0.00	0.06	0.06	0.02	0.06	0.03	0.06	0.02	0.05	0.01	0.02
SKA1W9-12A72B120	0.05	0.03	0.05	0.06	0.02	0.06	0.05	0.01	0.06	0.02	0.05	0.03	0.06	0.03	0.01
SKA1W9-0A72B120	0.05	0.03	0.07	0.04	0.03	0.06	0.05	0.01	0.06	0.03	0.05	0.03	0.04	0.04	0.02
SKASUR	0.30	0.27	0.17	0.10	0.33	0.30	0.24	0.19	0.02	0.27	0.31	0.18	0.06	0.10	0.25

(b) DEC=-30, natural weighting

resbin	650MHz					800MHz					1000MHz				
	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5
SKA1REF2	0.13	0.07	0.08	0.06	0.02	0.09	0.08	0.06	0.08	0.03	0.07	0.07	0.05	0.04	0.02
SKA1W9-12A72B120	0.16	0.01	0.05	0.06	0.02	0.13	0.00	0.07	0.06	0.02	0.11	0.06	0.05	0.02	0.02
SKA1W9-0A72B120	0.16	0.00	0.04	0.08	0.03	0.13	0.02	0.07	0.07	0.03	0.12	0.07	0.08	0.02	0.00
SKASUR	0.38	0.29	0.24	0.02	0.42	0.39	0.22	0.19	0.08	0.33	0.34	0.20	0.01	0.09	0.25

(c) DEC=-50, natural weighting

resbin	650MHz					800MHz					1000MHz				
	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5
SKA1REF2	0.11	0.04	0.06	0.02	0.02	0.10	0.07	0.07	0.08	0.03	0.05	0.07	0.05	0.04	0.02
SKA1W9-12A72B120	0.14	0.01	0.05	0.02	0.01	0.10	0.00	0.05	0.06	0.05	0.09	0.06	0.03	0.02	0.01
SKA1W9-0A72B120	0.14	0.01	0.04	0.05	0.03	0.10	0.01	0.03	0.09	0.06	0.09	0.05	0.05	0.05	0.01
SKASUR	0.30	0.26	0.17	0.08	0.26	0.24	0.26	0.02	0.05	0.20	0.25	0.23	0.10	0.04	0.22

Table 4: Noise (in μJy) for a 50kHz band after an 8hr synthesis with a 60s integration for the different layouts at different angular scales. These values are generated at 650, 800 and 1000 MHz, at angular scales $\{0.4-1, 1-2, 2-3, 3-4, 600-3600\}$ arcsec and are labeled *resbin* $\{1, 2, 3, 4, 5\}$ respectively. This is done for natural weighting at declinations -10, -30 and -50 degrees. For each column, the intensity of the color increases with the value.

(a) DEC=-10, natural weighting

resbin	650MHz					800MHz					1000MHz				
	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5
SKA1REF2	120	120	160	190	390	100	120	160	190	490	100	120	160	190	630
SKA1W9-12A72B120	86.00	85.00	150	170	410	74.00	100	150	190	520	69.00	110	150	210	660
SKA1W9-0A72B120	89.00	92.00	170	200	410	78.00	110	170	200	490	72.00	120	170	240	660
SKASUR	1500	380	450	530	2600	660	350	430	540	2700	330	260	330	360	2500

(b) DEC=-30, natural weighting

resbin	650MHz					800MHz					1000MHz				
	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5
SKA1REF2	110	120	150	190	410	100	120	160	190	520	100	120	160	190	670
SKA1W9-12A72B120	82.00	88.00	150	180	440	72.00	100	150	190	550	67.00	110	160	220	710
SKA1W9-0A72B120	85.00	95.00	170	200	430	74.00	120	170	210	550	72.00	130	170	240	680
SKASUR	1400	370	440	570	2600	640	340	460	550	3000	330	260	340	340	2400

(c) DEC=-50, natural weighting

resbin	650MHz					800MHz					1000MHz				
	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5
SKA1REF2	110	120	150	190	400	100	120	160	190	510	100	120	160	190	660
SKA1W9-12A72B120	80.00	86.00	150	180	430	71.00	110	150	190	530	67.00	110	150	210	690
SKA1W9-0A72B120	85.00	93.00	170	200	430	76.00	120	170	200	530	73.00	130	170	240	700
SKASUR	1700	380	450	530	2700	700	340	460	520	3000	370	250	330	330	2500

Table 5: Noise (in μJy) for a 50MHz band after an 8hr synthesis with a 60s integration for the different layouts at different angular scales. These values are generated at 650, 800 and 1000 MHz, at angular scales $\{0.4\text{-}1, 1\text{-}2, 2\text{-}3, 3\text{-}4, 600\text{-}3600\}$ arcsec and are labeled *resbin* $\{1, 2, 3, 4, 5\}$ respectively. This is done for natural weighting at declinations -10, -30 and -50 degrees. For each column, the intensity of the color increases with the value.

