Pancakes

Problem Statement

In his spare time, Tom has taken on a part time job at a bakery. The bakery has a special item on the menu: chocolate pancakes. Tom's primary responsibility is to man the pancake station. However, Tom tends to be a bit overzealous, and he bakes huge quantities of pancakes in advance, which results in leftovers at the end of his shift.

To reduce wastage, his manager wants to store the baked pancakes in the fridge. However, before storing them in the fridge, his manager wants the pancakes sorted in a particular order. Tom has been working there for a while now, and he has mastered a cool technique with the wooden bakery paddle. He can place three adjacent pancakes on his paddle and flip them upwards in the air such that when they land, the right-most pancake has shifted to the left-most position, and the other two pancakes have moved one place to the right. In other words, he can rotate to the right any subsequence of three pancakes.

Before the end of the shift, Tom's coworkers will help him to place the pancakes in a long line, which Tom wants to sort using his paddle technique. He can flip any three consecutive pancakes along the line on his paddle, rotate them, and then put them back. However, there are certain arrangements of pancakes which Tom is unable to sort using the paddle technique, no matter how many times he uses the paddle. Can you help Tom determine if it is possible to sort a given sequence of pancakes in accordance with his manager's demands using the paddle technique?

Input

The first line of input contains a positive integer N (3 <= N <= 100000), denoting the number of pancakes. This is followed by two lines: a permutation of the integers 1 to N inclusive describing the line-up order for the pancakes, and a permutation of the integers 1 to N inclusive describing how Tom's manager wants the pancakes sorted.

<u>Output</u>

Output "Possible" if Tom can sort the pancakes with his paddle in accordance with his manager's wishes, otherwise output "Impossible".

CS2040 Lab #5C, AY22/23 Semester 1 - Pancakes

Sample Input 1

4

1342

4321

Sample Output 1

Possible

Sample Input 2

7

1234567

 $7\; 6\; 5\; 4\; 3\; 2\; 1$

Sample Output 2

Impossible

Explanation

For Sample Input 1, the pancakes can be sorted in the following manner to get the desired order.

$$(1, 3, 4, 2) \rightarrow (4, 1, 3, 2) \rightarrow (4, 2, 1, 3) \rightarrow (4, 3, 2, 1)$$

For Sample Input 2, the pancakes cannot be sorted to get the desired order no matter how many times the paddle technique is used.