



## Module 1: Logic (?q=onlinecourse/course/43493)

# Exercise: Predicate Logic

- **วิชชาภัทร จินดาภัก** previously submitted answers to this quiz/test on 18-Oct-2023 @ 02:06:51 and obtained **18** correct answers out of **18**.
- This test/quiz can be taken many times.
- Correct answers will NOT be revealed after submission.

Answer all the questions correctly within the deadline of this module. You can submit the answers as many times as you wish.

## 1 Use this information to answer Question 1-5

Let

- $P(x)$  denote the statement " $x > 0$ "
- $Q(x)$  denote the statement " $x < 0$ "
- $R(x)$  denote the statement " $x = 0$ "
- $S(x, y)$  denote the statement " $x + y = 2$ "

From previous attempt

What are these truth values when the domain of  $x$  is a set of real numbers?

$\forall x P(x)$

## 2 What are these truth values when the domain of $x$ is a set of real numbers?

$\exists! x P(x)$

From previous attempt

## 3 What are these truth values when the domain of $x$ is a set of real numbers?

$\forall x ((P(x) \wedge Q(x)) \rightarrow R(x))$

From previous attempt

4 What are these truth values when the domain of  $x$  is a set of real numbers?

$$\forall x \exists y S(x, y)$$

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From previous attempt

5 What are these truth values when the domain of  $x$  is a set of real numbers?

$$\exists x \forall y S(x, y)$$

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From previous attempt

6 Use this information to answer Question 6–8

Let  $P(x, y)$  denote the statement “ $x$  joins  $y$  class”

$Q(x)$  denote the statement “ $x$  likes studying math”

When the domain of  $x$  is a set of students in ABC university, and the domain of  $y$  is a set of classes in ABC university.

Express each statement in terms of quantifier:

Every student who joins DISCRETE class like studying math

- $\forall x (P(x, \text{DISCRETE}) \rightarrow Q(x))$
- $\forall x (P(x, \text{DISCRETE}) \wedge Q(x))$

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From previous attempt

7 Express each statement in terms of quantifier:

There is a student who neither join DISCRETE class nor DIG LOGIC class

- $\exists x (\neg (P(x, \text{DISCRETE}) \wedge P(x, \text{DIG LOGIC})))$
- $\exists x (\neg (P(x, \text{DISCRETE}) \vee P(x, \text{DIG LOGIC})))$

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From previous attempt

8 Express each statement in terms of quantifier:

There is a student who does not join any class.

- $\neg \exists x \forall y P(x, y)$
- $\exists x \forall y (\neg P(x, y))$

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From previous attempt

9 Determine the truth value of these statements

If  $\forall x P(x)$  is true when  $x \in R$  then  $\forall x P(x)$  is always true when  $x \in I$

From previous attempt

----- From previous attempt

10 Determine the truth value of these statements

If  $\exists xP(x)$  is true when  $x \in \mathbb{R}$  then  $\exists xP(x)$  is always true when  $x \in \mathbb{I}$

----- From previous attempt

11 Determine the truth value of these statements

$\exists xP(x)$  is true when  $x \in \emptyset$

----- From previous attempt

12 Use this information to answer Question 12-14

Let  $P(x)$ ,  $Q(x)$  is the value of the propositional function at  $x$  and  $A$  is a proposition

Answer the following questions  $\forall xP(x) \rightarrow A \equiv ?$

- $\forall x(P(x) \rightarrow A)$
- $\exists x(P(x) \rightarrow A)$

----- From previous attempt

13  $\forall x(P(x) \vee Q(x)) \equiv \forall xP(x) \vee \forall xQ(x)$

----- From previous attempt

14 Determine whether it is valid.

Premise:

- $(p \vee \neg q) \rightarrow \neg r$
- $p \wedge q$
- $s \rightarrow r$

1.1. Conclusion:  $\neg s$

1.2. Conclusion:  $q \rightarrow r$

----- From previous attempt

15 Identify the error or errors in this argument that supposedly shows that if  $\exists xP(x) \wedge \exists xQ(x)$  is true then  $\exists x(P(x) \wedge Q(x))$  is true.

1.  $\exists xP(x) \wedge \exists xQ(x)$  Premise

From previous attempt

2.  $\exists xP(x)$  \_\_\_\_\_ from (1)
3.  $P(c)$  Existential instantiation from (2)
4.  $\exists xQ(x)$  Simplification from (1)
5.  $Q(c)$  Existential instantiation from (4)
6.  $P(c) \wedge Q(c)$  \_\_\_\_\_ from (3) and (5)
7.  $\exists x(P(x) \wedge Q(x))$  Existential generalization

16 From 15 which rule of inference are used for step 2 and step 6

From previous attempt

17 Which conclusion can we obtain from the argument (Hint: the domain of  $x$  is DS-TA)?

Premise:

- Every DS-TA either enjoys drinking frappe or enjoys drinking tea
- Every DS-TA either enjoys drinking coffee or does not enjoy drinking tea
- Every DS-TA who enjoys drinking milk does not enjoy drinking coffee
- Some DS-TA do not enjoy drinking frappe

Conclusion: Every DS-TA do not enjoy drinking milk

From previous attempt

18 From 17, Conclusion: Some DS-TA who enjoy drinking tea, enjoy drinking coffee

From previous attempt

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◀ Previous (?)

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