(a) DEC=-10, natural weighting

resbin	650MHz					800MHz					1000MHz				
	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5
SKA1REF2	3.70	3.70	5.00	5.90	12.00	3.30	3.80	5.00	6.00	15.00	3.20	3.80	5.10	6.00	20.00
SKA1W9-12A72B120	2.70	2.70	4.60	5.50	13.00	2.30	3.20	4.90	6.10	17.00	2.20	3.50	4.80	6.70	21.00
SKA1W9-0A72B120	2.80	2.90	5.30	6.20	13.00	2.50	3.60	5.40	6.40	16.00	2.30	3.90	5.40	7.60	21.00
SKASUR	47.00	12.00	14.00	17.00	84.00	21.00	11.00	13.00	17.00	85.00	10.00	8.10	11.00	11.00	78.00

(b) DEC=-30, natural weighting

resbin	650MHz					800MHz					1000MHz				
	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5
SKA1REF2	3.50	3.70	4.90	6.00	13.00	3.20	3.70	5.10	6.00	16.00	3.20	3.80	5.00	6.10	21.00
SKA1W9-12A72B120	2.60	2.80	4.70	5.80	14.00	2.30	3.30	4.70	6.10	17.00	2.10	3.60	5.00	6.90	22.00
SKA1W9-0A72B120	2.70	3.00	5.50	6.40	13.00	2.30	3.90	5.50	6.70	17.00	2.30	4.00	5.40	7.70	22.00
SKASUR	45.00	12.00	14.00	18.00	83.00	20.00	11.00	14.00	17.00	94.00	10.00	8.10	11.00	11.00	76.00

(c) DEC=-50, natural weighting

resbin	650MHz					800MHz					1000MHz				
	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5
SKA1REF2	3.50	3.70	4.90	6.00	13.00	3.30	3.70	5.10	6.10	16.00	3.30	3.80	5.10	6.20	21.00
SKA1W9-12A72B120	2.50	2.70	4.60	5.60	14.00	2.30	3.40	4.70	6.00	17.00	2.10	3.50	4.90	6.70	22.00
SKA1W9-0A72B120	2.70	2.90	5.50	6.40	14.00	2.40	3.80	5.50	6.40	17.00	2.30	4.00	5.40	7.60	22.00
SKASUR	53.00	12.00	14.00	17.00	84.00	22.00	11.00	14.00	16.00	94.00	12.00	8.00	10.00	10.00	80.00

Table 6: Noise (in μJy) for a 166MHz band after an 8hr synthesis with a 60s integration for the different layouts at different angular scales. These values are generated at 650, 800 and 1000 MHz, at angular scales $\{0.4\text{-}1, 1\text{-}2, 2\text{-}3, 3\text{-}4, 600\text{-}3600\}$ arcsec and are labeled *resbin* $\{1, 2, 3, 4, 5\}$ respectively. This is done for natural weighting at declinations -10, -30 and -50 degrees. For each column, the intensity of the color increases with the value.

(a) DEC=-10, natural weighting

resbin	650MHz					800MHz					1000MHz				
	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5
SKA1REF2	2.00	2.10	2.70	3.20	6.70	1.80	2.10	2.70	3.30	8.40	1.80	2.10	2.80	3.30	11.00
SKA1W9-12A72B120	1.50	1.50	2.50	3.00	7.10	1.30	1.80	2.70	3.30	9.10	1.20	1.90	2.60	3.70	11.00
SKA1W9-0A72B120	1.50	1.60	2.90	3.40	7.10	1.40	2.00	3.00	3.50	8.50	1.30	2.20	3.00	4.20	11.00
SKASUR	26.00	6.50	7.70	9.10	46.00	11.00	6.10	7.40	9.40	47.00	5.70	4.50	5.80	6.20	43.00

(b) DEC=-30, natural weighting

resbin	650MHz					800MHz					1000MHz				
	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5
SKA1REF2	1.90	2.10	2.70	3.30	7.00	1.80	2.00	2.80	3.30	9.10	1.80	2.10	2.80	3.40	12.00
SKA1W9-12A72B120	1.40	1.50	2.60	3.20	7.60	1.30	1.80	2.60	3.30	9.50	1.20	1.90	2.80	3.80	12.00
SKA1W9-0A72B120	1.50	1.70	3.00	3.50	7.40	1.30	2.10	3.00	3.70	9.50	1.20	2.20	3.00	4.20	12.00
SKASUR	25.00	6.40	7.60	9.90	46.00	11.00	6.00	7.90	9.50	52.00	5.70	4.40	5.90	5.90	42.00

(c) DEC=-50, natural weighting

resbin	650MHz					800MHz					1000MHz				
	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5
SKA1REF2	1.90	2.00	2.70	3.30	7.00	1.80	2.00	2.80	3.30	8.90	1.80	2.10	2.80	3.40	11.00
SKA1W9-12A72B120	1.40	1.50	2.50	3.10	7.40	1.20	1.80	2.60	3.30	9.20	1.20	1.90	2.70	3.70	12.00
SKA1W9-0A72B120	1.50	1.60	3.00	3.50	7.40	1.30	2.10	3.00	3.50	9.20	1.30	2.20	3.00	4.10	12.00
SKASUR	29.00	6.60	7.90	9.20	46.00	12.00	6.00	7.90	9.00	51.00	6.40	4.40	5.70	5.70	44.00

Table 7: SNR after 8 hours relative to a $10\mu\text{Jy}$ source at 1000Hz (166 MHz band) with a spectral index of -0.7 for the different layouts. These values are generated at 650, 800 and 1000 MHz, at angular scales $\{0.4\text{-}1, 1\text{-}2, 2\text{-}3, 3\text{-}4, 600\text{-}3600\}$ arcsec and are labeled *resbin* $\{1, 2, 3, 4, 5\}$ respectively. This is done for natural weighting at declinations -10, -30 and -50 degrees. For each column, the intensity of the color increases with the value.

(a) DEC=-10, natural weighting

	650MHz					800MHz					1000MHz				
resbin	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5
SKA1REF2	6.75	6.59	4.94	4.19	2.01	6.51	5.67	4.27	3.57	1.38	5.64	4.85	3.59	3.05	0.92
SKA1W9-12A72B120	9.08	9.13	5.31	4.47	1.89	9.07	6.62	4.37	3.49	1.29	8.37	5.23	3.80	2.72	0.87
SKA1W9-0A72B120	8.76	8.48	4.65	3.96	1.90	8.63	5.94	3.93	3.31	1.37	7.97	4.63	3.37	2.39	0.87
SKASUR	0.52	2.08	1.75	1.48	0.29	1.02	1.91	1.58	1.24	0.25	1.77	2.25	1.73	1.62	0.23

(b) DEC=-30, natural weighting

	650MHz					800MHz					1000MHz				
resbin	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5
SKA1REF2	7.00	6.58	5.07	4.11	1.92	6.62	5.73	4.19	3.54	1.29	5.63	4.84	3.61	2.97	0.87
SKA1W9-12A72B120	9.52	8.86	5.24	4.22	1.77	9.33	6.42	4.49	3.52	1.23	8.60	5.13	3.62	2.65	0.81
SKA1W9-0A72B120	9.15	8.18	4.50	3.88	1.83	9.12	5.52	3.91	3.20	1.23	8.02	4.59	3.38	2.37	0.84
SKASUR	0.54	2.10	1.79	1.37	0.30	1.06	1.96	1.48	1.23	0.23	1.75	2.25	1.69	1.69	0.24

(c) DEC=-50, natural weighting

	650MHz					800MHz					1000MHz				
resbin	1	2	3	4	5	1	2	3	4	5	1	2	3	4	5
SKA1REF2	6.96	6.61	5.05	4.08	1.92	6.53	5.75	4.16	3.52	1.31	5.59	4.79	3.55	2.96	0.87
SKA1W9-12A72B120	9.74	9.04	5.37	4.41	1.82	9.46	6.32	4.51	3.54	1.27	8.62	5.16	3.73	2.71	0.83
SKA1W9-0A72B120	9.20	8.36	4.47	3.85	1.82	8.87	5.66	3.90	3.34	1.27	7.94	4.53	3.36	2.41	0.82
SKASUR	0.46	2.05	1.71	1.47	0.29	0.96	1.96	1.48	1.31	0.23	1.57	2.28	1.75	1.76	0.23

Table 8: SNR after 8 hours relative to a $10\mu\text{Jy}$ source at 1000Hz (166 MHz band) with a spectral index of -0.7 averaged over 650,800 and 1000MHz, for the different layouts at different angular scales. These values are generated for angular scales $\{0.4\text{-}1, 1\text{-}2, 2\text{-}3, 3\text{-}4, 600\text{-}3600\}$ arcsec and are labeled *resbin* $\{1, 2, 3, 4, 5\}$ respectively. This is done for natural weighting at declinations -10, -30 and -50 degrees. For each column, the intensity of the color increases with the value.

(a) DEC=-10, natural weighting

resbin	1	2	3	4	5
SKA1REF2	10.94	9.95	7.45	6.29	2.61
SKA1W9-12A72B120	15.32	12.43	7.86	6.29	2.45
SKA1W9-0A72B120	14.65	11.34	6.96	5.69	2.50
SKASUR	2.11	3.60	2.92	2.52	0.45

(b) DEC=-30, natural weighting

resbin	1	2	3	4	5
SKA1REF2	11.16	9.98	7.51	6.19	2.47
SKA1W9-12A72B120	15.87	12.08	7.79	6.10	2.30
SKA1W9-0A72B120	15.21	10.89	6.85	5.56	2.36
SKASUR	2.12	3.65	2.87	2.50	0.44

(c) DEC=-50, natural weighting

resbin	1	2	3	4	5
SKA1REF2	11.06	9.98	7.44	6.15	2.49
SKA1W9-12A72B120	16.08	12.18	7.94	6.27	2.36
SKA1W9-0A72B120	15.04	11.07	6.82	5.64	2.37
SKASUR	1.90	3.64	2.86	2.64	0.43

Table 9: The hours required to reach a mean SNR of 10 (average over 650,800 and 1000MHz), relative to a $10\mu\text{Jy}$ source at 1000MHz with a spectral index of -0.7 for the different layouts at different angular scales. These values are generated for angular scales $\{0.4\text{-}1, 1\text{-}2, 2\text{-}3, 3\text{-}4, 600\text{-}3600\}$ arcsec and are labeled *resbin* $\{1, 2, 3, 4, 5\}$ respectively. This is done for natural weighting at declinations -10, -30 and -50 degrees. For each column, the intensity of the color increases with the value.

(a) DEC=-10, natural weighting

resbin	1	2	3	4	5
SKA1REF2	6.68	8.08	14.40	20.19	117.8
SKA1W9-12A72B120	3.41	5.18	12.96	20.23	133.3
SKA1W9-0A72B120	3.73	6.22	16.53	24.72	128
SKASUR	180.1	61.56	93.54	126.1	3923

(b) DEC=-30, natural weighting

resbin	1	2	3	4	5
SKA1REF2	6.42	8.04	14.20	20.90	131.2
SKA1W9-12A72B120	3.18	5.48	13.17	21.51	151
SKA1W9-0A72B120	3.46	6.75	17.05	25.90	143.8
SKASUR	178.7	60.08	97.28	128.3	4089

(c) DEC=-50, natural weighting

resbin	1	2	3	4	5
SKA1REF2	6.54	8.03	14.44	21.17	129.4
SKA1W9-12A72B120	3.09	5.39	12.69	20.34	143.1
SKA1W9-0A72B120	3.53	6.53	17.21	25.14	142.6
SKASUR	222	60.29	97.95	114.5	4237

Table 10: Relative (w.r.t SKASUR) average survey speeds for the different layouts, calculated using the FOV (PAF FOV for SKASUR) values given in the SRD [2] and the values in table 7. These values are generated for angular scales $\{0.4-1, 1-2, 2-3, 3-4, 600-3600\}$ arcsec and are labeled *resbin* $\{1, 2, 3, 4, 5\}$ respectively. This is done for natural weighting at declinations -10, -30 and -50 degrees. For each column, the intensity of the color increases with the value.

(a) DEC=-10, natural weighting					
resbin	1	2	3	4	5
SKA1REF2	1.48	0.57	0.51	0.48	3.14
SKA1W9-12A72B120	2.83	1.00	0.57	0.52	2.77
SKA1W9-0A72B120	2.50	0.86	0.45	0.42	2.82
SKASUR	1.00	1.00	1.00	1.00	1.00

(b) DEC=-30, natural weighting					
resbin	1	2	3	4	5
SKA1REF2	1.61	0.57	0.55	0.46	3.00
SKA1W9-12A72B120	3.05	1.00	0.58	0.48	2.52
SKA1W9-0A72B120	2.88	0.79	0.44	0.40	2.71
SKASUR	1.00	1.00	1.00	1.00	1.00

(c) DEC=-50, natural weighting					
resbin	1	2	3	4	5
SKA1REF2	1.96	0.58	0.53	0.41	3.15
SKA1W9-12A72B120	3.96	1.00	0.60	0.47	2.80
SKA1W9-0A72B120	3.54	0.86	0.43	0.36	2.85
SKASUR	1.00	1.00	1.00	1.00	1.00

3 Conclusions

The metrics we have used suggest that the science goals (at least those listed in the SRD in addition to cosmology with weak lensing and HI surveys) can be met by a layout which covers significantly less space compared to the baseline layout. The SKA1-W9-0A72B120 layout performs significantly better at smaller angular scales, up to a 42% improvement in terms of the noise properties and a 50% improvement in survey speed, without compromising the larger scales. Moreover, the performance the SKA1-Mid performance can be further enhanced by adding a handfull of dishes in the spairal arms as can be seen with the SKA1W9-12A72B120 layout.

Bringing in the dishes from the longer baselines translates to a greater sensitivity on the relevant (to the science goals of SKA1-Mid) smaller scales, as can be seen in Tables 4-9. Even more encouraging is the fact that this doesn't compromise the size or the symmetry of the PSF as seen in Tables 2 and 12. **We proffer the SKA1W9-0A72B120 configuration as a solution which allows for weak lensing, HI and continuum source morphology characterisation for galaxy evolution studies, as well as the other science cases detailed in the SRD. Although we note that such a configuration also needs to be analysed by other SWGs, in particular the HI SWG.**

References

- [1] http://www.skatelescope.org/wp-content/uploads/2013/05/SKA-TEL-SK0-DD-001-1_BaselineDesign1.pdf
- [2] https://www.skatelescope.org/wp-content/uploads/2014/03/SKA-TEL_SCI-SK0-SRQ-001-1_Level_0_Requirements-1.pdf

A PSF cross-sections

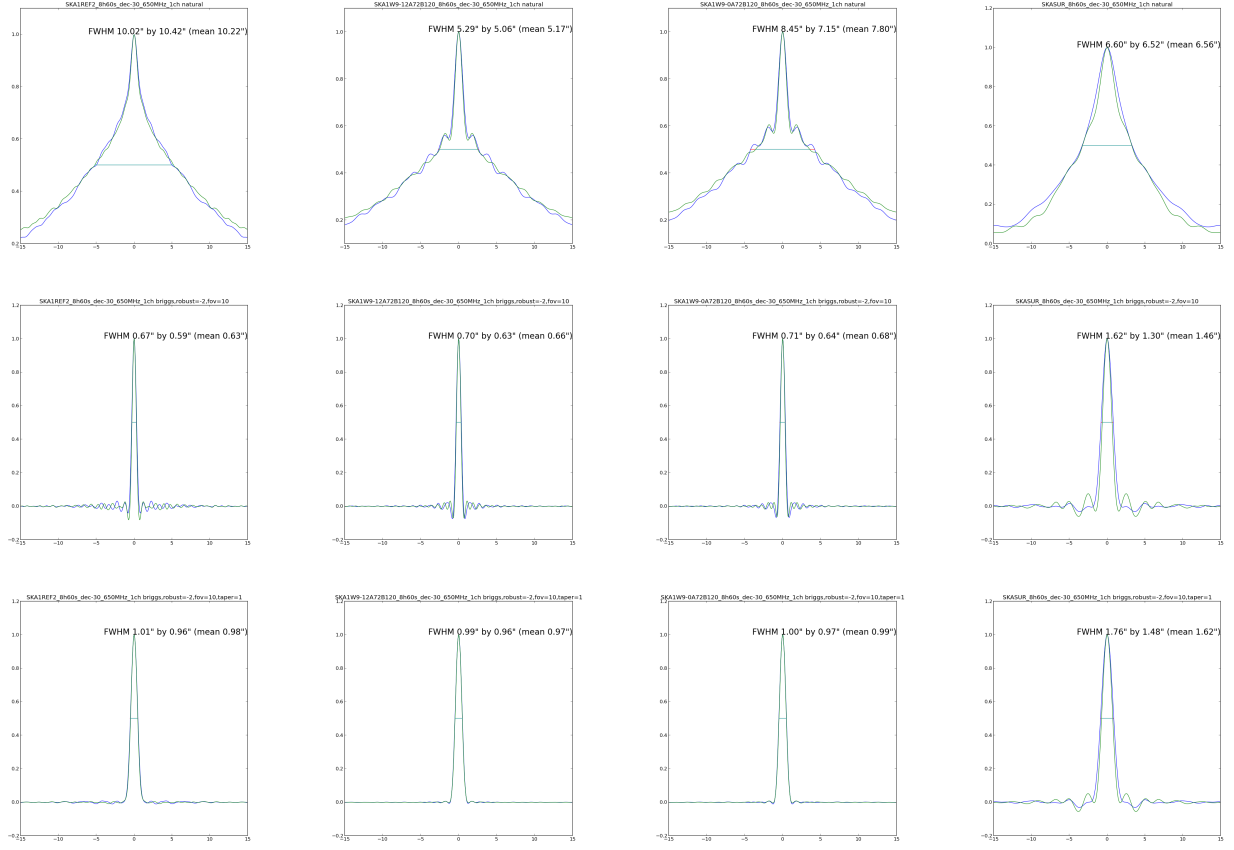


Figure 6: PSF cross-sections at Dec=-30 deg, Freq=650MHz for the different layouts. Row 1 and 2 are for natural and robust-2 weighting respectively, and row 3 is for robust-2 weighting with a 1 arcsec Gaussian taper. The blue and green curves are cross-sections along l and m respectively, and the horizontal line marks the FWHM. FWHM parameters are included in the plot.

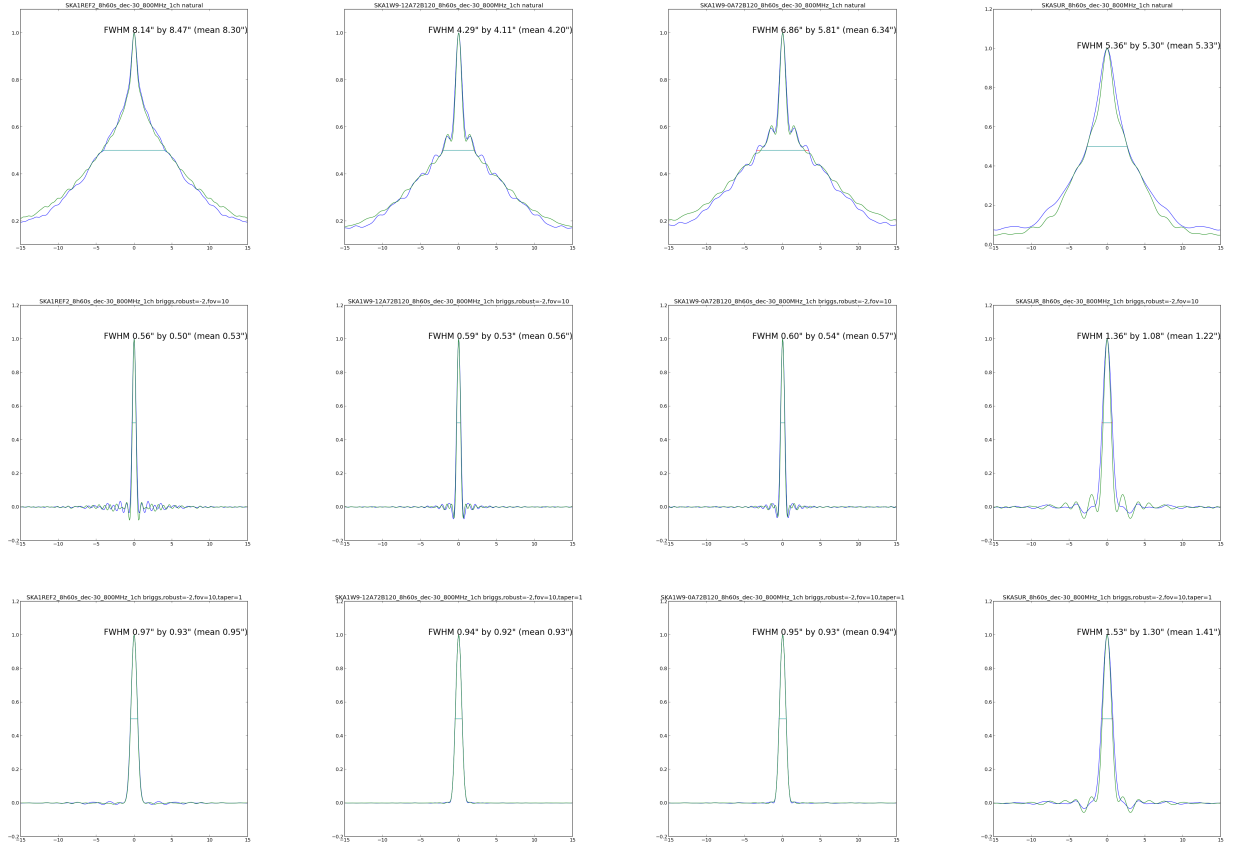


Figure 7: PSF cross-sections at Dec=-30 deg, Freq=800MHz. Row 1 and 2 are for natural and robust-2 weighting respectively, and row 3 is for robust-2 weighting with a 1 arcsec Gaussian taper. The blue and green curves are cross-sections along l and m respectively, and the horizontal line marks the FWHM. FWHM parameters are included in the plot.

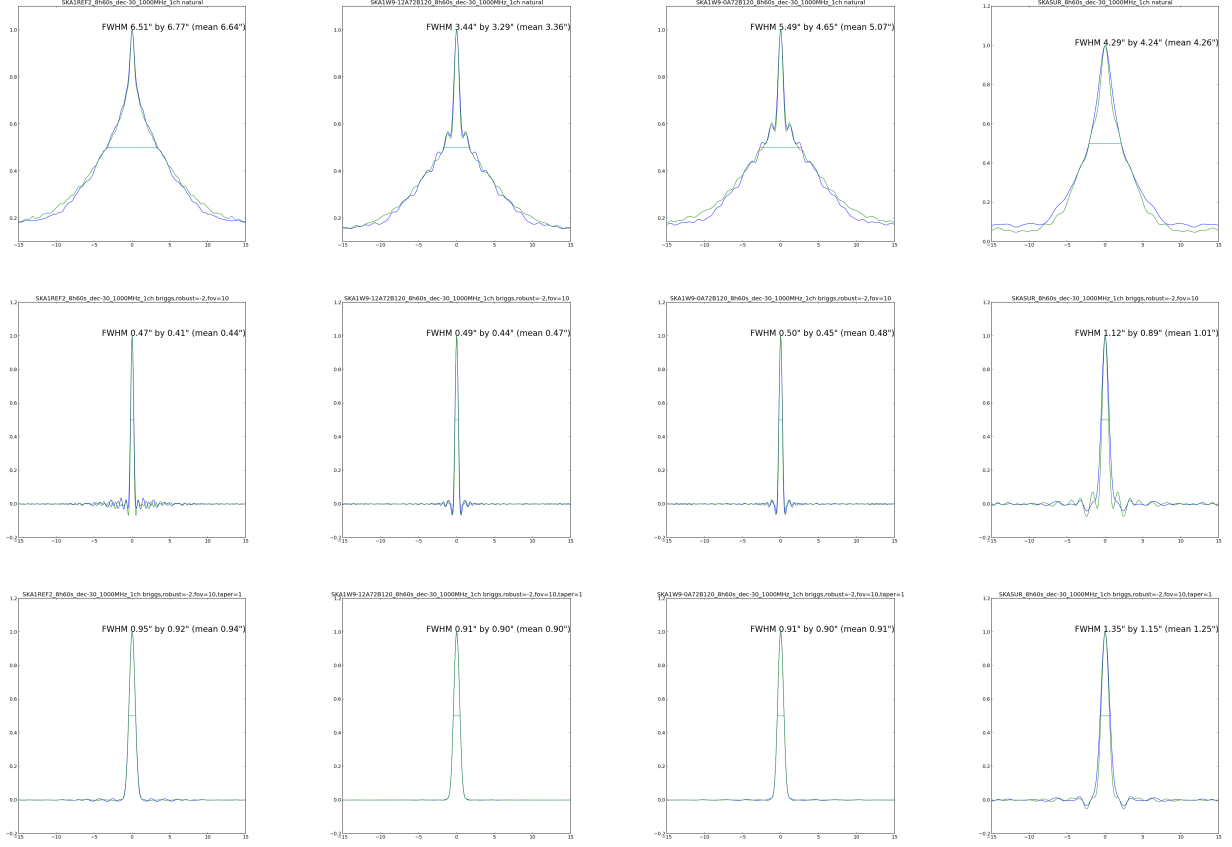


Figure 8: PSF cross-sections at Dec=-30 deg, Freq=1000MHz. Row 1 and 2 are for natural and robust-2 weighting respectively, and row 3 is for robust-2 weighting with a 1 arcsec Gaussian taper. The blue and green curves are cross-sections along l and m respectively, and the horizontal line marks the FWHM. FWHM parameters are included in the plot.

B Band 5 Scale-Dependent Sensitivity

The Tables below were generated using the BD's SEFD value of 528Jy for band 5. We make simulated measurement sets of 8hr tracks at a declination of -30 degrees at frequencies 8, 12 and 13.8GHz with a single 2.5GHz band and 60s integration time. MeerKAT do not have receivers at these frequencies, therefore the MeerKAT dishes were not considered for these simulations.

Table 11: FWHM PSF sizes (in arcseconds) for the different layouts at different angular scales. These values are generated at 8, 12 and 13.8GHz, for angular scales $\{0.04\text{-}0.05, 0.05\text{-}0.1, 0.1\text{-}1, 1\text{-}12\}$ arcsec and are labeled *resbin* $\{1, 2, 3, 4\}$ respectively. This is done for natural weighting at a declination of -30 degrees. For each column, the intensity of the color increases with the value.

(a) DEC=-30, natural weighting

	8GHz				12GHz				13.8GHz			
resbin	1	2	3	4	1	2	3	4	1	2	3	4
SKA1REF2	0.04	0.07	0.28	1.86	0.04	0.07	0.30	1.91	0.04	0.07	0.30	2.08
SKA1W9-12A72B120	0.04	0.07	0.24	1.76	0.04	0.06	0.27	1.81	0.04	0.06	0.28	1.86
SKA1W9-0A72B120	0.04	0.07	0.25	1.77	0.04	0.06	0.31	1.80	0.04	0.06	0.32	1.85

Table 12: PSF symmetry (see section 2) for the different layouts at different angular scales. These values are generated at 8, 12 and 13.8GHz, for angular scales $\{0.04-0.05, 0.05-0.1, 0.1-1, 1-12\}$ arcsec and are labeled *resbin* $\{1, 2, 3, 4\}$ respectively. This is done for natural weighting at a declination of -30 degrees. For each column, the intensity of the color increases with the value.

(a) DEC=-30, natural weighting

resbin	8GHz				12GHz				13.8GHz			
	1	2	3	4	1	2	3	4	1	2	3	4
SKA1REF2	0.11	0.07	0.10	0.06	0.01	0.09	0.09	0.01	0.09	0.08	0.09	0.04
SKA1W9-12A72B120	0.13	0.12	0.03	0.13	0.16	0.05	0.06	0.08	0.11	0.02	0.06	0.03
SKA1W9-0A72B120	0.12	0.12	0.03	0.13	0.17	0.05	0.05	0.08	0.11	0.03	0.04	0.06

Table 13: Noise (in μJy) for a 2.5GHz band after an 8hr synthesis with a 60s integration for the different layouts at different angular scales. These values are generated at 8, 12 and 13.8 GHz, at angular scales $\{0.04-0.05, 0.05-0.1, 0.1-1, 1-12\}$ arcsec and are labeled *resbin* $\{1, 2, 3, 4\}$ respectively. This is done for natural weighting at a declination of -30 degrees. For each column, the intensity of the color increases with the value.

(a) DEC=-30, natural weighting

resbin	8GHz				12GHz				13.8GHz			
	1	2	3	4	1	2	3	4	1	2	3	4
SKA1REF2	0.90	0.49	0.25	0.29	0.91	0.48	0.25	0.32	0.85	0.48	0.24	0.35
SKA1W9-12A72B120	1.30	0.30	0.24	0.31	0.50	0.32	0.25	0.36	0.45	0.39	0.25	0.40
SKA1W9-0A72B120	1.50	0.32	0.26	0.31	0.54	0.35	0.27	0.36	0.48	0.43	0.27	0.40

Table 14: SNR after 8 hours relative to a $10\mu\text{Jy}$ source at 13.8GHz (2.5GHz band) with a spectral index of -0.7 for the different layouts. These values are generated at 8, 12 and 13.8 GHz, at angular scales $\{0.04-0.05, 0.05-0.1, 0.1-1, 1-12\}$ arcsec and are labeled *resbin* $\{1, 2, 3, 4\}$ respectively. This is done for natural weighting at a declination of -30 degrees. For each column, the intensity of the color increases with the value.

(a) DEC=-30, natural weighting

resbin	8GHz				12GHz				13.8GHz			
	1	2	3	4	1	2	3	4	1	2	3	4
SKA1REF2	16.23	29.90	59.18	51.09	12.69	24.03	46.72	36.02	11.75	20.64	40.86	28.90
SKA1W9-12A72B120	11.16	48.78	61.58	47.14	23.23	35.44	46.87	31.82	22.06	25.84	40.14	25.13
SKA1W9-0A72B120	9.99	45.20	55.39	47.63	21.40	32.62	42.74	32.07	20.87	23.06	37.16	25.29

Table 15: SNR after 8 hours relative to a $10\mu\text{Jy}$ source at 13.8GHz (2.5GHz band) with a spectral index of -0.7 averaged over 8,12 and 13.8GHz, for the different layouts at different angular scales. These values are generated for angular scales $\{0.04-0.05, 0.05-0.1, 0.1-1, 1-12\}$ arcsec and are labeled *resbin* $\{1, 2, 3, 4\}$ respectively. This is done for natural weighting at a declination of -30 degrees. For each column, the intensity of the color increases with the value.

(a) DEC=-30, natural weighting

resbin	1	2	3	4
SKA1REF2	23.72	43.56	85.76	68.87
SKA1W9-12A72B120	33.92	65.60	87.18	62.18
SKA1W9-0A72B120	31.52	60.32	79.22	62.74

Table 16: The hours required to reach a mean SNR of 10 (average over 8, 12 and 13.8GHz), relative to a $10\mu\text{Jy}$ source at 13.8GHz with a spectral index of -0.7 for the different layouts at different angular scales. These values are generated for angular scales $\{0.04-0.05, 0.05-0.1, 0.1-1, 1-12\}$ arcsec and are labeled *resbin* $\{1, 2, 3, 4\}$ respectively. This is done for natural weighting at a declination of -30 and degrees. For each column, the intensity of the color increases with the value.

(a) DEC=-30, natural weighting

resbin	1	2	3	4
SKA1REF2	1.42	0.42	0.11	0.17
SKA1W9-12A72B120	0.70	0.19	0.11	0.21
SKA1W9-0A72B120	0.81	0.22	0.13	0.20